

# Notices

- Please submit your lab hash to my spreadsheet (**first lab is due tomorrow**).
- Please use the same spreadsheet to record your coursework pair, or to help you find a partner.

# Lecture 5: More parsing

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Compilers

# What we know so far

- Languages can be defined using a **grammar** made up of **production rules** featuring **non-terminals** and **terminals**.
- Grammars should be written to avoid **ambiguity**.
- **Regular grammars** are equivalent to regexes.
- **Context-free grammars** are more expressive than regular grammars.
- And **context-sensitive grammars** are more expressive still.
- Most programming languages can be defined using a grammar that is (more or less) context-free.

# Outline

- A lesson in **grammar**
- How to build a **recursive descent** parser
- How to build a **shift/reduce** parser
- How to use **Yacc** to generate a parser automatically

# Recursive descent

```
expr   ::= expr + term | expr - term | term  
term   ::= term * factor | factor  
factor ::= ( expr ) | N
```

# Recursive descent

```
expr   ::= term + expr | term - expr | term
term   ::= factor * term | factor
factor ::= ( expr ) | N
```

# Recursive descent

$$E ::= T + E \mid T - E \mid T$$
$$T ::= F * T \mid F$$
$$F ::= ( E ) \mid N$$

```
int pE() {  
    return pT() && p( '+' ) && pE()  
    || pT() && p( '-' ) && pE()  
    || pT();  
}  
...
```

NB: this is only  
the rough idea



# What's the problem here?

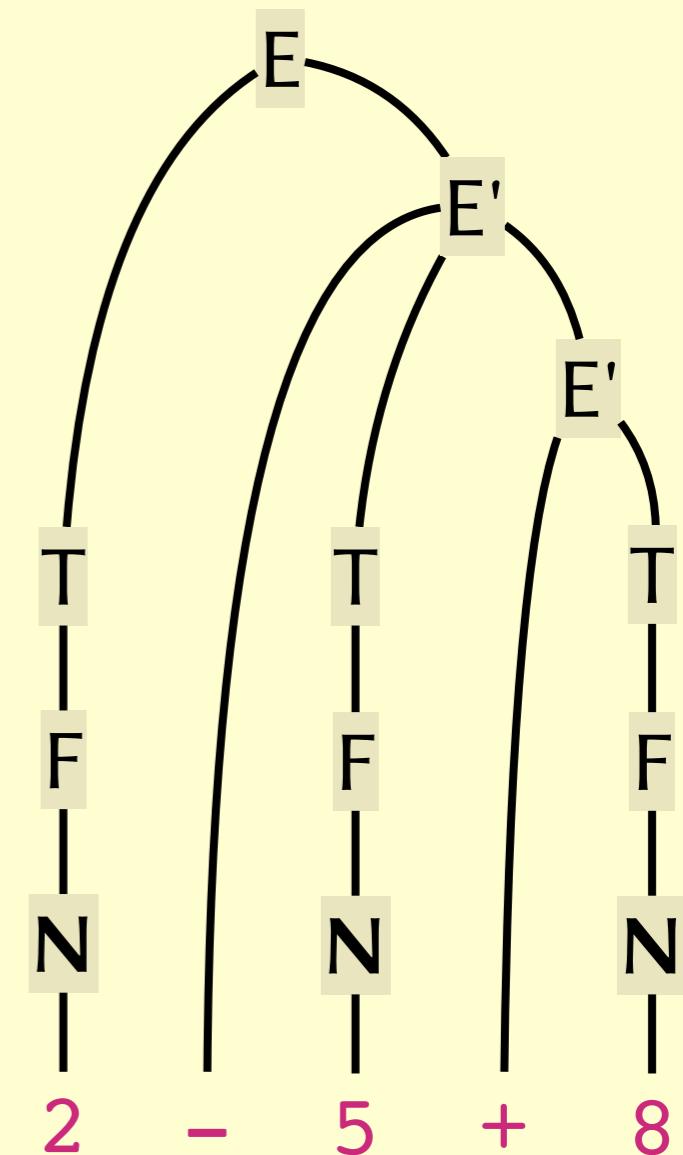
$$E ::= E + T \mid E - T \mid T$$
$$T ::= T * F \mid F$$
$$F ::= ( E ) \mid N$$

```
int pE() {
    return pE() && p( '+' ) && pT()
        || pE() && p( '-' ) && pT()
        || pT();
}
```

...

# Recursive descent

- **First problem.** Recursive descent cannot parse **left-recursive** grammars (those that contain a production of the form " $A \rightarrow A\dots$ ").
- **Solution.** Left-recursion can be removed by rewriting:

$$E ::= T E'$$
$$E' ::= + T E' \mid - T E' \mid \epsilon$$
$$T ::= F T'$$
$$T' ::= * F T' \mid \epsilon$$
$$F ::= ( E ) \mid N$$


# Recursive descent

- **Second problem.** Simple recursive descent involves **backtracking**.
- **Solution.** Can eliminate this using **lookahead**.
- This gives a **predictive** parser.

# FIRST and FOLLOW

- $\text{NULLABLE}(X)$  = can X generate the empty word?
- $\text{FIRST}(X)$  = which tokens can start words generated by X?
- $\text{FOLLOW}(X)$  = which tokens can follow words generated by X?

	NULLABLE	FIRST		FOLLOW	
$E ::= T E'$	<b>X</b>	(	N	\$	)
$E' ::= + T E' \mid - T E' \mid \epsilon$	✓	+	-	\$	)
$T ::= F T'$	<b>X</b>	(	N	+	- \$ )
$T' ::= * F T' \mid \epsilon$	✓	*		+	- \$ )
$F ::= ( E ) \mid N$	<b>X</b>	(	N	* + - \$ )	

# FIRST and FOLLOW

- $\text{NULLABLE}(X)$  = can X generate the empty word?
- $\text{FIRST}(X)$  = which tokens can start words generated by X?
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	NULLABLE	FIRST		FOLLOW	
$E ::= T E'$	<b>X</b>	(	N	\$	)
$E' ::= + T E' \mid - T E' \mid \epsilon$	✓	+	-	\$	)
$T ::= F T'$	<b>X</b>	(	N	+	- \$ )
$T' ::= * F T' \mid \epsilon$	✓	*		+	- \$ )
$F ::= ( E ) \mid N$	<b>X</b>	(	N	* + - \$ )	

	NULLABLE	FIRST	FOLLOW	
$E ::= T E'$	<b>X</b>	( N	\$	)
$E' ::= + T E' \mid - T E' \mid \epsilon$	<b>✓</b>	+ -	\$ )	
$T ::= F T'$	<b>X</b>	( N	+ - \$	)
$T' ::= * F T' \mid \epsilon$	<b>✓</b>	*	+ - \$ )	
$F ::= ( E ) \mid N$	<b>X</b>	( N	* + - \$ )	

	*	+	-	(	)	N	\$
E				$E \rightarrow T E'$		$E \rightarrow T E'$	
E'		$E' \rightarrow + T E'$	$E' \rightarrow - T E'$		$E' \rightarrow \epsilon$		$E' \rightarrow \epsilon$
T				$T \rightarrow F T'$		$T \rightarrow F T'$	
T'	$T' \rightarrow * F T'$	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$		$T' \rightarrow \epsilon$		$T' \rightarrow \epsilon$
F				$F \rightarrow ( E )$		$F \rightarrow N$	

