# toulbar2

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Fri Apr 8 2016 18:42:33

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## 1 Main Page

Weighted CSP Solver Copyright	toulbar2 INRA
	<pre>https://mulcyber.toulouse.inra fr/projects/toulbar2/</pre>

See the README for more details.

toulbar2 can be used as a stand-alone solver reading various problem file formats (wcsp, uai, wcnf, qpbo) or as a C++ library.

This document describes the wcsp native file format and the toulbar2 C++ library API.

Note

Use cmake flag LIBTB2 to get the toulbar2 C++ library libtb2.so

## 2 toulbar2

An exact solver for cost function networks

#### What is toulbar2?

toulbar2 is an open-source C++ solver for cost function networks. It solves various combinatorial optimization problems. The constraints and objective function are factorized in local functions on discrete variables. Each function returns a cost (a finite positive integer) for any assignment of its variables. Constraints are represented as functions with costs in {0,k} where k is a large integer representing forbidden assignments. toulbar2 looks for a non-forbidden assignment of all variables that minimizes the sum of all functions.

toulbar2 won several competitions on deterministic and probabilistic graphical models:

- Max-CSP 2008 Competition CPAIO8 (winner on 2-ARY-EXT and N-ARY-EXT)
- Probabilistic Inference Evaluation UAI 2008 (winner on several MPE tasks, inra entries)
- 2010 UAI APPROXIMATE INFERENCE CHALLENGE UAI 2010 (winner on 1200-second MPE task)
- The Probabilistic Inference Challenge PIC 2011 (second place by ficolofo on 1-hour MAP task)
- UAI 2014 Inference Competition UAI 2014 (winner on all MAP task categories, see Proteus, Robin, and IncTb entries)

#### Download

```
http://mulcyber.toulouse.inra.fr/projects/toulbar2/
```

Latest src/debian/windows x86\_64 releases:

- 2016: src0\_9\_8/deb0\_9\_8/win0\_9\_8 with hybrid best-first search and more soft global cost functions
- 2015: src0\_9\_7/deb0\_9\_7/win0\_9\_7 with local search INCOP solver after preprocessing
- 2014: src0\_9\_6/deb0\_9\_6/win0\_9\_6 with extra variable ordering heuristics and dominance pruning rules
- 2012: src0\_9\_5/deb0\_9\_5/win0\_9\_5 with soft global decomposable cost functions
- 2011: src0\_9\_4/deb0\_9\_4/win0\_9\_4 with more preprocessing techniques
- 2010: src0\_9\_3/deb0\_9\_3/win0\_9\_3 with soft global cost functions

### Installation

Library needed:

- · libgmp-dev
- · libboost-dev
- · libboost-graph-dev

#### Optional libraries

· libxml2-dev

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#### **Authors**

toulbar2 was originally developped by Toulouse (INRA MIAT) and Barcelona (UPC, IIIA-CSIC) teams, hence the name of the solver.

Additional contributions by:

- · The Chinese University of Hong Kong and Caen University, France (GREYC) for global cost functions
- · Marseille University, France (LSIS) for tree decomposition heuristics
- Ecole des Ponts ParisTech, France (CERMICS/LIGM) for INCOP local search solver
- University College Cork, Ireland (Insight) for a Python interface in NumberJack and a portfolio dedicated to UAI graphical models Proteus
- · Artois University, France (CRIL) for an XCSP 2.1 format reader of CSP and WCSP instances

#### Citing

Please use one of the following references for citing toulbar2:

Multi-Language Evaluation of Exact Solvers in Graphical Model Discrete Optimization Barry Hurley, Barry O'Sullivan, David Allouche, George Katsirelos, Thomas Schiex, Matthias Zytnicki, Simon de Givry In Proc. of CP-AI-OR, Banff, Canada, 2016.

Soft arc consistency revisited M. Cooper, S. de Givry, M. Sanchez, T. Schiex, M. Zytnicki, and T. Werner Artificial Intelligence, 174(7-8):449-478, 2010

What are the algorithms inside toulbar2?

- Soft arc consistencies (NC, AC, DAC, FDAC) In the quest of the best form of local consistency for Weighted CSP J. Larrosa & T. Schiex In Proc. of IJCAI-03. Acapulco, Mexico, 2003
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- Depth-first Branch and Bound exploiting a tree decomposition (BTD) Exploiting Tree Decomposition and Soft Local Consistency in Weighted CSP S. de Givry, T. Schiex, and G. Verfaillie In Proc. of AAAI-06, Boston, MA, 2006
- Virtual arc consistency (VAC) Virtual arc consistency for weighted csp M. Cooper, S. de Givry, M. Sanchez,
   T. Schiex, and M. Zytnicki In Proc. of AAAI-08, Chicago, IL, 2008
- Soft generalized arc consistencies (GAC, FDGAC) Towards Efficient Consistency Enforcement for Global Constraints in Weighted Constraint Satisfaction J. H. M. Lee and K. L. Leung In Proc. of IJCAI-09, Los Angeles, USA, 2010
- Russian doll search exploiting a tree decomposition (RDS-BTD) Russian doll search with tree decomposition
   M Sanchez, D Allouche, S de Givry, and T Schiex In Proc. of IJCAl'09, Pasadena (CA), USA, 2009
- Soft bounds are consistency (BAC) Bounds Are Consistency for Weighted CSPs M. Zytnicki, C. Gaspin, S. de Givry, and T. Schiex Journal of Artificial Intelligence Research, 35:593-621, 2009
- Counting solutions in satisfaction (#BTD, Approx\_::BTD) Exploiting problem structure for solution counting A.
  Favier, S. de Givry, and P. Jégou In Proc. of CP-09, Lisbon, Portugal, 2009
- Soft existential generalized arc consistency (EDGAC) A Stronger Consistency for Soft Global Constraints in Weighted Constraint Satisfaction J. H. M. Lee and K. L. Leung In Proc. of AAAI-10, Boston, MA, 2010
- Preprocessing techniques (combines variable elimination and cost function decomposition) Pairwise decomposition for combinatorial optimization in graphical models A Favier, S de Givry, A Legarra, and T Schiex In Proc. of IJCAI-11, Barcelona, Spain, 2011

Decomposable global cost functions (wregular, wamong, wsum) Decomposing global cost functions D Allouche, C Bessiere, P Boizumault, S de Givry, P Gutierrez, S Loudni, JP Métivier, and T Schiex In Proc. of AAAI-12, Toronto, Canada, 2012

- Pruning by dominance (DEE) Dead-End Elimination for Weighted CSP S de Givry, S Prestwich, and B O'Sullivan In Proc. of CP-13, pages 263-272, Uppsala, Sweden, 2013
- Hybrid best-first search exploiting a tree decomposition (HBFS) Anytime Hybrid Best-First Search with Tree Decomposition for Weighted CSP D Allouche, S de Givry, G Katsirelos, T Schiex, and M Zytnicki In Proc. of CP-15, Cork, Ireland, 2015

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### 3 Module Documentation

### 3.1 Weighted Constraint Satisfaction Problem file format (wcsp)

It is a text format composed of a list of numerical and string terms separated by spaces. Instead of using names for making reference to variables, variable indexes are employed. The same for domain values. All indexes start at zero.

Cost functions can be defined in intention (see below) or in extension, by their list of tuples. A default cost value is defined per function in order to reduce the size of the list. Only tuples with a different cost value should be given (not mandatory). All the cost values must be positive. The arity of a cost function in extension may be equal to zero. In this case, there is no tuples and the default cost value is added to the cost of any solution. This can be used to represent a global lower bound constant of the problem.

The wcsp file format is composed of three parts: a problem header, the list of variable domain sizes, and the list of cost functions.

· Header definition for a given problem:

```
<Problem name>
<Number of variables (N)>
<Maximum domain size>
<Number of cost functions>
<Initial global upper bound of the problem (UB)>
```

The goal is to find an assignment of all the variables with minimum total cost, strictly lower than UB. Tuples with a cost greater than or equal to UB are forbidden (hard constraint).

