

# Outliers Detection using the Instantaneous Degree within IP Traffic Modelled as a Stream Graph

Audrey Wilmet<sup>1</sup>, Matthieu Latapy<sup>1</sup>,  
Robin Lamarche-Perrin<sup>2</sup>

<sup>1</sup>Laboratoire d'informatique de Paris 6 (LIP6) - Complex  
Networks Team <http://www.complexnetworks.fr/>

<sup>2</sup>Institut des Systèmes Complexes Paris Île de France (ISC-PIF)

RESCOM 2018, Toulouse, January 18, 2018



# Context and Goals

- IP traffic:

Flow of data across the Internet:

- nodes: IP addresses;
- interactions: packet exchanges;
- temporal interactions.

- Goals:

- ① Detect outliers = irregular patterns:
  - global high activity of an IP address;
  - sharp variation in the activity of an IP address;
  - high activity at a particular moment.
- ② Identify them: find their exact cause in the data;
- ③ remove them precisely from the traffic.

## Introduction

Context and Goals

**Stream Graph**

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal  
Homogeneity

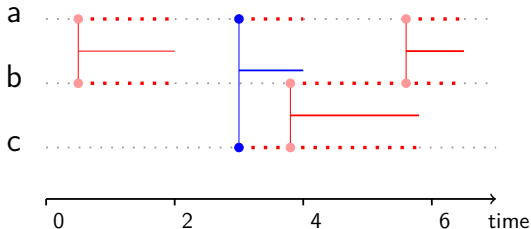
Detection

Identification &  
Removal

## Conclusion

# IP Traffic as a Stream Graph

Stream graph: 1h of real IP Traffic (MAWI)



ex:  $a$  and  $c$  interacted from  $t_1 = 3$  to  $t_2 = 4$

→ M. Latapy *et al.*, 2017 ; T. Viard *et al.*, 2017.

● **Other Data Modelling:** Signal, graph

→ Y. Himura *et al.*, 2013 ; H. Asai *et al.*, 2014.

# Our Approach

Data Modelling: temporal interactions = stream graph

---

Outlier = entity statistically deviating from others

1) **Entity**  $x$ :  $(uv, t) \quad uv \quad (v, t) \quad v \quad t \quad \Rightarrow (v, t)$

2) **Studied set**  $x \in X$ :

All entities of the same types or a subset of it ?

$$\Downarrow \\ t \in X = T$$

$$\Downarrow \\ t \in X \subset T$$

3) **Feature**  $\mathcal{F}$  on  $X$

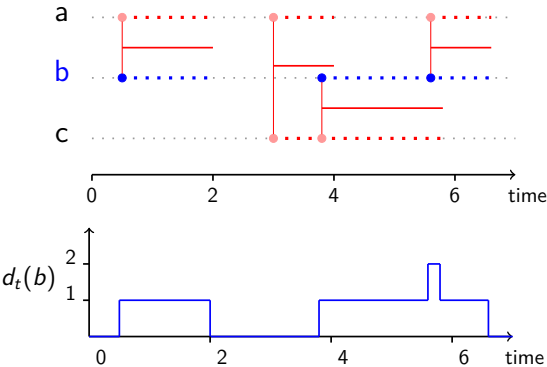
$\Rightarrow$  Instantaneous degree

# Instantaneous Degree of $(v, t)$

Number of neighbours of node  $v$  at time  $t$ :