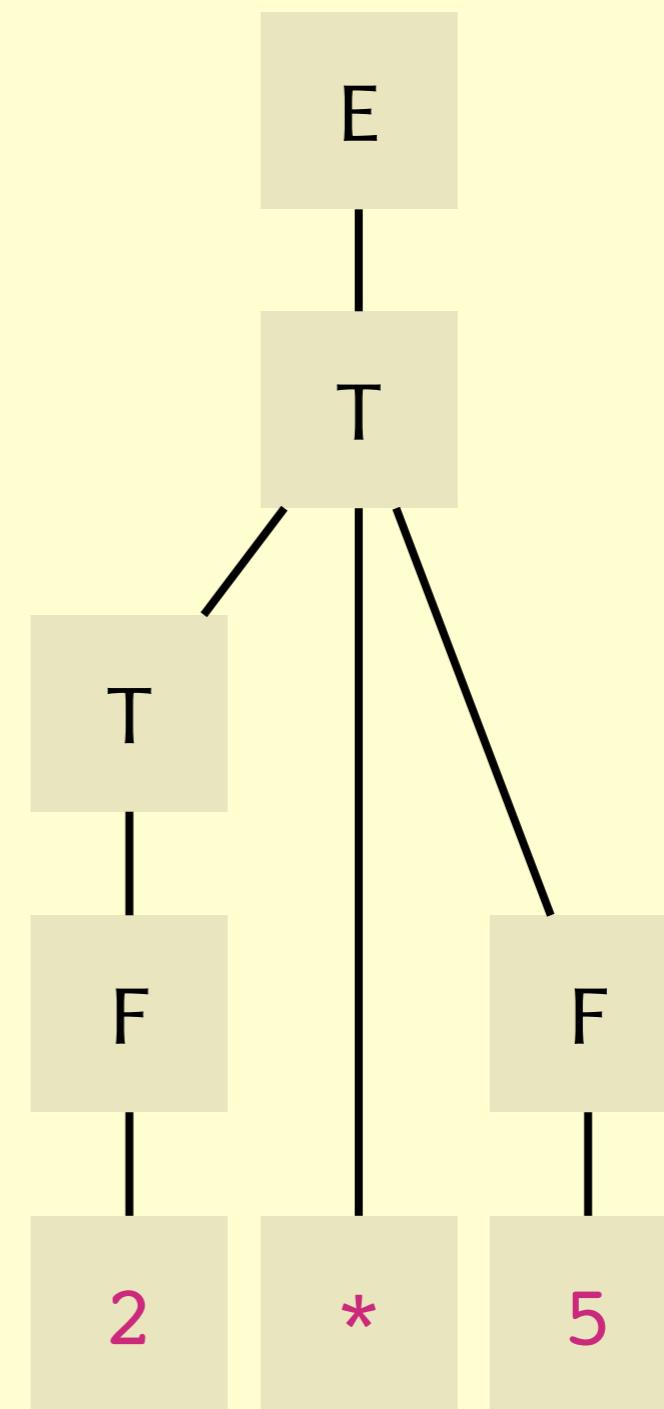
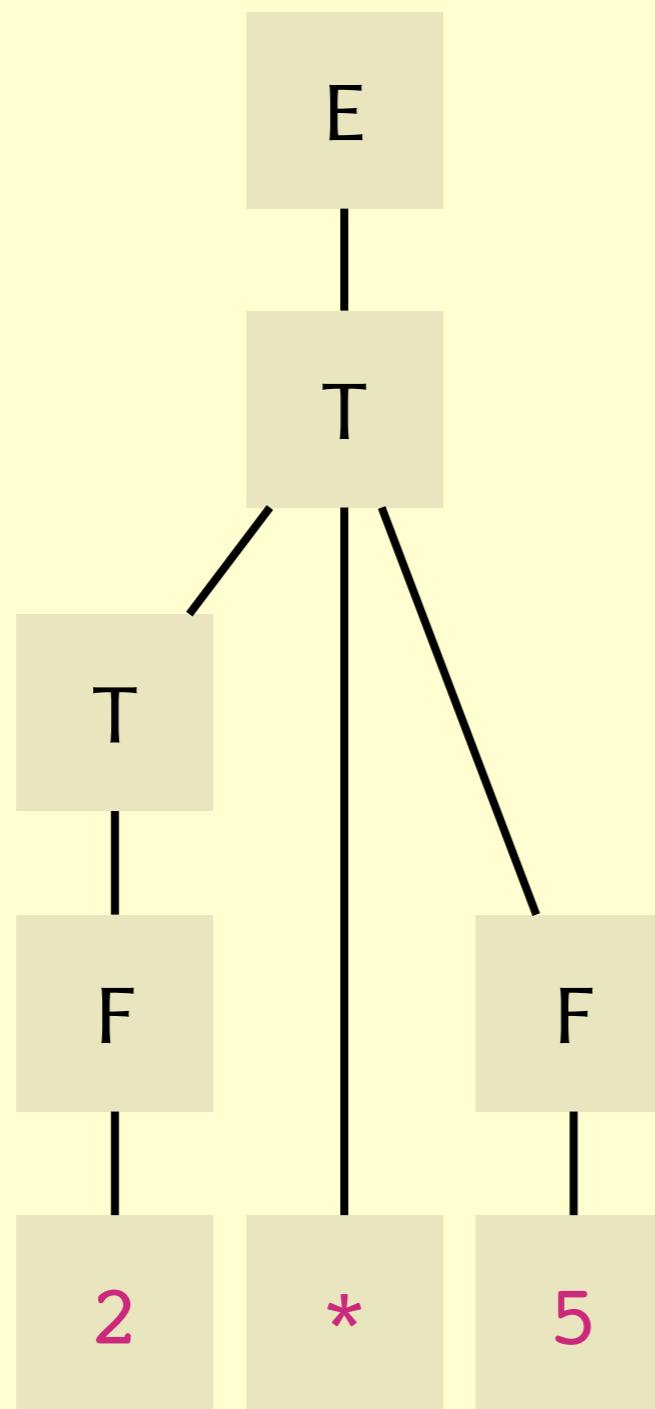
	NULLABLE	FIRST	FOLLOW	
$E ::= T E'$	<b>X</b>	( N	\$	)
$E' ::= + T E' \mid - T E' \mid \epsilon$	<b>✓</b>	+ -	\$ )	
$T ::= F T'$	<b>X</b>	( N	+ - \$	)
$T' ::= * F T' \mid \epsilon$	<b>✓</b>	*	+ - \$ )	
$F ::= ( E ) \mid N$	<b>X</b>	( N	* + - \$ )	

	*	+	-	(	)	N	\$
E	<b>X</b>	<b>X</b>	<b>X</b>	$E \rightarrow T E'$	<b>X</b>	$E \rightarrow T E'$	<b>X</b>
E'	<b>X</b>	$E' \rightarrow + T E'$	$E' \rightarrow - T E'$	<b>X</b>	$E' \rightarrow \epsilon$	<b>X</b>	$E' \rightarrow \epsilon$
T	<b>X</b>	<b>X</b>	<b>X</b>	$T \rightarrow F T'$	<b>X</b>	$T \rightarrow F T'$	<b>X</b>
T'	$T' \rightarrow * F T'$	$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$	<b>X</b>	$T' \rightarrow \epsilon$	<b>X</b>	$T' \rightarrow \epsilon$
F	<b>X</b>	<b>X</b>	<b>X</b>	$F \rightarrow ( E )$	<b>X</b>	$F \rightarrow N$	<b>X</b>

# Can we do better?

- Recursive descent and predictive parsers are **top-down**.
- Top down parsers can't handle left-recursive grammars.
- Can rewrite, but then grammar becomes hard to read!
- Alternative: **bottom-up** parsing.

# Top-down vs. Bottom-up



# Shift/reduce parsing

$E ::= E + T \mid E - T \mid T$

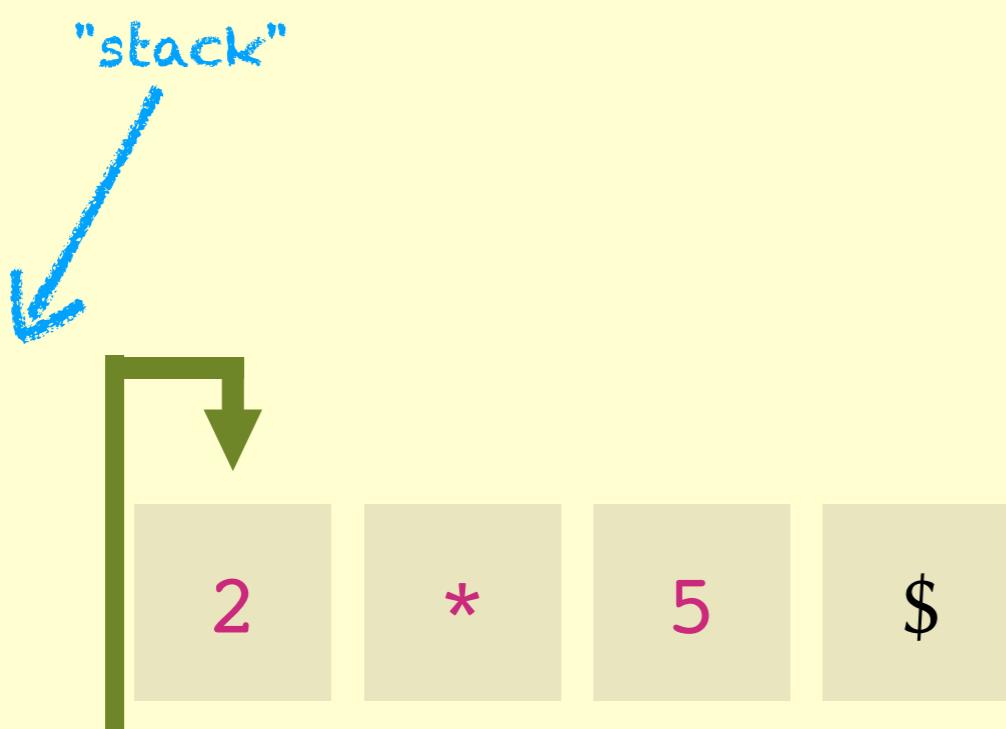
$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

