

toulbar2

Generated by Doxygen 1.8.6

Wed Aug 24 2016 11:13:30

## Contents

<b>1</b>	<b>Main Page</b>	<b>1</b>
<b>2</b>	<b>toulbar2</b>	<b>2</b>
<b>3</b>	<b>Module Documentation</b>	<b>4</b>
3.1	Weighted Constraint Satisfaction Problem file format (wcsp)	4
3.2	Variable and cost function modeling	11
3.3	Solving cost function networks	12
3.4	Output messages, verbosity options and debugging	13
3.5	Preprocessing techniques	14
3.6	Variable and value search ordering heuristics	15
3.7	Soft arc consistency and problem reformulation	16
3.8	Virtual Arc Consistency enforcing	17
3.9	NC bucket sort	18
3.10	Variable elimination	19
3.11	Propagation loop	20
3.12	Backtrack management	21
<b>4</b>	<b>Class Documentation</b>	<b>22</b>
4.1	WeightedCSP Class Reference	22
4.1.1	Detailed Description	26
4.1.2	Member Function Documentation	26
4.2	WeightedCSPSolver Class Reference	32
4.2.1	Detailed Description	33
4.2.2	Member Function Documentation	33
	<b>Index</b>	<b>35</b>

## 1 Main Page

<b>Weighted CSP Solver</b>	toulbar2
<b>Copyright</b>	INRA
<b>Source</b>	<a href="https://mulcyber.toulouse.inra.fr/projects/toulbar2/">https://mulcyber.toulouse.inra.fr/projects/toulbar2/</a>

See the [README](#) for more details.

toulbar2 can be used as a stand-alone solver reading various problem file formats (wcsp, uai, wcnf, qpbo) or as a C++ library.

This document describes the wcsp native file format and the toulbar2 C++ library API.

### Note

Use cmake flags LIBTB2=ON and TOULBAR2\_ONLY=OFF to get the toulbar2 C++ library libtb2.so and toulbar2test executable example.

### See Also

`./src/toulbar2test.cpp`

## 2 toulbar2

### An exact solver for cost function networks

#### What is toulbar2?

toulbar2 is an open-source C++ solver for cost function networks. It solves various combinatorial optimization problems. The constraints and objective function are factorized in local functions on discrete variables. Each function returns a cost (a finite positive integer) for any assignment of its variables. Constraints are represented as functions with costs in  $\{0, k\}$  where  $k$  is a large integer representing forbidden assignments. toulbar2 looks for a non-forbidden assignment of all variables that minimizes the sum of all functions.

toulbar2 won several competitions on deterministic and probabilistic graphical models:

- Max-CSP 2008 Competition [CPAI08](#) (winner on 2-ARY-EXT and N-ARY-EXT)
- Probabilistic Inference Evaluation [UAI 2008](#) (winner on several MPE tasks, intra entries)
- 2010 UAI APPROXIMATE INFERENCE CHALLENGE [UAI 2010](#) (winner on 1200-second MPE task)
- The Probabilistic Inference Challenge [PIC 2011](#) (second place by ficoloflo on 1-hour MAP task)
- UAI 2014 Inference Competition [UAI 2014](#) (winner on all MAP task categories, see Proteus, Robin, and IncTb entries)

#### Download

<http://mulcyber.toulouse.inra.fr/projects/toulbar2/>

Latest src/debian/windows x86\_64 releases:

- 2016: [src0\\_9\\_8/deb0\\_9\\_8/win0\\_9\\_8](#) with hybrid best-first search and more soft global cost functions
- 2015: [src0\\_9\\_7/deb0\\_9\\_7/win0\\_9\\_7](#) with local search [INCOP](#) solver after preprocessing
- 2014: [src0\\_9\\_6/deb0\\_9\\_6/win0\\_9\\_6](#) with extra variable ordering heuristics and dominance pruning rules
- 2012: [src0\\_9\\_5/deb0\\_9\\_5/win0\\_9\\_5](#) with soft global decomposable cost functions
- 2011: [src0\\_9\\_4/deb0\\_9\\_4/win0\\_9\\_4](#) with more preprocessing techniques
- 2010: [src0\\_9\\_3/deb0\\_9\\_3/win0\\_9\\_3](#) with soft global cost functions

#### Installation

Library needed:

- `libgmp-dev`
- `libboost-dev`
- `libboost-graph-dev`

Optional libraries:

- libxml2-dev

GNU C++ Symbols to be defined if using Linux Eclipse/CDT IDE (no value needed):

- LINUX
- LONGLONG\_COST
- WIDE\_STRING
- LONGDOUBLE\_PROB
- NARYCHAR
- WCSPFORMATONLY

Commands for compiling toulbar2 on Linux in directory toulbar2/src without cmake:

```
bash
cd src
echo '#define Toulbar_VERSION "0.9.8"' > ToulbarVersion.hpp
g++ -o toulbar2 -I. tb2*.cpp incop/*.cpp ToulbarVersion.cpp -O3 -std=c++11 -DNDEBUG -DLINUX \
-DLONGLONG_COST -DWIDE_STRING -DLONGDOUBLE_PROB -DNARYCHAR -DWCSPPFORMATONLY -lgmp -static
```

## Authors

toulbar2 was originally developed by Toulouse (INRA MIAT) and Barcelona (UPC, IIIA-CSIC) teams, hence the name of the solver.

Additional contributions by:

- The Chinese University of Hong Kong and Caen University, France (GREYC) for global cost functions
- Marseille University, France (LSIS) for tree decomposition heuristics
- Ecole des Ponts ParisTech, France (CERMICS/LIGM) for [INCOP](#) local search solver
- University College Cork, Ireland (Insight) for a Python interface in [NumberJack](#) and a portfolio dedicated to UAI graphical models [Proteus](#)
- Artois University, France (CRIL) for an XCSP 2.1 format reader of CSP and WCSP instances

## Citing

Please use one of the following references for citing toulbar2:

Multi-Language Evaluation of Exact Solvers in Graphical Model Discrete Optimization Barry Hurley, Barry O'Sullivan, David Allouche, George Katsirelos, Thomas Schiex, Matthias Zytnicki, Simon de Givry Constraints, 21(3):413-434, 2016

Tractability-preserving Transformations of Global Cost Functions David Allouche, Christian Bessiere, Patrice Boizumault, Simon de Givry, Patricia Gutierrez, Jimmy H.M. Lee, Ka Lun Leung, Samir Loudni, Jean-Philippe Métivier, Thomas Schiex, Yi Wu Artificial Intelligence, 238:166-189, 2016

Soft arc consistency revisited Martin Cooper, Simon de Givry, Marti Sanchez, Thomas Schiex, Matthias Zytnicki, and Thomas Werner Artificial Intelligence, 174(7-8):449-478, 2010

## What are the algorithms inside toulbar2?

- Soft arc consistencies (NC, AC, DAC, FDAC) In the quest of the best form of local consistency for Weighted CSP J. Larrosa & T. Schiex In Proc. of IJCAI-03. Acapulco, Mexico, 2003

- Soft existential arc consistency (EDAC) Existential arc consistency: Getting closer to full arc consistency in weighted csp S. de Givry, M. Zytnicki, F. Heras, and J. Larrosa In Proc. of IJCAI-05, Edinburgh, Scotland, 2005
- Depth-first Branch and Bound exploiting a tree decomposition (BTD) Exploiting Tree Decomposition and Soft Local Consistency in Weighted CSP S. de Givry, T. Schiex, and G. Verfaillie In Proc. of AAAI-06, Boston, MA, 2006
- Virtual arc consistency (VAC) Virtual arc consistency for weighted csp M. Cooper, S. de Givry, M. Sanchez, T. Schiex, and M. Zytnicki In Proc. of AAAI-08, Chicago, IL, 2008
- Soft generalized arc consistencies (GAC, FDGAC) Towards Efficient Consistency Enforcement for Global Constraints in Weighted Constraint Satisfaction J. H. M. Lee and K. L. Leung In Proc. of IJCAI-09, Los Angeles, USA, 2010
- Russian doll search exploiting a tree decomposition (RDS-BTD) Russian doll search with tree decomposition M Sanchez, D Allouche, S de Givry, and T Schiex In Proc. of IJCAI'09, Pasadena (CA), USA, 2009
- Soft bounds arc consistency (BAC) Bounds Arc Consistency for Weighted CSPs M. Zytnicki, C. Gaspin, S. de Givry, and T. Schiex Journal of Artificial Intelligence Research, 35:593-621, 2009
- Counting solutions in satisfaction (#BTD, Approx\_::BTD) Exploiting problem structure for solution counting A. Favier, S. de Givry, and P. Jégou In Proc. of CP-09, Lisbon, Portugal, 2009
- Soft existential generalized arc consistency (EDGAC) A Stronger Consistency for Soft Global Constraints in Weighted Constraint Satisfaction J. H. M. Lee and K. L. Leung In Proc. of AAAI-10, Boston, MA, 2010
- Preprocessing techniques (combines variable elimination and cost function decomposition) Pairwise decomposition for combinatorial optimization in graphical models A Favier, S de Givry, A Legarra, and T Schiex In Proc. of IJCAI-11, Barcelona, Spain, 2011
- Decomposable global cost functions (wregular, wamong, wsum) Decomposing global cost functions D Allouche, C Bessiere, P Boizumault, S de Givry, P Gutierrez, S Loudni, JP Métivier, and T Schiex In Proc. of AAAI-12, Toronto, Canada, 2012
- Pruning by dominance (DEE) Dead-End Elimination for Weighted CSP S de Givry, S Prestwich, and B O'Sullivan In Proc. of CP-13, pages 263-272, Uppsala, Sweden, 2013
- Hybrid best-first search exploiting a tree decomposition (HBFS) Anytime Hybrid Best-First Search with Tree Decomposition for Weighted CSP D Allouche, S de Givry, G Katsirelos, T Schiex, and M Zytnicki In Proc. of CP-15, Cork, Ireland, 2015

Copyright (C) 2006-2016, INRA. toulbar2 is currently maintained by Simon de Givry, INRA - MIAT, Toulouse, France ([simon.degivry@toulouse.inra.fr](mailto:simon.degivry@toulouse.inra.fr))

## 3 Module Documentation

### 3.1 Weighted Constraint Satisfaction Problem file format (wcsp)

It is a text format composed of a list of numerical and string terms separated by spaces. Instead of using names for making reference to variables, variable indexes are employed. The same for domain values. All indexes start at zero.

