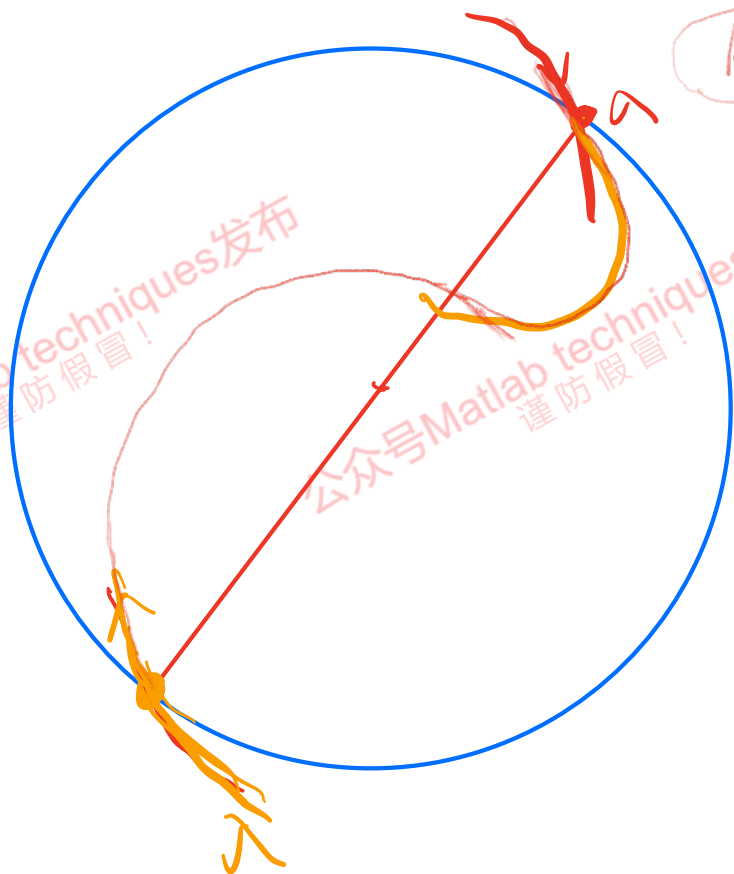
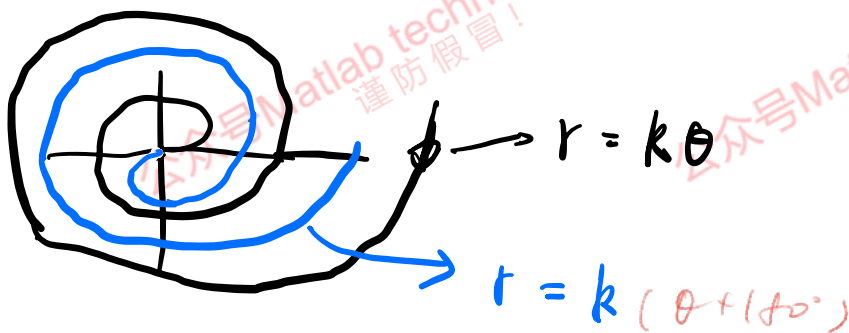


中心对称.