$$d_t(v) = |\{u, (t, uv) \in E\}|$$

*Example: degree profile of  $b$*



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

Detection

Identification &  
Removal

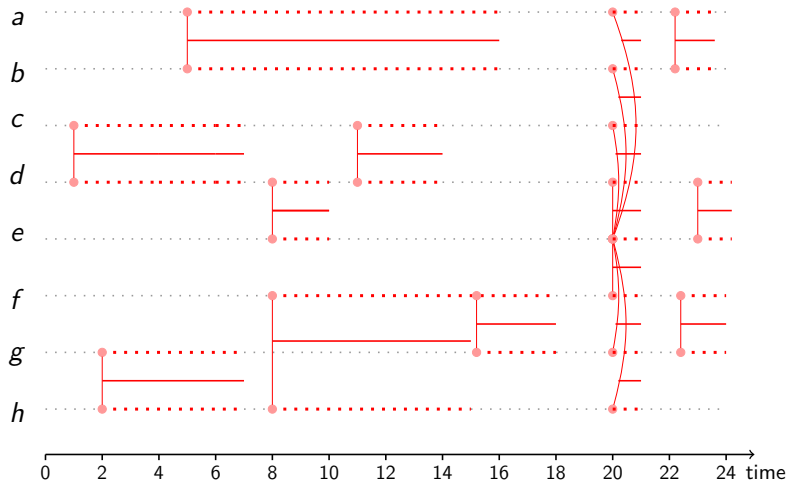
## Conclusion

# ① Detection

**Entity:**  $(v, t)$

**Feature:**  $d_t(v)$

**Studied set:**  $V \times T$

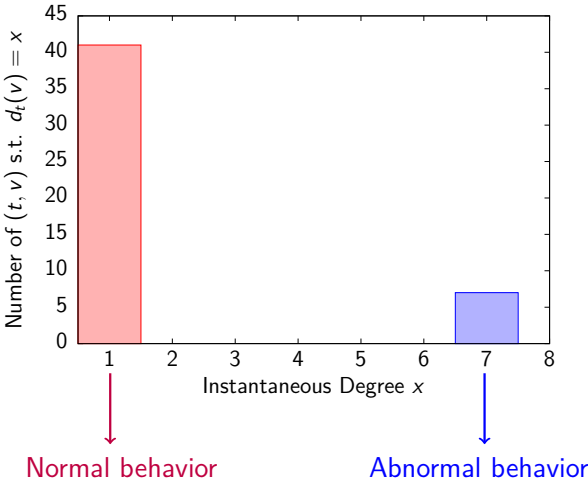


# ① Detection

Entity:  $(v, t)$

Feature:  $d_t(v)$

Studied set:  $V \times T$



Introduction

- Context and Goals
- Stream Graph
- Our Approach
- Instantaneous Degree

Detect, Identify, Remove

In Practice

- Degree Heterogeneity
- Difficulties

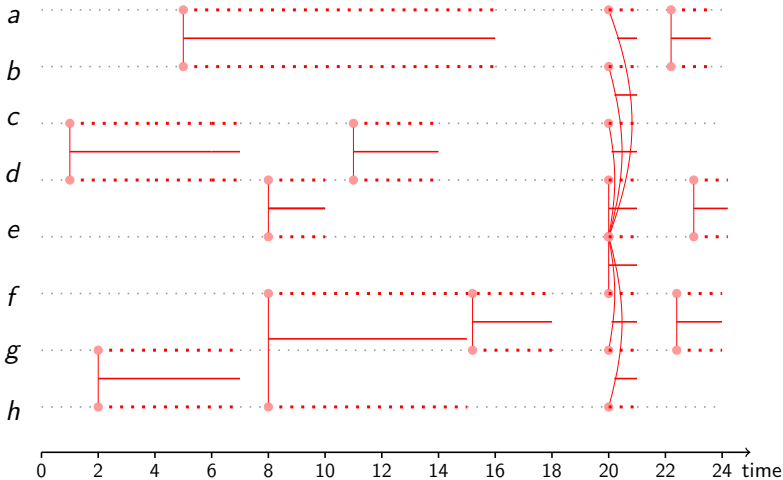
Our Method

- Temporal Homogeneity
- Detection
- Identification & Removal

Conclusion

① Detection

$\{(v, t) : d_t(v) = 7\} \Rightarrow$  Detected outlier





Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

In Practice

Degree Heterogeneity

Difficulties

Our Method

Temporal

Homogeneity

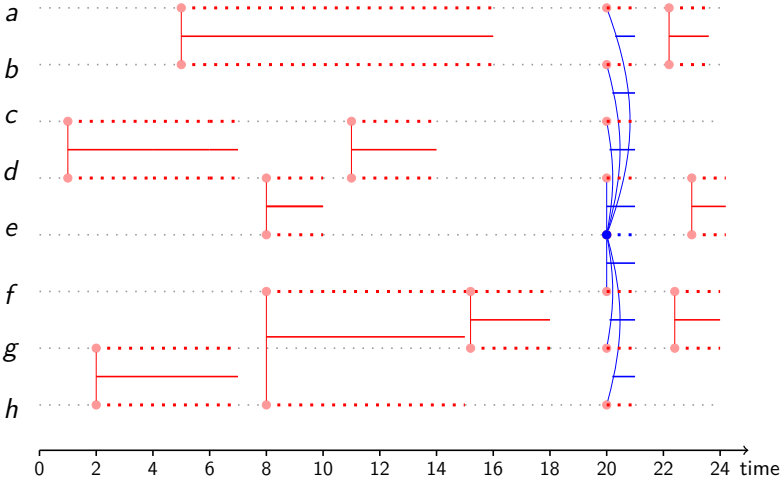
Detection

Identification &  
Removal

Conclusion

② Identification

$\{(e, t), t \in [20, 21]\} \Rightarrow \text{identified outlier}$



Introduction

- Context and Goals
- Stream Graph
- Our Approach
- Instantaneous Degree

Detect, Identify,  
Remove

In Practice

- Degree Heterogeneity
- Difficulties

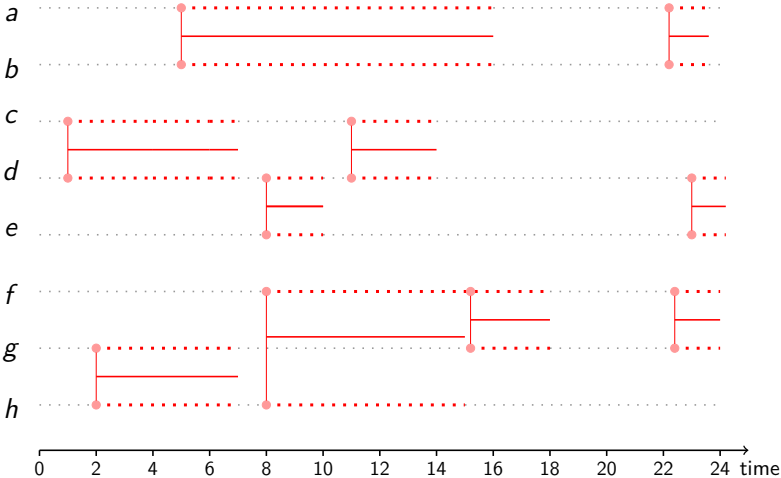
Our Method

- Temporal Homogeneity
- Detection
- Identification & Removal

Conclusion

③ Removal

$\{(e, t), t \in [20, 21]\}$



Introduction

- Context and Goals
- Stream Graph
- Our Approach
- Instantaneous Degree
- Detect, Identify, Remove

In Practice

- Degree Heterogeneity
- Difficulties

Our Method

- Temporal Homogeneity
- Detection
- Identification & Removal

Conclusion

# In Practice

## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

Detection

Identification &  
Removal

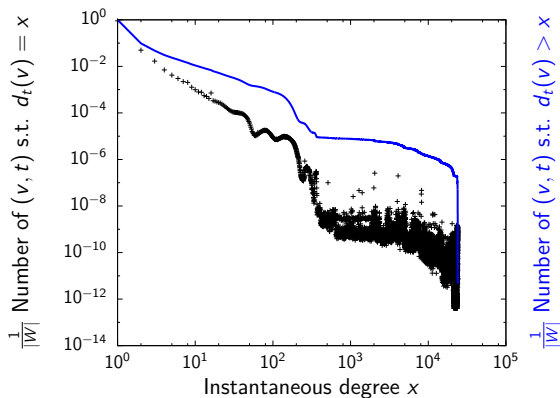
## Conclusion

# Global Degree Distribution

**Entity:**  $(v, t)$

**Feature:**  $d_t(v)$

**Studied Set:** Global,  $W = V \times T$ .



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal  
Homogeneity

Detection

Identification &  
Removal

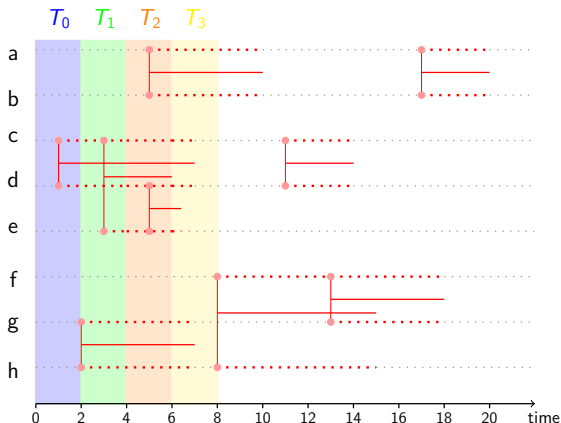
## Conclusion

# Local Degree Distribution (1/2)

**Entity:**  $(v, t)$

**Feature:**  $d_t(v)$

**Studied Set:** Local,  $W_i = T_i \times V$ ,  $T_i = [2i, 2i + 2[$ .



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

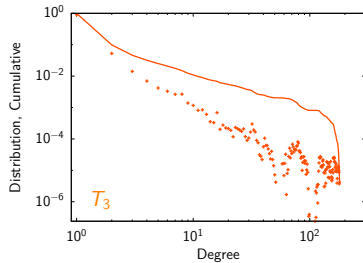
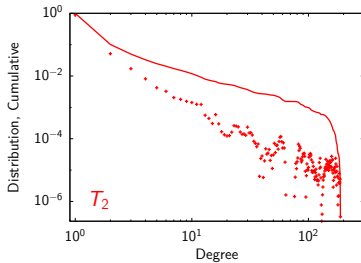
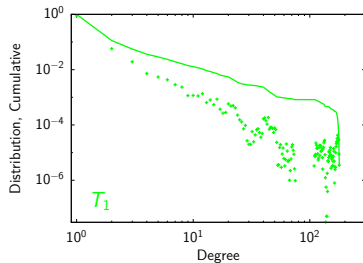
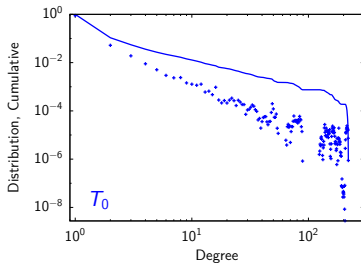
Temporal  
Homogeneity

Detection

Identification &  
Removal

## Conclusion

# Local Heterogeneity (2/2)

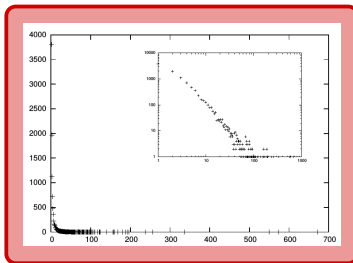


# Difficulties

Outlier = Activity that deviates from the usual one

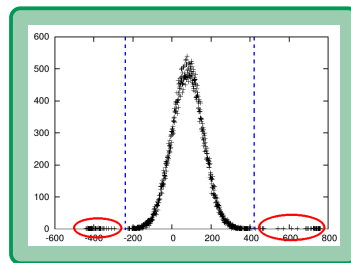
Find an outlier  $\iff$  Find the normality

X



Heterogeneous

✓



Homogeneous with outliers

Introduction

- Context and Goals
- Stream Graph
- Our Approach
- Instantaneous Degree
- Detect, Identify, Remove

In Practice

- Degree Heterogeneity
- Difficulties

Our Method

- Temporal Homogeneity
- Detection
- Identification & Removal

Conclusion

# Our Method



Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

In Practice

Degree Heterogeneity

Difficulties

Our Method

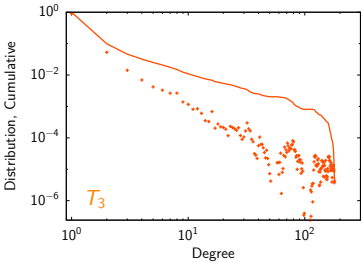
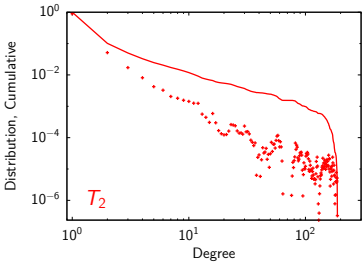
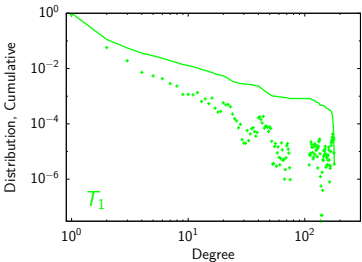
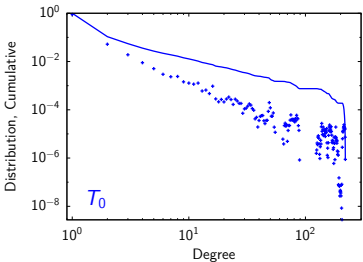
Temporal  
Homogeneity