Cost functions can be defined in intention (see below) or in extension, by their list of tuples. A default cost value is defined per function in order to reduce the size of the list. Only tuples with a different cost value should be given (not mandatory). All the cost values must be positive. The arity of a cost function in extension may be equal to zero. In this case, there is no tuples and the default cost value is added to the cost of any solution. This can be used to represent a global lower bound constant of the problem.

The wcsp file format is composed of three parts: a problem header, the list of variable domain sizes, and the list of cost functions.

- Header definition for a given problem:

```
<Problem name>
<Number of variables (N)>
<Maximum domain size>
<Number of cost functions>
<Initial global upper bound of the problem (UB)>
```

The goal is to find an assignment of all the variables with minimum total cost, strictly lower than UB. Tuples with a cost greater than or equal to UB are forbidden (hard constraint).

- Definition of domain sizes

```
<Domain size of variable with index 0>
...
<Domain size of variable with index N - 1>
```

#### Note

domain values range from zero to *size-1*

a negative domain size is interpreted as a variable with an interval domain in  $[0, -size - 1]$

#### Warning

variables with interval domains are restricted to arithmetic and disjunctive cost functions in intention (see below)

- General definition of cost functions

- Definition of a cost function in extension

```
<Arity of the cost function>
<Index of the first variable in the scope of the cost function>
...
<Index of the last variable in the scope of the cost function>
<Default cost value>
<Number of tuples with a cost different than the default cost>
```

followed by for every tuple with a cost different than the default cost:

```
<Index of the value assigned to the first variable in the scope>
...
<Index of the value assigned to the last variable in the scope>
<Cost of the tuple>
```

#### Note

Shared cost function: A cost function in extension can be shared by several cost functions with the same arity (and same domain sizes) but different scopes. In order to do that, the cost function to be shared must start by a negative scope size. Each shared cost function implicitly receives an occurrence number starting from 1 and incremented at each new shared definition. New cost functions in extension can reuse some previously defined shared cost functions in extension by using a negative number of tuples representing the occurrence number of the desired shared cost function. Note that default costs should be the same in the shared and new cost functions. Here is an example of 4 variables with domain size 4 and one AllDifferent hard constraint decomposed into 6 binary constraints.

- Shared CF used inside a small example in wcsp format:

```
AllDifferentDecomposedIntoBinaryConstraints 4 4 6 1
4 4 4 4
-2 0 1 0 4
0 0 1
1 1 1
2 2 1
3 3 1
2 0 2 0 -1
2 0 3 0 -1
2 1 2 0 -1
2 1 3 0 -1
2 2 3 0 -1
```

- Definition of a cost function in intension by replacing the default cost value by -1 and by giving its keyword name and its K parameters

```

<Arity of the cost function>
<Index of the first variable in the scope of the cost function>
...
<Index of the last variable in the scope of the cost function>
-1
<keyword>
<parameter1>
...
<parameterK>

```

Possible keywords of cost functions defined in intension followed by their specific parameters:

- $\geq$  *cst delta* to express soft binary constraint  $x \geq y + cst$  with associated cost function  $\max((y + cst - x \leq \text{delta})?(y + cst - x) : UB, 0)$
- $>$  *cst delta* to express soft binary constraint  $x > y + cst$  with associated cost function  $\max((y + cst + 1 - x \leq \text{delta})?(y + cst + 1 - x) : UB, 0)$
- $\leq$  *cst delta* to express soft binary constraint  $x \leq y + cst$  with associated cost function  $\max((x - cst - y \leq \text{delta})?(x - cst - y) : UB, 0)$
- $<$  *cst delta* to express soft binary constraint  $x < y + cst$  with associated cost function  $\max((x - cst + 1 - y \leq \text{delta})?(x - cst + 1 - y) : UB, 0)$
- $=$  *cst delta* to express soft binary constraint  $x = y + cst$  with associated cost function  $(|y + cst - x| \leq \text{delta})?|y + cst - x| : UB$
- *disj cstx csty penalty* to express soft binary disjunctive constraint  $x \geq y + csty \vee y \geq x + cstx$  with associated cost function  $(x \geq y + csty \vee y \geq x + cstx)?0 : \text{penalty}$
- *sdisj cstx csty xinfy yinfy costx costly* to express a special disjunctive constraint with three implicit hard constraints  $x \leq \text{xinfy}$  and  $y \leq \text{yinfy}$  and  $x < \text{xinfy} \wedge y < \text{yinfy} \Rightarrow (x \geq y + csty \vee y \geq x + cstx)$  and an additional cost function  $((x = \text{xinfy})?costx : 0) + ((y = \text{yinfy})?costy : 0)$
- Global cost functions using a flow-based propagator:
  - *salldiff var|dec|decbi cost* to express a soft alldifferent constraint with either variable-based (*var* keyword) or decomposition-based (*dec* and *decbi* keywords) cost semantic with a given *cost* per violation (*decbi* decomposes into a binary cost function complete network)
  - *sgcc var|dec|wdec cost nb\_values (value lower\_bound upper\_bound (shortage\_weight excess\_weight)?)\** to express a soft global cardinality constraint with either variable-based (*var* keyword) or decomposition-based (*dec* keyword) cost semantic with a given *cost* per violation and for each value its lower and upper bound (if *wdec* then violation cost depends on each value shortage or excess weights)
  - *ssame cost list\_size1 list\_size2 (variable\_index)\*(variable\_index)\** to express a permutation constraint on two lists of variables of equal size (implicit variable-based cost semantic)
  - *sregular var|edit cost nb\_states nb\_initial\_states (state)\* nb\_final\_states (state)\* nb\_transitions (start\_state symbol\_value end\_state)\** to express a soft regular constraint with either variable-based (*var* keyword) or edit distance-based (*edit* keyword) cost semantic with a given *cost* per violation followed by the definition of a deterministic finite automaton with number of states, list of initial and final states, and list of state transitions where symbols are domain values
- Global cost functions using a dynamic programming DAG-based propagator:
  - *sregulardp var cost nb\_states nb\_initial\_states (state)\* nb\_final\_states (state)\* nb\_transitions (start\_state symbol\_value end\_state)\** to express a soft regular constraint with a variable-based (*var* keyword) cost semantic with a given *cost* per violation followed by the definition of a deterministic finite automaton with number of states, list of initial and final states, and list of state transitions where symbols are domain values

- `sgrammar|sgrammardp var|weight cost nb_symbols nb_values start_symbol nb_rules ((0 terminal_ symbol value)|(1 nonterminal_in nonterminal_out_left nonterminal_out_right)|(2 terminal_symbol value weight)|(3 nonterminal_in nonterminal_out_left nonterminal_out_right weight))*` to express a soft/weighted grammar in Chomsky normal form
- `samong|samongdp var cost lower_bound upper_bound nb_values (value)*` to express a soft among constraint to restrict the number of variables taking their value into a given set of values
- `salldifdp var cost` to express a soft alldifferent constraint with variable-based (*var* keyword) cost semantic with a given *cost* per violation (decomposes into `samongdp` cost functions)
- `sgccdp var cost nb_values (value lower_bound upper_bound)*` to express a soft global cardinality constraint with variable-based (*var* keyword) cost semantic with a given *cost* per violation and for each value its lower and upper bound (decomposes into `samongdp` cost functions)
- `max|smaxdp defCost nbtuples (variable value cost)*` to express a weighted max cost function to find the maximum cost over a set of unary cost functions associated to a set of variables (by default, *defCost* if unspecified)
- `MST|smstdp hard` to express a spanning tree hard constraint where each variable is assigned to its parent variable index in order to build a spanning tree (the root being assigned to itself)
- Global cost functions using a cost function network-based propagator:
  - `wregular nb_states nb_initial_states (state and cost)* nb_final_states (state and cost)* nb_transitions (start_state symbol_value end_state cost)*` to express a weighted regular constraint with weights on initial states, final states, and transitions, followed by the definition of a deterministic finite automaton with number of states, list of initial and final states with their costs, and list of weighted state transitions where symbols are domain values
  - `walldiff hard|lin|quad cost` to express a soft alldifferent constraint as a set of `wamong` hard constraint (*hard* keyword) or decomposition-based (*lin* and *quad* keywords) cost semantic with a given *cost* per violation
  - `wgcc hard|lin|quad cost nb_values (value lower_bound upper_bound)*` to express a soft global cardinality constraint as either a hard constraint (*hard* keyword) or with decomposition-based (*lin* and *quad* keyword) cost semantic with a given *cost* per violation and for each value its lower and upper bound
  - `wsame hard|lin|quad cost` to express a permutation constraint on two lists of variables of equal size (implicitly concatenated in the scope) using implicit decomposition-based cost semantic
  - `wsamegcc hard|lin|quad cost nb_values (value lower_bound upper_bound)*` to express the combination of a soft global cardinality constraint and a permutation constraint
  - `wamong hard|lin|quad cost nb_values (value)* lower_bound upper_bound` to express a soft among constraint to restrict the number of variables taking their value into a given set of values
  - `wvamong hard cost nb_values (value)*` to express a hard among constraint to restrict the number of variables taking their value into a given set of values to be equal to the last variable in the scope
  - `woverlap hard|lin|quad cost comparator righthandside` overlaps between two sequences of variables *X*, *Y* (i.e. set the fact that *X<sub>i</sub>* and *Y<sub>i</sub>* take the same value (not equal to zero))
  - `wsum hard|lin|quad cost comparator righthandside` to express a soft sum constraint with unit coefficients to test if the sum of a set of variables matches with a given comparator and right-hand-side value
  - `wvarsum hard cost comparator` to express a hard sum constraint to restrict the sum to be *comparator* to the value of the last variable in the scope

