

已分欄

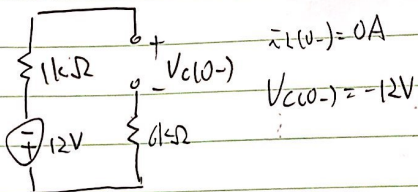
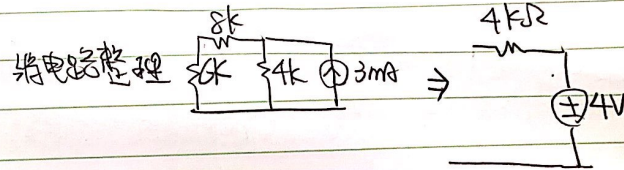
從此處開始寫起。試卷用紙務須節用，非經主試認可不得續用其他紙張作答。 / Please write from here.

$$1. F(s) = \frac{(s+4)(s+8)}{s(s^2+4s+8)} = \frac{k_0}{s} + \frac{(s+2)k_1}{(s+2)^2+2^2} + \frac{2k_2}{(s+2)^2+2^2}, \quad \begin{aligned} k_0 &= 4 \\ k_1 &= -3 \\ k_2 &= 1 \end{aligned}$$

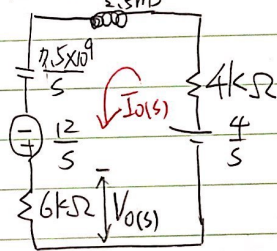
$$f(t) = \mathcal{L}^{-1}[F(s)] = [4 - 3e^{-t}\cos 2t + e^{-t}\sin 2t]u(t)$$

$$2. \quad f(t) = [2e^{-t} \cos 2t + 5e^{-t} \sin 2t] = \frac{2(s+1)}{(s+1)^2 + 2^2} + \frac{5 \times 2}{(s+1)^2 + 2^2} = \frac{2s+12}{s^2+2s+5}$$

3. At $t=0$.



At $t=0^+ (L.T)$



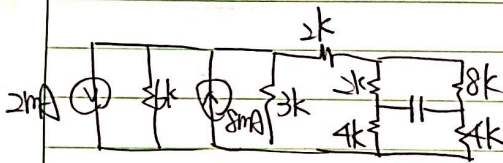
$$\frac{4}{s} + \frac{12}{s} = (0.1C I_0(s) + 2.5mS I_0(s) + \frac{7.5 \times 10^{-9}}{s} I_0(s))$$

$$I_0(s) = \frac{6400}{(s^2 + 4 \times 10^6 s + 3 \times 10^{12})} = \frac{1k_0}{(s+1M)} + \frac{k_1}{(s+3M)} \quad \begin{matrix} k_0 = -3200 \times 10^{-6} \\ k_1 = -3200 \times 10^{-6} \end{matrix}$$

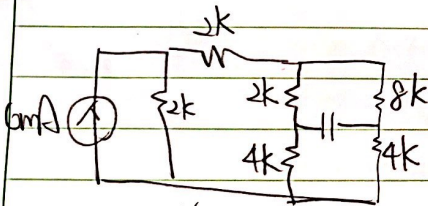
$$i_0(t) = \int [I_0(s)] = 3200 \times 10^{-6} e^{-1Mt} - 3200 \times 10^{-6} e^{-3Mt}$$

$$V_0(t) = 6k \times i_0(t) = 19.2 e^{-1Mt} - 19.2 e^{-3Mt}$$

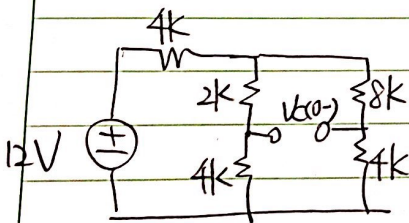
4. At $t=0_-$



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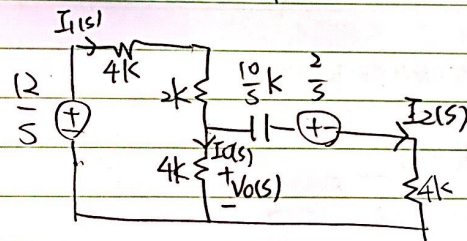