# Shift/reduce parsing

$$E ::= E + T \mid T$$
$$T ::= T * F \mid F$$
$$F ::= ( E ) \mid N$$

**ACTION LOG**  
shift



# Shift/reduce parsing

$E ::= E + T \mid T$

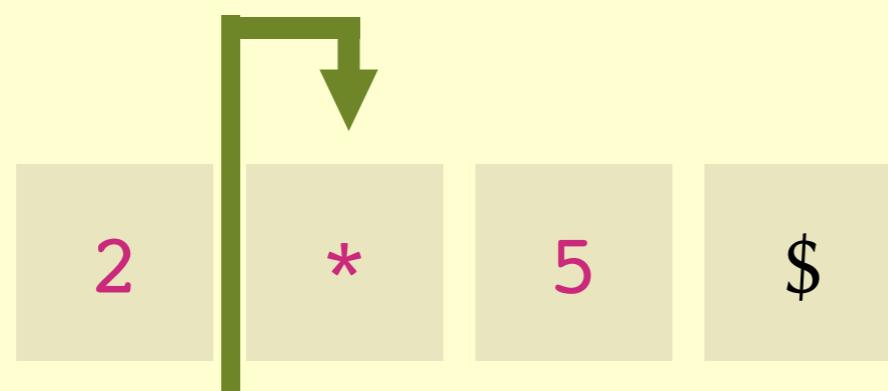
$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

**ACTION LOG**

shift

reduce ( $F \rightarrow N$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

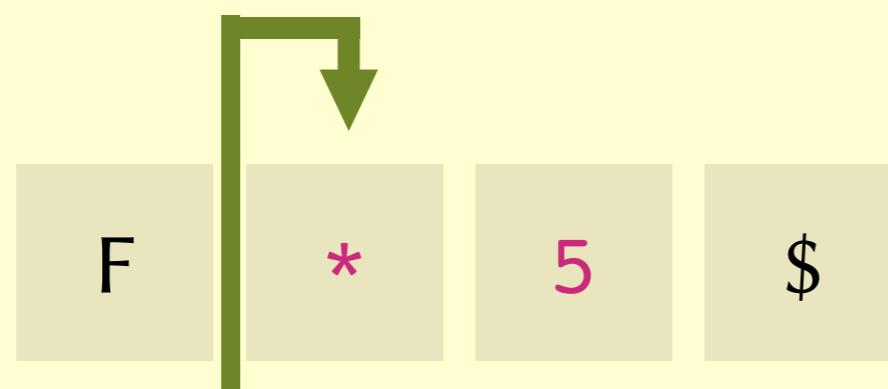
$F ::= ( E ) \mid N$

## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

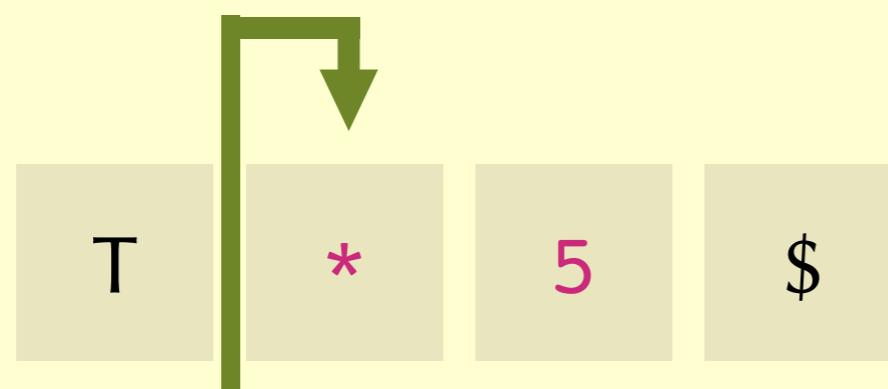
## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

shift



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

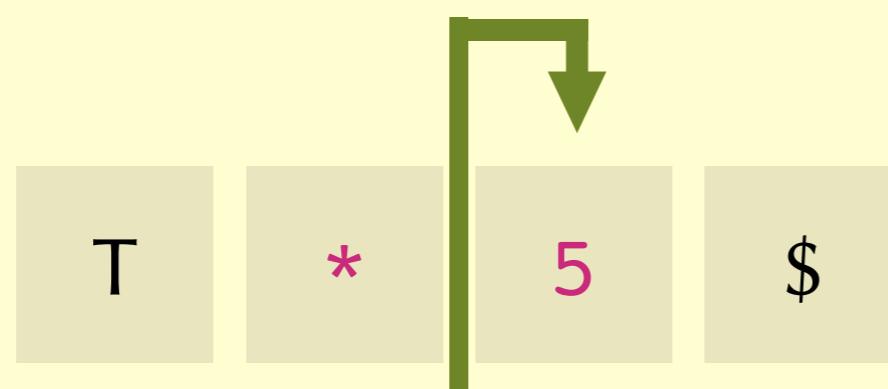
shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

shift

shift



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

shift

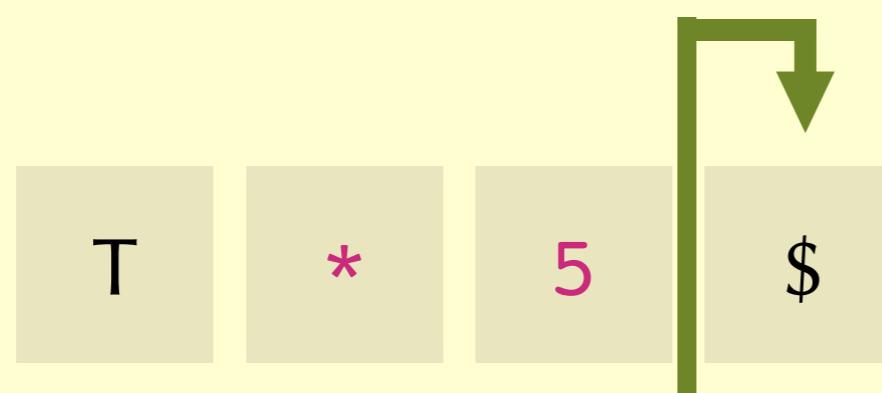
reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

shift

shift

reduce ( $F \rightarrow N$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

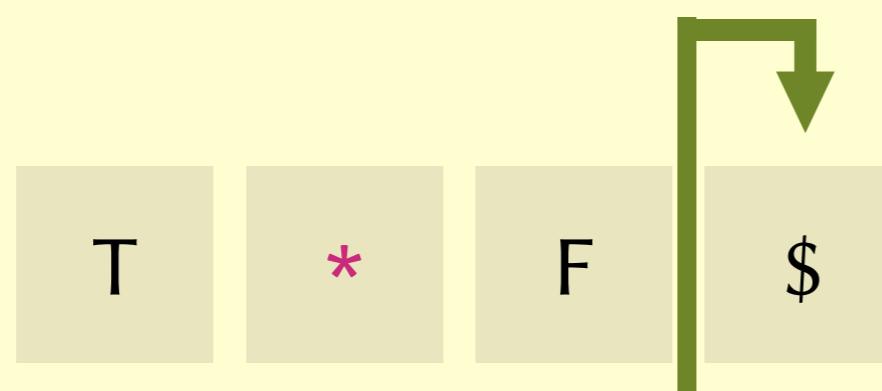
reduce ( $T \rightarrow F$ )

shift

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow T * F$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

shift

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow T * F$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

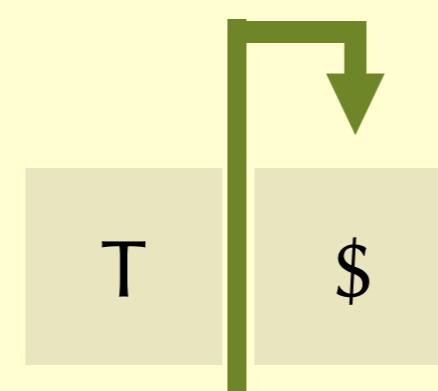
shift

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow T * F$ )

reduce ( $E \rightarrow T$ )



