

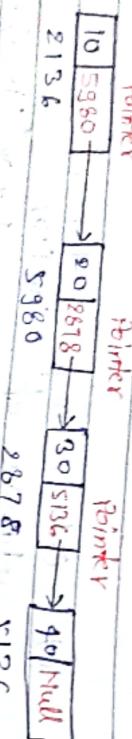
## x Linked List x

linked List is a linear data structure like array.

Note! In case of array all the elements are stored at successive memory location i.e. linear order is maintained implicitly.

But in the case of linked list, elements are not stored at successive memory locations. They are stored at random positions.

Ex:



Note! अगर ये दोनों ही field एक से type का होती हो तो इसे हम size के बहुत असर नहीं कर सकते। But यहाँ तक चोरी के fields (i.e. Data field & address/pointer field) int type का है।

How to implement a node in Linked List:



Note!

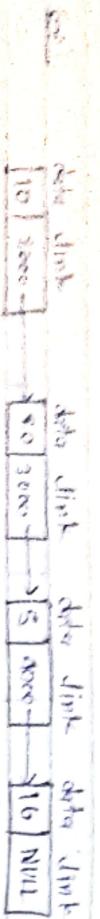
Linked List is not a collection of elements called nodes. It is a collection of elements called nodes so it will be implemented as —

1. Data information field of struct —
  2. Pointer, that contain address of next node.

struct Node

```
int data;
```

```
struct Node *Link;
```



1000

2000

3000

4000

5

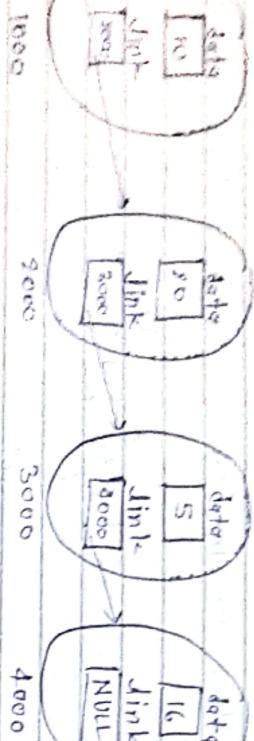
O/P → 16  
O/P → 3000

6

O/P → 16

7

O/P → 3000



**struct Node \* ptr ;**

O/P → 16  
O/P → 3000

O/P → 16

O/P → 3000

5

6

7

OR

ptr → data

ptr → Link

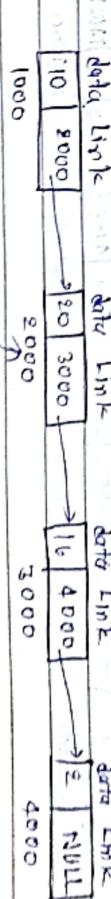
O/P → 16

O/P → 3000

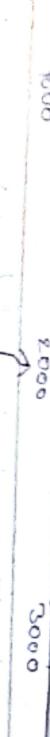
Hence we have two ways to access the members of a structure as discussed above.

Here every node in a structure and link is pointing to the next structure. Hence link is called as pointer to structure.

How to go to the next node in linked list:



ptr



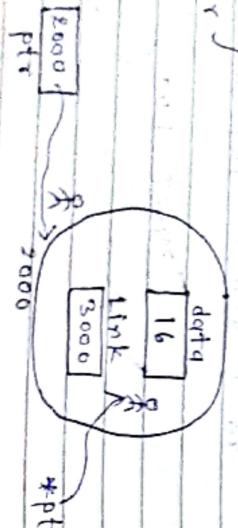
[10 2000]

[80 3000]

[15 4000]

[16 4000]

[5 NULL]



ptr

2000

\*ptr

Here initially ptr is pointing to the node 2. That means ptr value is 2000 (i.e. address of node 2)

[2000]

ptr

2000

ptr

so to go to the next node (i.e. node 3) we have to assign node 3 address 3000 to `ptr`.

and it will be assigned by writing following code —

```
ptr = ptr -> link;
```

What if linked list is empty?

It will hold the address of a node.  
so, declaration of `start` pointer should be like —

```
struct Node * start;
```

\* `start / head / front` pointer:



If linked list is empty that means there is no first node and hence there will not be any valid address of first or any node. so `start` pointer will contain `NULL`.  
That means `start` pointer will point to `NULL`. That means linked list is empty.

How to access the elements of a linked list.

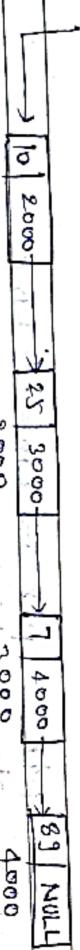
START

1000

start

(Pointer to first node)  
It holds address of first node in linked list.