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$$V_C(0_-) = 12 \times \left(\frac{6k/12k}{4k + 6k/12k} \right) \times \left[\frac{4}{4+2} - \frac{4}{8+4} \right] = 2V$$

L.T at $t=0_+$



$$I_1(s) = I_0(s) + I_2(s)$$

$$\frac{12/s - V_O(s)}{6k} = \frac{V_O(s)}{4k} + \frac{V_O(s) - 2/s}{4k + 10/s}$$

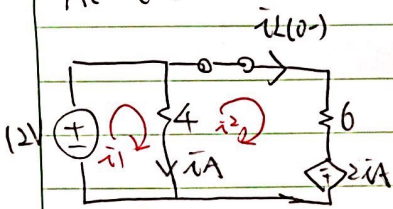
$$\Rightarrow V_O(s) = \frac{15}{4} \frac{(s+2)}{s(s + \frac{25}{16})} = \frac{k_0}{s} + \frac{k_1}{s + \frac{25}{16}}$$

$$k_0 = 4.8, \quad k_1 = -1.05 \left(\frac{-21}{20} \right)$$

$$V_O(t) = \mathcal{L}^{-1}[V_O(s)] = (4.8 - 1.05e^{-\frac{25}{16}t})u(t)$$

5.

At $t=0^-$

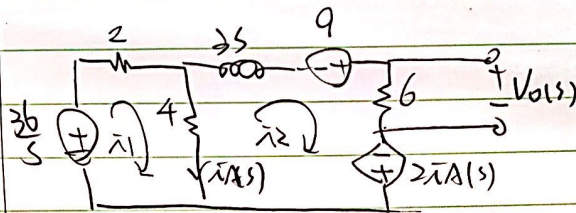


$$\begin{cases} 12 = 4(\bar{i}_1 - \bar{i}_2) & \text{①} \\ 2\bar{i}_1 = 10\bar{i}_2 - 4\bar{i}_1 & \text{②} \\ \bar{i}_1 - \bar{i}_2 = 1A & \text{③} \end{cases}$$

整理可得

$$\bar{i}_2 = \bar{i}_2(0^-) = 3A$$

L.T at $t > 0$



$$\begin{cases} \frac{36}{s} = 6\bar{i}_1(s) - 4\bar{i}_2(s) & \text{①} \\ 9 + 2\bar{i}_1(s) = (10 + 3s)\bar{i}_2(s) - 4\bar{i}_1(s) & \text{②} \end{cases}$$

由①②得

$$\bar{i}_2(s) = \frac{\frac{9s+36}{s}}{8+3s} = \frac{k_0}{s} + \frac{k_1}{s+\frac{8}{3}}, \quad k_0 = \frac{9}{2}, \quad k_1 = \frac{3}{2}$$

$$\bar{i}_2(t) = \mathcal{L}^{-1}[\bar{i}_2(s)] = \frac{9}{2} - \frac{3}{2}e^{-\frac{8}{3}t}$$

$$V_0(t) = \bar{i}_2(t) \times 6$$

$$= 27 - 9e^{-\frac{8}{3}t}$$

記分欄

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6. $\omega = 8$ (pole)

$\omega = 80$ (zero)

$\omega = 800$ (zero)