Definition of domain sizes

```
<Domain size of variable with index 0> \dots<Domain size of variable with index N - 1>
```

#### Note

domain values range from zero to  $\it size-1$  a negative domain size is interpreted as a variable with an interval domain in  $[0, -\it size-1]$ 

### Warning

variables with interval domains are restricted to arithmetic and disjunctive cost functions in intention (see below)

- · General definition of cost functions
  - Definition of a cost function in extension

```
<Arity of the cost function>
<Index of the first variable in the scope of the cost function>
...
<Index of the last variable in the scope of the cost function>
<Default cost value>
<Number of tuples with a cost different than the default cost>
```

#### followed by for every tuple with a cost different than the default cost:

```
<Index of the value assigned to the first variable in the scope>
...
<Index of the value assigned to the last variable in the scope>
<Cost of the tuple>
```

#### Note

Shared cost function: A cost function in extension can be shared by several cost functions with the same arity (and same domain sizes) but different scopes. In order to do that, the cost function to be shared must start by a negative scope size. Each shared cost function implicitly receives an occurrence number starting from 1 and incremented at each new shared definition. New cost functions in extension can reuse some previously defined shared cost functions in extension by using a negative number of tuples representing the occurrence number of the desired shared cost function. Note that default costs should be the same in the shared and new cost functions. Here is an example of 4 variables with domain size 4 and one AllDifferent hard constraint decomposed into 6 binary constraints.

- Shared CF used inside a small example in wcsp format:

 Definition of a cost function in intension by replacing the default cost value by -1 and by giving its keyword name and its K parameters

```
<Arity of the cost function>
<Index of the first variable in the scope of the cost function>
...
<Index of the last variable in the scope of the cost function>
-1
<keyword>
<parameterl>
...
<parameterK>
```

Possible keywords of cost functions defined in intension followed by their specific parameters:

- >= cst delta to express soft binary constraint  $x \ge y + cst$  with associated cost function  $max((y + cst x \le delta)?(y + cst x) : UB, 0)$
- > cst delta to express soft binary constraint x > y + cst with associated cost function  $max((y + cst + 1 x \le delta)?(y + cst + 1 x) : UB, 0)$
- <= cst delta to express soft binary constraint  $x \le y + cst$  with associated cost function  $max((x cst y \le delta)?(x cst y) : UB, 0)$
- < cst delta to express soft binary constraint x < y + cst with associated cost function  $max((x cst + 1 y \le delta)?(x cst + 1 y) : UB, 0)$
- = cst delta to express soft binary constraint x = y + cst with associated cost function  $(|y + cst x| \le delta)$ ?|y + cst x| : UB
- disj cstx csty penalty to express soft binary disjunctive constraint  $x \ge y + csty \lor y \ge x + cstx$  with associated cost function  $(x \ge y + csty \lor y \ge x + cstx)$ ?0: penalty

• sdisj cstx csty xinfty yinfty costx costy to express a special disjunctive constraint with three implicit hard constraints  $x \le xinfty$  and  $y \le yinfty$  and  $x < xinfty \land y < yinfty \Rightarrow (x \ge y + csty \lor y \ge x + cstx)$  and an additional cost function ((x = xinfty)?costx: 0) + ((y = yinfty)?costy: 0)

- Global cost functions using a flow-based propagator:
  - salldiff var|dec|decbi cost to express a soft alldifferent constraint with either variable-based (var keyword) or decomposition-based (dec and decbi keywords) cost semantic with a given cost per violation (decbi decomposes into a binary cost function complete network)
  - sgcc var|dec|wdec cost nb\_values (value lower\_bound upper\_bound (shortage\_weight excess\_weight)?)\* to express a soft global cardinality constraint with either variable-based (var keyword) or decomposition-based (dec keyword) cost semantic with a given cost per violation and for each value its lower and upper bound (if wdec then violation cost depends on each value shortage or excess weights)
  - ssame cost list\_size1 list\_size2 (variable\_index)\* (variable\_index)\* to express a permutation constraint
    on two lists of variables of equal size (implicit variable-based cost semantic)
  - sregular var|edit cost nb\_states nb\_initial\_states (state)\* nb\_final\_states (state)\* nb\_transitions (start\_state symbol\_value end\_state)\* to express a soft regular constraint with either variable-based (var keyword) or edit distance-based (edit keyword) cost semantic with a given cost per violation followed by the definition of a deterministic finite automaton with number of states, list of initial and final states, and list of state transitions where symbols are domain values
- Global cost functions using a dynamic programming DAG-based propagator:
  - sregulardp var cost nb\_states nb\_initial\_states (state)\* nb\_final\_states (state)\* nb\_transitions (start\_state symbol\_value end\_state)\* to express a soft regular constraint with a variable-based (var keyword) cost semantic with a given cost per violation followed by the definition of a deterministic finite automaton with number of states, list of initial and final states, and list of state transitions where symbols are domain values
  - sgrammar|sgrammardp var|weight cost nb\_symbols nb\_values start\_symbol nb\_rules ((0 terminal\_symbol value)|(1 nonterminal\_in nonterminal\_out\_left nonterminal\_out\_right)|(2 terminal\_symbol value weight)|(3 nonterminal\_in nonterminal\_out\_left nonterminal\_out\_right weight))\* to express a soft/weighted grammar in Chomsky normal form
  - samong|samongdp var cost lower\_bound upper\_bound nb\_values (value)\* to express a soft among constraint to restrict the number of variables taking their value into a given set of values
  - salldiffdp var cost to express a soft alldifferent constraint with variable-based (var keyword) cost semantic
    with a given cost per violation (decomposes into samongdp cost functions)
  - sgccdp var cost nb\_values (value lower\_bound upper\_bound)\* to express a soft global cardinality constraint with variable-based (var keyword) cost semantic with a given cost per violation and for each value its lower and upper bound (decomposes into samongdp cost functions)
  - max|smaxdp defCost nbtuples (variable value cost)\* to express a weighted max cost function to find the
    maximum cost over a set of unary cost functions associated to a set of variables (by default, defCost if
    unspecified)
  - MST|smstdp hard to express a spanning tree hard constraint where each variable is assigned to its
    parent variable index in order to build a spanning tree (the root being assigned to itself)
- Global cost functions using a cost function network-based propagator:
  - wregular nb\_states nb\_initial\_states (state and cost)\* nb\_final\_states (state and cost)\* nb\_transitions (start\_state symbol\_value end\_state cost)\* to express a weighted regular constraint with weights on initial states, final states, and transitions, followed by the definition of a deterministic finite automaton with number of states, list of initial and final states with their costs, and list of weighted state transitions where symbols are domain values
  - walldiff hard lin quad cost to express a soft all different constraint as a set of wamong hard constraint (hard keyword) or decomposition-based (lin and quad keywords) cost semantic with a given cost per violation
  - wgcc hard|lin|quad cost nb\_values (value lower\_bound upper\_bound)\* to express a soft global cardinality constraint as either a hard constraint (hard keyword) or with decomposition-based (lin and quad keyword) cost semantic with a given cost per violation and for each value its lower and upper bound

- wsame hard lin quad cost to express a permutation constraint on two lists of variables of equal size (implicitly concatenated in the scope) using implicit decomposition-based cost semantic
- wsamegcc hard lin | quad cost nb\_values (value lower\_bound upper\_bound)\* to express the combination
  of a soft global cardinality constraint and a permutation constraint
- wamong hard|lin|quad cost nb\_values (value)\* lower\_bound upper\_bound to express a soft among constraint to restrict the number of variables taking their value into a given set of values
- wvaramong hard cost nb\_values (value)\* to express a hard among constraint to restrict the number of variables taking their value into a given set of values to be equal to the last variable in the scope
- woverlap hard|lin|quad cost comparator righthandside overlaps between two sequences of variables X,
   Y (i.e. set the fact that Xi and Yi take the same value (not equal to zero))
- wsum hard lin quad cost comparator righthandside to express a soft sum constraint with unit coefficients to test if the sum of a set of variables matches with a given comparator and right-hand-side value
- wvarsum hard cost comparator to express a hard sum constraint to restrict the sum to be comparator to the value of the last variable in the scope

Let us note <> the comparator, K the right-hand-side value associated to the comparator, and Sum the result of the sum over the variables. For each comparator, the gap is defined according to the distance as follows:

```
* if <> is == : gap = abs(K - Sum)
* if <> is <= : gap = max(0,Sum - K)
* if <> is < : gap = max(0,Sum - K - 1)
* if <> is != : gap = 1 if Sum != K and gap = 0 otherwise
* if <> is > : gap = max(0,K - Sum + 1);
* if <> is >= : gap = max(0,K - Sum);
```

### Warning

The decomposition of wsum and wvarsum may use an exponential size (sum of domain sizes). list\_size1 and list\_size2 must be equal in ssame.

