

Trees Exercise

1. Name the three properties of a tree.

Answer: connected, acyclic, and undirected graph

2. Is a tree a forest?

Answer: Yes, but a forest is not a tree because it is not connected.

3. What do you call the special designated node in a tree?

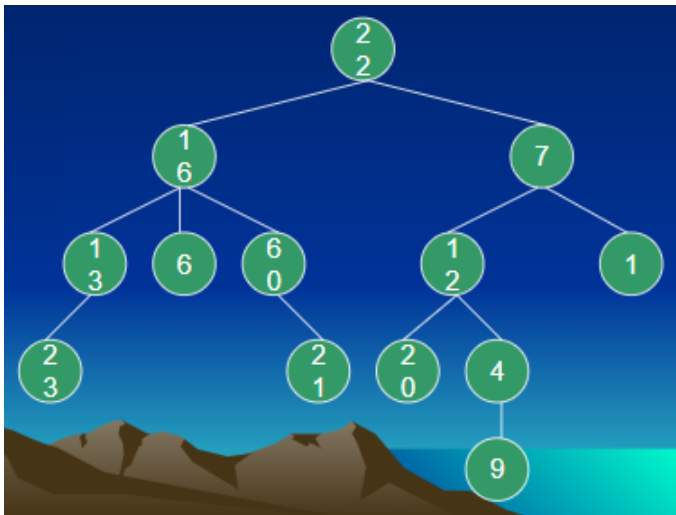
Answer: Root

4. What is the minimum number of nodes in a tree?

Answer: 1

5. Can a tree have no subtrees at all?

Answer: Yes



Given the tree, identify the ff.:

6. Children of node 16.

Answer: 13, 6, and 60

7. Parent of node 1.

Answer: 7

8. Siblings of 23.

Answer: None

9. Ancestors of 9.

Answer: 22, 7, 12, and 4

10. Descendants of 16.

Answer: 13, 6, 60, 23, and 21

11. Leaves

Answer: 23, 6, 21, 20, 9, and 1

12. Non-leaves

Answer: 22, 16, 7, 13, 60, 12, and 4

13. Depth of node 4.

Answer: Node 4 has depth 3.

14. Degree of the tree.

Answer: 3.

15. Height of the tree.

Answer: 4.

16. Weight of the tree.

Answer: 6.

17. Is the tree a binary tree?

Answer: Yes.

18. Removing 6, is the tree a full binary tree?

Answer: No.

19. Removing 6, is the tree a complete binary tree?

Answer: No.

20. Is a full binary tree complete?

Answer: No.

21. Is a complete binary tree full?

Answer: Yes.

22. How many leaves does a complete n-ary tree of height h have?

Answer: n^h

23. What is the height of a complete n-ary tree with m leaves?

Answer: $\log m$

24. What is the number of internal nodes of a complete n-ary tree of height h?

Answer: $1 + n + n^2 + \dots + n^{h-1} = \sum_{i=0}^{h-1} n^i = \frac{n^h - 1}{n - 1}$

25. What is the total number of nodes a complete n-ary tree height h have?

Answer: $2^h - 1$