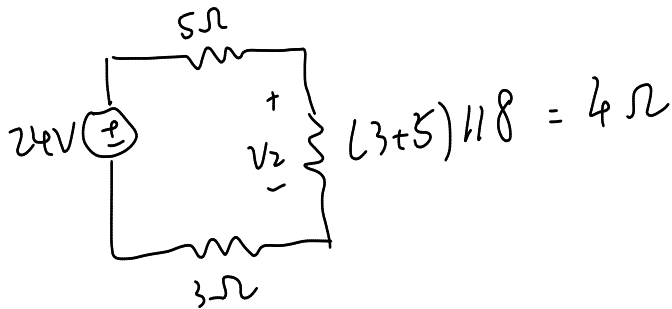
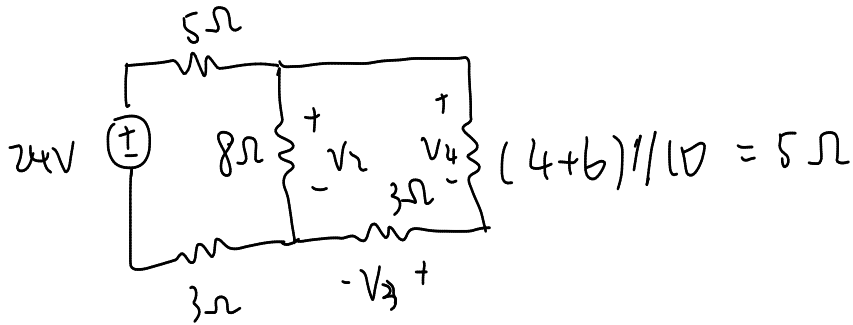
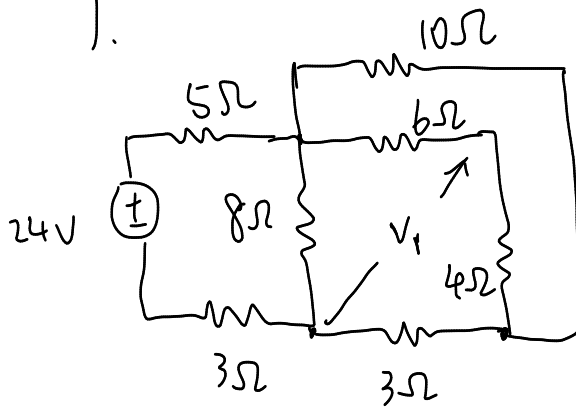


1.



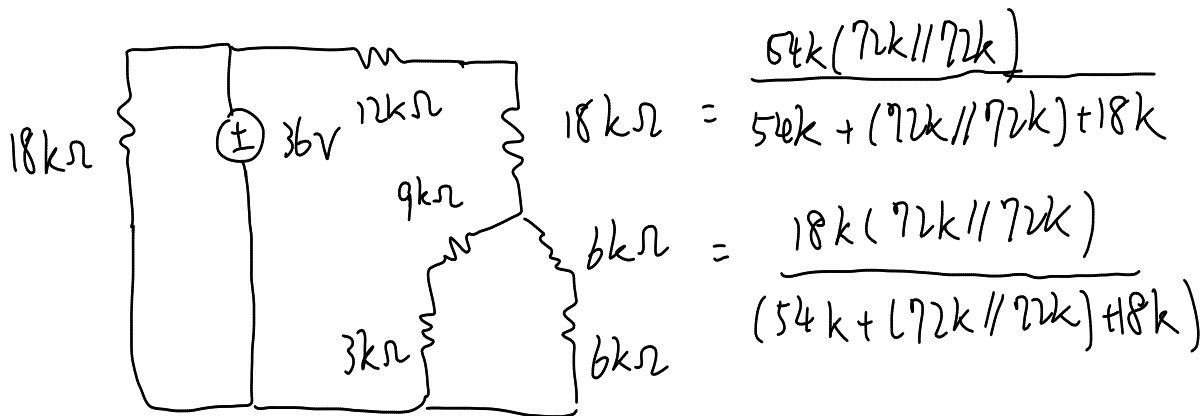
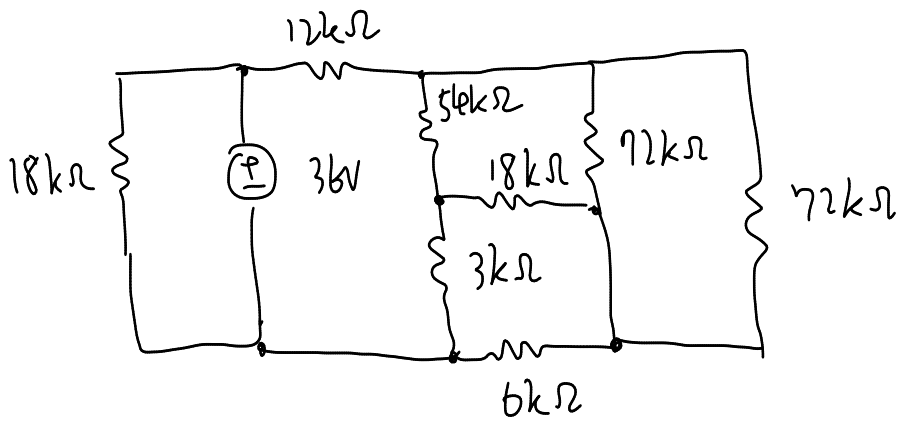
$$V_2 = \frac{24(4)}{5+4+3} = 8(V)$$

