

q++ demoTemplate.cpp -o a; ./ a

Polymorphism

Templates

```
A set of integers: 42 92 79 96 66 4 85 93
After InsertionSort: 4 42 66 79 85 92 93 96
A set of strings: machine intelligence system automation
After InsertionSort: automation intelligence machine system
#include "compare.h" // in which <iostream> is already included
using namespace std;
template <class Elem> inline void swap(Elem A[], int i, int j){
// Reflection: why the inline mechanism is adopted?
        Elem temp = A[i]; A[i] = A[j]; A[j] = temp;
template <class Elem, class Comp>
void InsertionSort(Elem A[], int n){
        for (int i=1; i<n; i++)</pre>
                for(int j=i; (j>0) && (Comp::lt(A[j], A[j-1])); j--)
                        swap(A, j, j-1);}
template <class Elem> void printA(Elem A[], int n){
        for(int i=0; i<n; i++) cout << A[i] << " "; cout << "\n";}</pre>
int main(){
        int n int=8,n char=4; int a int[] = \{42, 92, 79, 96, 66, 4, 85, 93\};
        // A double-quotes pair marked string terminates with '\0' by default
        const char *a char[] = {"machine", "intelligence", "system", "automation"};
        cout << "A set of integers: "; printA(a int, n int);</pre>
        InsertionSort<int,IntCompare>(a int, n int);
        cout << "After InsertionSort: "; printA(a int, n int);</pre>
        cout << "A set of strings: "; printA(a char, n char);</pre>
        InsertionSort<const char*,CharsCompare>(a char, n char);
        cout << "After InsertionSort: "; printA(a char, n char);</pre>
        return 0;
```



class V2EN: public V2{ // 2D vector with Euclidean norm

- **Inheritance**
 - Derived classes (members reusage)

```
public: V2EN(){} V2EN(float xi, float yi):V2(xi,yi){}
                                                                               V2EN(const V2 &c): V2(c){} // constructor overloading
                                                                               // which (different-type 'copy construction') allows both
                                                                               // 1) {V2EN}={V2} (different-type 'copy assignment')
                                                                               // 2) V2EN {FUNC}{... return {V2};}
#include <iostream>
                                                                                //V2EN& operator=(const V2& c){x=c.E(1);y=c.E(2); return *this;}
#include <cmath>
                                                                               // which (different-type 'copy assignment') allows only
using namespace std;
                                                                                // 1) {V2EN}={V2} but not 2) V2EN {FUNC}{... return {V2};}
                                                                                double ENorm() // 'protected' x,y in V2 for derived classes
class V2{ // two-dimensional vector space
                                                                                {return sqrt(x*x+y*y);} // if private x,y in V2, what happens?}
protected:float x,y;
//private:float x,y;
                                                                                //double ENorm() // 'private/protected' for general public
public: V2(){} V2(const V2 &c){x=c.x;y=c.y;}
                                                                               //\{\text{return sqrt}(\text{pow}(\text{this}\rightarrow\text{E}(1),2)+\text{pow}(\text{this}\rightarrow\text{E}(2),2));\}
        V2(float xi, float yi){x=xi;y=yi;} // constructor overloading
        float E(int i) const{return 1==i?x:y;} // get element {1,2}
                                                                       // explicit V2 conversion without taking advantage of slicing
        // function 'const' indicates it does not modify the object
                                                                       V2EN operator+(V2EN a, V2EN b){return (V2)a+(V2)b;}
        // for which it is called (e.g. involved with const arguments)
                                                                       V2EN operator-(V2EN a, V2EN b){return (V2)a-(V2)b;}
        void S(){cout<<'['<<x<<','<<y<<']';}</pre>
                                                                       V2EN operator*(float a, V2EN c){return a*(V2)c;}
        friend V2 operator +(V2,V2); friend V2 operator -(V2,V2);
                                                                       V2EN operator*(V2EN c, float a){return (V2)c*a;}
        friend V2 operator *(float, V2); friend V2 operator *(V2, float);
                                                                       /* if 'V2EN& operator=' is used instead of 'V2EN(const V2&c):V2(c)'
                                                                       V2 operator+(V2EN a, V2EN b){return (V2)a+(V2)b;}
V2 operator+(V2 a, V2 b){return V2(a.x+b.x,a.y+b.y);}
                                                                       V2 operator-(V2EN a, V2EN b){return (V2)a-(V2)b;}
V2 operator-(V2 a, V2 b){return V2(a.x-b.x,a.y-b.y);}
                                                                       V2 operator*(float a, V2EN c){return a*(V2)c;}
V2 operator*(float a, V2 c){return V2(a*c.x,a*c.y);}
                                                                       V2 operator*(V2EN c, float a){return (V2)c*a;}*/
V2 operator*(V2 c, float a){return V2(a*c.x,a*c.y);}
```



