

考試時間：107 年 11 月 08 日 下午 13:20 至 15:10 (雙面試題，不可使用工程計算機)

1. (25%) Consider an OP-AMP circuit in Fig. 1. (a) Please determine the relation between the output voltage and the input voltages. (10%) (b) If $1V \leq V_1 \leq 2V$ and $2V \leq V_2 \leq 3V$, please determine the range of V_o . (5%) (c) Whether this circuit will produce the full range of V_o given that the dc supplies are $\pm 10V$. If the answer is no, what is the practical output range of V_o . (10%)

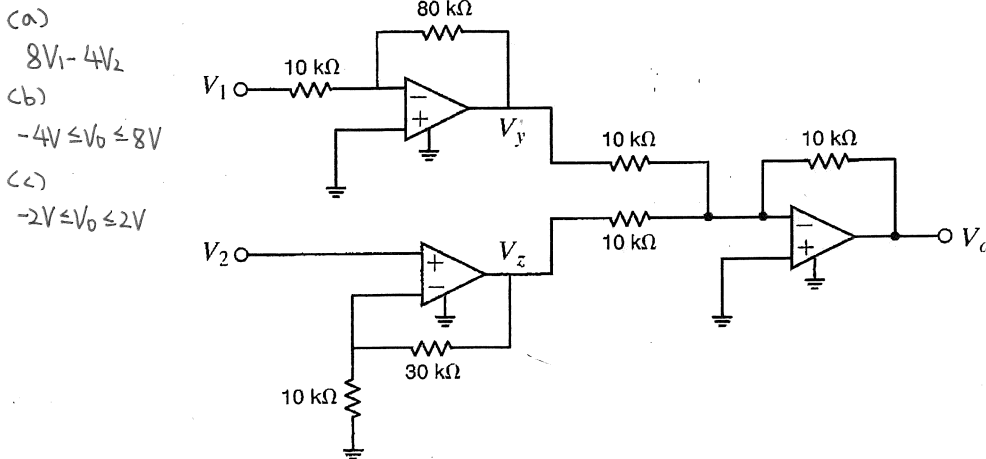


Fig. 1.

2. (15%) Please find R_L for maximum power transfer and the maximum power transferred to this load in the following circuit.

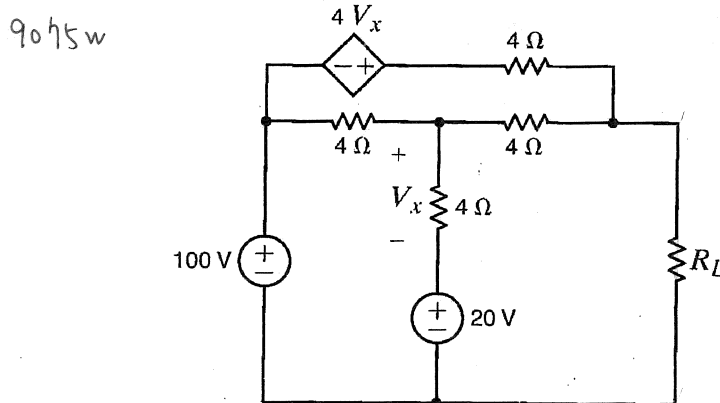


Fig. 2.

3. (15%) Please calculate I_o in Fig. 3.

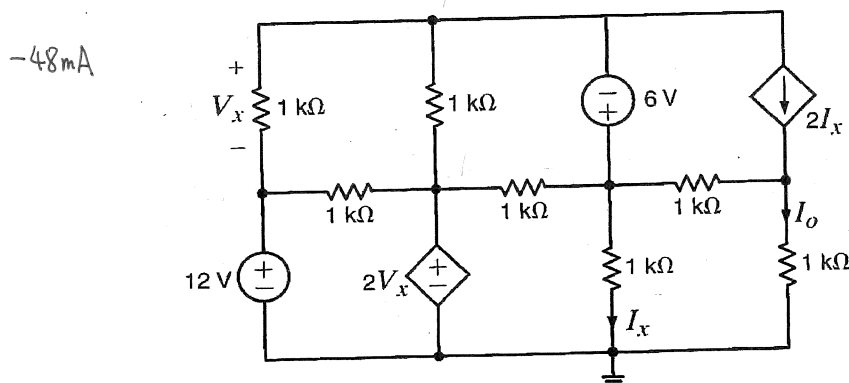


Fig. 3.

4. (15%) Please calculate V_o in Fig. 4 by using Norton's theorem.