Detection

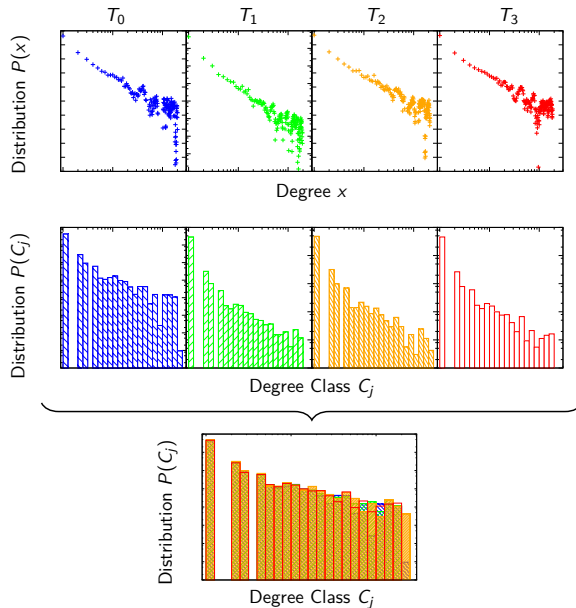
Identification &  
Removal

Conclusion

# Temporal Homogeneity



# Comparison of Local Distributions



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

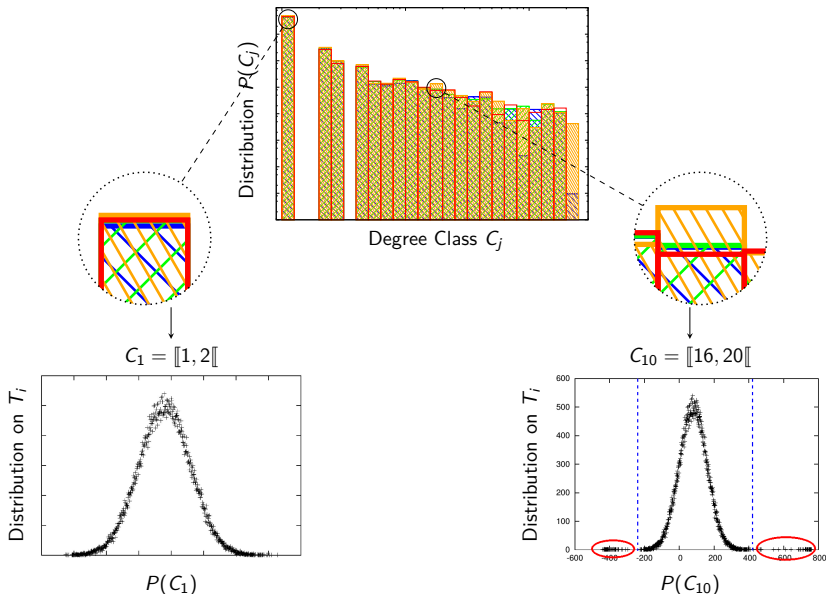
Temporal  
Homogeneity

Detection

Identification &  
Removal

## Conclusion

# Comparison of Local Distributions



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

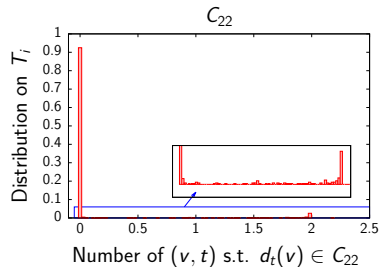
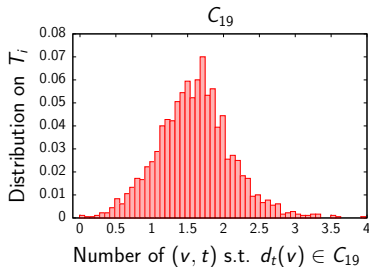
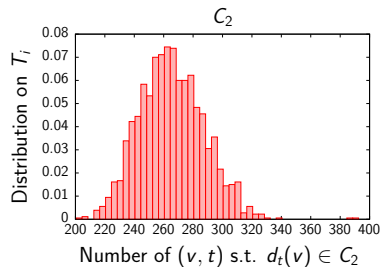
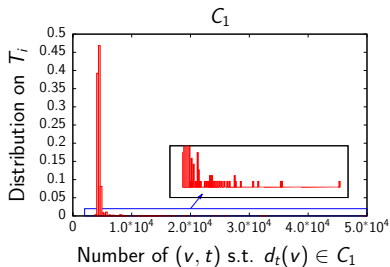
Temporal  
Homogeneity

Detection

Identification &  
Removal

## Conclusion

# Results: Homogeneous Distributions



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

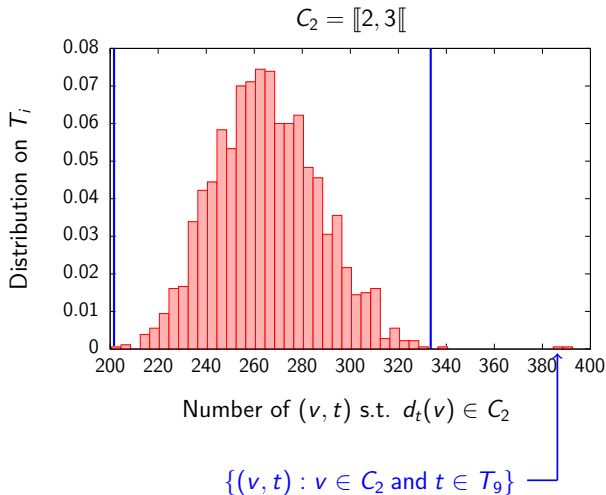
Temporal  
Homogeneity

**Detection**

Identification &  
Removal

## Conclusion

# Results: Homogeneous Distributions



Outlier = temporal  $T_i$  + structural  $C_j$  information.

## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal  
Homogeneity

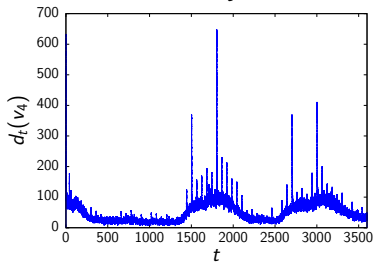
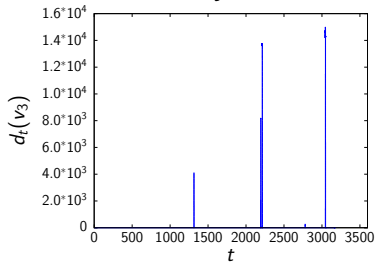
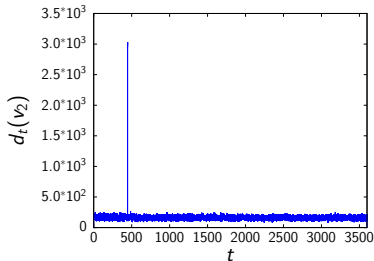
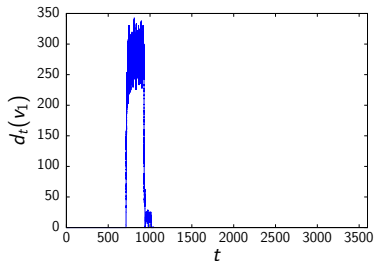
Detection

Identification &  
Removal

## Conclusion

# Identification and Removal - Degree Profiles

⇒ Suspicious couples  $(v, T_i)$ .



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

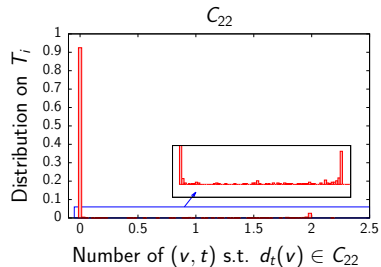
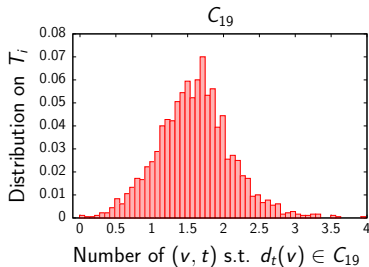
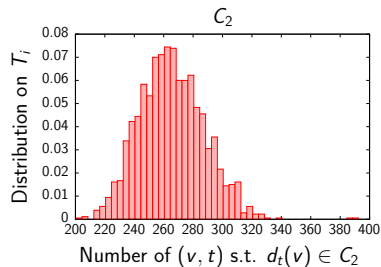
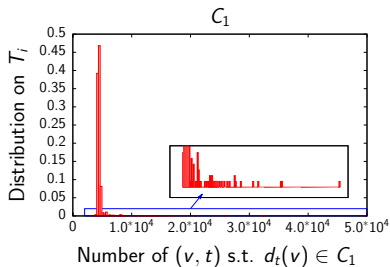
Temporal  
Homogeneity

Detection

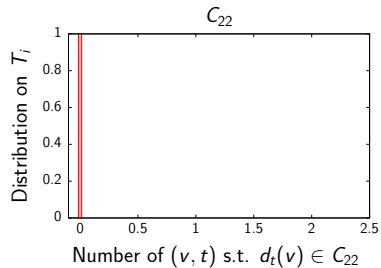
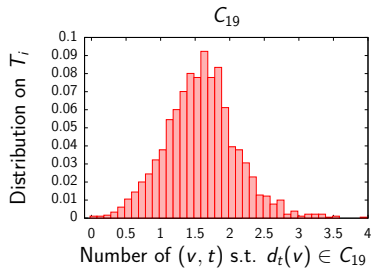
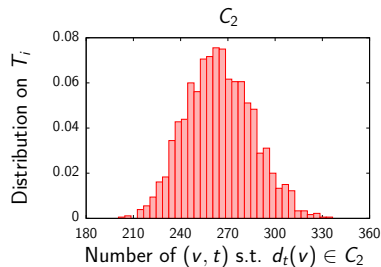
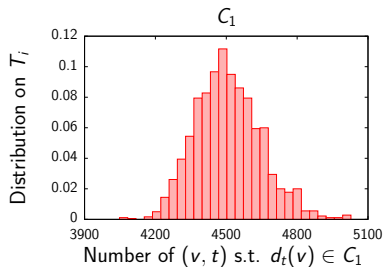
Identification &  
Removal

