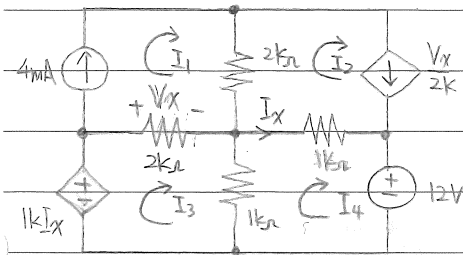


1. $R_{AB} = 4\Omega$

2.

find I_1, I_2, I_3 and I_4



$$I_1 = 4\text{mA}, I_2 = \frac{V_x}{2k}, \frac{V_x}{2k} = I_3 - I_1 \Rightarrow V_x = 2kI_3 - 8, I_x = I_4 - I_2 = I_4 - \frac{V_x}{2k}$$

$$\begin{cases} 1kI_x = V_x + 1k(I_3 - I_4) \\ -12 = 1kI_x + 1k(I_4 - I_3) \end{cases} \Rightarrow \begin{cases} I_4 - I_3 + 4\text{mA} = 2I_3 - 8\text{mA} + I_3 - I_4 \\ -12\text{mA} = I_4 - I_3 + 4\text{mA} + I_4 - I_3 \end{cases} \Rightarrow \begin{cases} I_4 - I_3 + 4\text{mA} = 2I_3 - 8\text{mA} + I_3 - I_4 \\ -12\text{mA} = I_4 - I_3 + 4\text{mA} + I_4 - I_3 \end{cases}$$

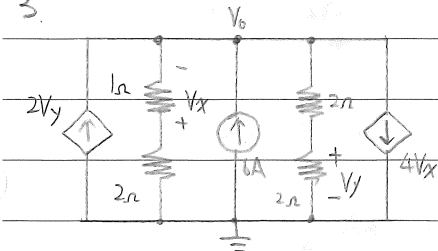
$$\Rightarrow \begin{cases} 4I_3 - 2I_4 = 12\text{mA} \\ 2I_3 - 2I_4 = 16\text{mA} \end{cases} \Rightarrow \begin{cases} 4I_3 - 2I_4 = 12\text{mA} \\ 4I_3 - 4I_4 = 32\text{mA} \end{cases} \Rightarrow I_4 = 10\text{mA}, I_3 = -2\text{mA}, I_1 = 4\text{mA}, I_2 = -6\text{mA}$$

$$V_x = -12\text{V}, I_x = -4\text{mA}$$

#

3.

find V_0



$$2V_y + 6 - 4V_x = \frac{V_0}{3} + \frac{V_0}{4}$$

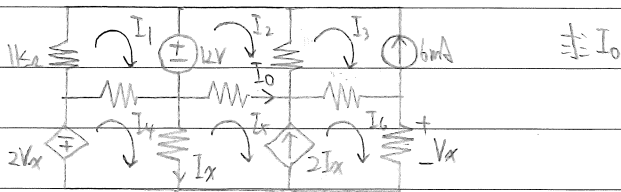
$$12(2V_y + 6 - 4V_x) = 7V_0 \Rightarrow 12(V_0 + 6 + \frac{4V_0}{3}) = 7V_0$$

$$\frac{V_0}{3} \times 1 = -V_x, \frac{V_0}{4} \times 2 = V_y$$

$$\Rightarrow 21V_0 = 72 \Rightarrow V_0 = \frac{24}{7}\text{V}$$

#

4.



$$I_3 = -6, 2I_x = I_6 - I_5, V_x = I_6, I_x = I_4 - I_5$$

$$12 = -2I_1 + I_4 \Rightarrow 2I_1 = I_4 - 12 \quad I_6 = 2I_4 - I_5$$

$$12 = 2I_2 - I_3 - I_5 \Rightarrow 12 = 2I_2 + 6 - I_5 \Rightarrow 2I_2 - I_5 = 6$$

$$-2V_x = 2I_4 - I_1 - I_5 \Rightarrow 2I_4 - I_1 - I_5 + 2I_6 = 0 \Rightarrow 6I_4 - I_1 - 3I_5 = 0$$

$$-V_x = 2I_5 + I_6 - I_4 - I_2 - I_3 \Rightarrow 2I_5 + 2I_6 - I_4 - I_2 = -6 \Rightarrow 11I_4 - 6I_5 = -12$$

$$\Rightarrow 3I_4 - I_2 = -6$$

$$\begin{cases} 2I_2 - I_5 = 6 \\ 11I_4 - 6I_5 = -12 \\ -I_2 + 3I_4 = -6 \end{cases}$$

$$\Delta = \begin{vmatrix} 2 & 0 & -1 \\ 0 & 11 & -6 \\ -1 & 3 & 0 \end{vmatrix} = -(11 - 36) = 25$$

$$\Delta I_2 = \begin{vmatrix} 6 & 0 & -1 \\ -12 & 11 & -6 \\ -6 & 3 & 0 \end{vmatrix} = (36) - (66 - 108) = 18$$

$$I_2 = \frac{18}{25} = 3.12 \text{ mA}$$

$$\Delta I_4 = \begin{vmatrix} 2 & 6 & -1 \\ 0 & -12 & -6 \\ -1 & -6 & 0 \end{vmatrix} = (36) - (-12 + 12) = -24$$

$$I_4 = \frac{-24}{25} = -0.96 \text{ mA}$$

$$I_5 = \frac{6}{25} = 0.24 \text{ mA}$$

$$\Delta I_5 = \begin{vmatrix} 2 & 0 & 6 \\ 0 & 11 & -12 \\ -1 & 3 & -6 \end{vmatrix} = (-132) - (-66 - 12) = 6$$

$$I_0 = I_5 - I_2 = 0.24 \text{ mA} - 3.12 \text{ mA} = -2.88 \text{ mA} \quad \#$$

5.

$$V_1 = 3 \text{ V}, V_2 = 2 \times \left(\frac{20 \text{ k}}{5 \text{ k}} \right) = -8 \text{ V}, V_3 = 3 \times \left(1 + \frac{50 \text{ k}}{30 \text{ k}} \right) = 8 \text{ V}$$

$$V_{th} = \left(\frac{-8}{40 \text{ k}} + \frac{8}{80 \text{ k}} \right) (80 \text{ k} \parallel 40 \text{ k}) = \frac{-8}{80 \text{ k}} \times \frac{80 \text{ k}}{3} = \frac{-8}{3} \text{ V}$$

$$R_{th} = 40 \text{ k} \parallel 80 \text{ k} = \frac{80}{3} \text{ k}, V_0 = \frac{-8}{3} \times \left(\frac{100 \text{ k}}{\frac{80}{3} \text{ k}} \right) = 10 \text{ V} \quad \#$$

6. (a)

$$V_0 = -2V_1 + \frac{7}{2}V_2$$

(b)

$$V_0 = 6 \text{ V}$$

(c)

$$-4 \text{ V} \leq V_1 \leq 11 \text{ V} \quad \#$$