

## ODD SEMESTER EXAMINATION, 2024 – 25

**IIIrd Year (Vth Sem) B.Tech.: CS&E/ CS&E(Data Science)/AI&ML/IT**

**DESIGN & ANALYSIS OF ALGORITHMS**

**Duration: 3:00 hrs****Max Marks: 100**

**Note:** - Attempt all questions. All Questions carry equal marks. In case of any ambiguity or missing data, the same may be assumed and state the assumption made in the answer.

Q 1.	<p>Answer any two parts of the following. (10x2= 20)</p> <p>a) (i) Discuss in brief Asymptotic Analysis with best, average &amp; worst-case complexities. (5 marks)  (ii) Show that the worst-case running time of the quick-sort algorithm is <math>\Theta(n^2)</math>. (5 marks)</p> <p>b) What is heap? Explain. Illustrate the performance of the heap sort algorithm on the following input sequence: 2, 5, 16, 4, 10, 23, 39, 18, 26, 15 (10 marks)</p> <p>c) Using merge-sort algorithm to sort the following elements: 15,10,5,20,25,30,40,45. Also show that the running time of the merge-sort algorithm on the n-element sequence is <math>\Theta(n\log n)</math>. (10 marks)</p>
Q 2.	<p>Answer any two parts of the following. (10x2= 20)</p> <p>a) (i) What is activity selection problem? Write a greedy approach to solve Activity Selection problem. (5 marks)  (ii) What is difference between dynamic and greedy approach? Explain knapsack problem. (5 marks)</p> <p>b) What is the sum of subsets problem? Let <math>w=\{5,7,10,12,15,18,20\}</math> and <math>m=35</math>. Find all possible subsets of <math>w</math> that sum to <math>m</math> using recursive backtracking algorithm for it. Draw the portion of the state-space tree that is generated. (10 marks)</p> <p>c) What is dynamic programming? Find the order of parenthesization for the optimal chain multiplication of the following matrices:  <math>A_1 = 15 \times 5 \quad A_2 = 5 \times 10 \quad A_3 = 10 \times 20 \quad A_4 = 20 \times 25</math> (10 marks)</p>
Q 3.	<p>Answer any two parts of the following. (10x2= 20)</p> <p>a) (i) What are single source shortest paths? Write down Dijkstra's algorithm for it. (5 marks)  (ii) What is Fibonacci Heap? Discuss the application of Fibonacci Heap. (5 marks)</p> <p>b) Write and explain the Kruskal algorithm to find the minimum spanning tree of a graph with suitable example. (10 marks)</p> <p>c) Write the properties of binomial tree. Draw a binomial heap whose keys are elements of <math>A = (7,2,4,17,1,11,6,8,15,10,20)</math>. (10 marks)</p>
Q 4.	<p>Answer any two parts of the following. (10x2= 20)</p> <p>a) (i) Explain Satisfiability problem. (5 marks)  (ii) Write and explain the Cooks theorem. (5 marks)</p> <p>b) What is non-deterministic algorithm. Prove that the Travelling Salesman Problem is NP-Complete. (10 marks)</p> <p>c) Discuss in detail about the class P, NP, NP-hard and NP-complete problems. Show the</p>

	relationship between them.	(10 marks)
Q 5.	<p>Answer any two parts of the following.</p> <p>a) (i) Explore set cover problem using approximation algorithm. (5 marks)</p> <p>(ii) What are Distributed Hash Tables? Explain the characteristics of Distributed Hash Tables. (5 marks)</p> <p>b) Define approximation algorithms. What is approximation ratio? Approximate the travelling salesman problem with triangle inequality. (10 marks)</p> <p>c) What is randomized algorithm? Write advantage and disadvantage of randomized algorithm. Also explain the types of randomized algorithm. (10 marks)</p>	

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