

1. (8%) Assume the following two circuits in Figs. 1(a) and Fig. 1(b) have the same driving point impedances, please determine  $R_{eq}$  and  $L_{eq}$  in terms of  $L_1$ ,  $L_2$  and  $R$ . The mutual inductance  $M$  is assumed to be the maximum value.

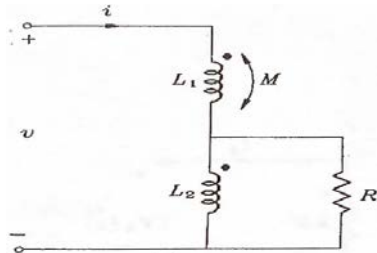


Fig. 1(a).

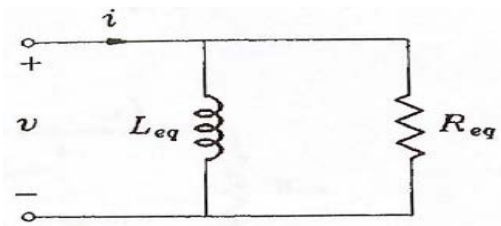


Fig. 1(b).

2. (20%) There is a critically-damped RLC 2nd order parallel resonant circuit. The  $R$  is the equivalent resistor  $R_{ab}$  in Fig. 2(a), the  $L$  is the equivalent inductor  $L_{ae}$  of the three-winding structure transformer in Fig. 2(b), and the  $C$  is the equivalent capacitor  $C_{eq}$  in Fig. 2(c), please answer the following questions:
- (7%) (a) Please derive the equivalent inductor  $L_{ae}$  in Fig. 2(b) and the equivalent capacitor  $C_{eq}$  in Fig. 2(c).
- (3%) (b) Please design the approximate value of  $R_x$  in Fig. 2(a) for this system.
- (10%) (c) What is the resonant angular frequency  $\omega_0$ , quality factor  $Q$ , bandwidth  $B_w$ , impedance pole-zero locations, half-power angular frequency  $\omega_H$  and  $\omega_L$  of this system?

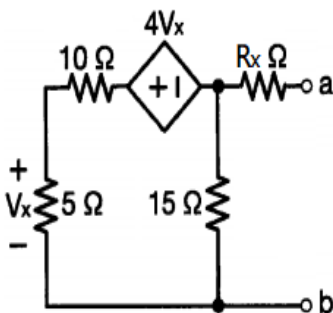


Fig. 2(a).

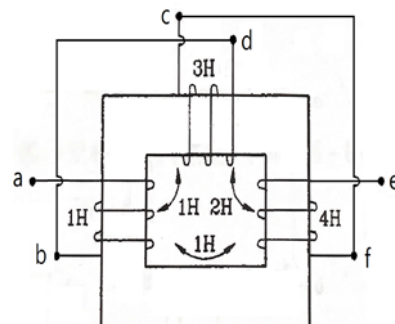


Fig. 2(b).

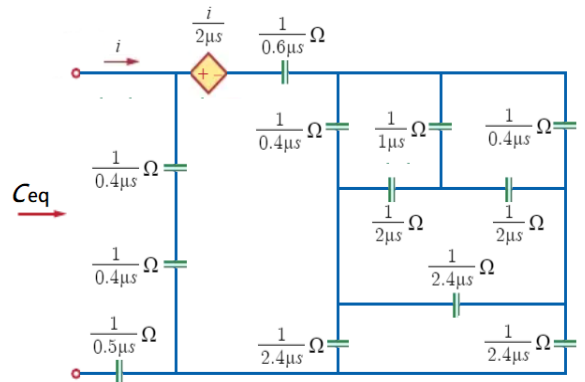
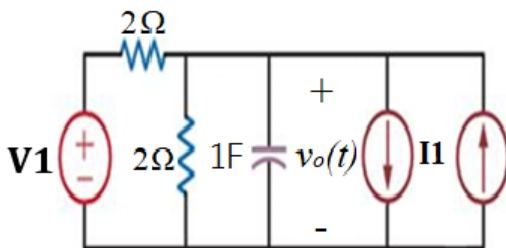


Fig. 2(c).

3. (14%) Consider a circuit arrangement where two same values  $R$  of the resistors and one reactance value  $jX_L$  of the inductor as the three-phase Y-connected load. Two resistors form the loads in two lines A and B; while the inductor forms a load in line C. All line impedances are negligible. Let  $V_{AB}=V_A-V_B=V \angle 45^\circ$  V,  $V_{BC}=V_B-V_C=V \angle -75^\circ$  V and  $V_{CA}=V_C-V_A=V \angle 165^\circ$  V. Please answer the following questions:
- (2%) (a) Please draw three-phase load with the appropriate circuit parameter data. Note that the symbol and parameter must be specified clearly.
- (8%) (b) Assume that  $X_L=R$ . Please calculate the total apparent power consumptions at the three-phase load side and verify that whether the neutral current is zero or not.
- (4%) (c) Please determine the appropriate reactive power to upgrade the overall power factor of the load to 0.98 for  $X_L=R=1$ . Moreover, what's the advantage or disadvantage of raising the load power factor?
4. (13%) Please write the output voltage  $v_o(t)$  in Fig. 3 if the initial voltage in the capacitor is zero.



$$\begin{cases} V1 = \sin\left[3\left(4t - \frac{\pi}{6}\right)\right] u(4t - 6\pi) \text{ V} \\ I1 = \frac{\sin(4t)}{t} u(t) \text{ A} \\ I2 = \frac{t-10}{4} \sin[2(t-10)] u(t-10) \text{ A} \end{cases}$$

Fig. 3.