Note: `start` is not a node, it is a pointer to a node. That means



START = 1000 { .Pointer to first node } / Pointer to structure

(3) printf("%d", \*ptr);  
(4) if (ptr == NULL)

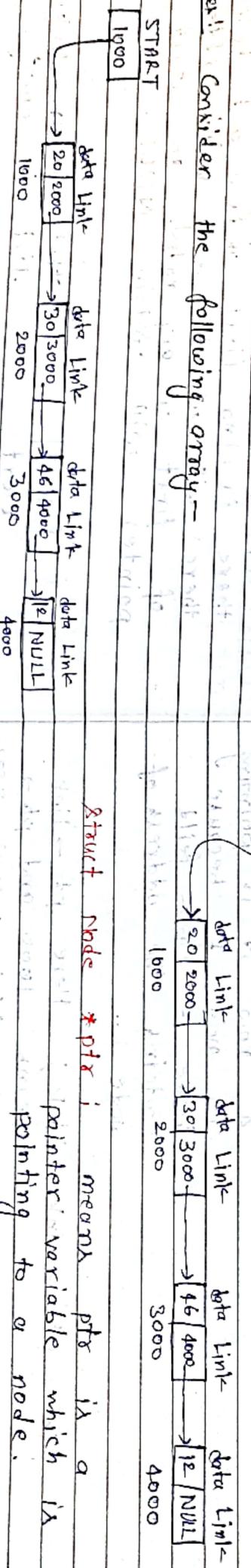
START → data = 10  
START → Link = 2000 (Pointer to end of structure)

START → Link → data = 20

START → Link → Link = 3000 (Pointer to 3rd node)

START

Ques! Consider the following array -



\*ptr means ptr is a pointer variable which is

pointing to a node.

What will be the output after executing

ptr = START; because START is 1000.

struct Node \*ptr;  
ptr = START;

ptr = ptr → Link → Link; Here ptr → Link

ptr → Link = START; means 1000 and  
ptr → Link → Link means 2000. So ptr is now

`ptr = Link = START;` Now `START` value which is 1000 will be assigned to `ptr = Link`. That means in node 3, we will go to the

Link field and will write there 1000 in the place of 4000. That means now node 3 is not pointing to the node 4. Now if it is pointing to node 1, because

node 3's Link field contains the address of node 1.

`ptr = ptr -> Link -> Link;` Here `ptr -> Link` means 1000 and `ptr -> Link -> Link` means 2000. So now `ptr` is 2000.

`ptr = ptr -> Link;` Here `ptr -> Link`

means 3000. So now

`printf("%d", ptr -> data)`)

Now it will

print the data at

Hence the address of the node

Note: In Linked List we will always avoid the situation like —

**NULL →**

It will give NULL pointer dereferencing error. Because NULL is not a valid address so it never can point to any data or address.

Basic operations on a linked list:

There are various operations we can perform on a linked list as —

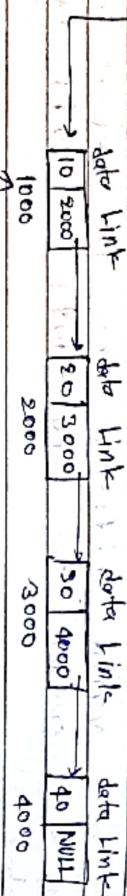
**1. Traversal.** That means इस element के बातें जानना (जैसा करता है) (जो इस element की print करता है).



1. Traversal : `ptr = START; //ptr = NULL`

`START`

`1000`



Note : `ptr` value is `NULL`

Note : `ptr = START` तो `ptr` के लिए `ptr = NULL` हो जायेगा।

so this traversal mechanism can be implemented using while loop -

`struct Node * ptr;`

`ptr = START;`

`while( ptr != NULL )`

`printf("%d", ptr->data);`

`ptr = ptr->Link;`

`printf("%d", ptr->data);` `O/P → 20`

Note : Here, `START` pointer is global

`ptr = START → Link;` `//ptr = 3000`

`printf("%d", ptr->data);` `O/P → 30`

`ptr = ptr->Link;` `//ptr = 4000`

`printf("%d", ptr->data);` `O/P → 40`

```
struct Node
{
    int data;
    struct Node * Link;
};

int count()
{
    struct Node * START = NULL;
    struct Node * pte;
    int count = 0;
    if(START == NULL)
        return 0;
    else
    {
        pte = START;
        while(pte != NULL)
        {
            count++;
            pte = pte->Link;
        }
    }
    return count;
}

void Traverse()
{
    struct Node * START;
    if(START == NULL)
        return;
    else
    {
        START = START->Link;
        printf("%d\n", START->data);
        Traverse();
    }
}
```

Ques: WAP to count no. of nodes in a linked list:

Sol:

```
int count()
{
    struct Node * START;
    int count = 0;
    if(START == NULL)
        return 0;
    else
    {
        START = START->Link;
        count++;
        while(START->Link != NULL)
        {
            START = START->Link;
            count++;
        }
    }
    return count;
}
```



heap

**Ques:** Given a linked list print second just node data . otherwise just return.

**Sol:** struct Node \* ptr = START;

```
if (*ptr == NULL || ptr->link == NULL)
    return;
```

for O node

temp

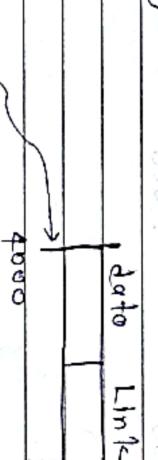
```
while (ptr->link != NULL)
```

```
ptr = ptr->link;
```

```
printf("%d", ptr->data);
```

Step 10  
②

Put the data into the node :



**2. Insertion in a linked list :**  
To insert a node into a linked list first of all we have to create that node with the help of malloc () as -

~~step 1~~ creating a node :

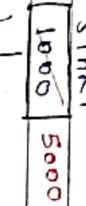
Now temp → data in = x, i.e.  
temp → link = NULL;

struct Node \* temp;  
temp = malloc ( sizeof( struct Node ));

~~step 3~~ ③ Insert this node to the linked list ;  
we can insert this node to the linked list —

- A. Insert at the beginning of the linked list.  
B. Insert at the end of the linked list.

A. at the beginning of the linked list:



B. At the ending of the linked list:



```

void main()
{
    Insert(100);
}

void Insert (int x)
{
    struct Node * temp;
    temp = malloc (sizeof (struct Node));
    temp->data = x;
    temp->link = START;
    START = temp;
}

struct Node * temp;
if (temp == NULL)
{
    temp = malloc (sizeof (struct Node));
    temp->data = START->data;
    temp->link = START;
    START = temp;
}

```

`temp → data = ∞;`  
`temp → Link = NULL;`

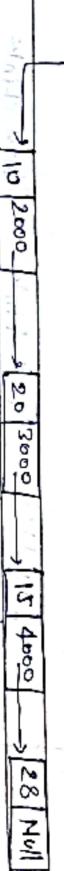
3. Search a key in the Linked list:

`START`

```
if ( START == NULL ) {
    return;
}
```

```
START = temp;
```

```
return;
```



Here we have to search an element "key" in the linked list. If it is present then we will return 0 (that means no) will be returned.

```
while ( ptr → Link != NULL ) {
    if ( ptr → data == key )
        return 1;
    else
        ptr = ptr → Link;
}
```

```
void search ( int key ) {
```

```
struct Node * ptr = START;
```

```
while ( ptr != NULL ) {
```

```
}
```

```
if ( ptr → data == key )
    return 1;
else
    ptr = ptr → Link;
```

Note: Here in all the implementations we have assumed that `START` is a global variable.

```
} // End of the function
```

```
return 0;
```

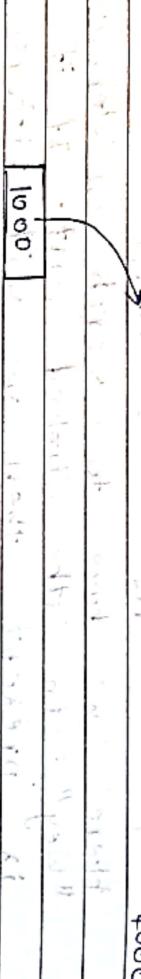
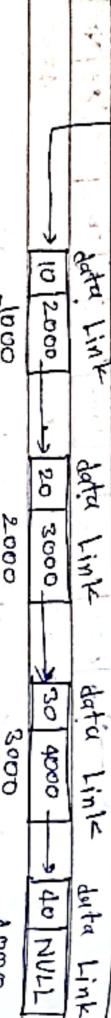
#### 4. Deletion in a Linked List:

##### B. Delete the Last Node:

```
struct Node *ptr, *pre;
```

```
if (START == NULL)
```

```
return;
```



A. Delete the First Node:

```
ptr = START;
```

```
START = NULL;
```

```
free(ptr);
```

```
else
```

```
pre = START;
```

```
ptr = START->Link;
```

```
while (ptr->Link != NULL)
```

```
    pre = ptr;
    ptr = ptr->Link;
```

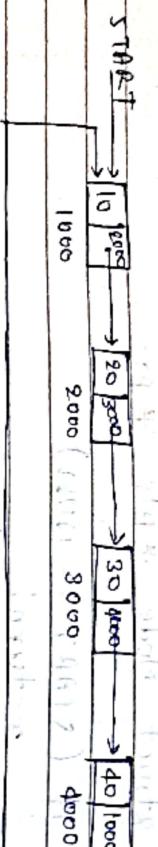
```
free(ptr);
```

```
}
```

```
}
```



## Circular Linked List:



Each node in a circular linked list contains 3 fields —

In circular linked list NULL pointer of last node is replaced by address of first node.