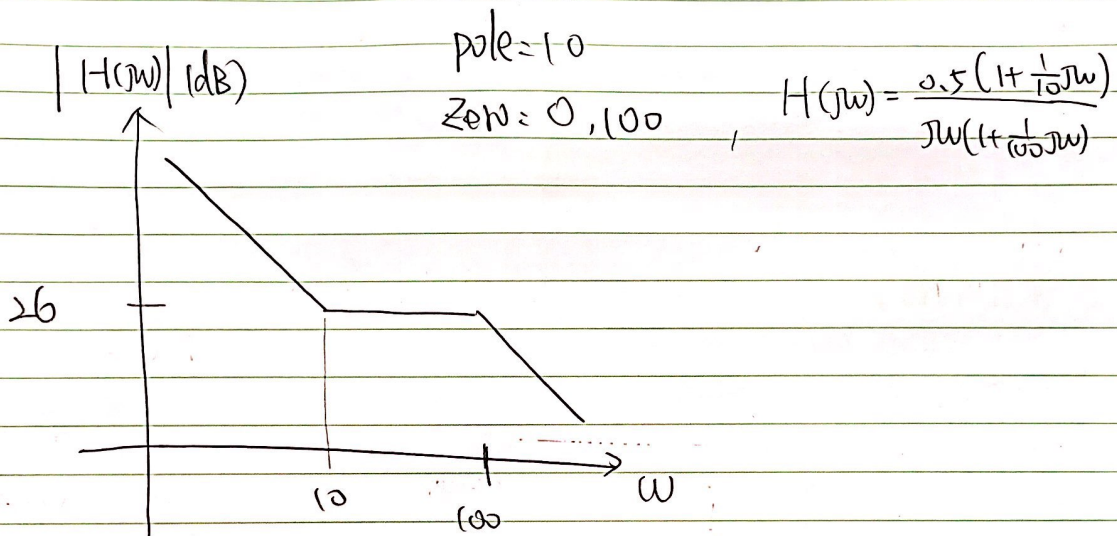
$\omega = 8000$ (pole)

$$\Rightarrow H(j\omega) = \frac{K_0 \left(\frac{1}{80} j\omega + 1 \right) \left(\frac{1}{800} j\omega + 1 \right)}{\left(\frac{1}{8} j\omega + 1 \right) \left(\frac{1}{8000} j\omega + 1 \right)}$$

$$\text{when } \omega = 8, \quad 20 \log |H(j\omega)| = 20 \log K_0 + 20 \log |1 + j0.1| + 20 \log |1 + j0.01| \\ - 20 \log |1 + j1| - 20 \log |1 + j0.001|$$

$$0 - 3 \text{ dB} = 20 \log K_0 - 3 \text{ dB} \Rightarrow K_0 = 1$$

7.



when $\omega = 10$, $20 \log |H(j\omega)|$

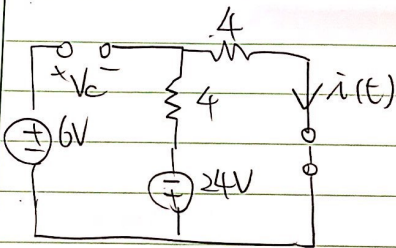
$$= 20 \log 0.5 + 20 \log |1 + j| - 20 \log |10| - 20 \log |1 + j0.1|$$

$$= 20 \log |0.05| + 3 \text{ dB}$$

$$= 20 \log 10^{-2} + 20 \log 5 + 3 \text{ dB} = -40 + 20 \log 5 + 3 \text{ dB} = 26 \text{ dB}$$

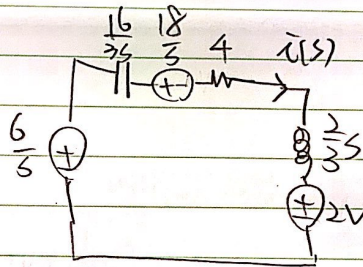
可轉頁再寫。

Q1

At $t=0^-$ 

$$i(0^-) = \frac{-24}{4+4} = -3A$$

$$V_c(0^-) = 6 + 24 + 4 \times i(0^-) \\ = 18V$$

At $t=0^+$ 

$$i(s) = \frac{\frac{6}{s} - \frac{18}{s}}{\frac{16}{3s} + 4 + \frac{2}{3s}} = \frac{-3s-18}{(s+4)(s+2)} \\ = \frac{3}{s+4} + \frac{-6}{s+2}$$

$$i(t) = \mathcal{L}^{-1}[i(s)] = (3e^{-4t} - 6e^{-2t})u(t)$$

$$i(0^+) = 3e^{-360m} - 6e^{-180m}$$