Let us note  $\langle \rangle$  the comparator, *K* the right-hand-side value associated to the comparator, and *Sum* the result of the sum over the variables. For each comparator, the gap is defined according to the distance as follows:

  - \* if  $\langle \rangle$  is `==` :  $gap = abs(K - Sum)$
  - \* if  $\langle \rangle$  is `<=` :  $gap = max(0, Sum - K)$
  - \* if  $\langle \rangle$  is `<` :  $gap = max(0, Sum - K - 1)$
  - \* if  $\langle \rangle$  is `!=` :  $gap = 1$  if  $Sum \neq K$  and  $gap = 0$  otherwise
  - \* if  $\langle \rangle$  is `>` :  $gap = max(0, K - Sum + 1)$ ;
  - \* if  $\langle \rangle$  is `>=` :  $gap = max(0, K - Sum)$ ;



**Warning**

The decomposition of `wsum` and `wvarsum` may use an exponential size (sum of domain sizes).  
`list_size1` and `list_size2` must be equal in `ssame`.  
 Cost functions defined in intention cannot be shared.

**Note**

More about network-based global cost functions can be found here <https://metivier.users.-greyc.fr/decomposable/>

**Examples:**

- quadratic cost function  $x0 * x1$  in extension with variable domains  $\{0, 1\}$  (equivalent to a soft clause  $\neg x0 \vee \neg x1$ ):

```
2 0 1 0 1 1 1 1
```

- simple arithmetic hard constraint  $x1 < x2$ :

```
2 1 2 -1 < 0 0
```

- hard temporal disjunction  $x1 \geq x2 + 2 \vee x2 \geq x1 + 1$ :

```
2 1 2 -1 disj 1 2 UB
```

- `soft_alldifferent({x0,x1,x2,x3})`:

```
4 0 1 2 3 -1 salldiff var 1
```

- `soft_gcc({x1,x2,x3,x4})` with each value  $v$  from 1 to 4 only appearing at least  $v-1$  and at most  $v+1$  times:

```
4 1 2 3 4 -1 sgcc var 1 4 1 0 2 2 1 3 3 2 4 4 3 5
```

- `soft_same({x0,x1,x2,x3},{x4,x5,x6,x7})`:

```
8 0 1 2 3 4 5 6 7 -1 ssame 1 4 4 0 1 2 3 4 5 6 7
```

- `soft_regular({x1,x2,x3,x4})` with DFA  $(3^*)+(4^*)$ :

```
4 1 2 3 4 -1 sregular var 1 2 1 0 2 0 1 3 0 3 0 0 4 1 1 4 1
```

- `soft_grammar({x0,x1,x2,x3})` with hard cost (1000) producing well-formed parenthesis expressions:

```
4 0 1 2 3 -1 sgrammardp var 1000 4 2 0 6 1 0 0 0 1 0 1 2 1 0 1 3 1 2 0 3 0 1 0 0 3 1
```

- `soft_among({x1,x2,x3,x4})` with hard cost (1000) if  $\sum_{i=1}^4 (x_i \in \{1, 2\}) < 1$  or  $\sum_{i=1}^4 (x_i \in \{1, 2\}) > 3$ :

```
4 1 2 3 4 -1 samongdp var 1000 1 3 2 1 2
```

- `soft_max({x0,x1,x2,x3})` with cost equal to  $\max_{i=0}^3 ((x_i \neq i) ? 1000 : (4 - i))$ :

```
4 0 1 2 3 -1 smaxdp 1000 4 0 0 4 1 1 3 2 2 2 3 3 1
```

- `wregular({x0,x1,x2,x3})` with DFA  $(0(10)^*2^*)$ :

```
4 0 1 2 3 -1 wregular 3 1 0 0 1 2 0 9 0 0 1 0 0 1 1 1 0 2 1 1 1 1 0 0 1 0 0 1 1 2 0 1 1 2 2 0 1 0 2 1 1 1 2
1
```

- `wamong ({x1,x2,x3,x4})` with hard cost (1000) if  $\sum_{i=1}^4 (x_i \in \{1, 2\}) < 1$  or  $\sum_{i=1}^4 (x_i \in \{1, 2\}) > 3$ :

```
4 1 2 3 4 -1 wamong hard 1000 2 1 2 1 3
```

- **wvamong** ( $\{x_1, x_2, x_3, x_4\}$ ) with hard cost (1000) if  $\sum_{i=1}^3 (x_i \in \{1, 2\}) \neq x_4$ :

```
4 1 2 3 4 -1 wvamong hard 1000 2 1 2
```

- **woverlap** ( $\{x_1, x_2, x_3, x_4\}$ ) with hard cost (1000) if  $\sum_{i=1}^2 (x_i = x_{i+2}) \geq 1$ :

```
4 1 2 3 4 -1 woverlap hard 1000 < 1
```

- **wsum** ( $\{x_1, x_2, x_3, x_4\}$ ) with hard cost (1000) if  $\sum_{i=1}^4 (x_i) \neq 4$ :

```
4 1 2 3 4 -1 wsum hard 1000 == 4
```

- **wvarsum** ( $\{x_1, x_2, x_3, x_4\}$ ) with hard cost (1000) if  $\sum_{i=1}^3 (x_i) \neq x_4$ :

```
4 1 2 3 4 -1 wvarsum hard 1000 ==
```

Latin Square 4 x 4 crisp CSP example in wcsp format:

```
latin4 16 4 8 1
4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
4 0 1 2 3 -1 salldiff var 1
4 4 5 6 7 -1 salldiff var 1
4 8 9 10 11 -1 salldiff var 1
4 12 13 14 15 -1 salldiff var 1
4 0 4 8 12 -1 salldiff var 1
4 1 5 9 13 -1 salldiff var 1
4 2 6 10 14 -1 salldiff var 1
4 3 7 11 15 -1 salldiff var 1
```

4-queens binary weighted CSP example with random unary costs in wcsp format:

```
4-WQUEENS 4 4 10 5
4 4 4 4
2 0 1 0 10
0 0 5
0 1 5
1 0 5
1 1 5
1 2 5
2 1 5
2 2 5
2 3 5
3 2 5
3 3 5
2 0 2 0 8
0 0 5
0 2 5
1 1 5
1 3 5
2 0 5
2 2 5
3 1 5
3 3 5
2 0 3 0 6
0 0 5
0 3 5
1 1 5
2 2 5
3 0 5
3 3 5
2 1 2 0 10
0 0 5
0 1 5
1 0 5
1 1 5
1 2 5
2 1 5
2 2 5
2 3 5
3 2 5
3 3 5
2 1 3 0 8
0 0 5
0 2 5
```

1 1 5  
1 3 5  
2 0 5  
2 2 5  
3 1 5  
3 3 5  
2 2 3 0 10  
0 0 5  
0 1 5  
1 0 5  
1 1 5  
1 2 5  
2 1 5  
2 2 5  
2 3 5  
3 2 5  
3 3 5  
1 0 0 2  
1 1  
3 1  
1 1 0 2  
1 1  
2 1  
1 2 0 2  
1 1  
2 1  
1 3 0 2  
0 1  
2 1

### 3.2 Variable and cost function modeling

Modeling a Weighted CSP consists in creating variables and cost functions.

Domains of variables can be of two different types:

- enumerated domain allowing direct access to each value (array) and iteration on current domain in times proportional to the current number of values (double-linked list)
- interval domain represented by a lower value and an upper value only (useful for large domains)

#### Warning

Current implementation of `toulbar2` has limited modeling and solving facilities for interval domains. There is no cost functions accepting both interval and enumerated variables for the moment, which means all the variables should have the same type.

Cost functions can be defined in extension (table or maps) or having a specific semantic.