**Advantage:**

- We can traverse all nodes from any given node

**Disadvantage:**

- Nodes can be accessed easily.
- Deletion of a node is much easier.

## Doubly Linked List:



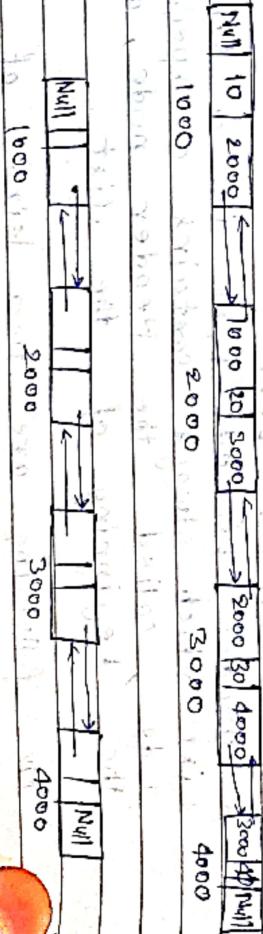
**Advantage:**

- It provides Bi-directional traversing.

### Type of Doubly Linked List :

#### 1. Linear Doubly Linked List :

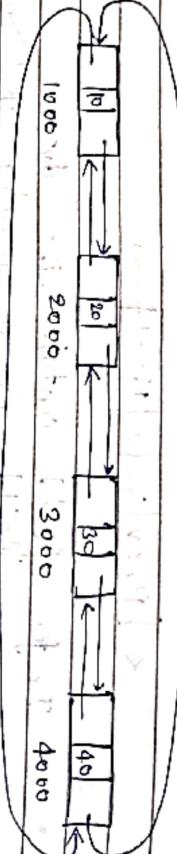
- We may enter in an infinite loop.
- HEAD / START node is required to indicate the START or END of the circular linked list.
- Back traversing is not possible.



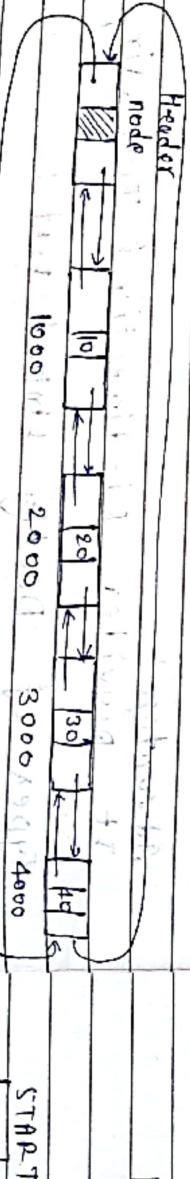
## 2. Circular Doubly Linked List:

### A. Grounded Header List:

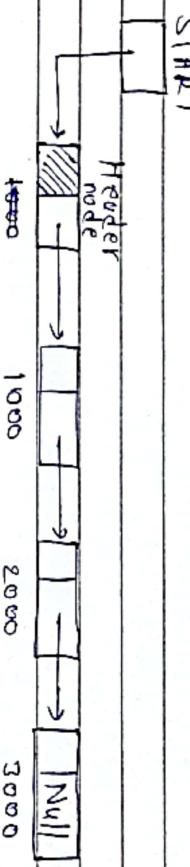
Here the just node contains the Null pointer.



### B. With a Header :



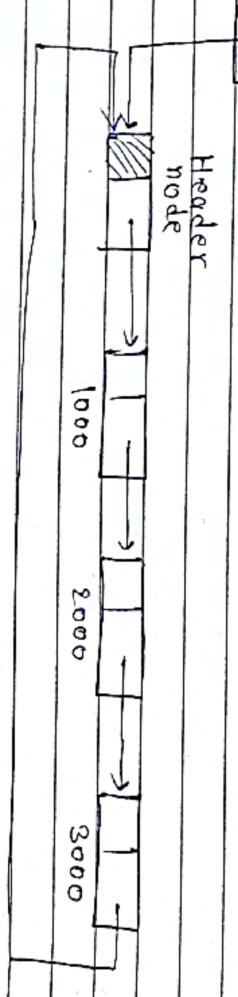
Last node points back to the Header Node.



### Header Linked List:

A Header Linked List is a Linked List which always contains a special node, called the Header node, at the beginning of the list.

The following are two kinds of Header lists.



Q: What is Data Structure?

A: How to organize the data in such a way that we can retrieve/manipulate it efficiently in future.

Q: What are the various types of Data Structure?