# Shift/reduce parsing

$E ::= E + T \mid T$

$T ::= T * F \mid F$

$F ::= ( E ) \mid N$

## ACTION LOG

shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow F$ )

shift

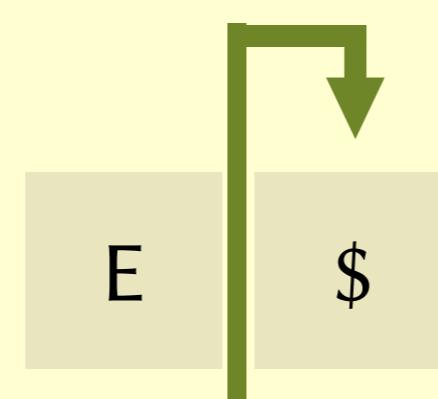
shift

reduce ( $F \rightarrow N$ )

reduce ( $T \rightarrow T * F$ )

reduce ( $E \rightarrow T$ )

accept



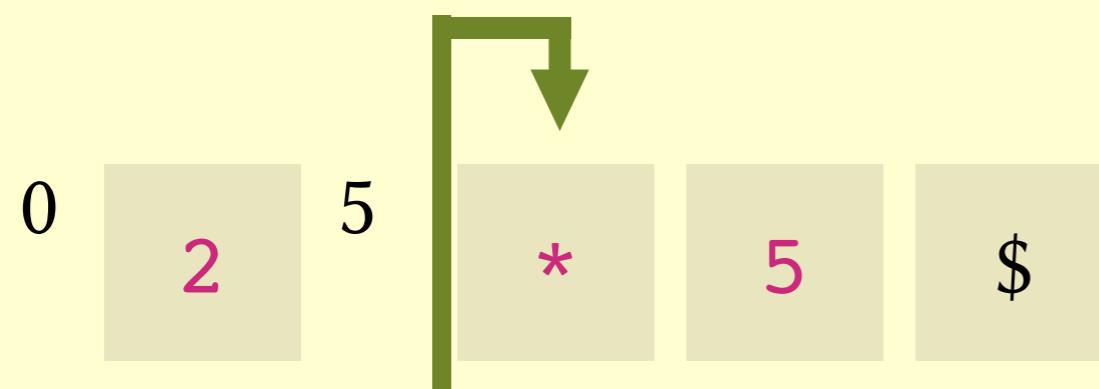
# Shift/reduce parsing

- **Problem.** How do we know whether to shift or reduce?
- **Solution.** Consult the **parsing table**.

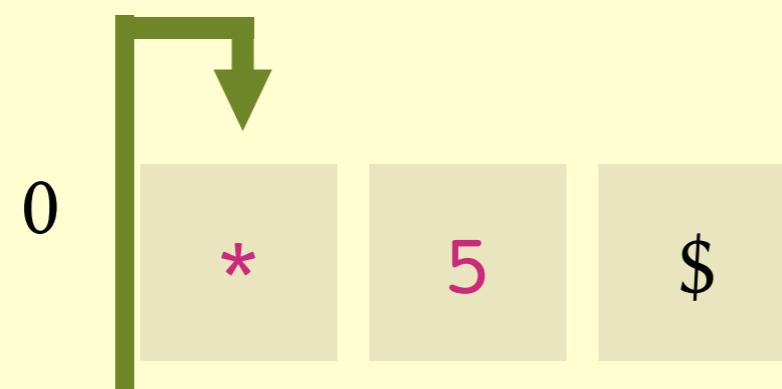
STATE	ACTION						GOTO		
	*	+	(	)	N	\$		E	T
0			s4		s5		1	2	3
1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
4			s4		s5		8	2	3
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
6			s4		s5		9	3	
7			s4		s5				10
8		s6		s11					
9	s7	r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )			
10	r( $T \rightarrow T * F$ )	r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )			
11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			



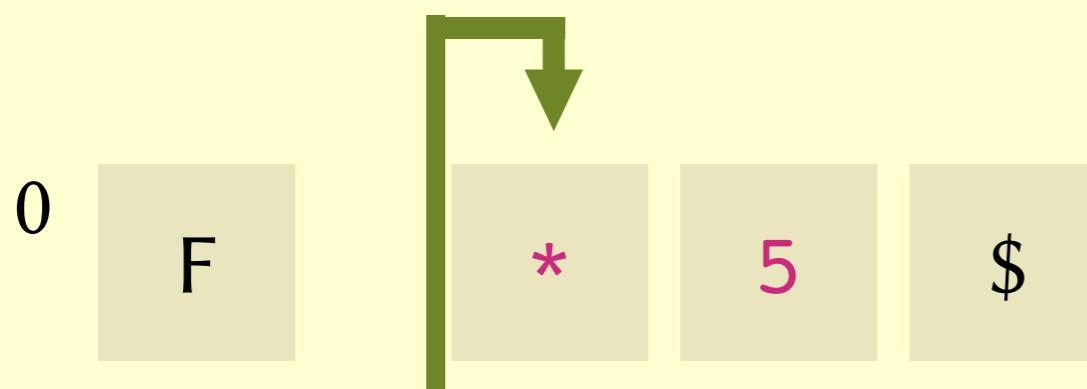
STATE	ACTION							GOTO		
	*	+	(	)	N	\$	E	T	F	
0			s4		s5		1	2	3	
1		s6				acc				
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )				
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )				
4			s4		s5		8	2	3	
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )				
6			s4		s5		9	3		
7			s4		s5				10	
8		s6		s11						
9	s7	r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )				
10	r( $T \rightarrow T * F$ )	r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )				
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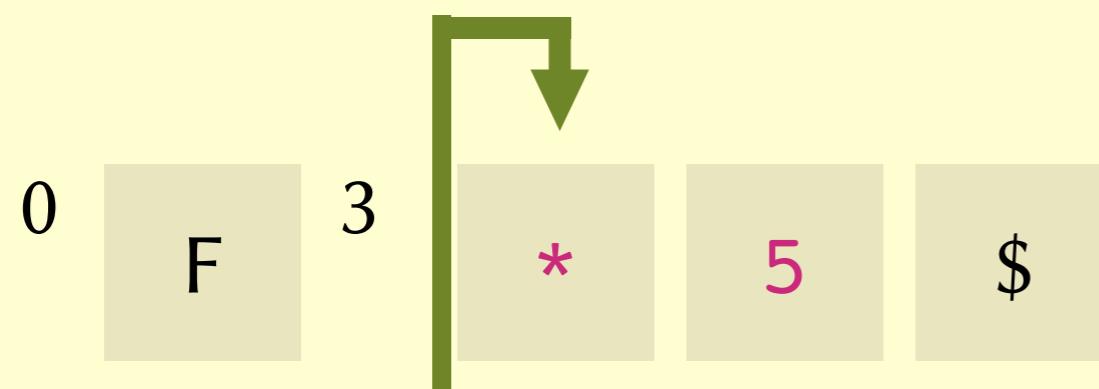
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	*	+	(	)	N	\$	E	T	F
0			s4		s5		1	2	3
1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
4			s4		s5		8	2	3
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
6			s4		s5		9	3	
7			s4		s5				10
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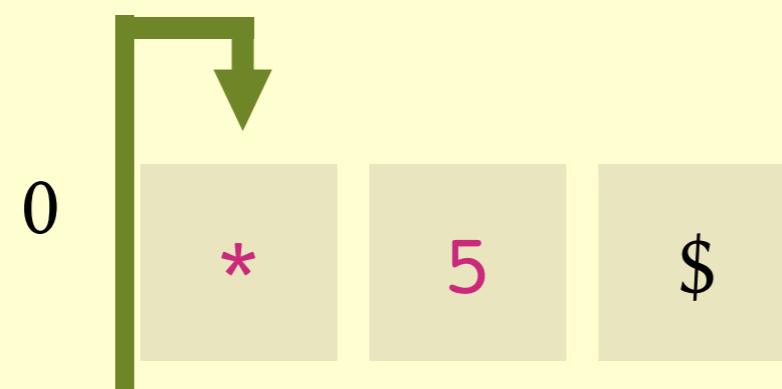
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	*	+	(	)	N	\$	E	T	F
0			s4		s5		1	2	3
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3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
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5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
6			s4		s5			9	3
7			s4		s5				10
8		s6		s11					
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10	r( $T \rightarrow T * F$ )	r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )			
11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			