$$V_3 = \frac{V_2(3)}{5+3} = 3(V)$$

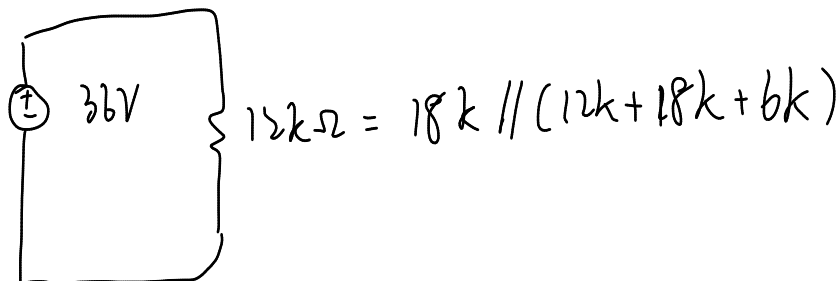
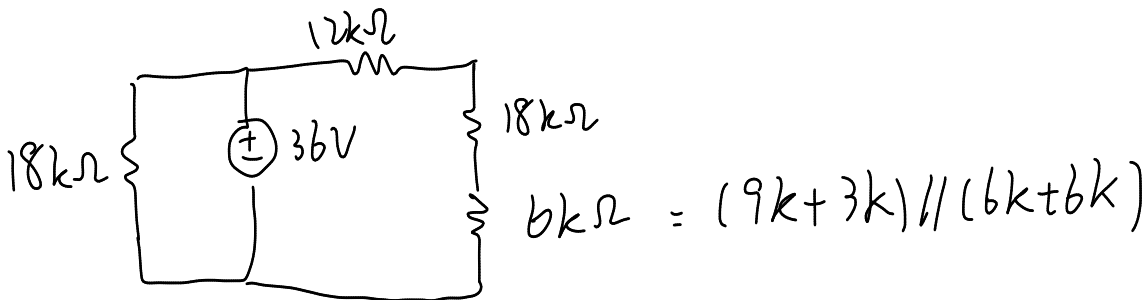
$$V_4 = V_2 - V_3 = 5(V)$$

$$V_1 = \frac{V_4(4)}{6+4} + V_3 = 2+3 = 5(V) \quad \#$$

2.