Cost functions defined in intention cannot be shared.

### Note

More about network-based global cost functions can be found here https://metivier.users.-greyc.fr/decomposable/

### Examples:

• quadratic cost function x0\*x1 in extension with variable domains  $\{0,1\}$  (equivalent to a soft clause  $\neg x0 \lor \neg x1$ ):

```
2 0 1 0 1 1 1 1
```

• simple arithmetic hard constraint x1 < x2:

```
2 1 2 -1 < 0 0
```

• hard temporal disjunction  $x1 > x2 + 2 \lor x2 > x1 + 1$ :

```
2 1 2 -1 disj 1 2 UB
```

soft alldifferent({x0,x1,x2,x3}):

```
4 0 1 2 3 -1 salldiff var 1
```

soft\_gcc({x1,x2,x3,x4}) with each value v from 1 to 4 only appearing at least v-1 and at most v+1 times:

```
4 1 2 3 4 -1 sgcc var 1 4 1 0 2 2 1 3 3 2 4 4 3 5
          • soft_same({x0,x1,x2,x3},{x4,x5,x6,x7}):
                8 0 1 2 3 4 5 6 7 -1 ssame 1 4 4 0 1 2 3 4 5 6 7
           • soft regular({x1,x2,x3,x4}) with DFA (3*)+(4*):
                4 1 2 3 4 -1 sregular var 1 2 1 0 2 0 1 3 0 3 0 0 4 1 1 4 1
           • soft_grammar({x0,x1,x2,x3}) with hard cost (1000) producing well-formed parenthesis expressions:
                4\ 0\ 1\ 2\ 3\ -1\ \text{sgrammardp var }1000\ 4\ 2\ 0\ 6\ 1\ 0\ 0\ 0\ 1\ 0\ 1\ 2\ 1\ 0\ 1\ 3\ 1\ 2\ 0\ 3\ 0\ 1\ 0\ 0\ 3\ 1
          \bullet \ \ \mathsf{soft\_among}(\{\mathsf{x1},\mathsf{x2},\!\mathsf{x3},\!\mathsf{x4}\}) \ \mathsf{with} \ \mathsf{hard} \ \mathsf{cost} \ (\mathsf{1000}) \ \mathsf{if} \ \Sigma_{i=1}^4(x_i \in \{1,2\}) < 1 \ \mathsf{or} \ \Sigma_{i=1}^4(x_i \in \{1,2\}) > 3 \\ : \ \ \mathsf{x_i} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} = \{1,2\} 
                4 1 2 3 4 -1 samongdp var 1000 1 3 2 1 2
          • soft max(\{x0,x1,x2,x3\}) with cost equal to \max_{i=0}^{3}((x_{i}!=i)?1000:(4-i)):
                4 0 1 2 3 -1 smaxdp 1000 4 0 0 4 1 1 3 2 2 2 3 3 1
           wregular({x0,x1,x2,x3}) with DFA (0(10)*2*):
                4 0 1 2 3 -1 wregular 3 1 0 0 1 2 0 9 0 0 1 0 0 1 1 1 0 2 1 1 1 0 0 1 0 0 1 1 2 0 1 1 2 2 0 1 0 2 1 1 1 2
           • wamong ({x1,x2,x3,x4}) with hard cost (1000) if \sum_{i=1}^4 (x_i \in \{1,2\}) < 1 or \sum_{i=1}^4 (x_i \in \{1,2\}) > 3:
                4 1 2 3 4 -1 wamong hard 1000 2 1 2 1 3
           • wvaramong ({x1,x2,x3,x4}) with hard cost (1000) if \sum_{i=1}^{3} (x_i \in \{1,2\}) \neq x_4:
                4 1 2 3 4 -1 wvaramong hard 1000 2 1 2
           • woverlap(\{x1,x2,x3,x4\}) with hard cost (1000) if \sum_{i=1}^{2} (x_i = x_{i+2}) \ge 1:
                4 1 2 3 4 -1 woverlap hard 1000 < 1
          • wsum ({x1,x2,x3,x4}) with hard cost (1000) if \sum_{i=1}^{4} (x_i) \neq 4:
                4\ 1\ 2\ 3\ 4\ -1\ \text{wsum hard}\ 1000\ ==\ 4
           • wvarsum (\{x1,x2,x3,x4\}) with hard cost (1000) if \sum_{i=1}^{3} (x_i) \neq x_4:
                4 1 2 3 4 -1 wvarsum hard 1000 ==
Latin Square 4 x 4 crisp CSP example in wcsp format:
latin4 16 4 8 1
4 4 5 6 7 -1 salldiff var 1
4 8 9 10 11 -1 salldiff var 1
4 12 13 14 15 -1 salldiff var 1
4 0 4 8 12 -1 salldiff var 1
4 1 5 9 13 -1 salldiff var 1
```

4-queens binary weighted CSP example with random unary costs in wcsp format:

4 2 6 10 14 -1 salldiff var 1 4 3 7 11 15 -1 salldiff var 1

#### 3.2 Variable and cost function modeling

Modeling a Weighted CSP consists in creating variables and cost functions.

Domains of variables can be of two different types:

- enumerated domain allowing direct access to each value (array) and iteration on current domain in times proportional to the current number of values (double-linked list)
- · interval domain represented by a lower value and an upper value only (useful for large domains)

#### Warning

Current implementation of toulbar2 has limited modeling and solving facilities for interval domains. There is no cost functions accepting both interval and enumerated variables for the moment, which means all the variables should have the same type.

Cost functions can be defined in extension (table or maps) or having a specific semantic.

Cost functions in extension depend on their arity:

- unary cost function (directly associated to an enumerated variable)
- binary and ternary cost functions (table of costs)
- n-ary cost functions (n >= 4) defined by a list of tuples with associated costs and a default cost for missing tuples (allows for a compact representation)

Cost functions having a specific semantic (see Weighted Constraint Satisfaction Problem file format (wcsp)) are:

- · simple arithmetic and scheduling (temporal disjunction) cost functions on interval variables
- global cost functions (*eg* soft alldifferent, soft global cardinality constraint, soft same, soft regular, etc) with three different propagator keywords:
  - flow propagator based on flow algorithms with "s" prefix in the keyword (salldiff, sgcc, ssame, sregular)
  - DAG propagator based on dynamic programming algorithms with "s" prefix and "dp" postfix (samongdp, salldiffdp, sgccdp, sregulardp, sgrammardp, smstdp, smaxdp)
  - network propagator based on cost function network decomposition with "w" prefix (wsum, wvarsum, walldiff, wgcc, wsame, wsamegcc, wregular, wamong, wvaramong, woverlap)

#### Note

The default semantics (using *var* keyword) of monolithic (flow and DAG-based propagators) global cost functions is to count the number of variables to change in order to restore consistency and to multiply it by the basecost. Other particular semantics may be used in conjunction with the flow-based propagator

The semantics of the network-based propagator approach is either a hard constraint ("hard" keyword) or a soft constraint by multiplying the number of changes by the basecost ("lin" or "var" keyword) or by multiplying the square value of the number of changes by the basecost ("quad" keyword)

A decomposable version exists for each monolithic global cost function, except grammar and MST. The decomposable ones may propagate less than their monolithic counterpart and they introduce extra variables but they can be much faster in practice

### Warning

Each global cost function may have less than three propagators implemented

Current implementation of toulbar2 has limited solving facilities for monolithic global cost functions (no BTD-like methods nor variable elimination)

Current implementation of toulbar2 disallows global cost functions with less than or equal to three variables in their scope (use cost functions in extension instead)

Before modeling the problem using make and post, call ::tb2init method to initialize toulbar2 global variables After modeling the problem using make and post, call WeightedCSP::sortConstraints method to initialize correctly the model before solving it

#### 3.3 Solving cost function networks

After creating a Weighted CSP, it can be solved using a local search method INCOP (see WeightedCSPSolver-::narycsp) and/or an exact B&B search method (see WeightedCSPSolver::solve).

Various options of the solving methods are controlled by ::Toulbar2 static class members (see files src/tb2types.hpp and src/tb2main.cpp).

A brief code example reading a wcsp problem given as a single command-line parameter and solving it:

```
#include "toulbar2lib.hpp"
#include <string.h>
#include <stdio.h>
 #include <stdlib.h>
#include <unistd.h>
int main(int argc, char **argv) {
           tb2init(); // must be call before setting specific ToulBar2 options and creating a model
            // Create a solver object
           WeightedCSPSolver *solver =
                WeightedCSPSolver::makeWeightedCSPSolver(MAX_COST);
           // Read a problem file in wcsp format
           solver->read_wcsp(argv[1]);
           ToulBar2::verbose = -1; // change to 0 or higher values to see more trace information
           // \ {\tt Uncomment if solved using INCOP local search followed by a partial Limited Discrepancy Search with a partial content of the content
                   maximum discrepancy of one
           // ToulBar2::incop_cmd = "0 1 3 idwa 100000 cv v 0 200 1 0 0";
// ToulBar2::lds = -1; // remove it or change to a positive value then the search continues by a
                   complete B&B search method
           if (solver->solve()) {
                       // show (sub-)optimal solution
                      vector<Value> sol;
                      Cost ub = solver->getSolution(sol);
                      cout << "Best solution found cost: " << ub << endl;</pre>
                      cout << "Best solution found:";</pre>
                      for (unsigned int i=0; i<sol.size(); i++) cout << ((i>0)?",":"") << " x" << i << " = " << sol[i];
                      cout << endl;
           } else {
                      cout << "No solution found!" << endl;</pre>
           delete solver;
```

### See Also

}

another code example in src/toulbar2test.cpp

#### Warning

variable domains must start at zero, otherwise recompile libtb2.so without flag WCSPFORMATONLY

### 3.4 Output messages, verbosity options and debugging

Depending on verbosity level given as option "-v=level", toulbar2 will output:

(level=0, no verbosity) default output mode: shows version number, number of variables and cost functions
read in the problem file, number of unassigned variables and cost functions after preprocessing, problem
upper and lower bounds after preprocessing. Outputs current best solution cost found, ends by giving the
optimum or "No solution". Last output line should always be: "end."

- (level=-1, no verbosity) restricted output mode: do not print current best solution cost found
- 1. (level=1) shows also search choices ("["search\_depth problem\_lower\_bound problem\_upper\_bound sum\_of\_current\_domain\_sizes"] Try" variable\_index operator value) with operator being assignment ("=="), value removal ("!="), domain splitting ("<=" or ">=", also showing EAC value in parenthesis)
- (level=2) shows also current domains (variable\_index list\_of\_current\_domain\_values "/" number\_of\_cost-\_functions (see approximate degree in Variable elimination) "/" weighted\_degree list\_of\_unary\_costs "s:" support\_value) before each search choice and reports problem lower bound increases, NC bucket sort data (see NC bucket sort), and basic operations on domains of variables
- 3. (level=3) reports also basic arc EPT operations on cost functions (see Soft arc consistency and problem reformulation)
- 4. (level=4) shows also current list of cost functions for each variable and reports more details on arc EPT operations (showing all changes in cost functions)
- 5. (level=5) reports more details on cost functions defined in extension giving their content (cost table by first increasing values in the current domain of the last variable in the scope)

For debugging purposes, another option "-Z=level" allows to monitor the search:

- 1. (level 1) shows current search depth (number of search choices from the root of the search tree) and reports statistics on nogoods for BTD-like methods
- 2. (level 2) idem
- 3. (level 3) also saves current problem into a file before each search choice

#### Note

toulbar2, compiled in debug mode, can be more verbose and it checks a lot of assertions (pre/post conditions in the code)

 $\verb|toulbar2| \textbf{ will output an help message giving available options if run without any parameters}|$ 

### 3.5 Preprocessing techniques

Depending on toulbar2 options, the sequence of preprocessing techniques applied before the search is:

- 1. i-bounded variable elimination with user-defined i bound
- 2. pairwise decomposition of cost functions (binary cost functions are implicitly decomposed by soft AC and empty cost function removals)
- 3. MinSumDiffusion propagation (see VAC)
- 4. projects&substracts n-ary cost functions in extension on all the binary cost functions inside their scope (3 < n < max, see toulbar2 options)
- 5. functional variable elimination (see Variable elimination)
- 6. projects&substracts ternary cost functions in extension on their three binary cost functions inside their scope (before that, extends the existing binary cost functions to the ternary cost function and applies pairwise decomposition)
- 7. creates new ternary cost functions for all triangles (ie occurences of three binary cost functions xy, yz, zx)
- 8. removes empty cost functions while repeating #1 and #2 until no new cost functions can be removed

Note

the propagation loop is called after each preprocessing technique (see WCSP::propagate)

### 3.6 Variable and value search ordering heuristics

### See Also

Boosting Systematic Search by Weighting Constraints . Frederic Boussemart, Fred Hemery, Christophe Lecoutre, Lakhdar Sais. Proc. of ECAI 2004, pages 146-150. Valencia, Spain, 2004. Last Conflict Based Reasoning . Christophe Lecoutre, Lakhdar Sais, Sebastien Tabary, Vincent Vidal. Proc. of ECAI 2006, pages 133-137. Trentino, Italy, 2006.

### 3.7 Soft arc consistency and problem reformulation

Soft arc consistency is an incremental lower bound technique for optimization problems. Its goal is to move costs from high-order (typically arity two or three) cost functions towards the problem lower bound and unary cost functions. This is achieved by applying iteratively local equivalence-preserving problem transformations (EPTs) until some terminating conditions are met.

#### Note

eg an EPT can move costs between a binary cost function and a unary cost function such that the sum of the two functions remains the same for any complete assignment.

#### See Also

Arc consistency for Soft Constraints. T. Schiex. Proc. of CP'2000. Singapour, 2000.

#### Note

Soft Arc Consistency in toulbar2 is limited to binary and ternary and some global cost functions (*eg* alldifferent, gcc, regular, same). Other n-ary cost functions are delayed for propagation until their number of unassigned variables is three or less.

#### See Also

Towards Efficient Consistency Enforcement for Global Constraints in Weighted Constraint Satisfaction. Jimmy Ho-Man Lee, Ka Lun Leung. Proc. of IJCAI 2009, pages 559-565. Pasadena, USA, 2009.

### 3.8 Virtual Arc Consistency enforcing

The three phases of VAC are enforced in three different "Pass". Bool(P) is never built. Instead specific functions (getVACCost) booleanize the WCSP on the fly. The domain variables of Bool(P) are the original variable domains (saved and restored using trailing at each iteration) All the counter data-structures (k) are timestamped to avoid clearing them at each iteration.

Note

Simultaneously AC (and potentially DAC, EAC) are maintained by proper queuing.

See Also

Soft Arc Consistency Revisited. Cooper et al. Artificial Intelligence. 2010.

3.9 NC bucket sort

### 3.9 NC bucket sort

maintains a sorted list of variables having non-zero unary costs in order to make NC propagation incremental.