## Conclusion

# Distributions after removals



# Distributions after removals





## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

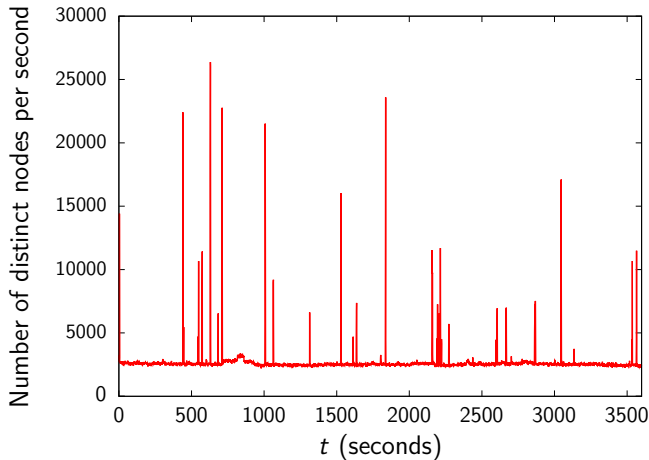
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v, T_i$ )

⇒ Consequence on the number of distinct nodes per second.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

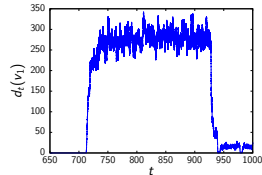
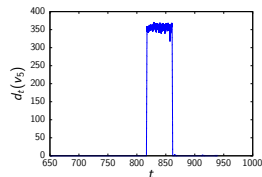
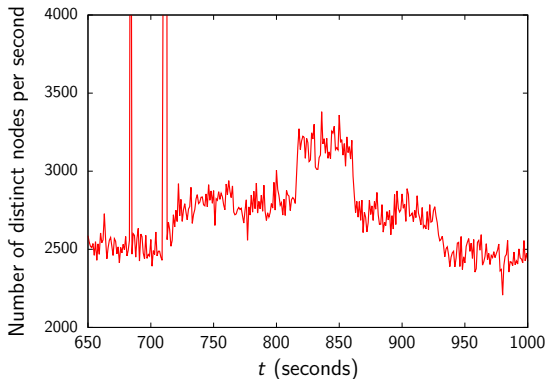
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v$ , $T_i$ )

⇒ Consequence on the number of distinct nodes per second.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

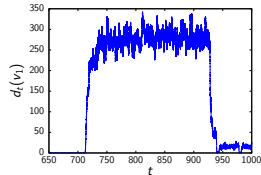
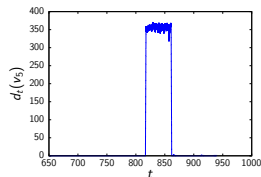
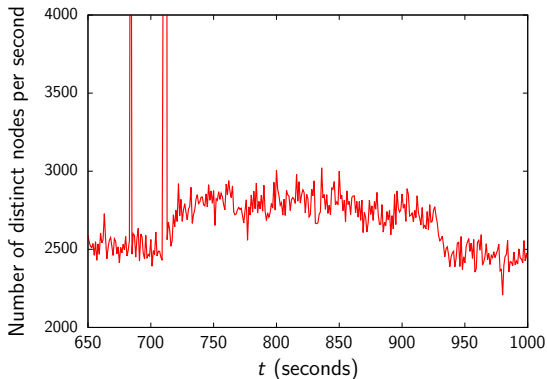
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v$ , $T_i$ )

⇒ Consequence on the number of distinct nodes per second.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