$k(\theta + 2\pi)$

$k(\theta + 2\pi)$

$k(\theta + 2\pi) = k\theta + 2\pi k$

$k\theta - r = 2\pi k$

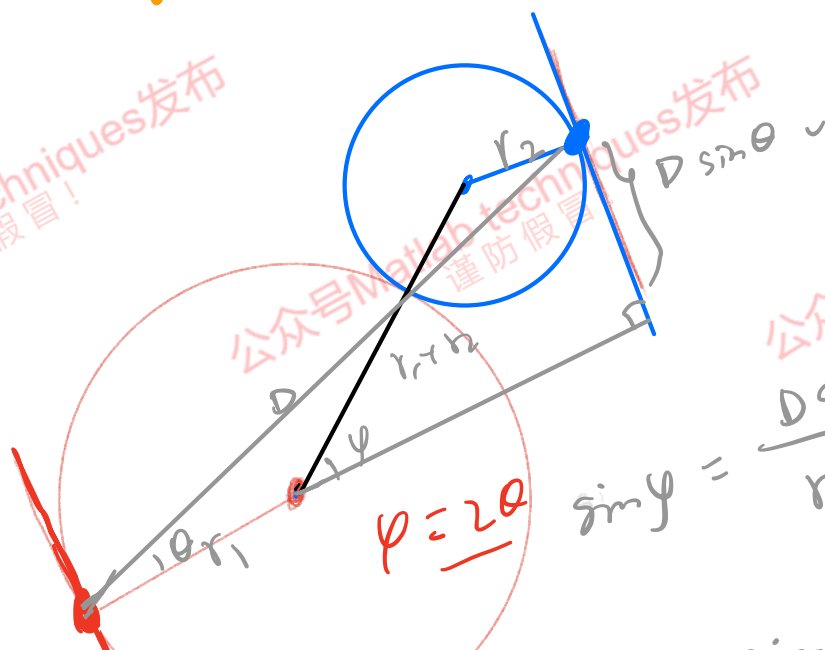
$r = k\theta$

$x = r \cos \theta$

$y = r \sin \theta$

$\frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{r' \sin \theta + r \cos \theta}{r' \cos \theta - r \sin \theta}$

$\lambda = \frac{r'}{r}$



$\sin \phi = \frac{D \sin \theta}{r_1 + r_2}$

$\frac{D \sin \theta}{r_1 + r_2}$

$\lambda = \frac{r'}{r}$

$$y \neq \arcsin \frac{r_1 + r_2}{D}$$

$$r_1 + r_2 + (r_1 + r_2) \cos \varphi = D \cos \theta$$

$$S = \frac{r_1 (\pi - \varphi) + r_2 (\pi - \varphi)}{2} = (r_1 + r_2) \pi - (r_1 + r_2) \varphi$$