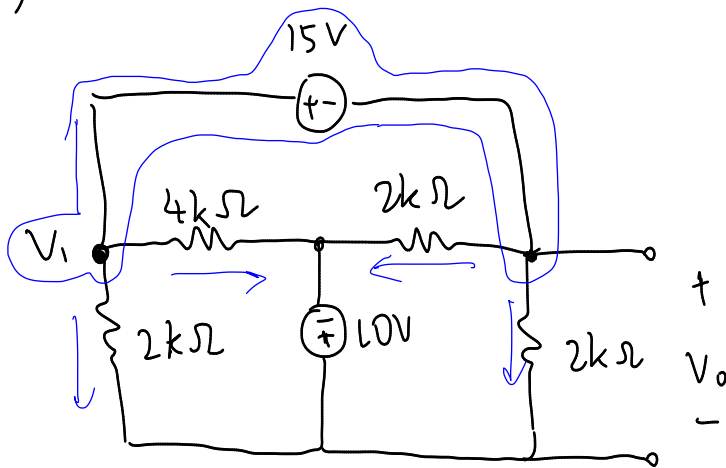


$$9k\Omega = \frac{18k(54k)}{(54k + (72k // 72k) + 18k)}$$



$$P_{36V} = \frac{V^2}{R} = \frac{36^2}{12k} = 108 \text{ (mW)} \quad \#$$

3



by nodal analysis :

$$\frac{V_1}{2k} + \frac{V_1 - (-10)}{4k} + \frac{V_0 - (-10)}{2k} + \frac{V_0}{2k} = 0$$

$$3V_1 + 4V_0 = -30 \quad \dots (1)$$

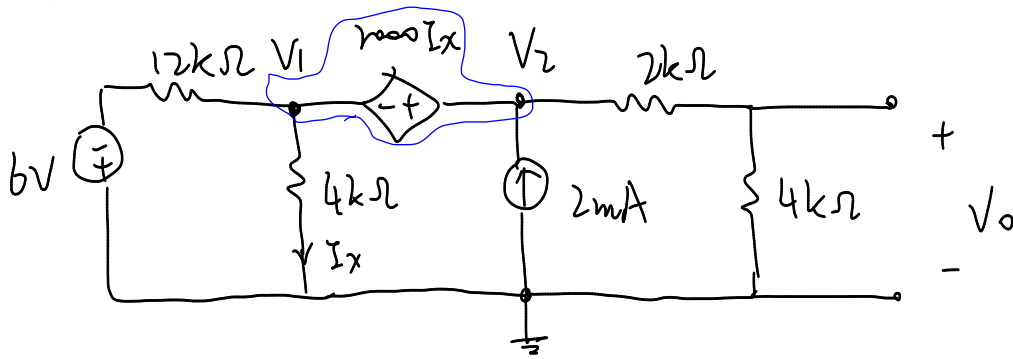
$$V_1 - 15 = V_0$$

$$V_1 - V_0 = 15 \quad \dots (2)$$

by (1), (2)

$$7V_0 = -75, \quad V_0 = -10.714 \text{ (V)} \quad \#$$

4.



by nodal analysis :

$$I_x = \frac{V_1}{4k}$$

$$\frac{V_1 + 6}{12k} + \frac{V_1}{4k} + (-2m) + \frac{V_2}{(2k + 4k)} = 0$$

$$\Rightarrow 4V_1 + 2V_2 = 18 \quad \dots (1)$$

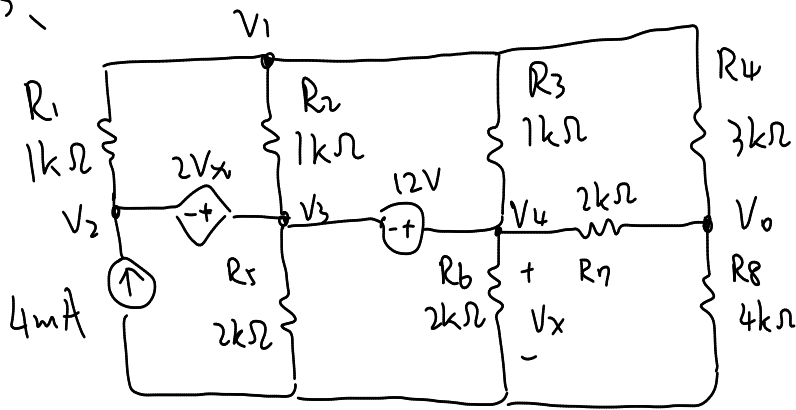
$$V_1 - V_2 = -2m \left(\frac{V_1}{4k} \right)$$

$$\Rightarrow 3V_1 - 2V_2 = 0 \quad \dots (2)$$

$$(1) + (2) = 7V_1 = 18, \quad V_1 = \frac{18}{7} (V), \quad V_2 = \frac{27}{7} (V)$$

$$V_0 = V_2 \times \frac{4k}{2k + 4k} = \frac{36}{14} = 2.57 (V) \quad \#$$

5.