- · variables are sorted into buckets
- each bucket is associated to a single interval of non-zero costs (using a power-of-two scaling, first bucket interval is [1,2[, second interval is [2,4[, etc.)
- each variable is inserted into the bucket corresponding to its largest unary cost in its domain
- variables having all unary costs equal to zero do not belong to any bucket

NC propagation will revise only variables in the buckets associated to costs sufficiently large wrt current objective bounds.

#### 3.10 Variable elimination

• *i-bounded* variable elimination eliminates all variables with a degree less than or equal to *i*. It can be done with arbitrary i-bound in preprocessing only and iff all their cost functions are in extension.

- i-bounded variable elimination with i-bound less than or equal to two can be done during the search.
- functional variable elimination eliminates all variables which have a bijective or functional binary hard constraint (*ie* ensuring a one-to-one or several-to-one value mapping) and iff all their cost functions are in extension. It can be done without limit on their degree, in preprocessing only.

#### Note

Variable elimination order used in preprocessing is either lexicographic or given by an external file \*.order (see toulbar2 options)

2-bounded variable elimination during search is optimal in the sense that any elimination order should result in the same final graph

#### Warning

It is not possible to display/save solutions when bounded variable elimination is applied in preprocessing toulbar2 maintains a list of current cost functions for each variable. It uses the size of these lists as an approximation of variable degrees. During the search, if variable x has three cost functions xy, xz, xyz, its true degree is two but its approximate degree is three. In toulbar2 options, it is the approximate degree which is given by the user for variable elimination during the search (thus, a value at most three). But it is the true degree which is given by the user for variable elimination in preprocessing.

### 3.11 Propagation loop

Propagates soft local consistencies and bounded variable elimination until all the propagation queues are empty or a contradiction occurs.

While (queues are not empty or current objective bounds have changed):

- 1. queue for bounded variable elimination of degree at most two (except at preprocessing)
- 2. BAC queue
- 3. EAC queue
- 4. DAC queue
- 5. AC queue
- 6. monolithic (flow-based and DAG-based) global cost function propagation (partly incremental)
- 7. NC queue
- 8. returns to #1 until all the previous queues are empty
- 9. DEE queue
- 10. returns to #1 until all the previous queues are empty
- 11. VAC propagation (not incremental)
- 12. returns to #1 until all the previous queues are empty (and problem is VAC if enable)
- 13. exploits goods in pending separators for BTD-like methods

Queues are first-in / first-out lists of variables (avoiding multiple insertions). In case of a contradiction, queues are explicitly emptied by WCSP::whenContradiction

### 3.12 Backtrack management

Used by backtrack search methods. Allows to copy / restore the current state using Store::store and Store::restore methods. All storable data modifications are trailed into specific stacks.

Trailing stacks are associated to each storable type:

- Store::storeValue for storable domain values ::StoreValue (value supports, etc)
- Store::storeCost for storable costs ::StoreCost (inside cost functions, etc)
- Store::storeDomain for enumerated domains (to manage holes inside domains)
- Store::storeConstraint for backtrackable lists of constraints
- Store::storeVariable for backtrackable lists of variables
- Store::storeSeparator for backtrackable lists of separators (see tree decomposition methods)
- · Store::storeBigInteger for very large integers ::StoreBigInteger used in solution counting methods

Memory for each stack is dynamically allocated by part of  $2^x$  with x initialized to ::STORE\_SIZE and increased when needed.

#### Note

storable data are not trailed at depth 0.

### Warning

::StoreInt uses Store::storeValue stack (it assumes Value is encoded as int!).

Current storable data management is not multi-threading safe! (Store is a static virtual class relying on Store-Basic<T> static members)

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### 4 Class Documentation

### 4.1 WeightedCSP Class Reference

**Public Member Functions** 

• virtual int getIndex () const =0

instantiation occurrence number of current WCSP object

• virtual string getName () const =0

WCSP filename (without its extension)

• virtual void \* getSolver () const =0

special hook to access solver information

• virtual Cost getLb () const =0

gets problem lower bound

• virtual Cost getUb () const =0

gets problem upper bound

virtual void updateUb (Cost newUb)=0

sets initial problem upper bound and each time a new solution is found

virtual void enforceUb ()=0

enforces problem upper bound when exploring an alternative search node

virtual void increaseLb (Cost addLb)=0

increases problem lower bound thanks to eg soft local consistencies

• virtual Cost finiteUb () const =0

computes the worst-case assignment finite cost (sum of maximum finite cost over all cost functions plus one)

virtual void setInfiniteCost ()=0

updates infinite costs in all cost functions accordingly to the problem global lower and upper bounds

virtual bool enumerated (int varIndex) const =0

true if the variable has an enumerated domain

- virtual string getName (int varIndex) const =0
- virtual Value getInf (int varIndex) const =0

minimum current domain value

virtual Value getSup (int varIndex) const =0

maximum current domain value

• virtual Value getValue (int varIndex) const =0

current assigned value

virtual unsigned int getDomainSize (int varIndex) const =0

current domain size

• virtual bool getEnumDomain (int varIndex, Value \*array)=0

gets current domain values in an array

virtual bool getEnumDomainAndCost (int varIndex, ValueCost \*array)=0

gets current domain values and unary costs in an array

virtual unsigned int getDomainInitSize (int varIndex) const =0

gets initial domain size (warning! assumes EnumeratedVariable)

virtual Value toValue (int varIndex, unsigned int idx)=0

gets value from index (warning! assumes EnumeratedVariable)

• virtual unsigned int tolndex (int varIndex, Value value)=0

gets index from value (warning! assumes EnumeratedVariable)

virtual int getDACOrder (int varIndex) const =0

index of the variable in the DAC variable ordering

virtual Value nextValue (int varIndex, Value v) const =0

first value after v in the current domain or v if there is no value

virtual void increase (int varIndex, Value newInf)=0

changes domain lower bound

virtual void decrease (int varIndex, Value newSup)=0

changes domain upper bound

virtual void assign (int varIndex, Value newValue)=0

assigns a variable and immediately propagates this assignment

• virtual void remove (int varIndex, Value remValue)=0

removes a domain value (valid if done for an enumerated variable or on its domain bounds)

virtual void assignLS (vector< int > &varIndexes, vector< Value > &newValues)=0

assigns a set of variables at once and propagates (used by Local Search methods such as Large Neighborhood Search)

virtual Cost getUnaryCost (int varIndex, Value v) const =0

unary cost associated to a domain value

virtual Cost getMaxUnaryCost (int varIndex) const =0

maximum unary cost in the domain

virtual Value getMaxUnaryCostValue (int varIndex) const =0

a value having the maximum unary cost in the domain

virtual Value getSupport (int varIndex) const =0

NC/EAC unary support value.

virtual Value getBestValue (int varIndex) const =0

hint for some value ordering heuristics (only used by RDS)

virtual void setBestValue (int varIndex, Value v)=0

hint for some value ordering heuristics (only used by RDS)

virtual bool getIsPartOfOptimalSolution ()=0

special flag used for debugging purposes only

virtual void setIsPartOfOptimalSolution (bool v)=0

special flag used for debugging purposes only

virtual int getDegree (int varIndex) const =0

approximate degree of a variable (ie number of active cost functions, see Variable elimination)

• virtual int getTrueDegree (int varIndex) const =0

degree of a variable

virtual Long getWeightedDegree (int varIndex) const =0

weighted degree heuristic

• virtual void resetWeightedDegree (int varIndex)=0

initialize weighted degree heuristic

virtual void preprocessing ()=0

applies various preprocessing techniques to simplify the current problem

• virtual void sortConstraints ()=0

sorts the list of cost functions associated to each variable based on smallest problem variable indexes

virtual void whenContradiction ()=0

after a contradiction, resets propagation queues

• virtual void propagate ()=0

propagates until a fix point is reached (or throws a contradiction)