$$r + r \cos \varphi = D \cos \theta$$

$$r \sin \varphi = D \sin \theta$$

$$(r_1 + r_2) \pi - (r_1 + r_2) \arccos \frac{D \cos \theta}{r_1 + r_2}$$

$$D^2 = (D \cos \theta - r)^2 + D^2 \sin^2 \theta$$

$$t \pi - t \arccos \frac{D \sin \theta}{t}$$

$$\Rightarrow D^2 + t^2 - 2tD \cos \theta$$

$$S =$$

$$t \pi - t \arccos \frac{D \sin \theta}{t}$$

$$t \cos \theta = \frac{D}{2}$$

代数法, 几何法

$$t \cos \theta = \frac{D}{2}$$

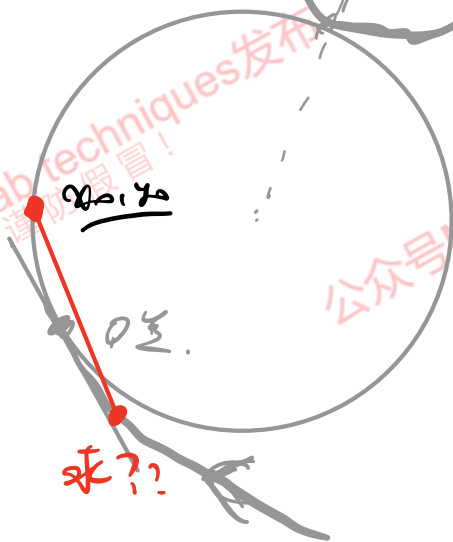
$$t \sim \frac{D}{2 \cos \theta}$$

$$r_1 + r_2 = 3r_2$$

$$r_1 = 2r_2$$

下面讨论运动



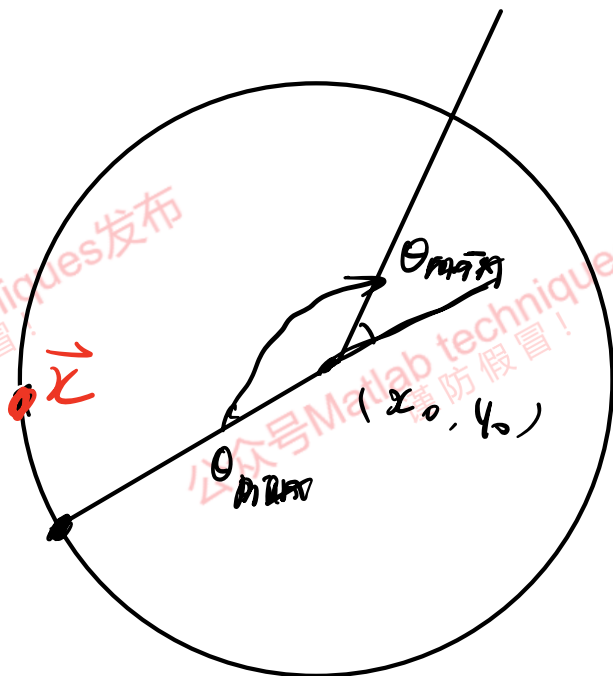


① 你看后把子, 依书去写吧

所以会错!!

~~求?~~

$$(k_0 \cos \theta - x_0)^2 + (k_0 \sin \theta - y_0)^2 = r^2$$



①

$$x = r_1 \cos \theta + x_0$$

$$y = r_1 \sin \theta + y_0$$

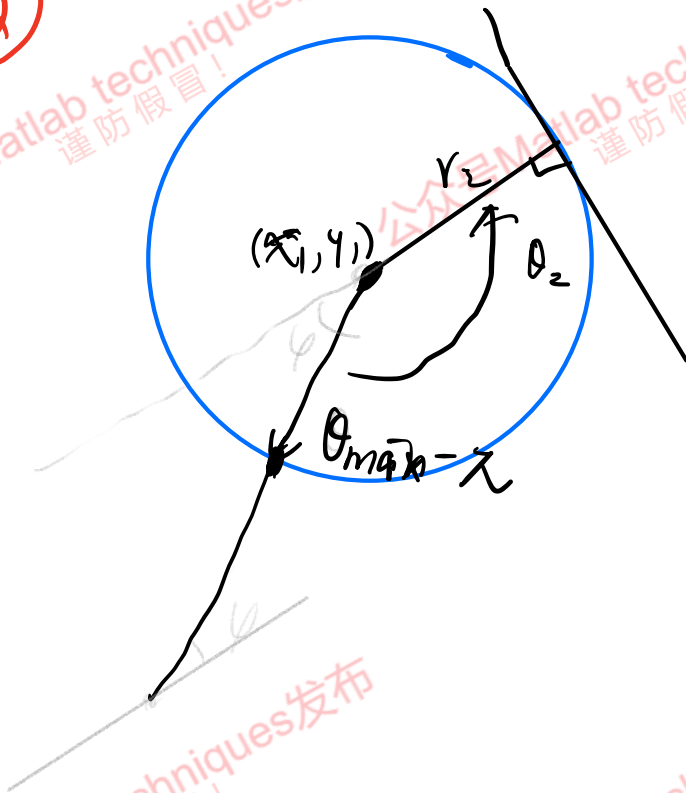
$$ds = \sqrt{x'^2 + y'^2} d\theta$$

$$\frac{ds}{d\theta} = r \Rightarrow r^2 \sin^2 \theta + r^2 \cos^2 \theta = r^2 \Rightarrow \frac{ds}{d\theta} = r$$

$$\theta = \frac{1}{r} + k \quad \downarrow \quad \theta_{\min} \sim \theta_{\max}$$

$$\frac{d\theta}{dr} = -\frac{r}{r^2}$$

②



$$\theta = \frac{t}{r_2} + c$$

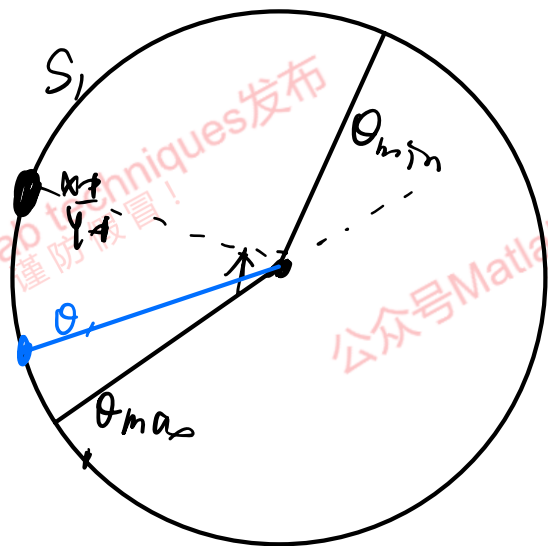
$$\theta(0) \sim \theta_{\max} - \alpha$$

$$\theta \sim \frac{t}{r_2} + \theta_{\max} - \alpha$$

分四段

①  $\theta - \alpha \sim 0$  s. 在  $\alpha$  直接到  $v$ .