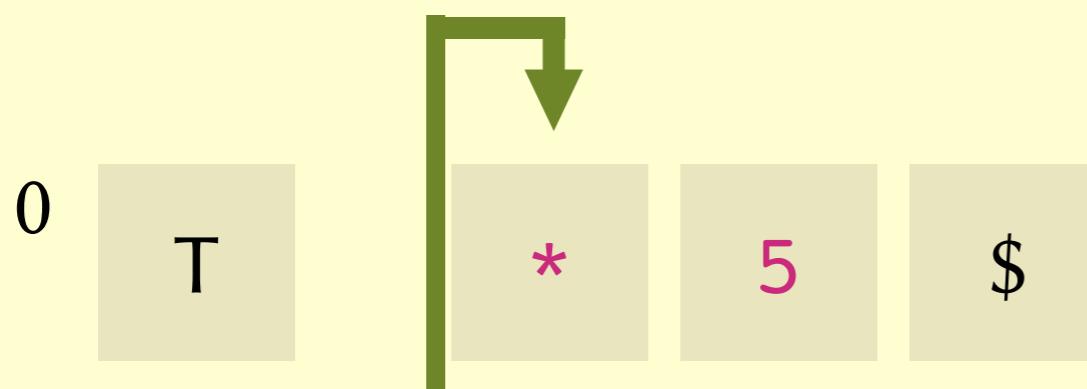
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	*	+	(	)	N	\$	E	T	F
0			s4		s5		1	2	3
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3	r(T → F)		r(T → F)		r(T → F)		r(T → F)		
4			s4		s5		8	2	3
5	r(F → N)	r(F → N)		r(F → N)		r(F → N)			
6			s4		s5			9	3
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8		s6		s11					
9	s7	r(E → E+T)		r(E → E+T)		r(E → E+T)			
10	r(T → T*F)	r(T → T*F)		r(T → T*F)		r(T → T*F)			
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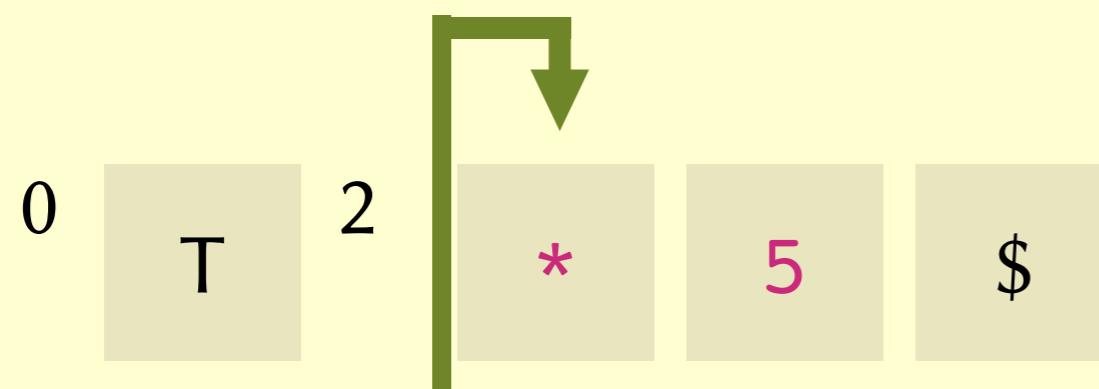
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0			s4		s5		1	2	3
1		s6				acc			
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3	r(T → F)		r(T → F)		r(T → F)		r(T → F)		
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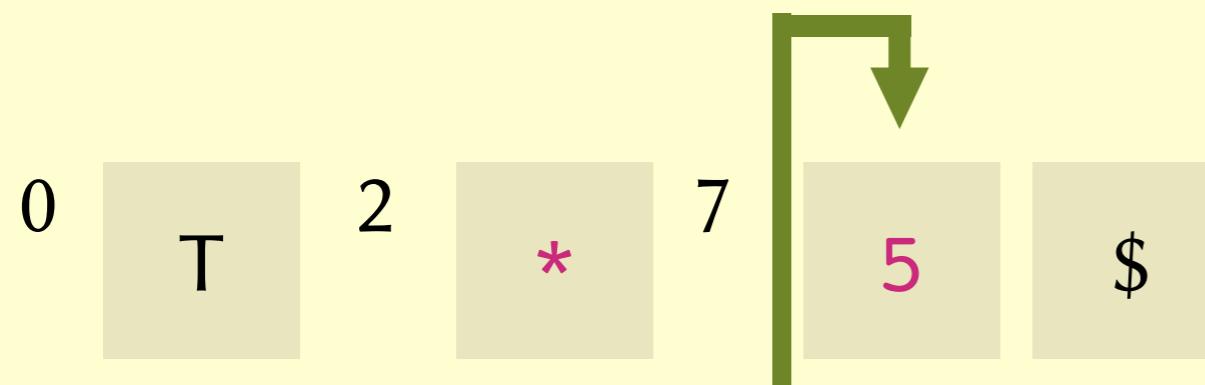
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3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )				
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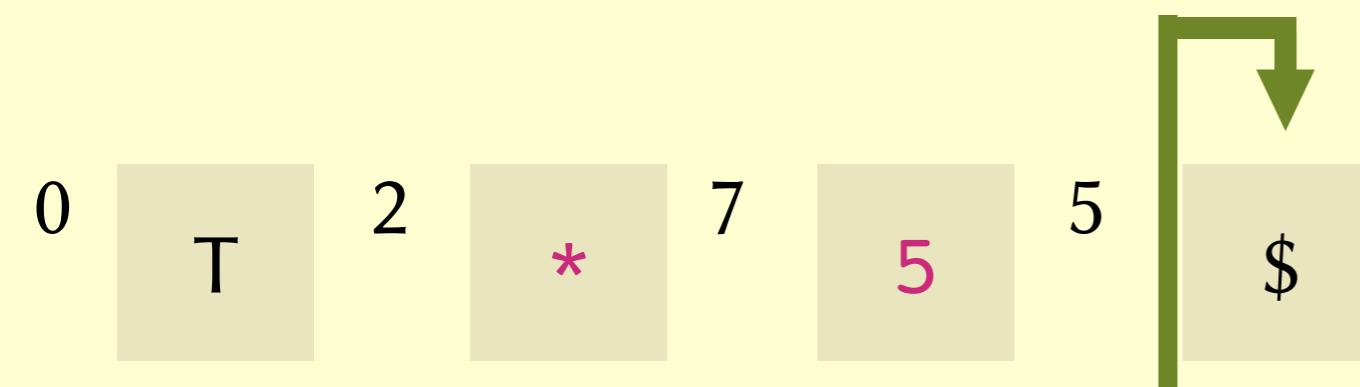
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1		s6				acc			
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3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
4			s4		s5		8	2	3
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
6			s4		s5		9	3	
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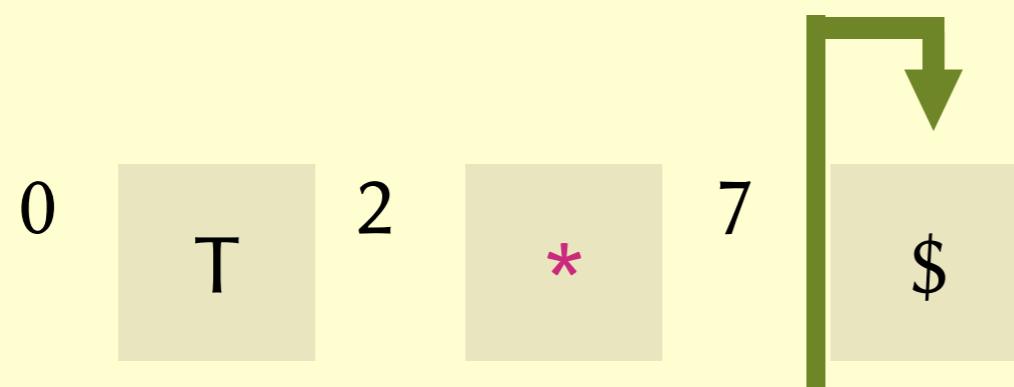
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1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
4			s4		s5		8	2	3
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
6			s4		s5		9	3	
7			s4		s5				10
8		s6		s11					
9	s7	r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )			
10	r( $T \rightarrow T * F$ )	r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )		r( $T \rightarrow T * F$ )			
11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			