• virtual bool verify ()=0

checks the propagation fix point is reached

• virtual unsigned int numberOfVariables () const =0

number of created variables

virtual unsigned int numberOfUnassignedVariables () const =0

current number of unassigned variables

virtual unsigned int numberOfConstraints () const =0

initial number of cost functions (before variable elimination)

virtual unsigned int numberOfConnectedConstraints () const =0

current number of cost functions

virtual unsigned int numberOfConnectedBinaryConstraints () const =0

current number of binary cost functions

virtual unsigned int medianDomainSize () const =0

median current domain size of variables

virtual unsigned int medianDegree () const =0

median current degree of variables

virtual int getMaxDomainSize ()=0

maximum initial domain size found in all variables

virtual Value getDomainSizeSum ()=0

total sum of current domain sizes

virtual void cartProd (BigInteger &cartesianProduct)=0

Cartesian product of current domain sizes.

virtual Long getNbDEE () const =0

number of value removals due to dead-end elimination

• virtual int makeEnumeratedVariable (string n, Value iinf, Value isup)=0

create an enumerated variable with its domain bounds

• virtual int makeEnumeratedVariable (string n, Value \*d, int dsize)=0

create an enumerated variable with its domain values

• virtual int makeIntervalVariable (string n, Value iinf, Value isup)=0

create an interval variable with its domain bounds

- virtual void postUnary (int xIndex, vector < Cost > &costs)=0
- virtual void postNaryConstraintTuple (int ctrindex, Value \*tuple, int arity, Cost cost)=0
- virtual int postUnary (int xIndex, Value \*d, int dsize, Cost penalty)=0
- virtual int postGlobalConstraint (int \*scopeIndex, int arity, string &gcname, istream &file, int \*constrcounter=N-ULL)=0
- virtual int postWAmong (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, const vector< Value > &values, int lb, int ub)=0

post a soft among cost function

- virtual void postWAmong (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nb-Values, int lb, int ub)=0
- virtual void postWVarAmong (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int varIndex)=0

post a weighted among cost function with the number of values encoded as a variable with index varIndex (network-based propagator only)

virtual int postWRegular (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, int nbStates, const vector< WeightedObj< int > > &initial\_States, const vector< WeightedObj< int > > &accepting\_States, const vector< DFATransition > &Wtransitions)=0

post a soft or weighted regular cost function

- virtual void postWRegular (int \*scopeIndex, int arity, int nbStates, vector< pair< int, Cost >> initial\_States, vector< pair< int, Cost >> accepting\_States, int \*\*Wtransitions, vector< Cost > transitionsCosts)=0
- virtual int postWAllDiff (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost)=0

post a soft all different cost function

- virtual void postWAllDiff (int \*scopeIndex, int arity, string semantics, Cost baseCost)=0
- virtual int postWGcc (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost base-Cost, const vector< BoundedObj< Value > > &values)=0

post a soft global cardinality cost function

- virtual void postWGcc (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nb-Values, int \*lb, int \*ub)=0
- virtual int postWSame (int \*scopeIndexG1, int arityG1, int \*scopeIndexG2, int arityG2, const string &semantics, const string &propagator, Cost baseCost)=0

post a soft same cost function (a group of variables being a permutation of another group with the same size)

- virtual void postWSame (int \*scopeIndex, int arity, string semantics, Cost baseCost)=0
- virtual void postWSameGcc (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int \*lb, int \*ub)=0

post a combination of a same and gcc cost function decomposed as a cost function network

 virtual int postWGrammarCNF (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, int nbSymbols, int startSymbol, const vector< CFGProductionRule > WRuleToTerminal)=0

post a soft/weighted grammar cost function with the dynamic programming propagator and grammar in Chomsky normal form

 virtual int postMST (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost base-Cost)=0

post a Spanning Tree hard constraint

 virtual int postMaxWeight (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, const vector< WeightedVarValPair > weightFunction)=0

post a weighted max cost function (maximum cost of a set of unary cost functions associated to a set of variables)

 virtual void postWSum (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes)=0

post a soft linear constraint with unit coefficients

virtual void postWVarSum (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int varIndex)=0

post a soft linear constraint with unit coefficients and variable right-hand side

 virtual void postWOverlap (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes)=0

post a soft overlap cost function (a group of variables being point-wise equivalent – and not equal to zero – to another group with the same size)

virtual vector< vector< int > > \* getListSuccessors ()=0

generating additional variables vector created when berge decomposition are included in the WCSP

• virtual bool isGlobal ()=0

true if there are soft global constraints defined in the problem

virtual void read wcsp (const char \*fileName)=0

load problem in native wcsp format (Weighted Constraint Satisfaction Problem file format (wcsp))

virtual void read\_uai2008 (const char \*fileName)=0

load problem in UAI 2008 format (see http://graphmod.ics.uci.edu/uai08/FileFormat and http://www.cs.huji.ac.il/project/UAI10/fileFormat.php)

virtual void read\_random (int n, int m, vector< int > &p, int seed, bool forceSubModular=false, string global-name="")=0

create a random WCSP with n variables, domain size m, array p where the first element is a percentage of tuples with a nonzero cost and next elements are the number of random cost functions for each different arity (starting with arity two), random seed, a flag to have a percentage (last element in the array p) of the binary cost functions being permutated submodular, and a string to use a specific global cost function instead of random cost functions in extension

virtual void read\_wcnf (const char \*fileName)=0

load problem in (w)cnf format (see http://www.maxsat.udl.cat/08/index.php?disp=requirements)

virtual void read qpbo (const char \*fileName)=0

load quadratic pseudo-Boolean optimization problem in unconstrained quadratic programming text format (first text line with n, number of variables and m, number of triplets, followed by the m triplets (x,y,cost) describing the sparse symmetric nXn cost matrix with variable indexes such that x < = y and any positive or negative real numbers for costs)

virtual const vector< Value > & getSolution ()=0

returns current best solution

virtual void setSolution (TAssign \*sol=NULL)=0

set best solution from current assigned values or from a given assignment (for BTD-like methods)

virtual void printSolution (ostream &os)=0

prints current best solution

virtual void print (ostream &os)=0

print current domains and active cost functions (see Output messages, verbosity options and debugging)

virtual void dump (ostream &os, bool original=true)=0
 output the current WCSP into a file in wcsp format

#### Static Public Member Functions

• static WeightedCSP \* makeWeightedCSP (Cost upperBound, void \*solver=NULL) Weighted CSP factory.

#### 4.1.1 Detailed Description

Abstract class WeightedCSP representing a weighted constraint satisfaction problem

- · problem lower and upper bounds
- list of variables with their finite domains (either represented by an enumerated list of values, or by a single interval)
- list of cost functions (created before and during search by variable elimination of variables with small degree)
- local consistency propagation (variable-based propagation) including cluster tree decomposition caching (separator-based cache)

#### Note

Variables are referenced by their lexicographic index number (as returned by *eg* WeightedCSP::make-EnumeratedVariable)

Cost functions are referenced by their lexicographic index number (as returned by *eg* WeightedCSP::post-BinaryConstraint)

### 4.1.2 Member Function Documentation

**4.1.2.1** virtual void WeightedCSP::assignLS (vector< int > & varIndexes, vector< Value > & newValues ) [pure virtual]

assigns a set of variables at once and propagates (used by Local Search methods such as Large Neighborhood Search)

#### **Parameters**

varIndexes	vector of variable indexes as returned by makeXXXVariable
newValues	vector of values to be assigned to the corresponding variables

4.1.2.2 virtual void WeightedCSP::cartProd ( BigInteger & cartesianProduct ) [pure virtual]

Cartesian product of current domain sizes.