by nodal analysis :

$$V_3 - V_2 = 2V_x \quad \dots (1)$$

$$V_4 - V_3 = 12V \quad \dots (2)$$

$$V_x = V_4 \quad \dots (3)$$

$$\text{KCL @ } V_1 : \frac{V_1 - V_2}{R_1} + \frac{V_1 - V_3}{R_2} + \frac{V_1 - V_4}{R_3} + \frac{V_1 - V_0}{R_4} = 0$$

$$-3V_4 - 3V_3 - 3V_2 + 10V_1 - V_0 = 0 \quad \dots (4)$$

$$\text{KCL @ reference} : \frac{V_3}{R_5} + \frac{V_4}{R_6} + \frac{V_0}{R_8} = 4 \text{ mA}$$

$$4V_3 + V_0 = -8 \quad \dots (5)$$

$$\text{KCL @ } V_0 : \frac{V_0 - V_1}{R_4} + \frac{V_0 - V_4}{R_7} + \frac{V_0}{R_8} = 0$$

$$V_1 = \frac{13V_0 - 6V_4}{4} \quad \dots (6)$$

by solving (1), (2), (3), (6), (4)

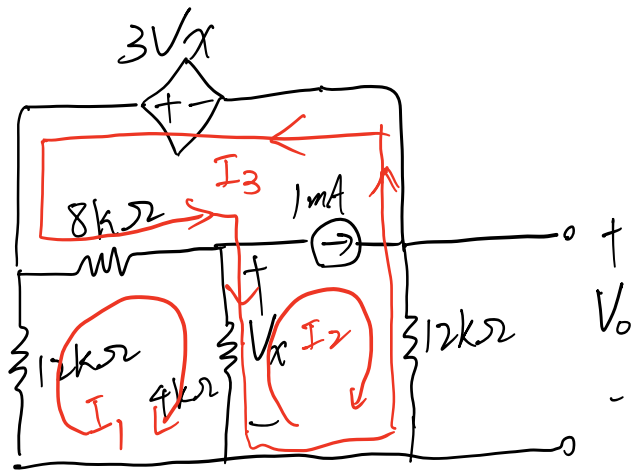
$$-3V_4 - 3V_3 - 3V_2 + 10 \cdot \left(\frac{13V_0 - 6V_4}{4} \right) - V_0 = 0$$

$$-18(12 + V_3) - 3V_3 - 3(V_3 - 2(12 + V_3)) + \frac{63}{2}V_0 = 0$$

$$-4V_3 + 7V_0 = 32 \quad \dots (7)$$

by (5), (7) $V_0 = 3 \text{ (V)}$ #

6.



$$I_2 = 1 \text{ mA} , V_x = 4k(I_1 + I_3 - \underbrace{I_2}_{1 \text{ mA}})$$

loop I_3 :

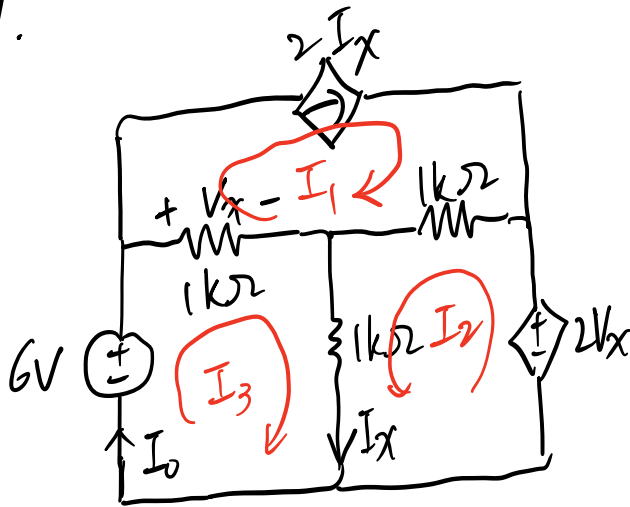
$$3V_x = 8k(I_3 + I_1) + V_x + 12k(I_3 - I_2)$$