Cost functions in extension depend on their arity:

- unary cost function (directly associated to an enumerated variable)
- binary and ternary cost functions (table of costs)
- n-ary cost functions ( $n \geq 4$ ) defined by a list of tuples with associated costs and a default cost for missing tuples (allows for a compact representation)

Cost functions having a specific semantic (see [Weighted Constraint Satisfaction Problem file format \(wcsp\)](#)) are:

- simple arithmetic and scheduling (temporal disjunction) cost functions on interval variables
- global cost functions (eg soft alldifferent, soft global cardinality constraint, soft same, soft regular, etc) with three different propagator keywords:
  - *flow* propagator based on flow algorithms with "s" prefix in the keyword (*salldiff*, *sgcc*, *ssame*, *sregular*)
  - *DAG* propagator based on dynamic programming algorithms with "s" prefix and "dp" postfix (*samongdp*, *salldifdp*, *sgccdp*, *sregulardp*, *sgrammardp*, *smstdp*, *smaxdp*)
  - *network* propagator based on cost function network decomposition with "w" prefix (*wsum*, *wvarsum*, *walldiff*, *wgcc*, *wsame*, *wsamegcc*, *wregular*, *wamong*, *wvamong*, *woverlap*)

#### Note

The default semantics (using *var* keyword) of monolithic (flow and DAG-based propagators) global cost functions is to count the number of variables to change in order to restore consistency and to multiply it by the basecost. Other particular semantics may be used in conjunction with the flow-based propagator

The semantics of the network-based propagator approach is either a hard constraint ("hard" keyword) or a soft constraint by multiplying the number of changes by the basecost ("lin" or "var" keyword) or by multiplying the square value of the number of changes by the basecost ("quad" keyword)

A decomposable version exists for each monolithic global cost function, except grammar and MST. The decomposable ones may propagate less than their monolithic counterpart and they introduce extra variables but they can be much faster in practice

#### Warning

Each global cost function may have less than three propagators implemented

Current implementation of `toulbar2` has limited solving facilities for monolithic global cost functions (no BTD-like methods nor variable elimination)

Current implementation of `toulbar2` disallows global cost functions with less than or equal to three variables in their scope (use cost functions in extension instead)

Before modeling the problem using `make` and `post`, call `::tb2init` method to initialize `toulbar2` global variables

After modeling the problem using `make` and `post`, call [WeightedCSP::sortConstraints](#) method to initialize correctly the model before solving it

### 3.3 Solving cost function networks

After creating a Weighted CSP, it can be solved using a local search method INCOP (see [WeightedCSPSolver::narycsp](#)) and/or an exact B&B search method (see [WeightedCSPSolver::solve](#)).

Various options of the solving methods are controlled by `::Toulbar2` static class members (see files `src/tb2types.hpp` and `src/tb2main.cpp`).

A brief code example reading a wcsp problem given as a single command-line parameter and solving it:

```
#include "toulbar2lib.hpp"
#include <string.h>
#include <stdio.h>
#include <stdlib.h>
#include <unistd.h>
int main(int argc, char **argv) {

    tb2init(); // must be call before setting specific ToulBar2 options and creating a model

    // Create a solver object
    WeightedCSPSolver *solver =
        WeightedCSPSolver::makeWeightedCSPSolver(MAX_COST);

    // Read a problem file in wcsp format
    solver->read_wcsp(argv[1]);

    ToulBar2::verbose = -1; // change to 0 or higher values to see more trace information

    // Uncomment if solved using INCOP local search followed by a partial Limited Discrepancy Search with a
    // maximum discrepancy of one
    // ToulBar2::incop_cmd = "0 1 3 idwa 100000 cv v 0 200 1 0 0";
    // ToulBar2::lds = -1; // remove it or change to a positive value then the search continues by a
    // complete B&B search method

    if (solver->solve()) {
        // show (sub-)optimal solution
        vector<Value> sol;
        Cost ub = solver->getSolution(sol);
        cout << "Best solution found cost: " << ub << endl;
        cout << "Best solution found:";
        for (unsigned int i=0; i<sol.size(); i++) cout << ((i>0)?",":"") << " x" << i << " = " << sol[i];
        cout << endl;
    } else {
        cout << "No solution found!" << endl;
    }
    delete solver;
}
```

#### See Also

another code example in `src/toulbar2test.cpp`

#### Warning

variable domains must start at zero, otherwise recompile `libtb2.so` without flag `WCSPFORMATONLY`

### 3.4 Output messages, verbosity options and debugging

Depending on verbosity level given as option "-v=level", `toulbar2` will output:

- (level=0, no verbosity) default output mode: shows version number, number of variables and cost functions read in the problem file, number of unassigned variables and cost functions after preprocessing, problem upper and lower bounds after preprocessing. Outputs current best solution cost found, ends by giving the optimum or "No solution". Last output line should always be: "end."
  - (level=-1, no verbosity) restricted output mode: do not print current best solution cost found
1. (level=1) shows also search choices ("*search\_depth problem\_lower\_bound problem\_upper\_bound sum\_of\_current\_domain\_sizes*") Try" *variable\_index operator value*) with *operator* being assignment ("="), value removal ("!="), domain splitting ("<=" or ">=", also showing EAC value in parenthesis)
  2. (level=2) shows also current domains (*variable\_index list\_of\_current\_domain\_values "/" number\_of\_cost\_functions* (see approximate degree in [Variable elimination](#)) "/" *weighted\_degree list\_of\_unary\_costs "s:" support\_value*) before each search choice and reports problem lower bound increases, NC bucket sort data (see [NC bucket sort](#)), and basic operations on domains of variables
  3. (level=3) reports also basic arc EPT operations on cost functions (see [Soft arc consistency and problem reformulation](#))
  4. (level=4) shows also current list of cost functions for each variable and reports more details on arc EPT operations (showing all changes in cost functions)
  5. (level=5) reports more details on cost functions defined in extension giving their content (cost table by first increasing values in the current domain of the last variable in the scope)

For debugging purposes, another option "-Z=level" allows to monitor the search:

1. (level 1) shows current search depth (number of search choices from the root of the search tree) and reports statistics on nogoods for BTD-like methods
2. (level 2) idem
3. (level 3) also saves current problem into a file before each search choice

#### Note

`toulbar2`, compiled in debug mode, can be more verbose and it checks a lot of assertions (pre/post conditions in the code)

`toulbar2` will output an help message giving available options if run without any parameters

### 3.5 Preprocessing techniques

Depending on `toulbar2` options, the sequence of preprocessing techniques applied before the search is:

1. *i*-bounded variable elimination with user-defined *i* bound
2. pairwise decomposition of cost functions (binary cost functions are implicitly decomposed by soft AC and empty cost function removals)
3. MinSumDiffusion propagation (see VAC)
4. projects&subtracts n-ary cost functions in extension on all the binary cost functions inside their scope ( $3 < n < \text{max}$ , see `toulbar2` options)
5. functional variable elimination (see [Variable elimination](#))
6. projects&subtracts ternary cost functions in extension on their three binary cost functions inside their scope (before that, extends the existing binary cost functions to the ternary cost function and applies pairwise decomposition)
7. creates new ternary cost functions for all triangles (*ie* occurrences of three binary cost functions *xy*, *yz*, *zx*)
8. removes empty cost functions while repeating #1 and #2 until no new cost functions can be removed

#### Note

the propagation loop is called after each preprocessing technique (see `WCSP::propagate`)

### 3.6 Variable and value search ordering heuristics

#### See Also

*Boosting Systematic Search by Weighting Constraints* . Frederic Boussemart, Fred Hemery, Christophe Lecoutre, Lakhdar Sais. Proc. of ECAI 2004, pages 146-150. Valencia, Spain, 2004.

*Last Conflict Based Reasoning* . Christophe Lecoutre, Lakhdar Sais, Sebastien Tabary, Vincent Vidal. Proc. of ECAI 2006, pages 133-137. Trentino, Italy, 2006.



### 3.7 Soft arc consistency and problem reformulation

Soft arc consistency is an incremental lower bound technique for optimization problems. Its goal is to move costs from high-order (typically arity two or three) cost functions towards the problem lower bound and unary cost functions. This is achieved by applying iteratively local equivalence-preserving problem transformations (EPTs) until some terminating conditions are met.

#### Note

*eg* an EPT can move costs between a binary cost function and a unary cost function such that the sum of the two functions remains the same for any complete assignment.

#### See Also

*Arc consistency for Soft Constraints.* T. Schiex. Proc. of CP'2000. Singapour, 2000.

#### Note

Soft Arc Consistency in *toulbar2* is limited to binary and ternary and some global cost functions (*eg* *alldifferent*, *gcc*, *regular*, *same*). Other *n*-ary cost functions are delayed for propagation until their number of unassigned variables is three or less.

#### See Also

*Towards Efficient Consistency Enforcement for Global Constraints in Weighted Constraint Satisfaction.* Jimmy Ho-Man Lee, Ka Lun Leung. Proc. of IJCAI 2009, pages 559-565. Pasadena, USA, 2009.

### 3.8 Virtual Arc Consistency enforcing

The three phases of VAC are enforced in three different "Pass". Bool(P) is never built. Instead specific functions (getVACCost) booleanize the WCSP on the fly. The domain variables of Bool(P) are the original variable domains (saved and restored using trailing at each iteration) All the counter data-structures (k) are timestamped to avoid clearing them at each iteration.

#### Note

Simultaneously AC (and potentially DAC, EAC) are maintained by proper queuing.

#### See Also

*Soft Arc Consistency Revisited.* Cooper et al. Artificial Intelligence. 2010.

### 3.9 NC bucket sort

maintains a sorted list of variables having non-zero unary costs in order to make NC propagation incremental.

- variables are sorted into buckets
- each bucket is associated to a single interval of non-zero costs (using a power-of-two scaling, first bucket interval is  $[1,2[$ , second interval is  $[2,4[$ , etc.)
- each variable is inserted into the bucket corresponding to its largest unary cost in its domain
- variables having all unary costs equal to zero do not belong to any bucket

NC propagation will revise only variables in the buckets associated to costs sufficiently large wrt current objective bounds.

