

Homework 2. Logic

In the questions 1, 2 and 3 you have to choose one or several correct answers from the list, in the questions 4 and 5 you have to give a solution.

Question 1. Which of the following sentences are logical statements?

- ☐ A Find the square root of 4.
- ☐ B The number π is irrational.
- ☐ C Is the number 91 prime?
- ☐ D The lecture about combinatorics was fascinating!
- ☐ E The number 28 is a multiple of 7.
- ☐ F $e = 2,71828$.

Question 2. Which of the following statements is false?

- ☐ A If the angle of a regular triangle is acute then the number 97 is prime.
- ☐ B If the number 97 is prime then the elephants can play a piano.
- ☐ C If the elephants can play a piano then $\pi < 3$.
- ☐ D If $\pi < 3$ then the angle of a regular triangle is acute.

Question 3. Let x and y be integers. Which of the following statements are true?

- ☐ A $\forall x \exists y (x^2 = y^4)$;
- ☐ B $\forall x \exists y (x^4 = y^2)$;
- ☐ C $\forall x \exists y (xy \text{ is a perfect square})$;
- ☐ D $\forall x \exists y (xy = 1)$;
- ☐ E $\forall x \exists y (xy = 0)$.

Question 4. For a real number x , consider the open sentences $P(x) : x \geq 3$ and $Q(x) : x^2 > 9$. Give an example of x such that

- ☐ A the statement $P(x) \Rightarrow Q(x)$ is true;
- ☐ B the statement $P(x) \Rightarrow Q(x)$ is false.

Question 5. Construct the truth tables and check if it is always truth that:

- ☐ A $(\neg A \wedge B) \vee \neg B$;
- ☐ B $(A \vee B) \wedge \neg A$;