

## Integraaltoets / Integral Test §11.3

Gestel  $f$  is 'n kontinue, positiewe, dalende funksie (continuous, positive, decreasing function) op  $[1, \infty)$  en laat  $a_n = f(n)$ . Dan geld:

- As  $\int_1^{\infty} f(x) dx$  konvergent is, dan is  $\sum_{n=1}^{\infty} a_n$  konvergent.
- As  $\int_1^{\infty} f(x) dx$  divergent is, dan is  $\sum_{n=1}^{\infty} a_n$  divergent.

D.w.s.  $\int_1^{\infty} f(x) dx$  is konvergent as en slegs as  $\sum_{n=1}^{\infty} a_n$  konvergent is.

**$p$ -reeks /  $p$ -series:**

Die  $p$ -reeks  $\sum_{n=1}^{\infty} \frac{1}{n^p}$  is konvergent vir  $p > 1$

en divergent vir  $p \leq 1$ .

## Huiswerk

Ex. 11.3 nr. 5, 7, 11, 15, 17, 21, 29

Laat pp.763–765 uit.