### 3.10 Variable elimination

- *i*-bounded variable elimination eliminates all variables with a degree less than or equal to *i*. It can be done with arbitrary *i*-bound in preprocessing only and iff all their cost functions are in extension.
- *i*-bounded variable elimination with *i*-bound less than or equal to two can be done during the search.
- functional variable elimination eliminates all variables which have a bijective or functional binary hard constraint (*ie* ensuring a one-to-one or several-to-one value mapping) and iff all their cost functions are in extension. It can be done without limit on their degree, in preprocessing only.

#### Note

Variable elimination order used in preprocessing is either lexicographic or given by an external file \*.order (see toulbar2 options)

2-bounded variable elimination during search is optimal in the sense that any elimination order should result in the same final graph

#### Warning

It is not possible to display/save solutions when bounded variable elimination is applied in preprocessing. toulbar2 maintains a list of current cost functions for each variable. It uses the size of these lists as an approximation of variable degrees. During the search, if variable *x* has three cost functions *xy*, *xz*, *xyz*, its true degree is two but its approximate degree is three. In toulbar2 options, it is the approximate degree which is given by the user for variable elimination during the search (thus, a value at most three). But it is the true degree which is given by the user for variable elimination in preprocessing.

### 3.11 Propagation loop

Propagates soft local consistencies and bounded variable elimination until all the propagation queues are empty or a contradiction occurs.

While (queues are not empty or current objective bounds have changed):

1. queue for bounded variable elimination of degree at most two (except at preprocessing)
2. BAC queue
3. EAC queue
4. DAC queue
5. AC queue
6. monolithic (flow-based and DAG-based) global cost function propagation (partly incremental)
7. NC queue
8. returns to #1 until all the previous queues are empty
9. DEE queue
10. returns to #1 until all the previous queues are empty
11. VAC propagation (not incremental)
12. returns to #1 until all the previous queues are empty (and problem is VAC if enable)
13. exploits goods in pending separators for BTD-like methods

Queues are first-in / first-out lists of variables (avoiding multiple insertions). In case of a contradiction, queues are explicitly emptied by `WCSP::whenContradiction`

### 3.12 Backtrack management

Used by backtrack search methods. Allows to copy / restore the current state using `Store::store` and `Store::restore` methods. All storable data modifications are trailed into specific stacks.

Trailing stacks are associated to each storable type:

- `Store::storeValue` for storable domain values `::StoreValue` (value supports, etc)
- `Store::storeCost` for storable costs `::StoreCost` (inside cost functions, etc)
- `Store::storeDomain` for enumerated domains (to manage holes inside domains)
- `Store::storeConstraint` for backtrackable lists of constraints
- `Store::storeVariable` for backtrackable lists of variables
- `Store::storeSeparator` for backtrackable lists of separators (see tree decomposition methods)
- `Store::storeBigInteger` for very large integers `::StoreBigInteger` used in solution counting methods

Memory for each stack is dynamically allocated by part of  $2^x$  with  $x$  initialized to `::STORE_SIZE` and increased when needed.

#### Note

storable data are not trailed at depth 0.

#### Warning

`::StoreInt` uses `Store::storeValue` stack (it assumes `Value` is encoded as `int!`).

Current storable data management is not multi-threading safe! (`Store` is a static virtual class relying on `Store-Basic<T>` static members)

## 4 Class Documentation

### 4.1 WeightedCSP Class Reference

#### Public Member Functions

- virtual int [getIndex](#) () const =0  
*instantiation occurrence number of current WCSP object*
- virtual string [getName](#) () const =0  
*WCSP filename (without its extension)*
- virtual void \* [getSolver](#) () const =0  
*special hook to access solver information*
- virtual Cost [getLb](#) () const =0  
*gets problem lower bound*
- virtual Cost [getUb](#) () const =0  
*gets problem upper bound*
- virtual void [updateUb](#) (Cost newUb)=0  
*sets initial problem upper bound and each time a new solution is found*
- virtual void [enforceUb](#) ()=0  
*enforces problem upper bound when exploring an alternative search node*
- virtual void [increaseLb](#) (Cost addLb)=0  
*increases problem lower bound thanks to eg soft local consistencies*
- virtual Cost [finiteUb](#) () const =0  
*computes the worst-case assignment finite cost (sum of maximum finite cost over all cost functions plus one)*
- virtual void [setInfiniteCost](#) ()=0  
*updates infinite costs in all cost functions accordingly to the problem global lower and upper bounds*
- virtual bool [enumerated](#) (int varIndex) const =0  
*true if the variable has an enumerated domain*
- virtual string [getName](#) (int varIndex) const =0
- virtual Value [getInf](#) (int varIndex) const =0  
*minimum current domain value*
- virtual Value [getSup](#) (int varIndex) const =0  
*maximum current domain value*
- virtual Value [getValue](#) (int varIndex) const =0  
*current assigned value*
- virtual unsigned int [getDomainSize](#) (int varIndex) const =0  
*current domain size*
- virtual bool [getEnumDomain](#) (int varIndex, Value \*array)=0  
*gets current domain values in an array*
- virtual bool [getEnumDomainAndCost](#) (int varIndex, ValueCost \*array)=0  
*gets current domain values and unary costs in an array*
- virtual unsigned int [getDomainInitSize](#) (int varIndex) const =0  
*gets initial domain size (warning! assumes EnumeratedVariable)*
- virtual Value [toValue](#) (int varIndex, unsigned int idx)=0  
*gets value from index (warning! assumes EnumeratedVariable)*
- virtual unsigned int [toIndex](#) (int varIndex, Value value)=0  
*gets index from value (warning! assumes EnumeratedVariable)*
- virtual int [getDACOrder](#) (int varIndex) const =0  
*index of the variable in the DAC variable ordering*
- virtual Value [nextValue](#) (int varIndex, Value v) const =0  
*first value after v in the current domain or v if there is no value*

- virtual void [increase](#) (int varIndex, Value newInf)=0  
*changes domain lower bound*
- virtual void [decrease](#) (int varIndex, Value newSup)=0  
*changes domain upper bound*
- virtual void [assign](#) (int varIndex, Value newValue)=0  
*assigns a variable and immediately propagates this assignment*
- virtual void [remove](#) (int varIndex, Value remValue)=0  
*removes a domain value (valid if done for an enumerated variable or on its domain bounds)*
- virtual void [assignLS](#) (vector< int > &varIndexes, vector< Value > &newValues)=0  
*assigns a set of variables at once and propagates (used by Local Search methods such as Large Neighborhood Search)*
- virtual Cost [getUnaryCost](#) (int varIndex, Value v) const =0  
*unary cost associated to a domain value*
- virtual Cost [getMaxUnaryCost](#) (int varIndex) const =0  
*maximum unary cost in the domain*
- virtual Value [getMaxUnaryCostValue](#) (int varIndex) const =0  
*a value having the maximum unary cost in the domain*
- virtual Value [getSupport](#) (int varIndex) const =0  
*NC/EAC unary support value.*
- virtual Value [getBestValue](#) (int varIndex) const =0  
*hint for some value ordering heuristics (only used by RDS)*
- virtual void [setBestValue](#) (int varIndex, Value v)=0  
*hint for some value ordering heuristics (only used by RDS)*
- virtual bool [getIsPartOfOptimalSolution](#) ()=0  
*special flag used for debugging purposes only*
- virtual void [setIsPartOfOptimalSolution](#) (bool v)=0  
*special flag used for debugging purposes only*
- virtual int [getDegree](#) (int varIndex) const =0  
*approximate degree of a variable (ie number of active cost functions, see [Variable elimination](#))*
- virtual int [getTrueDegree](#) (int varIndex) const =0  
*degree of a variable*
- virtual Long [getWeightedDegree](#) (int varIndex) const =0  
*weighted degree heuristic*
- virtual void [resetWeightedDegree](#) (int varIndex)=0  
*initialize weighted degree heuristic*
- virtual void [preprocessing](#) ()=0  
*applies various preprocessing techniques to simplify the current problem*
- virtual void [sortConstraints](#) ()=0  
*sorts the list of cost functions associated to each variable based on smallest problem variable indexes*
- virtual void [whenContradiction](#) ()=0  
*after a contradiction, resets propagation queues*
- virtual void [propagate](#) ()=0  
*propagates until a fix point is reached (or throws a contradiction)*
- virtual bool [verify](#) ()=0  
*checks the propagation fix point is reached*
- virtual unsigned int [numberOfVariables](#) () const =0  
*number of created variables*
- virtual unsigned int [numberOfUnassignedVariables](#) () const =0  
*current number of unassigned variables*
- virtual unsigned int [numberOfConstraints](#) () const =0  
*initial number of cost functions (before variable elimination)*