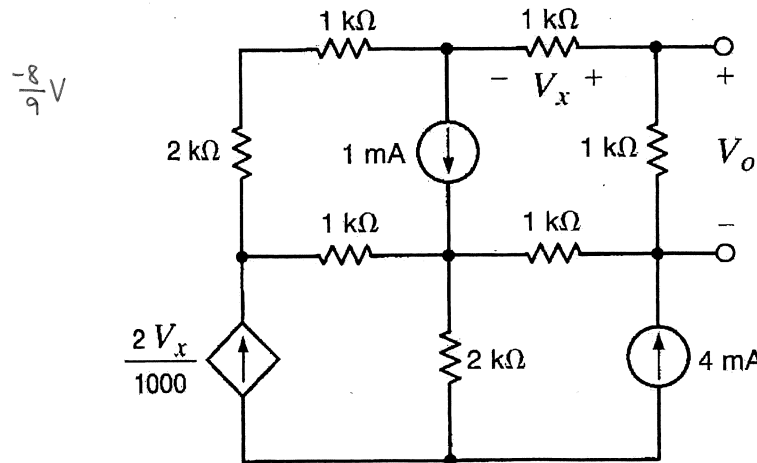


Fig. 4.

5. (15%) Please find the total energy stored in the circuit as shown in Fig. 5.

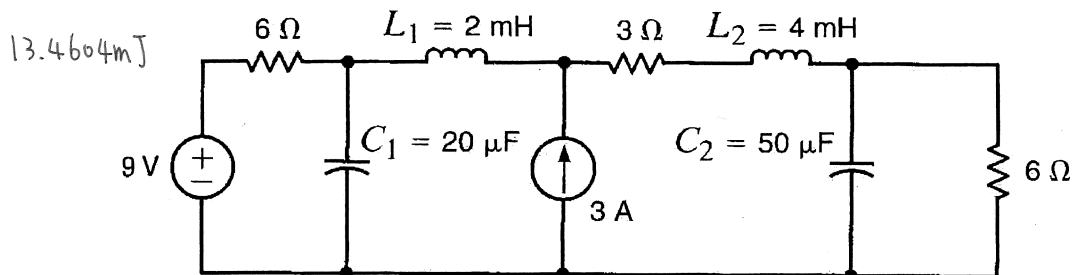


Fig. 5.

6. (15%) Please derive the expression of the output voltage v_o in Fig. 6. (a) What is the output voltage expressed by the input sources v_{s1} and v_{s2} ? (10%) (b) If the sources are given as $v_{s1} = 80 \cos 377t$ and $v_{s2} = 40 \cos 377t$, what is the value of the output voltage? (5%)

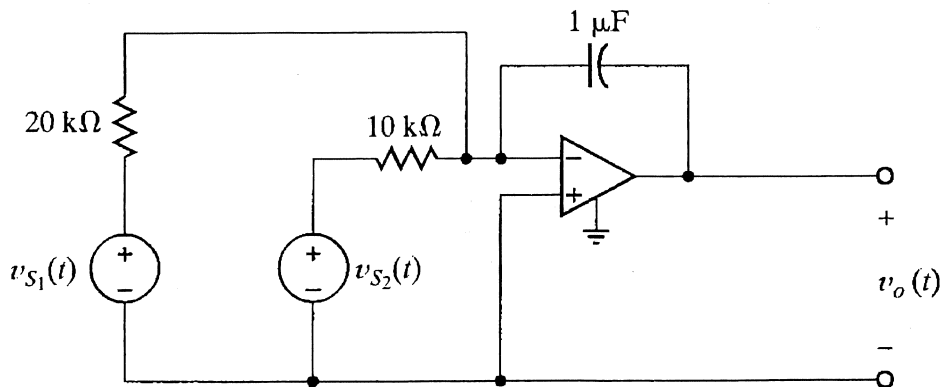


Fig. 6.

(a)

$$V_o = -50 \int (V_{s1} + 2V_{s2}) dt$$

(b)

$$V_o = -21.2 \sin 377t \text{ V}$$

1. $V_y = V_1 \times (-\frac{80k}{10k}) = -8V_1$, $V_z = V_2 \times (1 + \frac{30k}{10k}) = 4V_2$

(a) $V_0 = (-8V_1) \times (-\frac{10k}{10k}) + (4V_2) \times (-\frac{10k}{10k}) = 8V_1 - 4V_2$ #