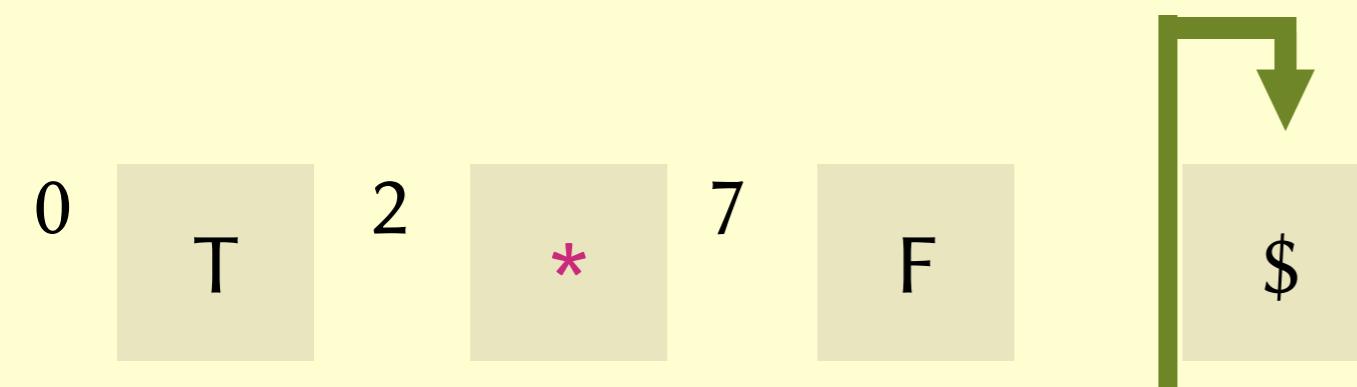
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	*	+	(	)	N	\$	E	T	F
0			s4		s5		1	2	3
1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
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11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			



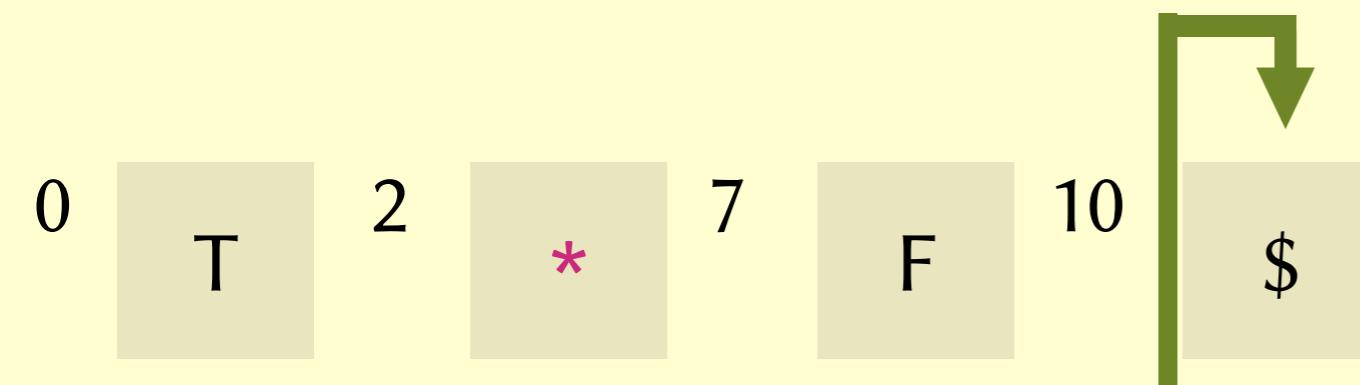
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	*	+	(	)	N	\$	E	T	F
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1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
4			s4		s5		8	2	3
5	r( $F \rightarrow N$ )	r( $F \rightarrow N$ )		r( $F \rightarrow N$ )		r( $F \rightarrow N$ )			
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9	s7	r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )		r( $E \rightarrow E + T$ )			
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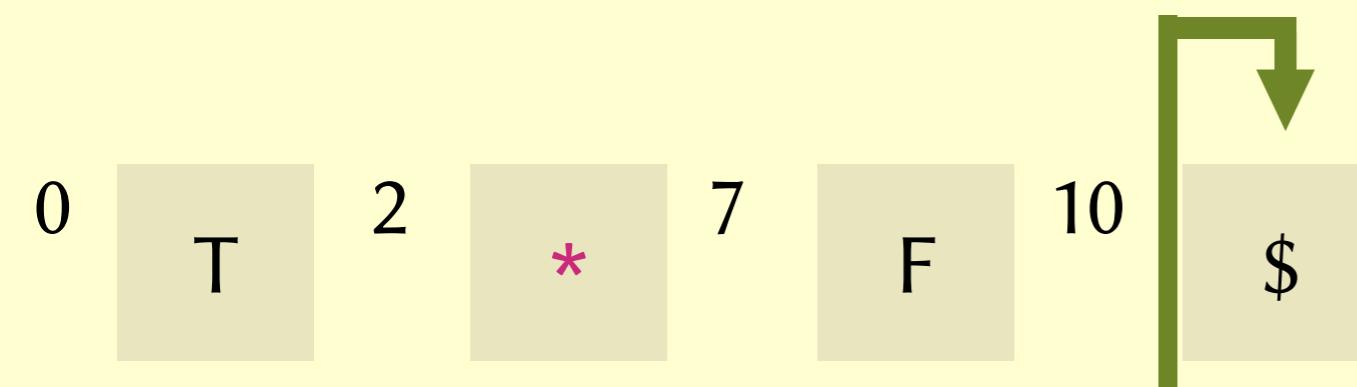
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1		s6				acc			
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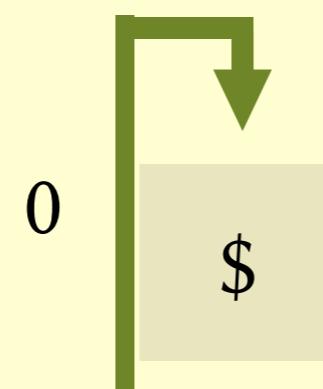
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	*	+	(	)	N	\$	E	T	F
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1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
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11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			



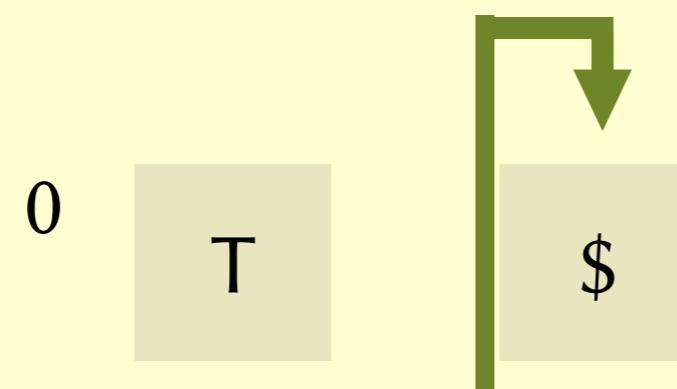
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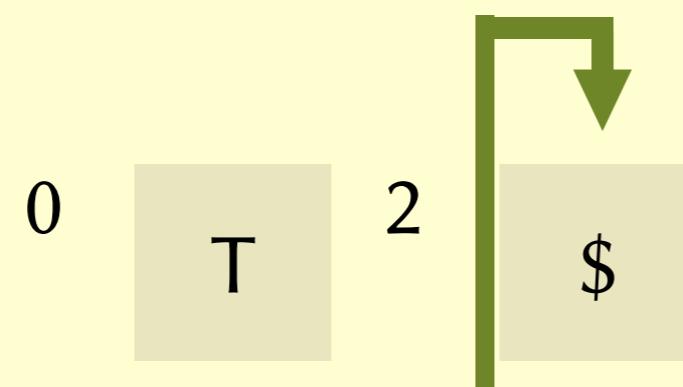
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1		s6				acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			
3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )			
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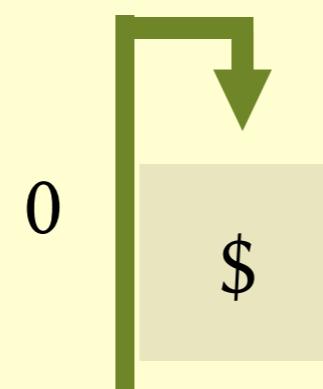
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1		s6				acc				
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3	r( $T \rightarrow F$ )	r( $T \rightarrow F$ )		r( $T \rightarrow F$ )		r( $T \rightarrow F$ )				
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6			s4		s5			9	3	
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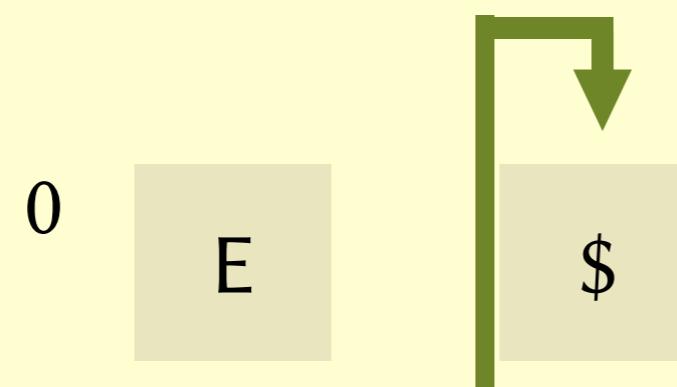
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1		s6					acc			
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11	r( $F \rightarrow (E)$ )	r( $F \rightarrow (E)$ )		r( $F \rightarrow (E)$ )			r( $F \rightarrow (E)$ )			