$$\Rightarrow 12kI_1 + 12kI_3 - 12 = 12kI_1 - 16 + 24kI_3$$

$$\Rightarrow 12kI_3 = 4 \Rightarrow I_3 = \frac{1}{3} \text{ mA}$$

$$V_o = 12k(1 \text{ m} - \frac{1}{3} \text{ m}) = 8 \text{ V}$$

7.



$$I_x = I_2 + I_3, \quad V_x = 1k(I_3 - I_1)$$

$$I_1 = 2I_x = 2I_2 + 2I_3$$

loop I_3 :

$$6 = V_x + 1k(I_3 + I_2)$$

$$\Rightarrow 6 = 1kI_3 - \underline{1kI_1} + 1kI_3 + 1kI_2$$

$$\Rightarrow 6 = -1kI_2$$

$$I_2 = -6 \text{ mA}$$

loop I_r :

$$2V_x = 1k(I_2 + I_1) + 1k(I_2 + I_3)$$

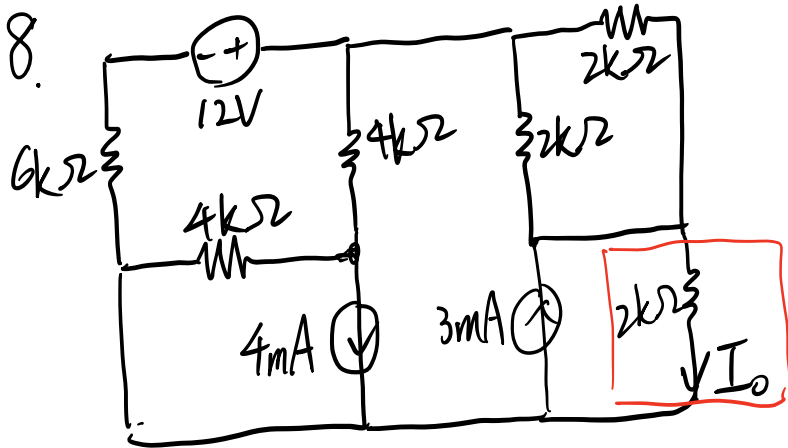
$$\Rightarrow 2kI_3 - 2kI_1 = 1kI_2 + 1kI_1 + 1kI_2 + 1kI_3$$

$$\Rightarrow 5kI_3 + 8kI_r = 0$$

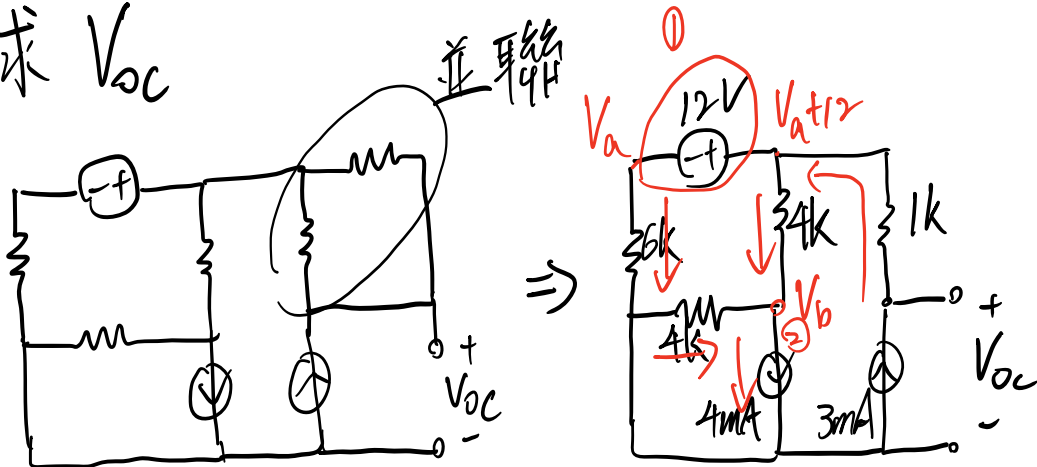
$$I_3 = -\frac{8}{5} \times -6m = \frac{48}{5} mA$$

$$\therefore I_0 = I_3$$

$$I_0 = \frac{48}{5} mA$$



求 V_{oc}



node 1:

$$3\text{m} = \frac{(V_a + 12) - V_b}{4\text{k}} + \frac{V_a}{6\text{k}} \Rightarrow 5V_a - 3V_b = 0 \quad \text{--- ①}$$

node 2:

$$4\text{m} = \frac{V_a - V_b}{4\text{k}} + \frac{(V_a + 12) - V_b}{4\text{k}} \Rightarrow V_a - 2V_b = 4 \quad \text{--- ②}$$

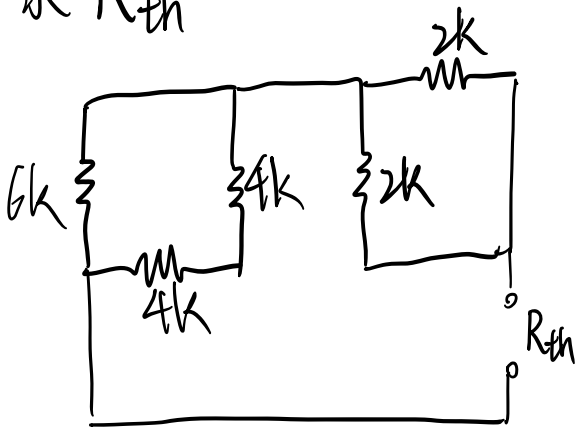
聯立 ①, ② 式, 解

$$V_a = -\frac{12}{7}\text{V}$$

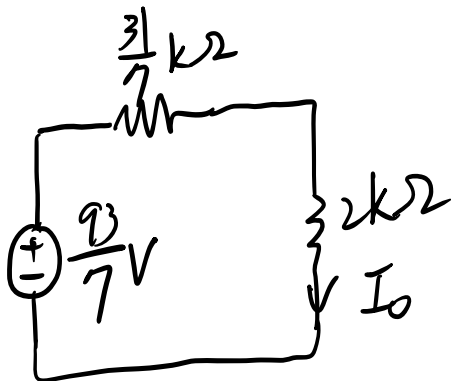
$$V_b = -\frac{20}{7}\text{V}$$

$$\begin{aligned}
 V_{OC} &= 3\text{mA} \times 1\text{k} + 12 + V_a \\
 &= 15 - \frac{12}{7} \\
 &= \frac{93}{7} \text{ (V)}
 \end{aligned}$$