- virtual unsigned int `numberOfConnectedConstraints` () const =0  
*current number of cost functions*
- virtual unsigned int `numberOfConnectedBinaryConstraints` () const =0  
*current number of binary cost functions*
- virtual unsigned int `medianDomainSize` () const =0  
*median current domain size of variables*
- virtual unsigned int `medianDegree` () const =0  
*median current degree of variables*
- virtual int `getMaxDomainSize` ()=0  
*maximum initial domain size found in all variables*
- virtual Value `getDomainSizeSum` ()=0  
*total sum of current domain sizes*
- virtual void `cartProd` (BigInteger &cartesianProduct)=0  
*Cartesian product of current domain sizes.*
- virtual Long `getNbDEE` () const =0  
*number of value removals due to dead-end elimination*
- virtual int `makeEnumeratedVariable` (string n, Value iinf, Value isup)=0  
*create an enumerated variable with its domain bounds*
- virtual int `makeEnumeratedVariable` (string n, Value \*d, int dsize)=0  
*create an enumerated variable with its domain values*
- virtual int `makeIntervalVariable` (string n, Value iinf, Value isup)=0  
*create an interval variable with its domain bounds*
- virtual void `postUnary` (int xIndex, vector< Cost > &costs)=0
- virtual void `postNaryConstraintTuple` (int ctrindex, Value \*tuple, int arity, Cost cost)=0
- virtual int `postUnary` (int xIndex, Value \*d, int dsize, Cost penalty)=0
- virtual int `postGlobalConstraint` (int \*scopeIndex, int arity, string &gname, istream &file, int \*constrcounter=N-ULL)=0
- virtual int `postWAmong` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, const vector< Value > &values, int lb, int ub)=0  
*post a soft among cost function*
- virtual void `postWAmong` (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int lb, int ub)=0
- virtual void `postWVarAmong` (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int varIndex)=0  
*post a weighted among cost function with the number of values encoded as a variable with index varIndex (network-based propagator only)*
- virtual int `postWRegular` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, int nbStates, const vector< WeightedObj< int > > &initial\_States, const vector< WeightedObj< int > > &accepting\_States, const vector< DFATransition > &Wtransitions)=0  
*post a soft or weighted regular cost function*
- virtual void `postWRegular` (int \*scopeIndex, int arity, int nbStates, vector< pair< int, Cost > > initial\_States, vector< pair< int, Cost > > accepting\_States, int \*\*Wtransitions, vector< Cost > transitionsCosts)=0
- virtual int `postWAlldiff` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost)=0  
*post a soft alldifferent cost function*
- virtual void `postWAlldiff` (int \*scopeIndex, int arity, string semantics, Cost baseCost)=0
- virtual int `postWGcc` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, const vector< BoundedObj< Value > > &values)=0  
*post a soft global cardinality cost function*
- virtual void `postWGcc` (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int \*lb, int \*ub)=0
- virtual int `postWSame` (int \*scopeIndexG1, int arityG1, int \*scopeIndexG2, int arityG2, const string &semantics, const string &propagator, Cost baseCost)=0

- post a soft same cost function (a group of variables being a permutation of another group with the same size)*
- virtual void `postWSame` (int \*scopeIndex, int arity, string semantics, Cost baseCost)=0
- virtual void `postWSameGcc` (int \*scopeIndex, int arity, string semantics, Cost baseCost, Value \*values, int nbValues, int \*lb, int \*ub)=0
- post a combination of a same and gcc cost function decomposed as a cost function network*
- virtual int `postWGrammarCNF` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, int nbSymbols, int startSymbol, const vector< CFGProductionRule > WRuleToTerminal)=0
- post a soft/weighted grammar cost function with the dynamic programming propagator and grammar in Chomsky normal form*
- virtual int `postMST` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost)=0
- post a Spanning Tree hard constraint*
- virtual int `postMaxWeight` (int \*scopeIndex, int arity, const string &semantics, const string &propagator, Cost baseCost, const vector< WeightedVarValPair > weightFunction)=0
- post a weighted max cost function (maximum cost of a set of unary cost functions associated to a set of variables)*
- virtual void `postWSum` (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes)=0
- post a soft linear constraint with unit coefficients*
- virtual void `postWVarSum` (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int varIndex)=0
- post a soft linear constraint with unit coefficients and variable right-hand side*
- virtual void `postWOverlap` (int \*scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes)=0
- post a soft overlap cost function (a group of variables being point-wise equivalent – and not equal to zero – to another group with the same size)*
- virtual vector< vector< int > > \* `getListSuccessors` ()=0
- generating additional variables vector created when berge decomposition are included in the WCSP*
- virtual bool `isGlobal` ()=0
- true if there are soft global constraints defined in the problem*
- virtual void `read_wcsp` (const char \*fileName)=0
- load problem in native wcsp format (Weighted Constraint Satisfaction Problem file format (wcsp))*
- virtual void `read_uai2008` (const char \*fileName)=0
- load problem in UAI 2008 format (see <http://graphmod.ics.uci.edu/uai08/FileFormat> and <http://www.cs.huji.ac.il/project/UAI10/fileFormat.php>)*
- virtual void `read_random` (int n, int m, vector< int > &p, int seed, bool forceSubModular=false, string globalName="")=0
- create a random WCSP with n variables, domain size m, array p where the first element is a percentage of tuples with a nonzero cost and next elements are the number of random cost functions for each different arity (starting with arity two), random seed, a flag to have a percentage (last element in the array p) of the binary cost functions being permuted submodular, and a string to use a specific global cost function instead of random cost functions in extension*
- virtual void `read_wcnf` (const char \*fileName)=0
- load problem in (w)cnf format (see <http://www.maxsat.udl.cat/08/index.php?disp=requirements>)*
- virtual void `read_qpbo` (const char \*fileName)=0
- load quadratic pseudo-Boolean optimization problem in unconstrained quadratic programming text format (first text line with n, number of variables and m, number of triplets, followed by the m triplets (x,y,cost) describing the sparse symmetric nXn cost matrix with variable indexes such that x <= y and any positive or negative real numbers for costs)*
- virtual const vector< Value > & `getSolution` ()=0
- returns current best solution*
- virtual void `setSolution` (TAssign \*sol=NULL)=0
- set best solution from current assigned values or from a given assignment (for BTD-like methods)*
- virtual void `printSolution` (ostream &os)=0
- prints current best solution*
- virtual void `print` (ostream &os)=0

*print current domains and active cost functions (see [Output messages, verbosity options and debugging](#))*

- virtual void `dump` (ostream &os, bool original=true)=0

*output the current WCSP into a file in wcsp format*

#### Static Public Member Functions

- static `WeightedCSP * makeWeightedCSP` (Cost upperBound, void \*solver=NULL)

*Weighted CSP factory.*

#### 4.1.1 Detailed Description

Abstract class `WeightedCSP` representing a weighted constraint satisfaction problem

- problem lower and upper bounds
- list of variables with their finite domains (either represented by an enumerated list of values, or by a single interval)
- list of cost functions (created before and during search by variable elimination of variables with small degree)
- local consistency propagation (variable-based propagation) including cluster tree decomposition caching (separator-based cache)

#### Note

Variables are referenced by their lexicographic index number (as returned by eg `WeightedCSP::makeEnumeratedVariable`)

Cost functions are referenced by their lexicographic index number (as returned by eg `WeightedCSP::postBinaryConstraint`)

#### 4.1.2 Member Function Documentation

**4.1.2.1** virtual void `WeightedCSP::assignLS` ( vector< int > & *varIndexes*, vector< Value > & *newValues* ) [pure virtual]

assigns a set of variables at once and propagates (used by Local Search methods such as Large Neighborhood Search)

##### Parameters

<i>varIndexes</i>	vector of variable indexes as returned by <code>makeXXXVariable</code>
<i>newValues</i>	vector of values to be assigned to the corresponding variables

**4.1.2.2** virtual void `WeightedCSP::cartProd` ( BigInteger & *cartesianProduct* ) [pure virtual]

Cartesian product of current domain sizes.

##### Parameters

<i>cartesianProduct</i>	result obtained by the GNU Multiple Precision Arithmetic Library GMP
-------------------------	--

**4.1.2.3** virtual void `WeightedCSP::dump` ( ostream & *os*, bool *original* =true ) [pure virtual]

output the current WCSP into a file in wcsp format

## Parameters

<i>os</i>	output file
<i>original</i>	if true then keeps all variables with their original domain size else uses unassigned variables and current domains recoding variable indexes

## 4.1.2.4 virtual Cost WeightedCSP::finiteUb ( ) const [pure virtual]

computes the worst-case assignment finite cost (sum of maximum finite cost over all cost functions plus one)

## Returns

the worst-case assignment finite cost

## Warning

current problem should be completely loaded and propagated before calling this function

## 4.1.2.5 virtual string WeightedCSP::getName ( int varIndex ) const [pure virtual]

## Note

by default, variables names are integers, starting at zero

## 4.1.2.6 virtual Value WeightedCSP::getValue ( int varIndex ) const [pure virtual]

current assigned value

## Warning

undefined if not assigned yet

## 4.1.2.7 virtual void WeightedCSP::increaseLb ( Cost addLb ) [pure virtual]

increases problem lower bound thanks to *eg* soft local consistencies

## Parameters

<i>addLb</i>	increment value to be <b>added</b> to the problem lower bound
--------------	---

## 4.1.2.8 virtual int WeightedCSP::postGlobalConstraint ( int \* scopeIndex, int arity, string &amp; gcname, istream &amp; file, int \* constrcounter = NULL ) [pure virtual]

## 4.1.2.9 virtual int WeightedCSP::postMaxWeight ( int \* scopeIndex, int arity, const string &amp; semantics, const string &amp; propagator, Cost baseCost, const vector&lt; WeightedVarValPair &gt; weightFunction ) [pure virtual]

post a weighted max cost function (maximum cost of a set of unary cost functions associated to a set of variables)

## Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of <i>scopeIndex</i>
<i>semantics</i>	the semantics of the global cost function: "val"
<i>propagator</i>	the propagation method ("DAG" only)

<i>baseCost</i>	if a variable-value pair does not exist in <i>weightFunction</i> , its weight will be mapped to base-Cost.
<i>weightFunction</i>	a vector of <code>WeightedVarValPair</code> containing a mapping from variable-value pairs to their weights.