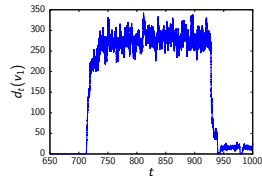
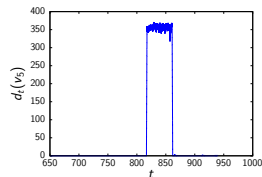
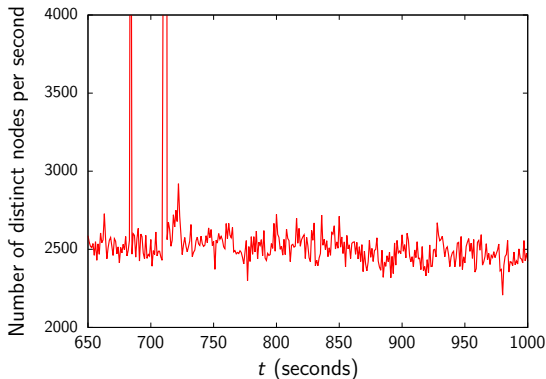
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v$ , $T_i$ )

⇒ Consequence on the number of distinct nodes per second.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal  
Homogeneity

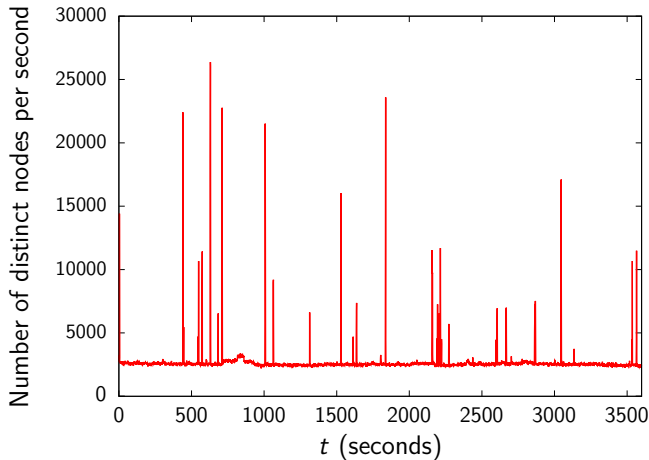
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v, T_i$ )

⇒ Consequence on the number of distinct nodes per second.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal

Homogeneity

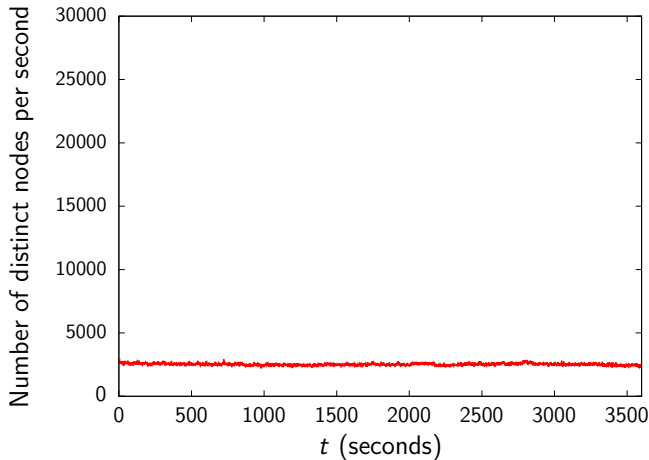
Detection

Identification &  
Removal

## Conclusion

# Removal of identified outliers ( $v, T_i$ )

⇒ Consequence on the number of distinct nodes per second.



Introduction

- Context and Goals
- Stream Graph
- Our Approach
- Instantaneous Degree
- Detect, Identify, Remove

In Practice

- Degree Heterogeneity
- Difficulties

Our Method

- Temporal Homogeneity
- Detection
- Identification & Removal

Conclusion

# Conclusion

# Conclusion

- **Contributions:**

- Modelling of IP traffic as a **stream graph**
  - Design of a method to **detect outliers** in **heterogeneous distributions**
    - IP with anomalous degree profile, network scans.
  - **Iterative removal** of identified outliers
    - Return to normal traffic (w.r.t  $d_t(v)$ ).
- ⇒ **Method applicable over temporal interactions in general.**

- **Several possible improvements:**

- Identification of couples  $(v, t)$  instead of couples  $(v, T_i)$ ,
- more complex feature: **clustering coefficient**,
- exploring other assumptions:
  - T. Schieber *et al.*, Q. Zhang *et al.*, 2017.



## Introduction

Context and Goals

Stream Graph

Our Approach

Instantaneous Degree

Detect, Identify,  
Remove

## In Practice

Degree Heterogeneity

Difficulties

## Our Method

Temporal  
Homogeneity

Detection

Identification &  
Removal

## Conclusion

# Thanks for your attention !