5. (18%) In Fig. 4, a system is composed of an active filter and a convolution operation unit. Please answer the following questions:
- (6%) (a) Please construct asymptotic Bode plot of the magnitude for the transfer function  $G(s)$ . Note that the critical points, slopes and amplitude gain in dB must be specified clearly.
- (3%) (b) Please identify the filter properties. Let the coefficient  $n$  is a positive real variable to modulate the resistance value.
- (3%) (c) Please design the first corner frequency to be 50 Hz with passband gain to be 21. Let the coefficient  $n$  be in the range of 0.001 to 12, all the resistors be in the range of 15 to 150 k  $\Omega$  and the capacitors be in the range of 35 to 350 nF.
- (6%) (d) If  $n=1$ ,  $C=1\text{mF}$ ,  $R=10\text{k}\Omega$ ,  $X(t)=t^2\delta(t-2)\text{V}$  and change  $g(t)$  to  $5u(t-1)u(t+1)$ , what's the value of  $Z(3)$ ?

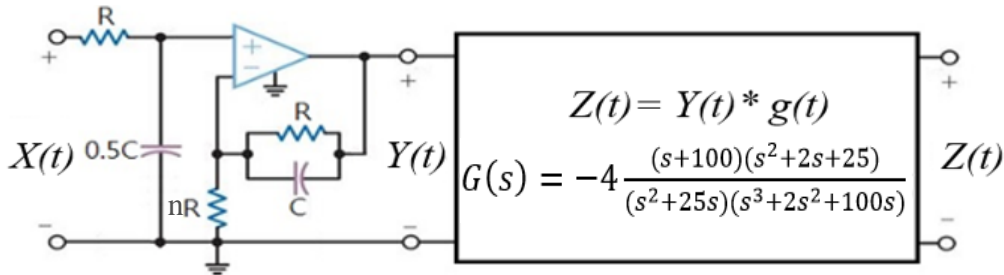


Fig. 4.

6. (7%) In Fig. 5,  $v_2(0^+)=20\text{V}$  and there is no initial energy stored in the inductor. For  $t < 2$ , what's the value range of  $\mu$  making the circuit stable and s-domain circuit? For  $t \geq 2$ , please find the voltage  $v_1(t)$  as  $\mu=4$ .

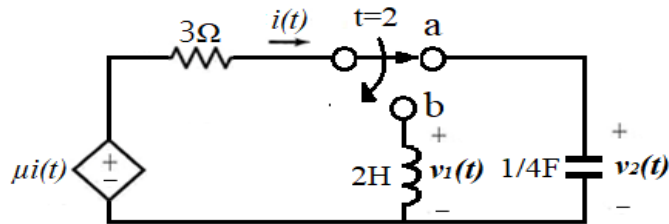


Fig. 5.

7. (13%) As for Fig. 6(b), two-port A and two-port B are connected in series, two-port B is also the network in Fig. 6(a), and the angular frequency is two radians per second. Please answer the following questions:
- (2%) (a) Please sketch an equivalent circuit by using one dependent current source and one dependent voltage source to model the ideal transformer of Fig. 6(a).
- (11%) (b) What is the total Z parameters of the series two-port network and the maximum active power transferred to  $R_L$ ?

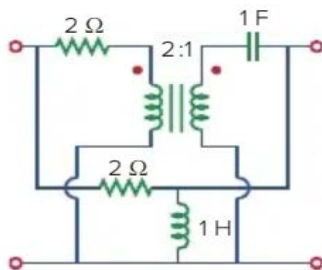


Fig. 6(a).

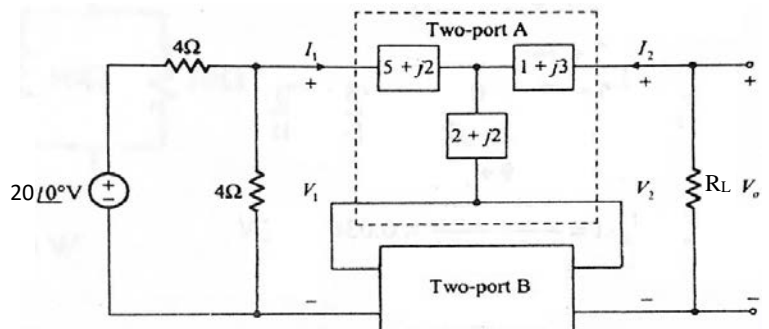


Fig. 6(b).

8. (7%) Please plot the waveform of the inverse transform  $f(t)$  for the following frequency domain function.

$$F(j\omega) = \frac{1}{j\omega(1 - e^{\frac{j\omega\pi}{2}})} + \frac{j\omega e^{\frac{-j\omega\pi}{2}} - 1}{(1 - \omega^2)(1 - e^{\frac{-j\omega\pi}{2}})}$$