### **Parameters**

cartesianProduct	result obtained by the GNU Multiple Precision Arithmetic Library GMP
------------------	--

**4.1.2.3** virtual void WeightedCSP::dump (ostream & os, bool original = true) [pure virtual] output the current WCSP into a file in wcsp format

#### **Parameters**

os	output file
original	if true then keeps all variables with their original domain size else uses unassigned variables
	and current domains recoding variable indexes

4.1.2.4 virtual Cost WeightedCSP::finiteUb() const [pure virtual]

computes the worst-case assignment finite cost (sum of maximum finite cost over all cost functions plus one)

#### Returns

the worst-case assignment finite cost

#### Warning

current problem should be completely loaded and propagated before calling this function

**4.1.2.5** virtual string WeightedCSP::getName (int varIndex) const [pure virtual]

Note

by default, variables names are integers, starting at zero

4.1.2.6 virtual Value WeightedCSP::getValue (int varIndex) const [pure virtual]

current assigned value

### Warning

undefined if not assigned yet

**4.1.2.7** virtual void WeightedCSP::increaseLb ( Cost addLb ) [pure virtual]

increases problem lower bound thanks to eg soft local consistencies

### Parameters

addLb	increment value to be <b>added</b> to the problem lower bound

- 4.1.2.8 virtual int WeightedCSP::postGlobalConstraint (int \* scopeIndex, int arity, string & gcname, istream & file, int \* constrcounter = NULL ) [pure virtual]
- 4.1.2.9 virtual int WeightedCSP::postMaxWeight ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, const vector< WeightedVarValPair > weightFunction ) [pure virtual]

post a weighted max cost function (maximum cost of a set of unary cost functions associated to a set of variables)

### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of scopeIndex
semantics	the semantics of the global cost function: "val"
propagator	the propagation method ("DAG" only)

baseCost	if a variable-value pair does not exist in <i>weightFunction</i> , its weight will be mapped to base- Cost.
weightFunction	a vector of WeightedVarValPair containing a mapping from variable-value pairs to their weights.

4.1.2.10 virtual int WeightedCSP::postMST ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost ) [pure virtual]

post a Spanning Tree hard constraint

#### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of scopeIndex
semantics	the semantics of the global cost function: "hard"
propagator	the propagation method ("DAG" only)
baseCost	unused in the current implementation (MAX_COST)

**4.1.2.11** virtual void WeightedCSP::postNaryConstraintTuple( int *ctrindex*, Value \* *tuple*, int *arity*, Cost *cost* ) [pure virtual]

#### Warning

must call WeightedCSP::postNaryConstraintEnd after giving cost tuples

- **4.1.2.12** virtual void WeightedCSP::postUnary (int xIndex, vector < Cost > & costs ) [pure virtual]
- 4.1.2.13 virtual int WeightedCSP::postUnary (int xIndex, Value \* d, int dsize, Cost penalty ) [pure virtual]

### Warning

must call WeightedCSP::sortConstraints after all cost functions have been posted (see WeightedCSP::sort-Constraints)

4.1.2.14 virtual int WeightedCSP::postWAllDiff ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost ) [pure virtual]

post a soft all different cost function

### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of the array
semantics	the semantics of the global cost function: for flow-based propagator: "var" or "dec" or "decbi" (decomposed into a binary cost function complete network), for DAG-based propagator: "var", for network-based propagator: "hard" or "lin" or "quad" (decomposed based on wamong)
propagator	the propagation method ("flow", "DAG", "network")
baseCost	the scaling factor of the violation

- **4.1.2.15** virtual void WeightedCSP::postWAllDiff ( int \* scopelndex, int arity, string semantics, Cost baseCost ) [pure virtual]
- 4.1.2.16 virtual int WeightedCSP::postWAmong ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, const vector < Value > & values, int lb, int ub ) [pure virtual]

post a soft among cost function

#### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of the array
semantics	the semantics of the global cost function: "var" or – "hard" or "lin" or "quad" (network-based
	propagator only)-
propagator	the propagation method (only "DAG" or "network")
baseCost	the scaling factor of the violation
values	a vector of values to be restricted
lb	a fixed lower bound for the number variables to be assigned to the values in values
ub	a fixed upper bound for the number variables to be assigned to the values in <i>values</i>

- 4.1.2.17 virtual void WeightedCSP::postWAmong ( int \* scopeIndex, int arity, string semantics, Cost baseCost, Value \* values, int nbValues, int lb, int ub ) [pure virtual]
- 4.1.2.18 virtual int WeightedCSP::postWGcc (int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, const vector < BoundedObj < Value > > & values ) [pure virtual]

post a soft global cardinality cost function

#### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of the array
semantics	the semantics of the global cost function: "var" (DAG-based propagator only) or - "var" or
	"dec" or "wdec" (flow-based propagator only) or - "hard" or "lin" or "quad" (network-based
	propagator only)-
propagator	the propagation method ("flow", "DAG", "network")
baseCost	the scaling factor of the violation
values	a vector of BoundedObj, specifying the lower and upper bounds of each value, restricting the
	number of variables can be assigned to them

- 4.1.2.19 virtual void WeightedCSP::postWGcc ( int \* scopeIndex, int arity, string semantics, Cost baseCost, Value \* values, int nbValues, int \* lb, int \* ub ) [pure virtual]
- 4.1.2.20 virtual int WeightedCSP::postWGrammarCNF ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, int nbSymbols, int startSymbol, const vector < CFGProductionRule > WRuleToTerminal

  ) [pure virtual]

post a soft/weighted grammar cost function with the dynamic programming propagator and grammar in Chomsky normal form

#### **Parameters**

scopeIndex	an array of the first group of variable indexes as returned by WeightedCSP::make-
	EnumeratedVariable
arity	the size of scopeIndex
semantics	the semantics of the global cost function: "var" or "weight"
propagator	the propagation method ("DAG" only)
baseCost	the scaling factor of the violation
nbSymbols	the number of symbols in the corresponding grammar. Symbols are indexed as 0, 1,,
	nbSymbols-1
startSymbol	the index of the starting symbol
WRuleTo-	a vector of ::CFGProductionRule. Note that:
Terminal	<ul> <li>if order in CFGProductionRule is set to 0, it is classified as A -&gt; v, where A is the index of the terminal symbol and v is the value.</li> <li>if order in CFGProductionRule is set to 1, it is classified as A -&gt; BC, where A,B,C the index of the nonterminal symbols.</li> <li>if order in CFGProductionRule is set to 2, it is classified as weighted A -&gt; v, where A is the index of the terminal symbol and v is the value.</li> <li>if order in CFGProductionRule is set to 3, it is classified as weighted A -&gt; BC, where A,B,C the index of the nonterminal symbols.</li> </ul>
	• if order in CFGProductionRule is set to values greater than 3, it is ignored.

4.1.2.21 virtual void WeightedCSP::postWOverlap ( int \* scopelndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes ) [pure virtual]

post a soft overlap cost function (a group of variables being point-wise equivalent – and not equal to zero – to another group with the same size)

### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of scopeIndex (should be an even value)
semantics	the semantics of the global cost function: "hard" or "lin" or "quad" (network-based propagator
	only)
propagator	the propagation method ("network" only)
baseCost	the scaling factor of the violation.
comparator	the point-wise comparison operator applied to the number of equivalent variables ("==", "!=",
	"<", "<=", ">,", ">=")
rightRes	right-hand side value of the comparison

4.1.2.22 virtual int WeightedCSP::postWRegular ( int \* scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, int nbStates, const vector< WeightedObj< int > > & initial\_States, const vector<

WeightedObj< int > > & accepting\_States, const vector< DFATransition > & Wtransitions ) [pure virtual]

post a soft or weighted regular cost function

### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of the array

semantics	the semantics of the soft global cost function: "var" or "edit" (flow-based propagator) or – "var"
	(DAG-based propagator)— (unused parameter for network-based propagator)
propagator	the propagation method ("flow", "DAG", "network")
baseCost	the scaling factor of the violation ("flow", "DAG")
nbStates	the number of the states in the corresponding DFA. The states are indexed as 0, 1,, nb-
	States-1
initial_States	a vector of WeightedObj specifying the starting states with weight
accepting	a vector of WeightedObj specifying the final states
States	
Wtransitions	a vector of (weighted) transitions

#### Warning

Weights are ignored in the current implementation of DAG and flow-based propagators

- 4.1.2.23 virtual void WeightedCSP::postWRegular ( int \* scopelndex, int arity, int nbStates, vector < pair < int, Cost > > initial\_States, vector < pair < int, Cost > > accepting\_States, int \*\* Wtransitions, vector < Cost > transitionsCosts 
  ) [pure virtual]
- 4.1.2.24 virtual int WeightedCSP::postWSame (int \* scopeIndexG1, int arityG1, int \* scopeIndexG2, int arityG2, const string & semantics, const string & propagator, Cost baseCost) [pure virtual]

post a soft same cost function (a group of variables being a permutation of another group with the same size)

#### **Parameters**

scopeIndexG1	an array of the first group of variable indexes as returned by WeightedCSP::make-
	EnumeratedVariable
arityG1	the size of scopeIndexG1
scopeIndexG2	an array of the second group of variable indexes as returned by WeightedCSP::make-
	EnumeratedVariable
arityG2	the size of scopeIndexG2
semantics	the semantics of the global cost function: "var" or – "hard" or "lin" or "quad" (network-based
	propagator only)-
propagator	the propagation method ("flow" or "network")
baseCost	the scaling factor of the violation.