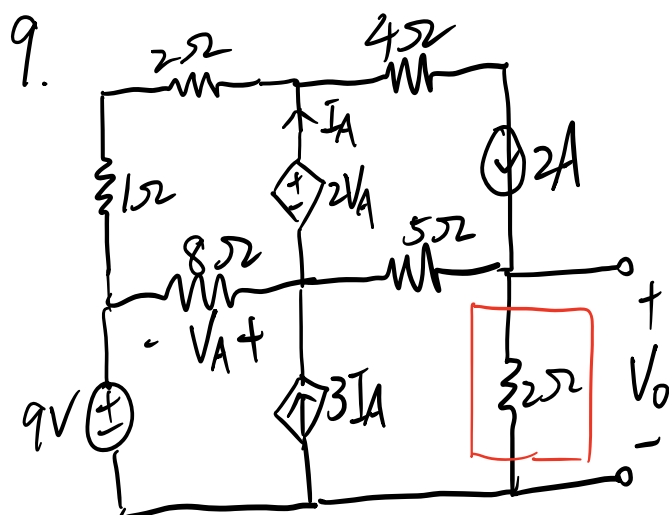
求 R_{th}



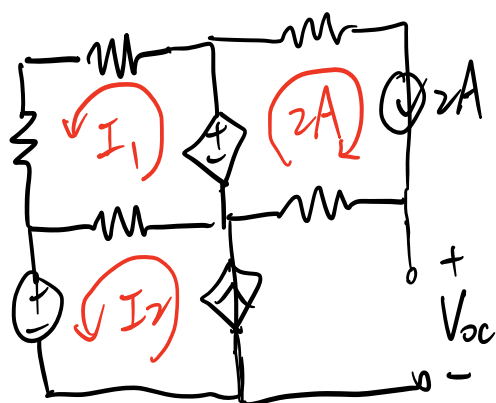
$$\begin{aligned}
 R_{th} &= [6\text{k} // (4\text{k} + 4\text{k})] + (2\text{k} // 2\text{k}) \\
 &= \frac{24}{7} \text{ k} + 1 \text{ k} \\
 &= \frac{31}{7} \text{ k} (\approx 4.43 \text{ k})
 \end{aligned}$$



$$I_0 = \frac{\frac{93}{7}}{\frac{31}{7} \text{ k} + 2\text{k}} = \frac{93}{45} \text{ mA}$$



求 V_{oc}



$$V_A = 8(I_2 - I_1)$$

$$I_A = I_1 + 2$$

$$I_2 = 3I_A = 3I_1 + 6 \quad \text{--- ①}$$

loop I_1 :

$$2V_A = 2I_1 + I_1 + 8(I_1 - I_2)$$

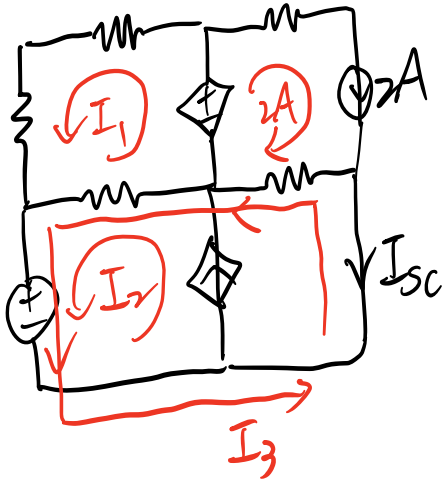
$$\Rightarrow 2I_1 - 24I_2 = 0 \quad \text{--- ②}$$

①式代入②式, 得 $I_1 = -3.2A$

$$I_2 = -3.6A$$

$$\begin{aligned}
 V_{oc} &= 5 \times 2 + V_A + 9 \\
 &= 19 + 8(-3.6 + 3.2) \\
 &= 15.8 \text{ V}
 \end{aligned}$$