②  $0 \leq t \leq S_1 \sim t, S_1 \sim r_1 \cdot \Delta \theta$

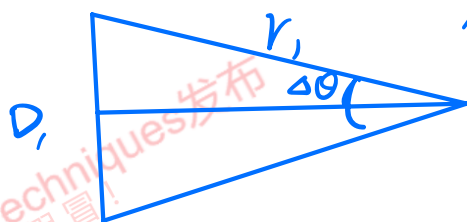


先求  $x_1, y_1$  和  $\alpha_1$  (x, y) 角度.

$$\theta_{max} - \Delta \theta = \theta_{max} - \frac{S_1}{r_1}$$

求  $\theta_1$  使  $\theta_{max} - \frac{S_1}{r_1} \leq 0, \in \theta_{max}$

$$\frac{\Delta \theta}{2} = \arcsin \frac{\frac{D_1}{2}}{r_1} \sim \Delta \theta \checkmark$$

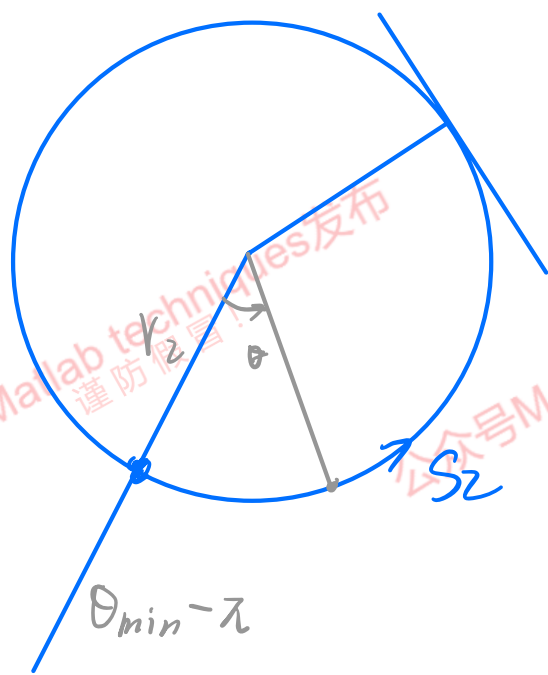


若  $\Delta \theta > \frac{S_1}{r_1}$ , 点在圆外

若  $\Delta \theta \leq \frac{S_1}{r_1}$ , 点在圆内

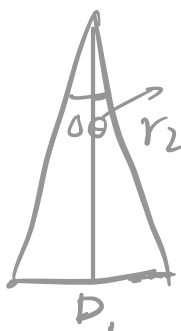
求下一个点. 可用一个子程序

①



$$S_1 < t \leq S_1 + S_2$$

$$\theta = \frac{t - S_1}{r_2} + \theta_{min} - \pi$$



$$\frac{\Delta \theta}{2} = \arcsin \frac{\frac{D_1}{2}}{r_2}$$

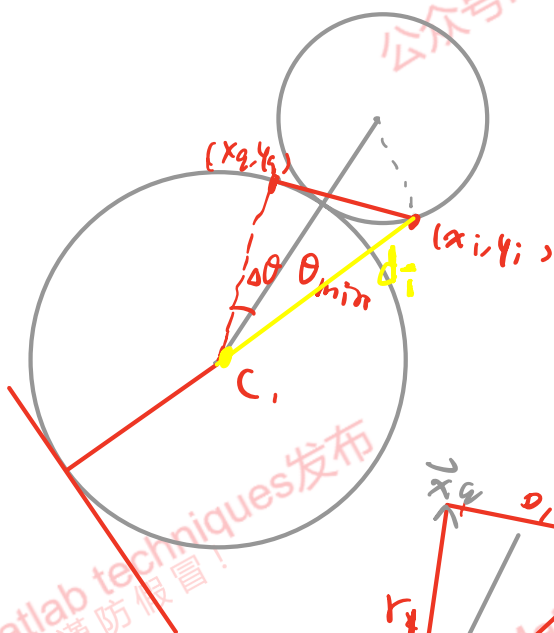
$$\Delta \theta = 2 \arcsin \frac{\frac{D_1}{2}}{r_2}$$