- **4.1.2.25** virtual void WeightedCSP::postWSame (int \* scopelndex, int arity, string semantics, Cost baseCost ) [pure virtual]
- 4.1.2.26 virtual void WeightedCSP::postWSum ( int \* scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes ) [pure virtual]

post a soft linear constraint with unit coefficients

#### **Parameters**

scopeIndex	an array of variable indexes as returned by WeightedCSP::makeEnumeratedVariable
arity	the size of scopeIndex
semantics	the semantics of the global cost function: "hard" or "lin" or "quad" (network-based propagator
	only)
propagator	the propagation method ("network" only)
baseCost	the scaling factor of the violation
comparator	the comparison operator of the linear constraint ("==", "!=", "<", "<=", ">,", ">=")

rightRes right-hand side value of the linear constraint

4.1.2.27 virtual void WeightedCSP::read\_uai2008 ( const char \* fileName ) [pure virtual]

load problem in UAI 2008 format (see http://graphmod.ics.uci.edu/uai08/FileFormat and http://www.cs.huji.ac.il/project/UAI10/fileFormat.php)

#### Warning

UAI10 evidence file format not recognized by toulbar2 as it does not allow multiple evidence (you should remove the first value in the file)

4.1.2.28 virtual void WeightedCSP::setInfiniteCost() [pure virtual]

updates infinite costs in all cost functions accordingly to the problem global lower and upper bounds

Warning

to be used in preprocessing only

**4.1.2.29** virtual void WeightedCSP::sortConstraints() [pure virtual]

sorts the list of cost functions associated to each variable based on smallest problem variable indexes

Warning

side-effect: updates DAC order according to an existing variable elimination order

Note

must be called after creating all the cost functions and before solving the problem

### 4.2 WeightedCSPSolver Class Reference

**Public Member Functions** 

virtual WeightedCSP \* getWCSP ()=0

access to its associated Weighted CSP

virtual Long getNbNodes () const =0

number of search nodes (see WeightedCSPSolver::increase, WeightedCSPSolver::decrease, WeightedCSPSolver::remove)

virtual Long getNbBacktracks () const =0

number of backtracks

• virtual void increase (int varIndex, Value value, bool reverse=false)=0

changes domain lower bound and propagates

virtual void decrease (int varIndex, Value value, bool reverse=false)=0

changes domain upper bound and propagates

• virtual void assign (int varIndex, Value value, bool reverse=false)=0

assigns a variable and propagates

virtual void remove (int varIndex, Value value, bool reverse=false)=0

removes a domain value and propagates (valid if done for an enumerated variable or on its domain bounds)

• virtual void read\_wcsp (const char \*fileName)=0

reads a WCSP from a file in wcsp text format (can be other formats if using specific ::ToulBar2 global variables)

virtual void read\_random (int n, int m, vector< int > &p, int seed, bool forceSubModular=false, string global-name="")=0

create a random WCSP, see WeightedCSP::read\_random

virtual bool solve ()=0

simplifies and solves to optimality the problem

virtual Cost narycsp (string cmd, vector< Value > &solution)=0

solves the current problem using INCOP local search solver by Bertrand Neveu

virtual bool solve\_symmax2sat (int n, int m, int \*posx, int \*posy, double \*cost, int \*sol)=0

quadratic unconstrained pseudo-Boolean optimization Maximize  $h' \times W \times h$  where W is expressed by all its non-zero half squared matrix costs (can be positive or negative, with  $\forall i, posx[i] \leq posy[i]$ )

• virtual void dump wcsp (const char \*fileName, bool original=true)=0

output current problem in a file

virtual void read\_solution (const char \*fileName)=0

read a solution from a file

virtual void parse solution (const char \*certificate)=0

read a solution from a string (see ToulBar2 option -x)

virtual Cost getSolution (vector < Value > &solution)=0

after solving the problem, add the optimal solution in the input/output vector and returns its optimum cost (warning! do not use it if doing solution counting or if there is no solution, see WeightedCSPSolver::solve output for that)

#### Static Public Member Functions

static WeightedCSPSolver \* makeWeightedCSPSolver (Cost initUpperBound)
 WeightedCSP Solver factory.

### 4.2.1 Detailed Description

Abstract class WeightedCSPSolver representing a WCSP solver

- link to a WeightedCSP
- generic complete solving method configurable through global variables (see ::ToulBar2 class and command line options)
- · optimal solution available after problem solving
- · elementary decision operations on domains of variables
- · statistics information (number of nodes and backtracks)
- problem file format reader (multiple formats, see Weighted Constraint Satisfaction Problem file format (wcsp))
- solution checker (output the cost of a given solution)

#### 4.2.2 Member Function Documentation

**4.2.2.1** virtual void WeightedCSPSolver::dump\_wcsp ( const char \* fileName, bool original = true ) [pure virtual]

output current problem in a file

#### See Also

WeightedCSP::dump

**4.2.2.2** virtual Cost WeightedCSPSolver::narycsp ( string cmd, vector < Value > & solution ) [pure virtual]

solves the current problem using INCOP local search solver by Bertrand Neveu

#### Returns

best solution cost found

#### **Parameters**

cmd	command line argument for narycsp INCOP local search solver (cmd format: lower-
	bound randomseed nbiterations method nbmoves neighborhoodchoice neighborhoodchoice2
	minnbneighbors maxnbneighbors neighborhoodchoice3 autotuning tracemode)
solution	best solution assignment found (MUST BE INITIALIZED WITH A DEFAULT COMPLETE A-
	SSIGNMENT)

#### Warning

cannot solve problems with global cost functions

#### Note

side-effects: updates current problem upper bound and propagates, best solution saved (using WCSP::set-BestValue)

4.2.2.3 virtual bool WeightedCSPSolver::solve( ) [pure virtual]

simplifies and solves to optimality the problem

#### Returns

false if there is no solution found

### Warning

after solving, the current problem has been modified by various preprocessing techniques DO NOT READ VALUES OF ASSIGNED VARIABLES USING WeightedCSP::getValue (temporally wrong assignments due to variable elimination in preprocessing) BUT USE WeightedCSPSolver::getSolution INST-EAD

4.2.2.4 virtual bool WeightedCSPSolver::solve\_symmax2sat ( int n, int m, int \* posx, int \* posy, double \* cost, int \* sol ) [pure virtual]

quadratic unconstrained pseudo-Boolean optimization Maximize  $h' \times W \times h$  where W is expressed by all its non-zero half squared matrix costs (can be positive or negative, with  $\forall i, posx[i] \leq posy[i]$ )

### Note

```
costs for posx \neq posy are multiplied by 2 by this method by convention: h=1 \equiv x=0 and h=-1 \equiv x=1
```

### Warning

does not allow infinite costs (no forbidden assignments, unconstrained optimization)

#### Returns

true if at least one solution has been found (array sol being filled with the best solution)

### See Also

::solvesymmax2sat for Fortran call