A: There are two types of data structure →

1. Linear Data Structure
2. Non-Linear Data Structure

Linear Data Structure: (at most 2 neighbours)

.....

Non Linear Data Structure: (any no. of neighbours)

.....

.....

.....

Linear Data Structure

→ Array

→ Linked List

→ Stack

→ Queue

Non-Linear Data Structure

→ Tree

→ Graph

So, we will cover the following 7 major topics in entire Data Structure.

1. Array
2. Linked List

Stack	
-------	--

3. Stack
4. Queue
5. Tree & Cmont (Imp.)
6. Graph
7. Hashing

Note! Generally array index starts from 0 but it's not mandatory theoretically and starting index can be anything in Data Structure.

### Array

Question Let's say we have an array  $A[20]$ . Each block size is 4 bytes. Then find the address of  $A[2]$ . Given that base address is 1000.

Sol:

int  $A[20]$

1	2	3	4	.....	18	19
0	1	2	3	4		

1000

Elements filled before  $A[2] = 0 \rightarrow 1$

1. Single Dimensional Array
2. Double Dimensional Array
3. Multi Dimensional Array

Note: In all the following examples we are going to consider integer size and bytes.

So, we will cover the following 7 major topics in entire Data Structure.

1. Array
2. Linked List
3. Stack
4. Queue
5. Tree \*\* (most Imp)
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Note: Generally array index starts from 0 but it's not mandatory theoretically and starting index can be anything in Data Structure.

### Array

Ques: Let's say we have an array  $A[20]$ .

Each block size is 4 bytes. Then find the address of  $A[2]$ . Given that base address is 1000.

Sol:

int A[20]

1	2	3	4	.....	18	19
0	1	2	3	4		

1. Single Dimensional Array
2. Double Dimensional Array
3. Multi Dimensional Array

Note: In all the following examples we are going to consider integer size as 4 bytes.

Each element size is 4 bytes. (Given)

Hence, memory already filled before  $A[2]$   
 $= 2 \times 4$  bytes  
 $= 8$  bytes

Hence address of  $A[2]$  is = base address + 8  
 $= 1000 + 8$  bytes  
 $= 1008$  bytes

Hence address of  $A[5]$  = Base address + 16  
 $= 1000 + 16$   
 $= 1016$

Hence address of  $A[5] = 1016$   
 $\leftarrow 16 \text{ byte} \rightarrow$   
 $1000$        $A[5]$

Hence address of  $A[5] = 1016$   
 $\leftarrow 16 \text{ byte} \rightarrow$   
 $1000$        $A[5]$

Ques: Let we have an array  $A[1 \dots 30]$ . Base

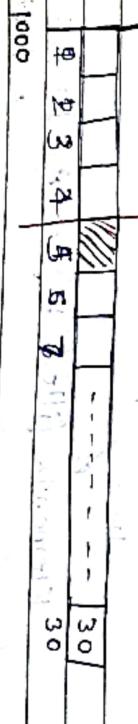
address is 1000 and size of each element  
 is 4 bytes. Find the address of  $A[5]$ .

Ans: Given  $A[1 \dots 30]$

Ques: Let we have an array  $A[5 \dots 5]$   
 $w = 2$  bytes - Base address = 1000

lowest highest index.

Find address of  $A[1]$ .



Elements filled before  $A[5]$  is 1 to 4

lowest highest index

## ② Double Dimensional Array : (2-D Array) (m rows, n columns)

-5	-4	-3	-2	-1	0	1	2
----	----	----	----	----	---	---	---

1000

0	1	2	
0	A <sub>00</sub>	A <sub>01</sub>	A <sub>02</sub>
1	A <sub>10</sub>	A <sub>11</sub>	A <sub>12</sub>

Elements filled before A[1] ix  $\leftarrow -5 \text{ to } 0$

$$= \text{last - first} + 1$$

Note: The Biggest Advantage of Array is its random accessing nature, That means we can directly go into the memory and can access data stored in any location.

memory already filled before A[1]  $\Rightarrow 0 - (-5) + 1 = 6$  elements.  
 $A[1] = 6 \times 2 = 12$  bytes  
 Hence address of A[1] is = Base address + 12  
 $= 1000 + 12 = 1012$ .

Ex: printf ("%.d", A[i][j]);

Ques: How we can store a 2-D array in memory?

Ans: There are 2 ways to store a 2-D array in memory —

1. Row wise (Row Major Order)
2. Column wise (Column Major Order)

Note:  
 $A[2][3]$

Row with index 0	$\rightarrow 0$	$A_{00} \quad A_{01} \quad A_{02}$
Row with index 1	$\rightarrow 1$	$A_{10} \quad A_{11} \quad A_{12}$
Row with index 2	$\rightarrow 2$	$A_{20} \quad A_{21} \quad A_{22}$

Row with index 1

Row with index 0 = 3 elements

Row with index 1 = 3 elements  
in  $A[2][3]$ , First Dimension 2 at  
index 2

Question: Represent the following 3D array in row major order.