Inheritance

Derived classes (members reusage)

```
q++ demoInheritance.cpp -o a; ./ a
                                                                          class V2EN: public V2{ // 2D vector with Euclidean norm
a=[4,3]; b=[3,4]; an=[4,3]; bn=[3,4]
a+b=[7,7]
                                                                          public: V2EN(){} V2EN(float xi, float yi):V2(xi,yi){}
2*a=[8,6]
                                                                                   V2EN(const V2 &c): V2(c){} // constructor overloading
an - bn = [1. - 1]
                                                                                   // which (different-type 'copy construction') allows both
bn*2=[6,8]
                                                                                   // 1) {V2EN}={V2} (different-type 'copy assignment')
|an|=5;|cn|=10;
                                                                                   // 2) V2EN {FUNC}{... return {V2};}
[4.3] - [3.4] = [1.-1]
                                                                                   //V2EN\& operator=(const V2& c){x=c.E(1);y=c.E(2); return *this;}
[4.3]*-2=[-8.-6]
[4,3]+[3,4]=[7,7]
                                                                                   // which (different-type 'copy assignment') allows only
-2*[3,4]=[-6,-8]
                                                                                   // 1) {V2EN}={V2} but not 2) V2EN {FUNC}{... return {V2};}
int main(){
                                                                                   double ENorm() // 'protected' x,y in V2 for derived classes
        V2 \ a(4,3), \ b(3,4), \ c; \ V2EN \ an(4,3), \ bn(3,4), \ cn;
                                                                                   \{\text{return sqrt}(x*x+y*y);\} // if private x,y in V2, what happens?
        cout<<"a=";a.S();cout<<";b=";b.S();cout<<';';
                                                                                   //double ENorm() // 'private/protected' for general public
        cout<<"an=";an.S();cout<<";bn=";bn.S();cout<<endl;</pre>
                                                                                   //\{\text{return sqrt}(\text{pow}(\text{this}\rightarrow\text{E}(1),2)+\text{pow}(\text{this}\rightarrow\text{E}(2),2));\}
        c=a+b; cout<<"a+b=";c.S(); cout<<endl;</pre>
        c=2*a;cout<<"2*a=";c.S();cout<<endl;
                                                                          // explicit V2 conversion without taking advantage of slicing
        cn=an-bn;cout<<"an-bn=";cn.S();cout<<endl;</pre>
                                                                          V2EN operator+(V2EN a, V2EN b){return (V2)a+(V2)b;}
        cn=bn*2;cout<<"bn*2=";cn.S();cout<<endl;</pre>
                                                                          V2EN operator-(V2EN a, V2EN b){return (V2)a-(V2)b;}
        cout<<" | an | = " << an . ENorm() << '; ' << " | cn | = " << cn . ENorm() << "; \n";
                                                                          V2EN operator*(float a, V2EN c){return a*(V2)c;}
                                                                          V2EN operator*(V2EN c, float a){return (V2)c*a;}
        c=a-b;a.S();cout<<'-';b.S();cout<<'=';c.S();cout<<endl;
                                                                          /* if 'V2EN& operator=' is used instead of 'V2EN(const V2&c):V2(c)'
        c=a*-2;a.S();cout<<'*'<<"-2=";c.S();cout<<endl;
                                                                          V2 operator+(V2EN a, V2EN b){return (V2)a+(V2)b;}
        cn=an+bn;an.S();cout<<'+';bn.S();cout<<'=';cn.S();cout<<endl;</pre>
                                                                          V2 operator-(V2EN a, V2EN b){return (V2)a-(V2)b;}
        cn=-2*bn;cout<<"-2*";bn.S();cout<<'=';cn.S();cout<<endl;</pre>
                                                                          V2 operator*(float a, V2EN c){return a*(V2)c;}
        return 0;
                                                                          V2 operator*(V2EN c, float a){return (V2)c*a;}*/
```



- Inheritance
 - Derived classes (members reusage)