(b) $1V \leq V_1 \leq 2V$ $V_0 = 0V, -4V, 8V, 4V$

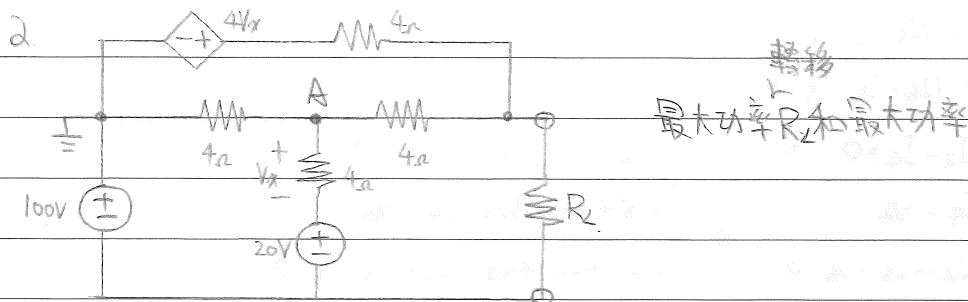
$2V \leq V_2 \leq 3V$

$-4V \leq V_0 \leq 8V$ #

(c) $V_y = -8V_1$, $-10V \leq V_y \leq -8V$

$V_z = 4V_2$, $8V \leq V_z \leq 10V$

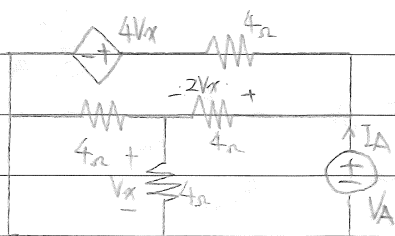
$-2V \leq V_0 \leq 2V$ #



$\frac{A-4Vx}{8} + \frac{A}{4} + \frac{A+80}{4} = 0 \Rightarrow 5A - 4Vx = -160$

$\frac{A+80}{4} \times 4 = Vx \Rightarrow A = Vx - 80$, $Vx = 240V$, $A = 160V$

$(\frac{-160-960}{8} \times 4) + 240 + 20 = 660V = V_{th}$



$V_A = 8V$

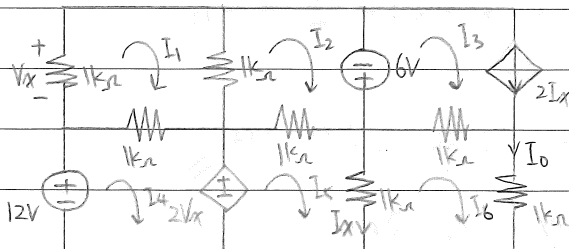
$V_x = 1V$

$I_A = \frac{3-4}{4} + \frac{3}{6} = -\frac{1}{4} + \frac{1}{2} = \frac{1}{4}$

$\frac{V_A}{I_A} = 12 \Omega$ #

$P_{max} = \frac{1}{4} (660)^2 / 12 = 9075W$ #

3.

find I_0

$$2I_x = I_3 = 2I_5 - 2I_6$$

$$2I_x = I_3, \quad I_x = I_5 - I_6, \quad V_x = -I_1$$

$$V_x = 2I_1 - I_2 - I_4 \Rightarrow 3I_1 - I_2 - I_4 = 0$$

$$-6 = 2I_2 - I_1 - I_5 \Rightarrow I_1 - 2I_2 + I_5 = -6 \Rightarrow I_1 = -6 + 2I_2 - I_5$$

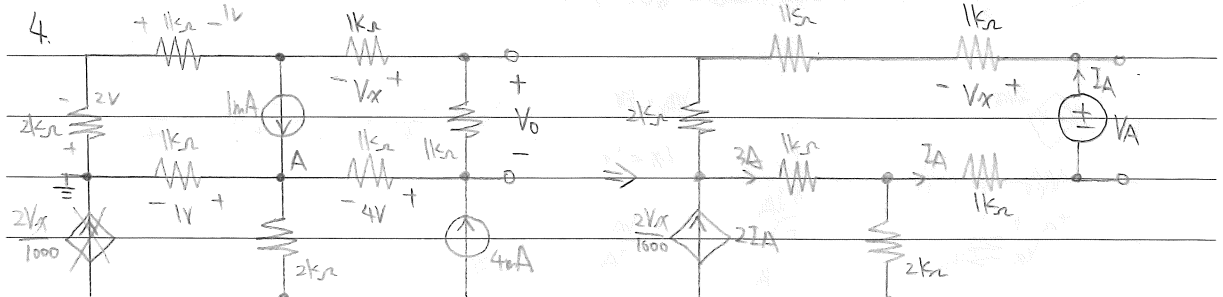
$$12 = I_4 - I_1 + 2V_x \Rightarrow 3I_1 - I_4 = -12$$

$$2V_x = 2I_5 - I_2 - I_6 \Rightarrow 2I_1 - I_2 + 2I_5 - I_6 = 0$$

$$0 = 3I_6 - I_3 - I_5 \Rightarrow I_3 + I_5 - 3I_6 = 0$$

$$\begin{cases} 3I_1 - I_2 - I_4 = 0 \\ 3I_1 - I_4 = -12 \\ 2I_1 - I_2 + 2I_5 - I_6 = 0 \\ I_3 + I_5 - 3I_6 = 0 \end{cases} \Rightarrow \begin{cases} -18 + 6I_2 - 3I_5 - I_4 = 0 \\ -18 + 6I_2 - 3I_5 - I_4 = -12 \\ -12 + 4I_2 - 2I_5 - I_2 + 2I_5 - I_6 = 0 \\ I_3 + I_5 - 3I_6 = 0 \end{cases}$$

$$\Rightarrow \begin{cases} 5I_2 - I_4 - 3I_5 = -18 \\ 6I_2 - I_4 - 3I_5 = -6 \\ 3I_2 - I_6 = 12 \\ I_3 + I_5 - 3I_6 = 0 \end{cases} \quad I_2 = -12 \text{ mA}, \quad I_6 = 48 \text{ mA} \quad \#$$

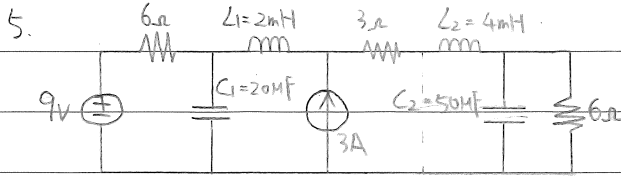


$$V_{th} = -8V$$

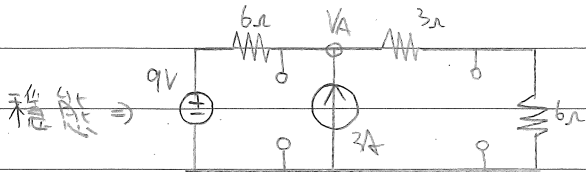
$$V_x = 1k\Omega I_A, \quad V_A = 8V_x$$

$$\frac{V_A}{I_A} = \frac{8V_x}{I_A} = \frac{8V_x}{\frac{V_x}{1k}} = 8k\Omega$$

$$V_0 = -8 \times \frac{1k}{9k} = -\frac{8}{9} V \quad \#$$



Find total energy



$$\frac{9 - V_A}{6} + 3 = \frac{V_A}{6} \Rightarrow 27.3V_A + 54 = 2V_A$$

$$\Rightarrow 5V_A = 81 \Rightarrow V_A = 16.2V$$

$$I_{L1} = (9 - 16.2) / 6 = -1.2A$$

$$I_{L2} = 1.8A$$

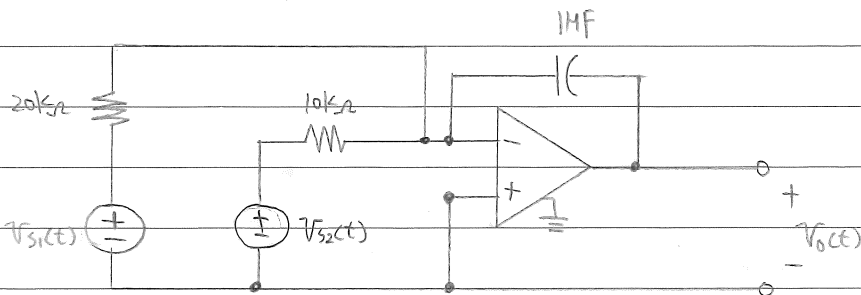
$$V_{C1} = 6 \times 1.2 + 9 = 16.2V$$

$$V_{C2} = 16.2 - 1.8 \times 3 = 10.8V$$

$$E = \frac{1}{2} (1.2^2 \times 2m + 1.8^2 \times 4m + 16.2^2 \times 20m + 10.8^2 \times 50m) = 13.46mJ$$

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6.



$$ca) \frac{V_{S1}(t)}{20k} + \frac{V_{S2}(t)}{10k} = -C \frac{dV}{dt} \Rightarrow V_{S1}(t) + 2V_{S2}(t) = -20m \frac{dV_{O}(t)}{dt}$$

$$\Rightarrow \int (V_{S1}(t) + 2V_{S2}(t)) dt = -20m \int \frac{dV_{O}(t)}{dt} dt$$

$$\Rightarrow V_{O}(t) = -50 \int (V_{S1}(t) + 2V_{S2}(t)) dt$$

$$cb) V_{O}(t) = -50 \int 160 \cos 377t dt$$

$$= -50 \times 160 \times \frac{1}{377} (\sin 377t) = -21.22 \sin 377t (V)$$

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