$A[3][4]$

0	$A_{00} \quad A_{01} \quad A_{02} \quad A_{03}$
1	$A_{10} \quad A_{11} \quad A_{12} \quad A_{13}$
2	$A_{20} \quad A_{21} \quad A_{22} \quad A_{23}$

Answer: in Row major order:

$A_{00} \quad A_{01} \quad A_{02} \quad A_{03}$	$A_{10} \quad A_{11} \quad A_{12} \quad A_{13}$	$A_{20} \quad A_{21} \quad A_{22} \quad A_{23}$
---	---	---

every index in 1st dimension  
represents 3 elements:

$\leftarrow$  0th index  $\rightarrow$  1st index  $\rightarrow$  2nd index  $\rightarrow$   
 $\leftarrow$   $A_0$  Row  $\rightarrow$   $\leftarrow$   $A_1$  Row  $\rightarrow$   $\leftarrow$   $A_2$  Row  $\rightarrow$

(A) Representation in Row major order:

2. in Column major order:

$A_{00} \quad A_{01} \quad A_{02}$	$A_{10} \quad A_{11} \quad A_{12}$
$\leftarrow$ $A_0$ Row $\rightarrow$	$\leftarrow$ $A_1$ Row $\rightarrow$

$A_{00} \quad A_{01} \quad A_{02} \quad A_{03}$	$A_{10} \quad A_{11} \quad A_{12} \quad A_{13}$	$A_{20} \quad A_{21} \quad A_{22} \quad A_{23}$
$\leftarrow$ col 1 $\rightarrow$	$\leftarrow$ col 2 $\rightarrow$	$\leftarrow$ col 3 $\rightarrow$



Given: Given an array  $A[5][4]$  whose address is 1000. If each element size is 4 bytes then find the address of  $A_{22}$ . Elements are stored in Row major order.

Hence total memory already filled before  $A_{22}$  =  $10 \times 4$   
 $= 1000 + 40$  bytes

Sol: How many rows are filled already before row with index 2. = index 0 row and index 1 row.

A <sub>00</sub>	A <sub>01</sub>	A <sub>02</sub>	A <sub>03</sub>	A <sub>10</sub>	A <sub>11</sub>	A <sub>12</sub>	A <sub>13</sub>	A <sub>20</sub>	A <sub>21</sub>	A <sub>22</sub>	A <sub>23</sub>
1000	1004	1008	1012	1016	1020	1024	1028	1032	1036	1040	1044

$$= \text{Jst} - \text{First} + 1$$

$$= 1 - 0 + 1$$

Hence

Address of  $A_{22}$  = Base address + 40

$$= 1000 + 40$$

since 1 row contains 4 elements

so 2 row contains 8 elements.

Ques:

Given an array -  $A[5 \dots 5][10 \dots 10]$

$$w = 2 \text{ bytes}, B.A = 1000$$

Now how many elements are already filled in index 2 row before  $A_{22}$ .

= 0 and 1 columns.

= last - first + 1

= 1 - 0 + 1

= 2 columns/elements.

so total elements filled before  $A_{22}$

= 2 rows + 2 elements

= 8 + 2

= 10 elements.

Each row contains how many elements = 10 to 10

= Jst - fi

$$\begin{array}{l} A_{01} \\ A_{02} \end{array}$$

$= 274 \text{ bytes} \rightarrow$   
 $A_{01} = 274$   
 $A_{02} = 274$

Q. 6. How many rows will contain how many elements

$$= 6 \times 21$$

= 126 elements.

Ques: Let's we have an array  $A[-100..10][-20..-20]$ .  $B.A = 1000$ .  $W = 2$  bytes.  $B.A = 1000$ .

How many elements are present in index row with index 1 before element  $A[1][1]$

$$= -10 \text{ to } 0$$

$$= \text{last} - \text{first} + 1$$

$$= 0 - (-10) + 1$$

$$= 11 \text{ elements}$$

$$= 1000$$

Ans:

so total elements present already filled before  $A[1][1] = 126 + 11$

$$= 137 \text{ elements.}$$

since each element takes 2 bytes

Hence 137 elements will take  $= 137 \times 2$

$$= 274 \text{ bytes.}$$

Q. memory already filled before element  $A[2][2]$

$$= 274 \text{ bytes.}$$

Hence address of  $A[2][2] = \text{Base Address} + 274$

$$= 1000 + 274$$

$$= 1274$$

Ans:

Q. If  $n$  rows will contain how many elements  
 $= n \times 41$   
 $n$  rows will contain how many elements.  
 $= 451$  elements.