若  $\Delta\theta < \frac{t-s}{r_2}$  在圆2内

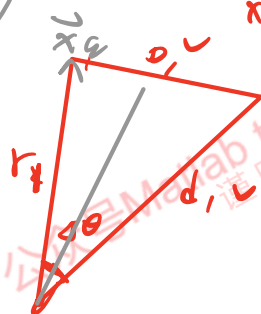
角为  $\theta_1, \theta_2$

$r_2 \cos(\theta_1), r_2 \sin(\theta_1)$

若  $\Delta\theta \geq \frac{t-s}{r_2}$  在圆1内



$(xg, yg)$  相对于  $C_1$  夹角  $\theta_{min} - \Delta\theta$



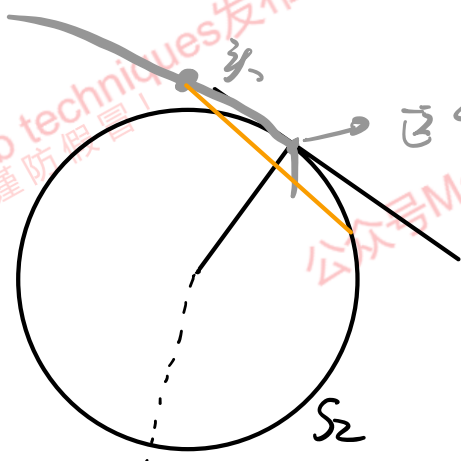
解三角形 求  $\Delta\theta$

求  $\Delta\theta$  到圆心角

它在圆  $C_1$  上

下一个圆  $C_1$  段判断

④  $t > s_1 + s_2$



这个角  $\theta$

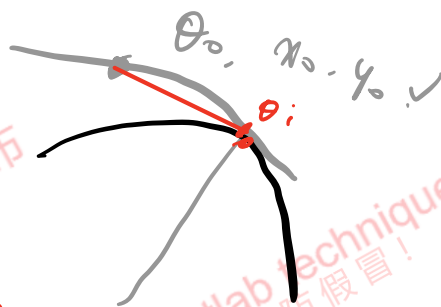
求  $r = k(\theta + \pi)$

$ds = \sqrt{r^2 + r'^2} d\theta$

$= \sqrt{k^2(\theta + \pi)^2 + k^2} d\theta$

$= k \sqrt{(\theta + \pi)^2 + 1} d\theta$

27 已知



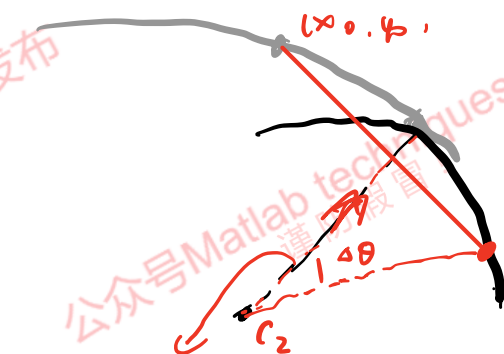
求  $\theta_1$  ( $\theta_1 < \theta_0$ )

在图 4.5.1 上

$$f(\theta_1) = 0, \text{ 求 } \theta_1$$

若  $\theta_1 > \theta_i \rightarrow$  在 4 线 1 上

若  $\theta_1 < \theta_i \rightarrow$  在  $C_2$  图上



$$\theta_2^m = \theta_{min} - \pi + \frac{S_2}{r_2} \text{ 角}$$

$$\theta_2^m = \theta \rightarrow r_2 \cos(\theta_2^m - \theta) = r_2 \sin \theta$$

$$\text{即: } f(\theta) = 0, \text{ 求 } \theta$$

只有 4 解! 4.5.1

而后, 用上一步迭代



直接代入

$$\frac{\sqrt{\Delta x^2 + \Delta y^2}}{\Delta t}$$

求速度!