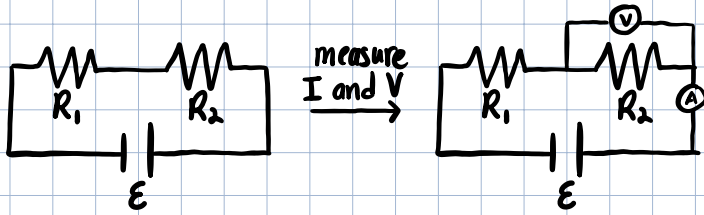


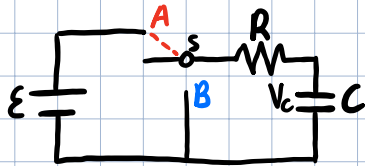
# Ammeters & Voltmeters

- Ammeters measure current and are denoted by  $\text{ⓐ}$  whereas voltmeters measure voltage and are denoted by  $\text{Ⓥ}$



- However, they are also objects and have their own resistance; to make as little change to the original circuit as possible, ammeter should have as little  $R$  as possible whereas voltmeter has as large as possible

## RC Circuits: resistor + capacitor



- Switching to position **A**

Loop Law:  $\epsilon - IR - \frac{q}{C} = 0$

$$\rightarrow \epsilon - \frac{dq}{dt}R - \frac{q}{C} = 0 \rightarrow dt = \frac{R dq}{\epsilon - \frac{q}{C}} \rightarrow t = -RC \ln\left(1 - \frac{Q}{\epsilon C}\right)$$

So  $Q$ , the charge on the capacitor, equals  $\epsilon C(1 - e^{-t/RC})$

$$I = \frac{dQ}{dt} = \frac{\epsilon}{R} e^{-t/RC}$$

$$V_C = \frac{Q}{C} = \epsilon(1 - e^{-t/RC})$$

At  $t = \infty$ ,  $I = 0$  so  $V_R = 0$  so  $V_C = \epsilon$ !

If  $Q = 0$ ,  $C$  acts like it's not there and if  $I = 0$ ,  $R$  acts like it's not there!

$RC$  is important!  $RC = \tau$ , time constant = time to decay  $37\%$  of initial or time to grow  $63\%$  of final

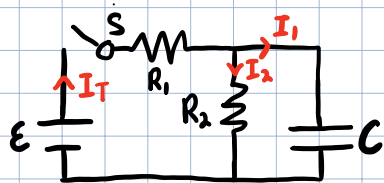
- After that, switch to position **B**

$$-IR - \frac{q}{C} = 0 \rightarrow \frac{dq}{dt}R + \frac{q}{C} = 0 \rightarrow -\frac{dq}{q} \frac{RC}{C} = dt \rightarrow t = -RC \ln\left(\frac{Q}{Q_0}\right) \rightarrow Q = Q_0 e^{-t/RC}$$

$$I = \frac{dQ}{dt} = -\frac{Q_0}{RC} e^{-t/RC}; \text{ negative b/c discharging}$$

$$V_C = \frac{Q}{C} = \frac{Q_0}{C} e^{-t/RC}$$

• Example:



At  $t=0$ ,  $C$  is uncharged and  $S$  open. Close  $S$ .

What is  $I_T$  right after  $S$  is closed?  $\frac{\epsilon}{R_1}$ ; no current through  $R_2$

What is  $I_2$  right after  $S$  is closed?  $I_T$ ; least resistance

$I_T$  tends to  $\frac{\epsilon}{R_1+R_2}$  as  $C$  charges and approaches infinite resistance

Graphs:

