

Homework 4 (Due date: 10/21)

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HW4.1: (20 points)

A differential amplifier is shown in Fig. 4.1.  $R_{D1}=R_{D2}=R_D$ ,  $M_1 \neq M_2$ , and  $I_{SS}$  has a output resistance  $R_{SS}$ . If only  $g_m$  mismatch is considered, prove that the differential gain is as follows,

$$|A_{DM}| = \frac{R_D}{2} \frac{g_{m1} + g_{m2} + 4g_{m1}g_{m2}R_{SS}}{1 + (g_{m1} + g_{m2})R_{SS}}$$

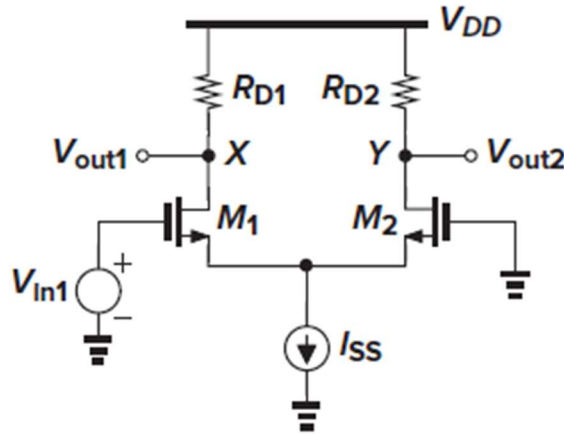


Fig. 4.1

HW4.2: (40 points)

Assuming that all the transistors in the circuits of Figs. 4.2 are saturated and  $\lambda \neq 0$ , calculate the small-signal differential voltage gain ( $A_v$ ) of each circuit. Assume both amplifiers have positive voltage gains.

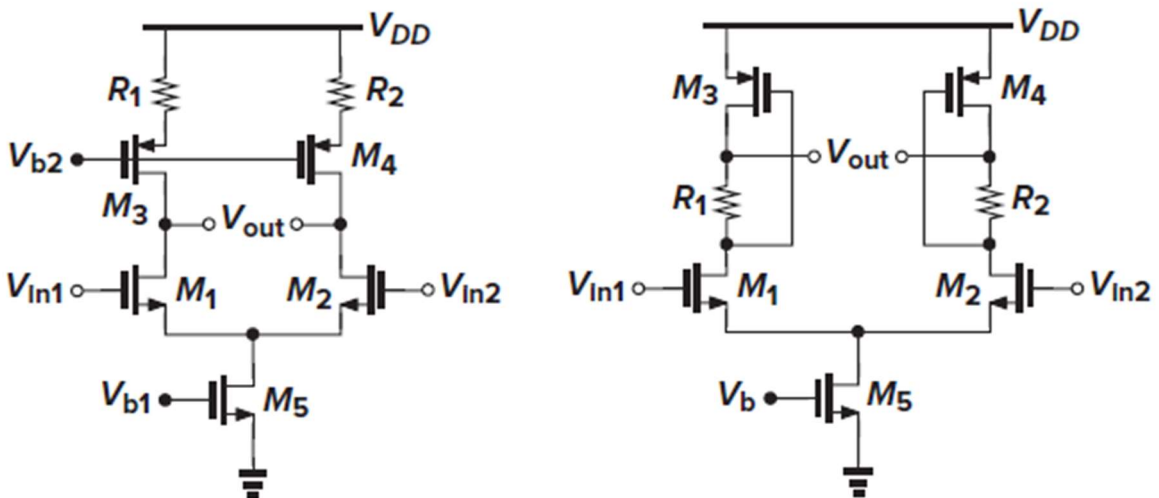


Fig. 4.2

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HW4.3: (40 points)

- (a) According to textbook or lecture, provide your derivation process to show that the equivalent transconductance ( $G_m$ ) is as follows,

$$\frac{\partial \Delta I_D}{\partial \Delta V_{in}} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \frac{\frac{4I_{SS}}{\mu_n C_{ox} W/L} - 2\Delta V_{in}^2}{\sqrt{\frac{4I_{SS}}{\mu_n C_{ox} W/L} - \Delta V_{in}^2}}$$

Hint: You can refer to Lecture 4, page 9 or Textbook, page 108

- (b) Find the maximum  $G_m$  ( $G_{m,max}$ ) and the  $\Delta V_{in}$  to get  $G_m = G_{m,max}/2$ .