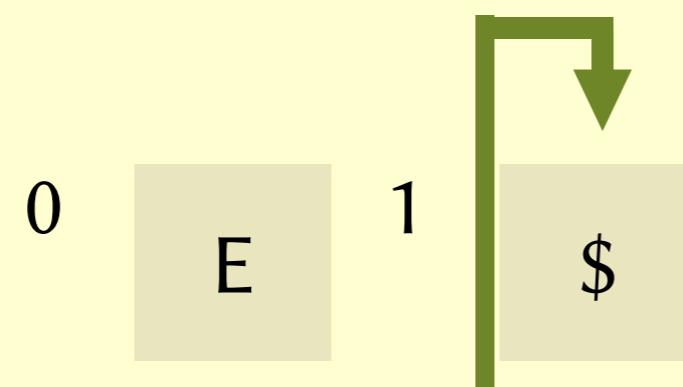
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1		s6					acc			
2	s7	r( $E \rightarrow T$ )		r( $E \rightarrow T$ )			r( $E \rightarrow T$ )			
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	*	+	(	)	N	\$		E	T
0			s4		s5		1	2	3
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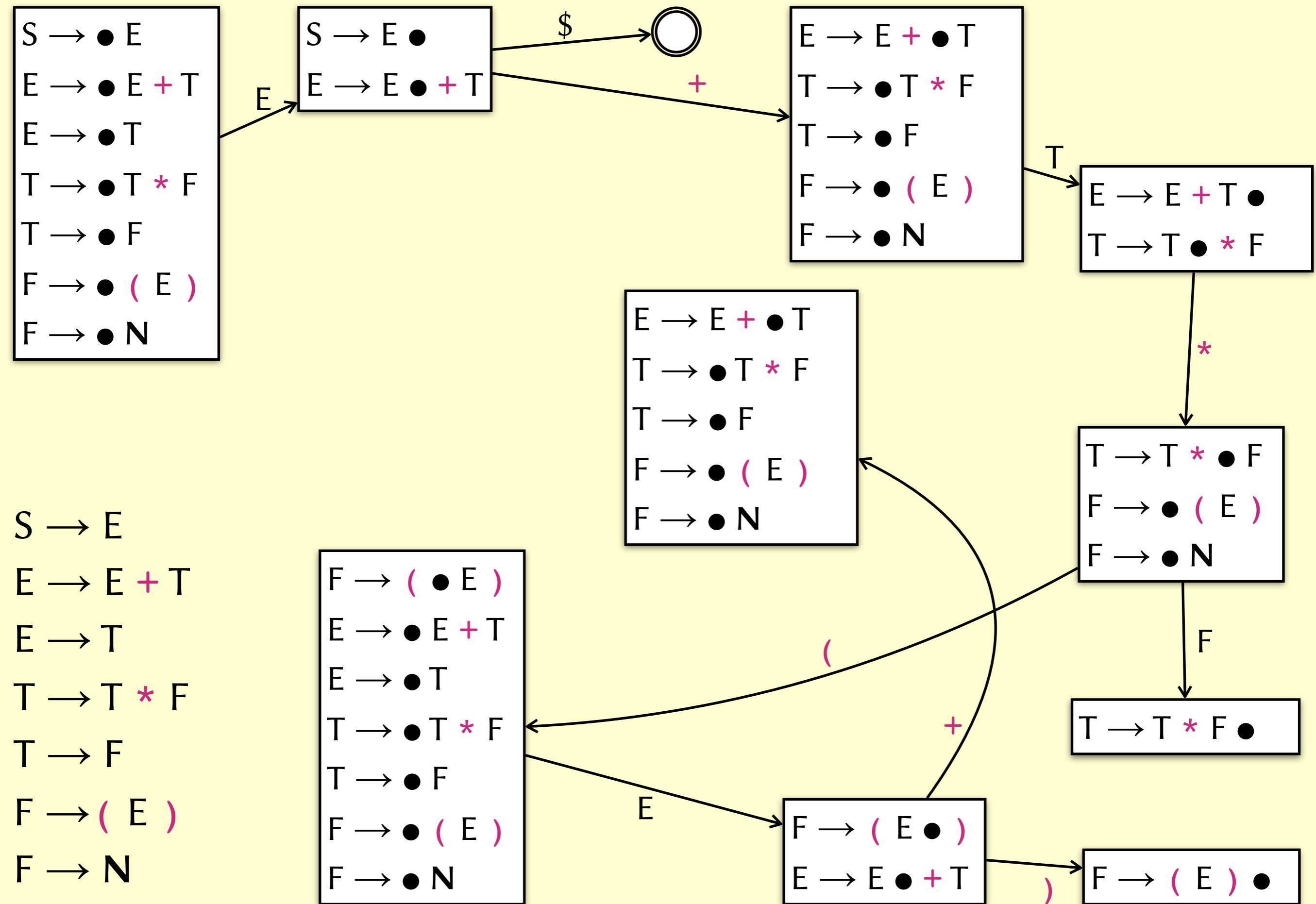


