

1. Find the domain and range of each function.

A. $f(x) = 1 + x^2$

B. $g(x) = \sqrt{x^2 - 3x}$

2. $f(x) = x - 1$ and $g(x) = 1/(x + 1)$, find the following.

A. $f(f(5))$

B. $g(f(8))$

3. Find the limits

A. $\lim_{u \rightarrow 1} \frac{u^4 - 1}{u^3 - 1}$

B. $\lim_{h \rightarrow 0^-} \frac{\sqrt{6} - \sqrt{5h^2 + 11h + 6}}{h}$

C. $\lim_{x \rightarrow 0} \frac{1 + x + \sin x}{3 \cos x}$

D. $\lim_{x \rightarrow \infty} \frac{\sqrt{x^2 + 1}}{x + 1}$

4. Show that $\lim_{x \rightarrow -3} \frac{x^2 - 9}{x + 3} = -6$ by the precise definition.

5. For what values of a and b is continuous at every x?

$$f(x) = \begin{cases} -2, & x \leq -1 \\ ax - b, & -1 < x < 1 \\ 3, & x \geq 1 \end{cases}$$

6. $\lim_{x^2 \rightarrow 4} \frac{1}{x^2 - 4}$

A. $x \rightarrow 2^+$

B. $x \rightarrow 2^-$

7. Use the definitions of right-hand and left-hand limits to prove the limit statements

$$\lim_{x \rightarrow 0^-} \frac{x}{|x|} = -1$$

8. find the average rate of change of the function over the given interval or intervals.

$$R(\theta) = \sqrt{4\theta + 1}; [0, 2]$$