CMPE 138

Homework 2

Problem 1: Disk Characteristics

(a) What is the total capacity of a track and what is its useful capacity (excluding interblock gaps)?

A track has 20 blocks. Each block has 512 bytes and an interblock gap of 128 bytes.

Total track capacity = (Block size + Gap size) × Blocks per track

 $= (512 + 128) \times 20 = 12,800 \text{ bytes } (12.8 \text{ KB})$

Useful track capacity = Block size × Blocks per track

 $= 512 \times 20 = 10,240 \text{ bytes } (10 \text{ KB})$

(b) How many cylinders are there?

A cylinder consists of all tracks at the same position on every disk surface.

There are 400 tracks per surface and 15 double-sided disks, meaning 30 surfaces.

Total cylinders = 400 (since a cylinder spans all surfaces but counts only per-track positioning). = 400 cylinders

(c) What is the total capacity and the useful capacity of a cylinder?

Total cylinder capacity = Total track capacity × Number of surfaces

 $= 12,800 \times 30 = 384,000$ bytes (384 KB)

Useful cylinder capacity = Useful track capacity × Number of surfaces

 $= 10,240 \times 30 = 307,200 \text{ bytes } (307.2 \text{ KB})$

(d) What is the total capacity and the useful capacity of a disk pack?

Total disk pack capacity = Total cylinder capacity × Number of cylinders

 $= 384,000 \times 400 = 153,600,000$ bytes (153.6 MB)

Useful disk pack capacity = Useful cylinder capacity × Number of cylinders

 $= 307,200 \times 400 = 122,880,000$ bytes (122.88 MB)

(e) Disk speed: Transfer rate, block transfer time, and average rotational delay

Revolutions per minute (RPM) = 2400

Revolutions per second = 2400 / 60 = 40

Time for one revolution = 1/40 = 25 ms

Block transfer time (BTT) = Time per track / Number of blocks per track

= 25 / 20 = 1.25 ms per block

Transfer rate = Total useful track capacity / Time per track

= 10,240 bytes / 25 ms = 409.6 bytes/ms Average rotational delay (RD) = ½ of one full revolution = 12.5 ms Bulk transfer rate = Total track capacity / Time per track = 12,800 / 25 = 512 bytes/ms

- (f) Average time to locate and transfer a block Seek time = 30 ms Rotational delay = 12.5 ms Block transfer time = 1.25 ms Total average time = Seek time + Rotational delay + BTT = 30 + 12.5 + 1.25 = 43.75 ms
- (g) Time to transfer 20 random blocks vs. 20 consecutive blocks using double buffering For random blocks: Each block requires a seek, rotational delay, and transfer time = $20 \times 43.75 = 875$ ms
 For consecutive blocks with double buffering:
 First block takes 43.75 ms
 Next 19 blocks only take block transfer time = $43.75 + (19 \times 1.25) = 67.5$ ms

Problem 2: B+ Tree Index

(a) How many pages can we store in the first (root) level? Second level? Tenth level? Fan-out (f) = 30

Root level (L1) = 1 pages Second level (L2) = 30^2 = 30 pages Tenth level (L10) = 30^9 pages

(b) Levels required and space usage per level

Number of rows = 2 billion (2×10^9)

Number of level = log_f(N) = log_30(2billion) = 6.29 (round up to 7) (where f is fan-out, N is number of rows) => so we will have 7 levels

Now we need to calculate number of space required:

- Number of leaf page = $2*10^9/30 = 66.7$ million

Level	Approx Pages (rounded up)	Calculation
L1 (Leaf)	66,667,000	2,000,000,000 /
L2	2,222,234	66,667,000 / 30
L3	74,075	2,222,234 / 30
L4	2,470	74,075 / 30
L5	83	2,470 / 30
L6	3	83 / 30
L7 (Root)	1	3/30

- Then we can calculate Space Required per Level = Number_of_Page *4 / 30

Level	Pages	Space (MB)	Rounded
L1	66,667,000	(66,667,000 × 4) / 1024 = 260,582.0	260,582.0 MB
L2	2,222,234	8,679.80	8,679.8 MB
L3	74,075	289.3	289.3 MB
L4	2,470	9.6	9.6 MB
L5	83	0.3	0.3 MB
L6	3	0.01	0.01 MB
L7	1	0.004	0.01 MB

(c) Worst-case IO (disk accesses) to find a record

Disk accesses per level = 1 Total levels = 7 Worst-case IO = 7 disk accesses

Problem 3: Join Costs

a)
$$IO = P(R)+T(R)*P(S)+P(R,S) = 20+1,600*200 +100 = 320,120$$

b)
$$IO = P(S) + T(S)*P(R)+P(R,S) = 200+15,000*20 +100 = 300,300$$

c)
$$IO(R,S) = P(R)+P(R)*P(S)/B+P(R,S) = 20+20*200/32+100=245$$

 $IO(RS,T) = P(R,S) + P(R,S)*P(T)/B + P(R,S,T) = 100+100*2000/32+500 = 6850$
 $IO(S,T) = P(S)+P(S)*P(T)/B+P(S,T) = 200+200*2000/32+1000 = 13600$
 $IO(ST,R) = P(S,T) + P(S,T)*P(R)/B+P(S,T,R) = 1000+1000*20/32+500 = 2125$

d)
$$IO(R,S) = \sim Sort(P(R)) + Sort(P(S)) + P(R) + P(S) = 40 + 800 + 20 + 200 = 1060$$

 $IO(RS,T) = \sim Sort(P(R,S)) + Sort(P(T)) + P(R,S) + P(T) = 400 + 8000 + 100 + 2000 = 10500$

e)
$$IO(S,T) = \sim Sort(P(S)) + Sort(P(T)) + P(S) + P(T) = 800 + 8000 + 200 + 2000 = 11000$$
 $IO(ST,R) = \sim Sort(P(S,T)) + Sort(P(R)) + P(S,T) + P(R) = 4000 + 40 + 1000 + 20 = 5060$

f)
$$IO(R,S) = \sim Sort(P(R)) + Sort(P(S)) + P(R) + P(S) = 40 + 800 + 20 + 200 = 1060$$

g)
$$IO(R,S) = 2 * (P(R) + P(S)) + (P(R) + P(S)) = 2 * (20 + 200) + (20 + 200) = 660$$

$$IO(RS,T) = 2 * (P(R,S) + P(T)) + (P(R,S) + P(T)) = 2 * (100 + 2000) + (100 + 2000) = 6300$$

h)
$$IO(S,T) = 2 * (P(S) + P(T)) + (P(S) + P(T)) = 2 * (200 + 2000) + (20 + 2000) = 6420$$

$$IO(ST,R) = 2 * (P(S,T) + P(R)) + (P(S,T) + P(R)) = 2 * (1000 + 20) + (1000 + 20) = 3060$$

Problem 4: Linear Hashing

(a) Buckets in primary area
Load factor = 0.7
Total records = 112,000
Records per bucket = 20
Buckets needed = 112,000 / (20 × 0.7) = 8000 buckets

(b) Number of bits for bucket addresses Buckets = 8000 Bits required = $\log_2(8000) \approx 13$ bits