How many elements are already filled in row with index 1 before element  $A[1][1]$

$$= -20 \text{ to } 0$$

$$= \text{last-first} + 1$$

$$= 0 - (-20) + 1$$

$$= 21 \text{ elements.}$$

No total elements already filled before element  $A_{11}$  is  $451 + 21$

$$= 472 \text{ elements}$$

Hence total memory already filled before element  $A_{11}$  is  $= 472 \times 2$

$$= 944 \text{ bytes.}$$

so Address of element  $A[1][1]$  in row major order we will store the elements of above matrix (array) in the following way -

Row	A000	A001	A010	A011	A020	A021	A100	A101	A110	A111	A120	A121
-----	------	------	------	------	------	------	------	------	------	------	------	------



Note! in  $A[2][3][2]$

Each number in first dimension represents how many numbers elements = 3  $\times$  2 = 6 elements.

Hence size of  $A[0] =$  size of  $A[1] = 3 \times 2$

### Ex: $A[2][3][2]$



in  $A[2][3][2]$

$A[-2]$	"	"	"	"	"	"	+
$A[-1]$	"	"	"	"	"	"	+
$A[0]$	"	"	"	"	"	"	+

Each number in 2nd dimension represents  
how many elements = 2

row with index -10	in $A[1]$ matrix +
row with index -8	" " " "+

Ques: given an array  $A[-5 \dots 5][10 \dots 10][5 \dots 5]$   
 $\omega = 2$  bytes ,  $B.A = 1000$

add ( $A[1][1][1]$ ) = ? using Row Major Order

row with index 0 " " " "+

Sol:  
size of first dimension =  $5 - (-5) + 1 = 11$

$n_1$  2nd " =  $10 - (-10) + 1 = 21$

$n_2$  3rd " " =  $5 - (-5) + 1 = 11$

Every index/number in 1st Dimension  
represents how many elements =  $21 \times 11$

= 231 elements

$$(21 \times 11) \times 6 + (41) \times 11 + 6 \\ = 1386 + 431 + 6 \\ = 1523$$

Every index/number in 2nd Dimension  
represents how many elements = 11 elements

Hence 1523 " " " =  $1523 \times 2$   
= 3046 bytes

How many elements are already filled before  
element  $A[1][1][1]$   
=  $A[5]$  matrix of size  $21 \times 11$  +  
 $A[-4]$  " " " " "+  
 $A[-3]$  " " " " "+  
= 4026 Ans



Column major Order:

Ex:  $A[2][3]$

0	0	1	2
0	$A_{00}$	$A_{01}$	$A_{02}$
1	$A_{10}$	$A_{11}$	$A_{12}$

How many columns filled already before  $A[1][1]$   
 col with index 0 to 0 index  
 col with index 1 to 1 index  
 col with index 2 to 2 index

index 0 index 1 index 2

Each column have how many elements  
 -5 index to 5 index

$$= 5 - (-5) + 1$$

$$= 11 \text{ elements.}$$

Ques:

$A[-5:-5][10:-1:10]$   
 $w = 2$  bytes.  $\&A[0] = 1000$

How many rows filled before  $A[1][1]$   
 index -5 to index 0

$$= 5 - (-5) + 1$$

$\text{odd}(A[1][1]) = ?$  consider column  
 major order.

Sol:

-10 - 9 - 8 - ... 1 - 0

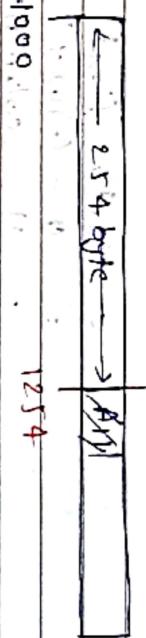
How many elements filled  
 to total How many elements filled  
 before element  $= 11 \times 11 + 6$

size of each element  $= 2 \text{ bytes}$ .  
 no size of 127 elements  $= 127 \times 2$   
 $= 254 \text{ bytes.}$

000	A00	A01	A02	A12
010	A10	A11	A12	
110				



That means  $2^{54}$  bytes are already filled before element  $A[1][1]$ .



Hence address of element  $A[1][1]$

$$\begin{aligned} &= \text{Base address} + 254 \\ &= 1000 + 254 \\ &= 1254. \end{aligned}$$

Any how many elements will be filled already in memory before  $A[1][1]$

@Ans:  $A[-5:-5][-10:-10][-5:-5]$

is —

$A[1][1][1]$

add  $(A[1][1][1]) = ?$  consider —

column major order

$$\begin{array}{c} -5 \rightarrow 0 \\ 0 - (-5) + 1 = 0 - (-5) + 1 = 6 \end{array}$$

$$-10 \rightarrow 0 \\ 0 - (-10) + 1 = 0 - (-10) + 1 = 11$$

$$-5 \rightarrow 0 \\ 0 - (-5) + 1 = 0 - (-5) + 1 = 6$$

$A[-5:-5][-10:-10][-5:-5]$

$\Rightarrow A[1][1][2][1][1]$

hence total elements already filled  
 $= 6 \times 2 \times 11 + 11 \times 11 + 6 = 1513$

every no. with  
represent  $= 2^{11} \times 11$   
element

since size of each element = 2 bytes  
size of  $15 \times 3$  =  $2 \times 15 \times 3$   
= 3026 bytes.

so total memory already filled before element  $A[1][1]$  is filled.