4.1.2.10 `virtual int WeightedCSP::postMST ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost ) [pure virtual]`

post a Spanning Tree hard constraint

Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of <i>scopeIndex</i>
<i>semantics</i>	the semantics of the global cost function: "hard"
<i>propagator</i>	the propagation method ("DAG" only)
<i>baseCost</i>	unused in the current implementation (MAX_COST)

4.1.2.11 `virtual void WeightedCSP::postNaryConstraintTuple ( int ctrindex, Value * tuple, int arity, Cost cost ) [pure virtual]`

Warning

must call `WeightedCSP::postNaryConstraintEnd` after giving cost tuples

4.1.2.12 `virtual void WeightedCSP::postUnary ( int xIndex, vector< Cost > & costs ) [pure virtual]`

4.1.2.13 `virtual int WeightedCSP::postUnary ( int xIndex, Value * d, int dsize, Cost penalty ) [pure virtual]`

Warning

must call [WeightedCSP::sortConstraints](#) after all cost functions have been posted (see [WeightedCSP::sortConstraints](#))

4.1.2.14 `virtual int WeightedCSP::postWAlldiff ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost ) [pure virtual]`

post a soft alldifferent cost function

Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of the array
<i>semantics</i>	the semantics of the global cost function: for flow-based propagator: "var" or "dec" or "decbi" (decomposed into a binary cost function complete network), for DAG-based propagator: "var", for network-based propagator: "hard" or "lin" or "quad" (decomposed based on wa-mong)
<i>propagator</i>	the propagation method ("flow", "DAG", "network")
<i>baseCost</i>	the scaling factor of the violation

4.1.2.15 `virtual void WeightedCSP::postWAlldiff ( int * scopeIndex, int arity, string semantics, Cost baseCost ) [pure virtual]`

4.1.2.16 `virtual int WeightedCSP::postWAmong ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, const vector< Value > & values, int lb, int ub ) [pure virtual]`

post a soft among cost function

## Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of the array
<i>semantics</i>	the semantics of the global cost function: "var" or – "hard" or "lin" or "quad" (network-based propagator only)–
<i>propagator</i>	the propagation method (only "DAG" or "network")
<i>baseCost</i>	the scaling factor of the violation
<i>values</i>	a vector of values to be restricted
<i>lb</i>	a fixed lower bound for the number variables to be assigned to the values in <i>values</i>
<i>ub</i>	a fixed upper bound for the number variables to be assigned to the values in <i>values</i>

4.1.2.17 `virtual void WeightedCSP::postWAmong ( int * scopeIndex, int arity, string semantics, Cost baseCost, Value * values, int nbValues, int lb, int ub )` [pure virtual]

4.1.2.18 `virtual int WeightedCSP::postWGcc ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, const vector< BoundedObj< Value > > & values )` [pure virtual]

post a soft global cardinality cost function

## Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of the array
<i>semantics</i>	the semantics of the global cost function: "var" (DAG-based propagator only) or – "var" or "dec" or "wdec" (flow-based propagator only) or – "hard" or "lin" or "quad" (network-based propagator only)–
<i>propagator</i>	the propagation method ("flow", "DAG", "network")
<i>baseCost</i>	the scaling factor of the violation
<i>values</i>	a vector of BoundedObj, specifying the lower and upper bounds of each value, restricting the number of variables can be assigned to them

4.1.2.19 `virtual void WeightedCSP::postWGcc ( int * scopeIndex, int arity, string semantics, Cost baseCost, Value * values, int nbValues, int * lb, int * ub )` [pure virtual]

4.1.2.20 `virtual int WeightedCSP::postWGrammarCNF ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, int nbSymbols, int startSymbol, const vector< CFGProductionRule > WRuleToTerminal )` [pure virtual]

post a soft/weighted grammar cost function with the dynamic programming propagator and grammar in Chomsky normal form

## Parameters

<i>scopeIndex</i>	an array of the first group of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of <i>scopeIndex</i>
<i>semantics</i>	the semantics of the global cost function: "var" or "weight"
<i>propagator</i>	the propagation method ("DAG" only)
<i>baseCost</i>	the scaling factor of the violation
<i>nbSymbols</i>	the number of symbols in the corresponding grammar. Symbols are indexed as 0, 1, ..., nbSymbols-1
<i>startSymbol</i>	the index of the starting symbol
<i>WRuleToTerminal</i>	a vector of <code>::CFGProductionRule</code> . Note that: <ul style="list-style-type: none"> <li>if <i>order</i> in <i>CFGProductionRule</i> is set to 0, it is classified as <math>A \rightarrow v</math>, where A is the index of the terminal symbol and v is the value.</li> <li>if <i>order</i> in <i>CFGProductionRule</i> is set to 1, it is classified as <math>A \rightarrow BC</math>, where A,B,C the index of the nonterminal symbols.</li> <li>if <i>order</i> in <i>CFGProductionRule</i> is set to 2, it is classified as weighted <math>A \rightarrow v</math>, where A is the index of the terminal symbol and v is the value.</li> <li>if <i>order</i> in <i>CFGProductionRule</i> is set to 3, it is classified as weighted <math>A \rightarrow BC</math>, where A,B,C the index of the nonterminal symbols.</li> <li>if <i>order</i> in <i>CFGProductionRule</i> is set to values greater than 3, it is ignored.</li> </ul>

4.1.2.21 `virtual void WeightedCSP::postWOverlap ( int * scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes ) [pure virtual]`

post a soft overlap cost function (a group of variables being point-wise equivalent – and not equal to zero – to another group with the same size)

## Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of <i>scopeIndex</i> (should be an even value)
<i>semantics</i>	the semantics of the global cost function: "hard" or "lin" or "quad" (network-based propagator only)
<i>propagator</i>	the propagation method ("network" only)
<i>baseCost</i>	the scaling factor of the violation.
<i>comparator</i>	the point-wise comparison operator applied to the number of equivalent variables ("==", "!=", "<", "<=", ">", ">=")
<i>rightRes</i>	right-hand side value of the comparison

4.1.2.22 `virtual int WeightedCSP::postWRegular ( int * scopeIndex, int arity, const string & semantics, const string & propagator, Cost baseCost, int nbStates, const vector< WeightedObj< int > > & initial_States, const vector< WeightedObj< int > > & accepting_States, const vector< DFATransition > & Wtransitions ) [pure virtual]`

post a soft or weighted regular cost function

## Parameters

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of the array

<i>semantics</i>	the semantics of the soft global cost function: "var" or "edit" (flow-based propagator) or – "var" (DAG-based propagator)– (unused parameter for network-based propagator)
<i>propagator</i>	the propagation method ("flow", "DAG", "network")
<i>baseCost</i>	the scaling factor of the violation ("flow", "DAG")
<i>nbStates</i>	the number of the states in the corresponding DFA. The states are indexed as 0, 1, ..., nb-States-1
<i>initial_States</i>	a vector of WeightedObj specifying the starting states with weight
<i>accepting_States</i>	a vector of WeightedObj specifying the final states
<i>Wtransitions</i>	a vector of (weighted) transitions

**Warning**

Weights are ignored in the current implementation of DAG and flow-based propagators

**4.1.2.23** `virtual void WeightedCSP::postWRegular ( int * scopeIndex, int arity, int nbStates, vector< pair< int, Cost > > initial_States, vector< pair< int, Cost > > accepting_States, int ** Wtransitions, vector< Cost > transitionsCosts )` [pure virtual]

**4.1.2.24** `virtual int WeightedCSP::postWSame ( int * scopeIndexG1, int arityG1, int * scopeIndexG2, int arityG2, const string & semantics, const string & propagator, Cost baseCost )` [pure virtual]

post a soft same cost function (a group of variables being a permutation of another group with the same size)

**Parameters**

<i>scopeIndexG1</i>	an array of the first group of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arityG1</i>	the size of <i>scopeIndexG1</i>
<i>scopeIndexG2</i>	an array of the second group of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arityG2</i>	the size of <i>scopeIndexG2</i>
<i>semantics</i>	the semantics of the global cost function: "var" or – "hard" or "lin" or "quad" (network-based propagator only)–
<i>propagator</i>	the propagation method ("flow" or "network")
<i>baseCost</i>	the scaling factor of the violation.

**4.1.2.25** `virtual void WeightedCSP::postWSame ( int * scopeIndex, int arity, string semantics, Cost baseCost )` [pure virtual]

**4.1.2.26** `virtual void WeightedCSP::postWSum ( int * scopeIndex, int arity, string semantics, Cost baseCost, string comparator, int rightRes )` [pure virtual]

post a soft linear constraint with unit coefficients

**Parameters**

<i>scopeIndex</i>	an array of variable indexes as returned by <a href="#">WeightedCSP::makeEnumeratedVariable</a>
<i>arity</i>	the size of <i>scopeIndex</i>
<i>semantics</i>	the semantics of the global cost function: "hard" or "lin" or "quad" (network-based propagator only)
<i>propagator</i>	the propagation method ("network" only)
<i>baseCost</i>	the scaling factor of the violation
<i>comparator</i>	the comparison operator of the linear constraint ("==", "!=", "<", "<=", ">", ">=")



<i>rightRes</i>	right-hand side value of the linear constraint
-----------------	--

4.1.2.27 `virtual void WeightedCSP::read_uai2008 ( const char * fileName ) [pure virtual]`

load problem in UAI 2008 format (see <http://graphmod.ics.uci.edu/uai08/FileFormat> and <http://www.cs.huji.ac.il/project/UAI10/fileFormat.php>)

#### Warning

UAI10 evidence file format not recognized by toulbar2 as it does not allow multiple evidence (you should remove the first value in the file)

