## AMATH 481 & 581 Fall 2018 Bose-Einstein Condensation in 3D

## Submission open until 11:59:59pm Tuesday December 11, 2018

Consider the Gross-Pitaevskii system (nonlinear Schrödinger equation with potential) modeling a condensed state of matter

$$i\psi_t + \frac{1}{2}\nabla^2\psi - |\psi|^2\psi + [A_1\sin^2(x) + B_1][A_2\sin^2(y) + B_2][A_3\sin^2(z) + B_3]\psi = 0$$
 (1)

where  $\nabla^2 = \partial_x^2 + \partial_y^2 + \partial_z^2$  (you can google this to learn more). Consider periodic boundaries and using the **3D FFT** (fftn) to solve for the evolution. Step forward using ode45. VISUALIZE USING isosurface or slice. WARNING: 3D problems involve working with vectors of size  $n^3$ , so pick n small to begin playing around.

## **ANSWERS:**

(a) With  $x, y, z \in [-\pi, \pi]$ , n = 16, tspan = 0:0.5:4 and parameters  $A_i = -1$  and  $B_i = -A_i$ , with initial conditions

$$\psi(x, y, z) = \cos(x)\cos(y)\cos(z)$$

write out the solution of your numerical evolution from ode45 as A1.dat (real part) and A2.dat (imaginary part) (NOTE: your solution will be in the Fourier domain when you write it out).

(b) Now solve with initial conditions

$$\psi(x, y, z) = \sin(x)\sin(y)\sin(z)$$

write out the solution of your numerical evolution from ode45 as A3.dat (real part) and A4.dat (imaginary part)(NOTE: your solution will be in the Fourier domain when you write it out).