0	$A_{00} - A_{01} - A_{02}$	$A_{03} - A_{04}$
1	$A_{10} - A_{11} - A_{12}$	$A_{13} - A_{14}$
2	$A_{20} - A_{21} - A_{22}$	$A_{23} - A_{24}$
3	$A_{30} - A_{31} - A_{32}$	$A_{33} - A_{34}$
4	$A_{40} - A_{41} - A_{42}$	$A_{43} - A_{44}$



How to store upper/lower triangular arrays in memory:

while storing such types of arrays in memory efficiently then no need to store zeros in memory.

$$= 1000 + 3026$$

Ex: Let's store the above lower triangular matrix in memory in row major order.

Ans.

Triangular Array:

① Lower Triangular Array:

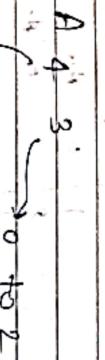
0	1	2	3	4
$A_{00}$	$A_{10}$	$A_{20}$	$A_{30}$	$A_{40}$
$A_{10}$	$A_{11}$	$A_{21}$	$A_{31}$	$A_{41}$
$A_{20}$	$A_{21}$	$A_{22}$	$A_{32}$	$A_{42}$
$A_{30}$	$A_{31}$	$A_{32}$	$A_{33}$	$A_{43}$
$A_{40}$	$A_{41}$	$A_{42}$	$A_{43}$	$A_{44}$

so let's try to check (find) the address of any element ( $A_{43}$  for example).

$A_{43}$ .

so how many elements are filled before the element  $A[4][3]$  (i.e.  $A_{43}$ )

$A[4][3]$



$0 \rightarrow 3 \rightarrow 1 \rightarrow 0 \rightarrow 2$   
 $\text{start} \cdot \text{first} + 1$

$2 - 0 + 1$

$0 \rightarrow 3 \rightarrow 1 \rightarrow 0 \rightarrow 1$   
 $\text{start} \cdot \text{first} + 1$

$3 - 0 + 1$

so 4 rows filled before  $A_{43}$ , filled 3 elements

so how many elements filled before  $A_{43}$

$A[4][3]$

Major operations performed on any linear data structure like Array, linked-list:

- ① Traversal: Processing each element in the list.
- ② Search: Finding the location of an element.
- ③ Insertion: Adding a new element to the list.
- ④ Deletion: Removing an element from the list.

so total elements filled in these 4 rows —  
 $= 1 + 2 + 3 + 4 = 10$  elements

Hence total elements filled before  $A_{43}$  —  
 $= 10 + 3$   
 $= 13$  elements.

since each element contains  $\approx 2$  bytes  
so  $13 \times 2 = 26$  bytes.

Hence address of  $A_{43}$  = Base Address + 26  
=  $1000 + 26$   
Ans

Formula for finding address of any element  
 $A[i][j]$  in a two-dimensional array  
 $A[m][n]$ :

① In row major order:

$$\text{Address of } A[i][j] = B + w(n(i-L_1) + j - L_2)$$

② In column major order:

$$\text{Address of } A[i][j] = B + w((i - L_1) + m(j - L_2))$$

Here

$B$  = Base Address

$w$  = Element size

$m \geq$  upper bound of rows

$n \geq$  upper bound of columns

$L_1 =$  lower bound of rows

$L_2 =$  lower bound of columns

$wm =$  no. of rows in memory

$n =$  no. of columns.

Ques: How is physically memory allocated for a two-dimensional array if each element of an array  $D[20][50]$  requires 4 bytes of storage? Base address of data is 2000. Determine the location of  $D[10][10]$ , when the array is stored as -

- i). Row major order
- ii). Column major order

sol: i). Row major order :

$$\text{Address of } D[10][10] = B + w(n(i-L_1) + (j-L_2))$$

$$= 2000 + 4(50(10-0) + (10-0))$$

$$= 2000 + 4(510)$$

$$= 4040$$

ii). Column major order :

$$\text{Address of } D[10][10] = B + w((i-L_1) + m(j-L_2))$$

$$= B + w((10-0) + 20(10-0))$$

$$= 2000 + 840$$

$$= 2840$$