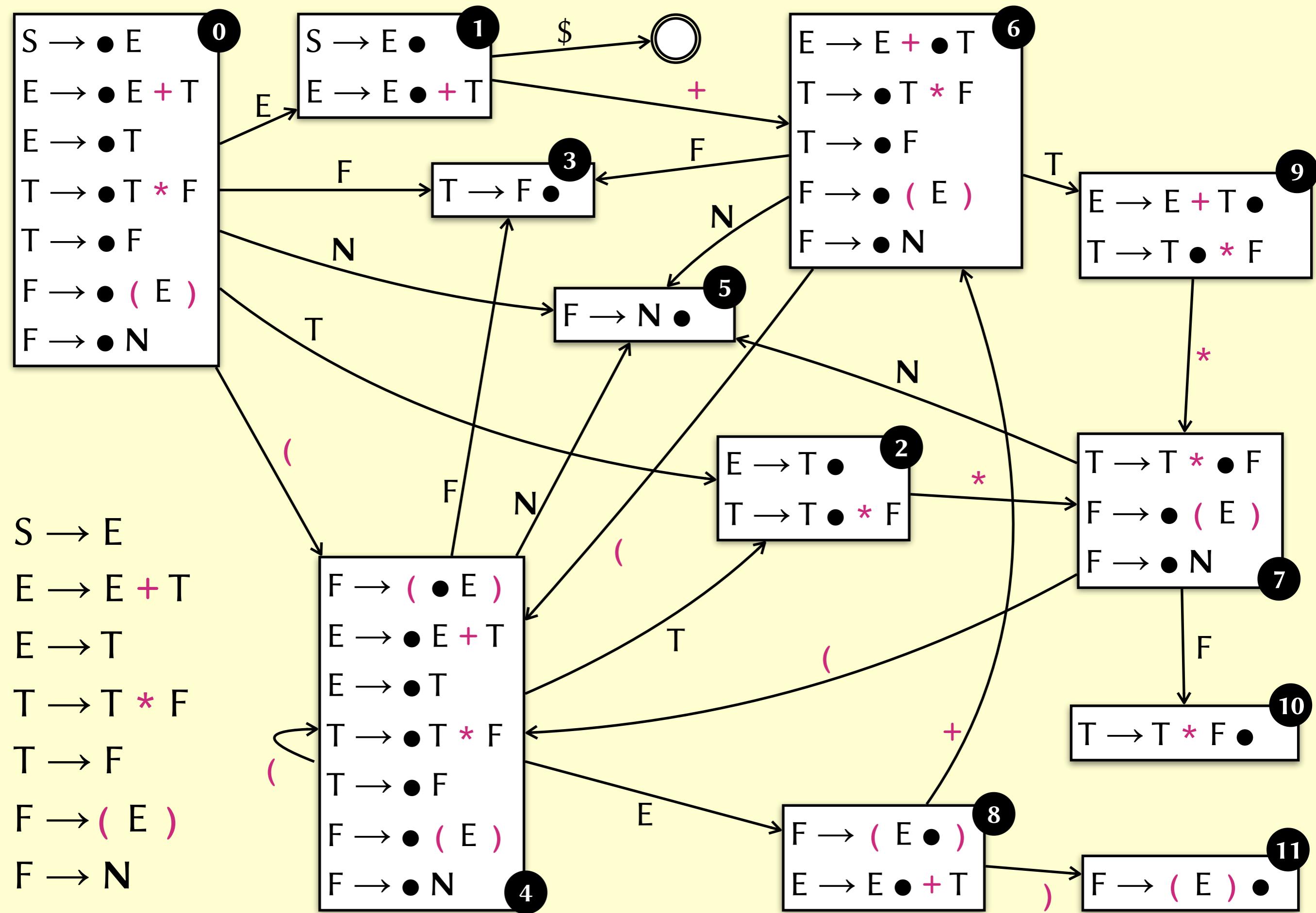
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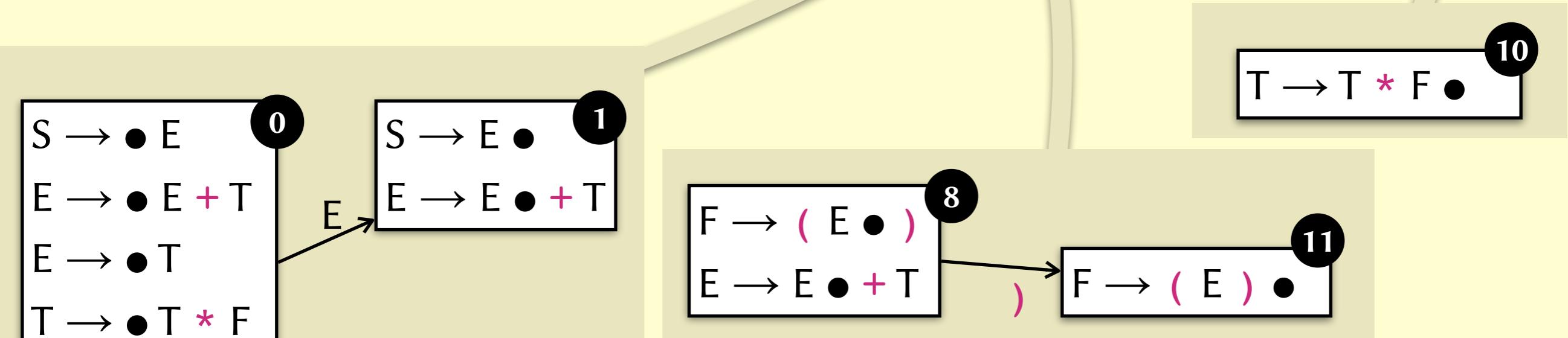
# Shift/reduce parsing

- **Problem.** How do we know whether to shift or reduce?
- **Solution.** Consult the **parsing table**.
- **Problem.** But how did we build the parsing table?
- **Solution.** Like this...

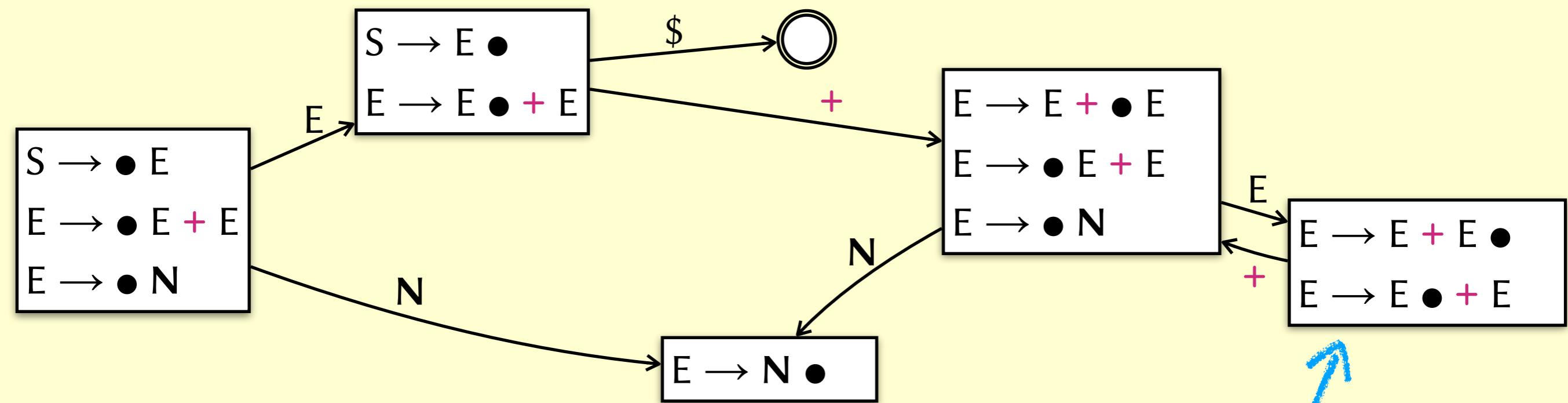




STATE	*	+	(	)	N	\$	E	T	F
0			s4		s5		1	2	3
1		s6				acc			
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11	r(F → ( E ))	r(F → ( E ))		r(F → ( E ))		r(F → ( E ))			



# What can go wrong?



$S \rightarrow E$   
 $E \rightarrow E + E$   
 $E \rightarrow N$

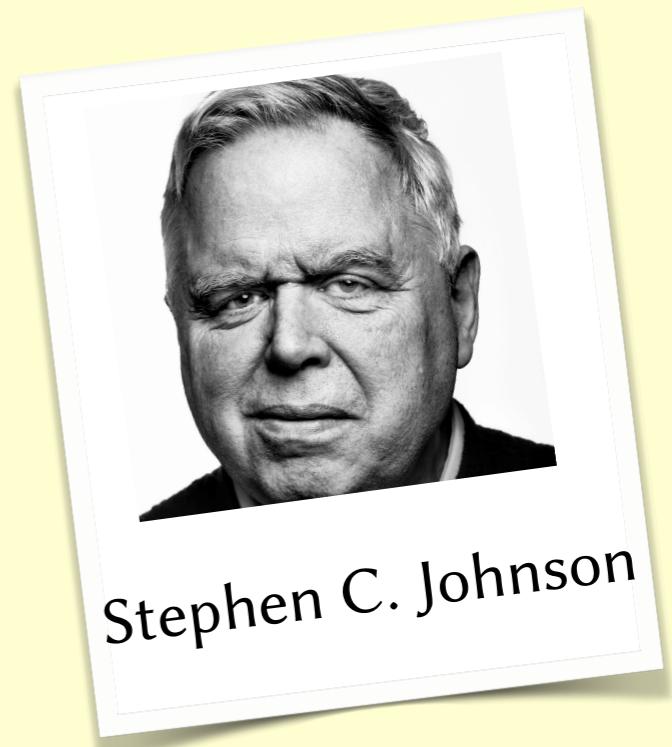
What to do when we  
read a + in this state?

# Shift/reduce parsing

- **Problem.** How do we know whether to shift or reduce?
- **Solution.** Consult the **parsing table**.
- **Problem.** But how did we build the parsing table?
- **Solution.** Like this...
- **Problem.** Seems like a lot of work!
- **Solution.** Use a tool to build the parsing table for you!

# Yacc

- Yacc (yet another compiler compiler) was written in the 1970s at AT&T Labs, and first published in 1975.
- There is an open-source equivalent called Bison.



Stephen C. Johnson

```
expr   : expr '+' term
       | expr '-' term
       | term
       ;
term   : term '*' factor
       | factor
       ;
factor : '(' expr ')'
       | N
       ;
```

```
%token N

%start line

%%

line   : expr '\n'          { return $1; }

;

expr   : expr '+' term     { $$ = $1 + $3; }
       | expr '-' term    { $$ = $1 - $3; }
       | term               { $$ = $1; }

;

term   : term '*' factor  { $$ = $1 * $3; }
       | factor             { $$ = $1; }

;

factor : '(' expr ')'     { $$ = $2; }
       | N                 { $$ = $1; }

;

%%

int main() {...}
```

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- **Shift/reduce parsers** build the parse-tree **bottom-up**. A state machine instructs the parser whether to shift or reduce each time it receives a token.
- **Yacc** can automatically generate a shift/reduce parser from a grammar.