求 I_{sc}



$$V_A = (I_2 + I_3 - I_1) \times 8$$

$$I_A = I_1 + 2$$

$$I_2 = 3I_A = 3I_1 + 6$$

loop I_1

$$2V_A = 3I_1 - V_A \Rightarrow 3I_1 - 3V_A = 0$$

$$\Rightarrow 27I_1 - 24I_2 - 24I_3 = 0$$

$$\Rightarrow -45I_1 - 24I_3 = 144 \quad \text{--- ①}$$

loop I_3

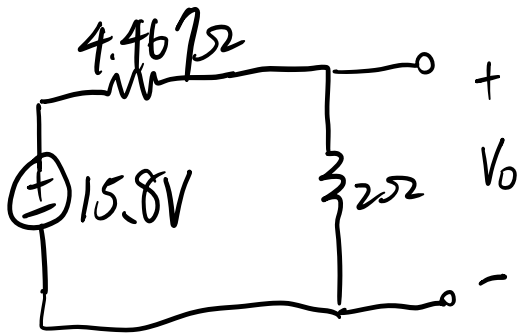
$$5(I_3 + 2) + V_A + 9 = 0$$

$$\Rightarrow -16 I_1 - 13 I_3 = 67 \quad \text{--- (2)}$$

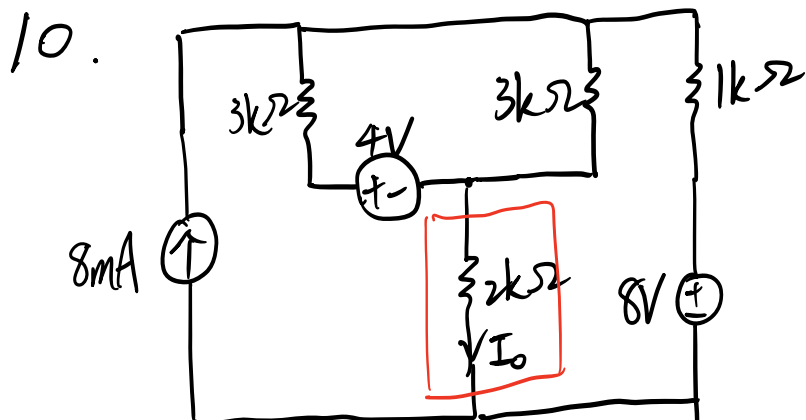
聯立 ①、② 式，解 $I_1 = -1.313 \text{ A}$
 $I_3 = -3.537 \text{ A}$

$$I_{sc} = -I_3 = 3.537 \text{ A}$$

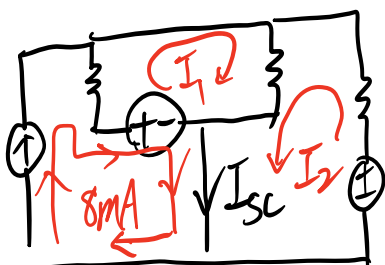
$$R_{th} = \frac{V_{oc}}{I_{sc}} = \frac{15.8}{3.537} = 4.467 \Omega$$



$$V_0 = 15.8 \times \frac{2}{4.467 + 2} = 4.886 \text{ V}$$



求 I_{sc}



loop I_1 :

$$4 = 3k(I_1 - 8m) + 3k(I_1 + I_2)$$

$$\Rightarrow 6k I_1 + 3k I_2 = 28 \quad \text{--- ①}$$

loop I_2 :

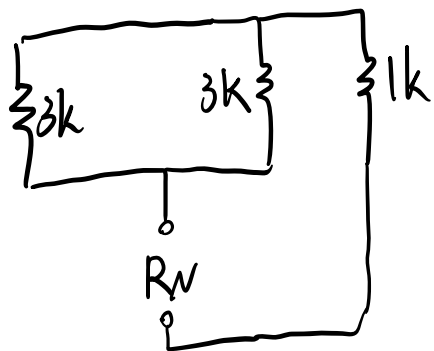
$$8 = 1k I_2 + 3k(I_2 + I_1)$$

$$\Rightarrow 3k I_1 + 4k I_2 = 8 \quad \text{--- ②}$$

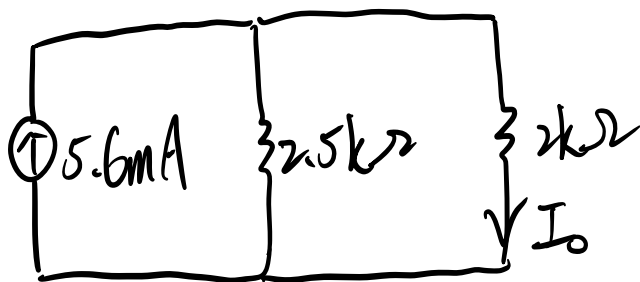
聯立 ①, ② 式, 解 $I_1 = 5.9 \text{ mA}$
 $I_2 = -2.4 \text{ mA}$

$$I_{SC} = 8 \text{ mA} + I_2 = 5.6 \text{ mA}$$

求 R_N



$$R_N = (3\text{k} // 3\text{k}) + 1\text{k} \\ = 2.5\text{k}\Omega$$



$$I_0 = 5.6 \text{ mA} \times \frac{2.5\text{k}}{2.5\text{k} + 2\text{k}} = \frac{28}{9} \text{ mA}$$