4.1.2.28 `virtual void WeightedCSP::setInfiniteCost ( ) [pure virtual]`

updates infinite costs in all cost functions accordingly to the problem global lower and upper bounds

#### Warning

to be used in preprocessing only

4.1.2.29 `virtual void WeightedCSP::sortConstraints ( ) [pure virtual]`

sorts the list of cost functions associated to each variable based on smallest problem variable indexes

#### Warning

side-effect: updates DAC order according to an existing variable elimination order

#### Note

must be called after creating all the cost functions and before solving the problem

## 4.2 WeightedCSPSolver Class Reference

### Public Member Functions

- virtual `WeightedCSP * getWCSP ()=0`  
*access to its associated Weighted CSP*
- virtual `Long getNbNodes () const =0`  
*number of search nodes (see `WeightedCSPSolver::increase`, `WeightedCSPSolver::decrease`, `WeightedCSPSolver::assign`, `WeightedCSPSolver::remove`)*
- virtual `Long getNbBacktracks () const =0`  
*number of backtracks*
- virtual `void increase (int varIndex, Value value, bool reverse=false)=0`  
*changes domain lower bound and propagates*
- virtual `void decrease (int varIndex, Value value, bool reverse=false)=0`  
*changes domain upper bound and propagates*
- virtual `void assign (int varIndex, Value value, bool reverse=false)=0`  
*assigns a variable and propagates*
- virtual `void remove (int varIndex, Value value, bool reverse=false)=0`  
*removes a domain value and propagates (valid if done for an enumerated variable or on its domain bounds)*
- virtual `void read_wcsp (const char *fileName)=0`  
*reads a WCSP from a file in wcsp text format (can be other formats if using specific `::ToulBar2` global variables)*

- virtual void [read\\_random](#) (int n, int m, vector< int > &p, int seed, bool forceSubModular=false, string global-name="")=0  
*create a random WCSP, see [WeightedCSP::read\\_random](#)*
- virtual bool [solve](#) ()=0  
*simplifies and solves to optimality the problem*
- virtual Cost [narycsp](#) (string cmd, vector< Value > &solution)=0  
*solves the current problem using INCOP local search solver by Bertrand Neveu*
- virtual bool [solve\\_symmax2sat](#) (int n, int m, int \*posx, int \*posy, double \*cost, int \*sol)=0  
*quadratic unconstrained pseudo-Boolean optimization Maximize  $h' \times W \times h$  where  $W$  is expressed by all its non-zero half squared matrix costs (can be positive or negative, with  $\forall i, posx[i] \leq posy[i]$ )*
- virtual void [dump\\_wcsp](#) (const char \*fileName, bool original=true)=0  
*output current problem in a file*
- virtual void [read\\_solution](#) (const char \*fileName)=0  
*read a solution from a file*
- virtual void [parse\\_solution](#) (const char \*certificate)=0  
*read a solution from a string (see ToulBar2 option -x)*
- virtual Cost [getSolution](#) (vector< Value > &solution)=0  
*after solving the problem, add the optimal solution in the input/output vector and returns its optimum cost (warning! do not use it if doing solution counting or if there is no solution, see [WeightedCSPSolver::solve](#) output for that)*

#### Static Public Member Functions

- static [WeightedCSPSolver](#) \* [makeWeightedCSPSolver](#) (Cost initUpperBound)  
*[WeightedCSP](#) Solver factory.*

#### 4.2.1 Detailed Description

Abstract class [WeightedCSPSolver](#) representing a WCSP solver

- link to a [WeightedCSP](#)
- generic complete solving method configurable through global variables (see `::ToulBar2` class and command line options)
- optimal solution available after problem solving
- elementary decision operations on domains of variables
- statistics information (number of nodes and backtracks)
- problem file format reader (multiple formats, see [Weighted Constraint Satisfaction Problem file format \(wcsp\)](#))
- solution checker (output the cost of a given solution)

#### 4.2.2 Member Function Documentation

**4.2.2.1** `virtual void WeightedCSPSolver::dump_wcsp ( const char * fileName, bool original = true )` [pure virtual]

output current problem in a file

See Also

[WeightedCSP::dump](#)

#### 4.2.2.2 virtual Cost WeightedCSPSolver::narycsp ( string cmd, vector< Value > & solution ) [pure virtual]

solves the current problem using INCOP local search solver by Bertrand Neveu

##### Returns

best solution cost found

##### Parameters

<i>cmd</i>	command line argument for narycsp INCOP local search solver (cmd format: lower-bound randomseed nbiterations method nbmoves neighborhoodchoice neighborhoodchoice2 minnbneighbors maxnbneighbors neighborhoodchoice3 autotuning tracemode)
<i>solution</i>	best solution assignment found (MUST BE INITIALIZED WITH A DEFAULT COMPLETE ASSIGNMENT)

##### Warning

cannot solve problems with global cost functions

##### Note

side-effects: updates current problem upper bound and propagates, best solution saved (using WCSP::set-BestValue)

#### 4.2.2.3 virtual bool WeightedCSPSolver::solve ( ) [pure virtual]

simplifies and solves to optimality the problem

##### Returns

false if there is no solution found

##### Warning

after solving, the current problem has been modified by various preprocessing techniques  
DO NOT READ VALUES OF ASSIGNED VARIABLES USING [WeightedCSP::getValue](#) (temporally wrong assignments due to variable elimination in preprocessing) BUT USE [WeightedCSPSolver::getSolution](#) INST-EAD

#### 4.2.2.4 virtual bool WeightedCSPSolver::solve\_symmax2sat ( int n, int m, int \* posx, int \* posy, double \* cost, int \* sol ) [pure virtual]

quadratic unconstrained pseudo-Boolean optimization Maximize  $h' \times W \times h$  where  $W$  is expressed by all its non-zero half squared matrix costs (can be positive or negative, with  $\forall i, posx[i] \leq posy[i]$ )

##### Note

costs for  $posx \neq posy$  are multiplied by 2 by this method  
by convention:  $h = 1 \equiv x = 0$  and  $h = -1 \equiv x = 1$

##### Warning

does not allow infinite costs (no forbidden assignments, unconstrained optimization)

##### Returns

true if at least one solution has been found (array sol being filled with the best solution)

##### See Also

::solvesymmax2sat\_ for Fortran call

## Index

- assignLS
  - WeightedCSP, [26](#)
- Backtrack management, [21](#)
- cartProd
  - WeightedCSP, [26](#)
- dump
  - WeightedCSP, [26](#)
- dump\_wcsp
  - WeightedCSPSolver, [33](#)
- finiteUb
  - WeightedCSP, [27](#)
- getName
  - WeightedCSP, [27](#)
- getValue
  - WeightedCSP, [27](#)
- increaseLb
  - WeightedCSP, [27](#)
- NC bucket sort, [18](#)
- narycsp
  - WeightedCSPSolver, [33](#)
- Output messages, verbosity options and debugging, [13](#)
- postGlobalConstraint
  - WeightedCSP, [27](#)
- postMST
  - WeightedCSP, [28](#)
- postMaxWeight
  - WeightedCSP, [27](#)
- postNaryConstraintTuple
  - WeightedCSP, [28](#)
- postUnary
  - WeightedCSP, [28](#)
- postWAllDiff
  - WeightedCSP, [28](#)
- postWAmong
  - WeightedCSP, [28](#), [29](#)
- postWGcc
  - WeightedCSP, [29](#)
- postWGrammarCNF
  - WeightedCSP, [29](#)
- postWOverlap
  - WeightedCSP, [30](#)
- postWRegular
  - WeightedCSP, [30](#), [31](#)
- postWSame
  - WeightedCSP, [31](#)
- postWSum
  - WeightedCSP, [31](#)
- Preprocessing techniques, [14](#)
- Propagation loop, [20](#)
- read\_uai2008
  - WeightedCSP, [32](#)
- setInfiniteCost
  - WeightedCSP, [32](#)
- Soft arc consistency and problem reformulation, [16](#)
- solve
  - WeightedCSPSolver, [34](#)
- solve\_symmax2sat
  - WeightedCSPSolver, [34](#)
- Solving cost function networks, [12](#)
- sortConstraints
  - WeightedCSP, [32](#)
- Variable and cost function modeling, [11](#)
- Variable and value search ordering heuristics, [15](#)
- Variable elimination, [19](#)
- Virtual Arc Consistency enforcing, [17](#)
- Weighted Constraint Satisfaction Problem file format
  - (wcsp), [4](#)
- WeightedCSP, [22](#)
  - assignLS, [26](#)
  - cartProd, [26](#)
  - dump, [26](#)
  - finiteUb, [27](#)
  - getName, [27](#)
  - getValue, [27](#)
  - increaseLb, [27](#)
  - postGlobalConstraint, [27](#)
  - postMST, [28](#)
  - postMaxWeight, [27](#)
  - postNaryConstraintTuple, [28](#)
  - postUnary, [28](#)
  - postWAllDiff, [28](#)
  - postWAmong, [28](#), [29](#)
  - postWGcc, [29](#)
  - postWGrammarCNF, [29](#)
  - postWOverlap, [30](#)
  - postWRegular, [30](#), [31](#)
  - postWSame, [31](#)
  - postWSum, [31](#)
  - read\_uai2008, [32](#)
  - setInfiniteCost, [32](#)
  - sortConstraints, [32](#)
- WeightedCSPSolver, [32](#)
  - dump\_wcsp, [33](#)
  - narycsp, [33](#)
  - solve, [34](#)
  - solve\_symmax2sat, [34](#)