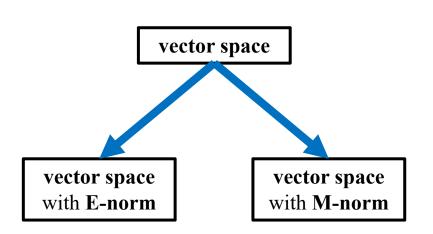
```
class V2EN: public V2{ // 2D vector with Euclidean norm
public: V2EN(){} V2EN(float xi, float yi):V2(xi,yi){}
       V2EN(const V2 &c): V2(c){} // constructor overloading
       // which (different-type 'copy construction') allows both
       // 1) {V2EN}={V2} (different-type 'copy assignment')
       // 2) V2EN {FUNC}{... return {V2};}
       //V2EN& operator=(const V2& c){x=c.E(1);y=c.E(2); return *this;}
       // which (different-type 'copy assignment') allows only
       // 1) {V2EN}={V2} but not 2) V2EN {FUNC}{... return {V2};}
       double ENorm() // 'protected' x,v in V2 for derived classes
        {return sqrt(x*x+y*y);} // if private x,y in V2, what happens?
       //double ENorm() // 'private/protected' for general public
       //{return sqrt(pow(this->E(1),2)+pow(this->E(2),2));}
};
// explicit V2 conversion without taking a vantage of slicing,
V2EN operator+(V2EN a, V2EN b)\{return (\sqrt{2})a+(\sqrt{2})b;\}
V2EN operator-(V2EN a, V2EN b){return (V2)a-(V2)b;}
V2EN operator*(float a, V25(Vc){return a*(V2)c;}
V2EN operator*(V2EN c, fllat a){return (V2)c*a;}
/* if 'V2EN& operator="is used instead of 'V2EN(const V2&c):V2(c)'
V2 operator+(V2) a, V2EN b){return (V2)a+(V2)b;}
V2 operator (V2)a-(V2)b;}
V2 operator*(float a, V2EN c){return a*(V2)c;}
V2 operator*(V2EN c, float a){return (V2)c*a;}*/
```

slicing

```
class V2EN: public V2{ // 2D vector with Euclidean norm
public: V2EN(){} V2EN(float xi, float vi):V2(xi,vi){}
       V2EN(const V2 &c): V2(c){} // constructor overloading
       // which (different-type 'copy construction') allows both
        // 1) {V2EN}={V2} (different-type 'copy assignment')
        // 2) V2EN {FUNC}{... return {V2};}
        //V2EN\& operator=(const V2& c){x=c.E(1);y=c.E(2); return *this;}
        // which (different-type 'copy assignment') allows only
        // 1) {V2EN}={V2} but not 2) V2EN {FUNC}{... return {V2};}
        double ENorm() // 'protected' x,y in V2 for derived classes
        {return sqrt(x*x+y*y);} // if private x,y in V2, what happens?
       //double ENorm() // 'private/protected' for general public
       //{return sqrt(pow(this->E(1),2)+pow(this->E(2),2));}
 ^\prime Slicing: partial copy when the derived converted to the base
  When \{V2EN\}\{+/...\}\{V2EN\}' is used, \{V2\}\{V2EN\}' is
  applied. The two operands {V2EN} are first sliced to {V2}, so
    {V2EN}{+/...}{V2EN}' does 'V2{V2EN}{+/...}V2{V2EN}' and returns {V2}
```



- Inheritance
 - Derived classes (members reusage)



- 1) Repetitive works avoidance
- 2) Concepts organization

```
class V2EN: public V2{ // 2D vector with Euclidean norm
public: V2EN(){} V2EN(float xi, float vi):V2(xi,vi){}
       V2EN(const V2 &c): V2(c){} // constructor overloading
       // which (different-type 'copy construction') allows both
       // 1) {V2EN}={V2} (different-type 'copy assignment')
       // 2) V2EN {FUNC}{... return {V2};}
       //V2EN\& operator=(const V2& c){x=c.E(1); v=c.E(2); return *this;}
       // which (different-type 'copy assignment') allows only
        // 1) {V2EN}={V2} but not 2) V2EN {FUNC}{... return {V2};}
        double ENorm() // 'protected' x,y in V2 for derived classes
        {return sqrt(x*x+y*y);} // if private x,y in V2, what happens?
       //double ENorm() // 'private/protected' for general public
       //{return sqrt(pow(this->E(1),2)+pow(this->E(2),2));}
  Slicing: partial copy when the derived converted to the base
   When \{V2EN\}\{+/...\}\{V2EN\}' is used, \{V2COPERTATE V2EN\}\{V2EN\}' is
  applied. The two operands {V2EN} are first sliced to {V2}, so
   '{V2EN}{+/...}{V2EN}' does 'V2{V2EN}{+/...}V2{V2EN}' and returns {V2}
 // Define a derived class V2MN in similar way
class V2MN: public V2{ // 2D vector with Mahalanobis norm
```



Inheritance

Derived classes (members reusage)

private	class's members & friends can use
protected	class's members & friends and derived classes's members & friends can use
public	general public can use

base class's members	private	protected	public
private inheritance	private	private	private
protected inheritance	private	protected	protected
public inheritance	private	protected	public

types of inherited members in derived classes



- Inheritance+Polymorphism
 - Virtual functions

```
virtual {TYPE} {FUNCTION}({ARGUMENTS});
```

virtual means "may be redefined later in a class derived from this one"

```
virtual {TYPE} {FUNCTION}({ARGUMENTS}) =0;
```

=0 says the **virtual** function is **pure virtual**, which means "not defined in this one, but *must* be defined later in any class derived from this one"



- Inheritance+Polymorphism

```
virtual \{TYPE\} \{FUNC\}(\{ARG\}) = 0;
```

pure virtual

```
g++ demoVirtual pure.cpp -o a; ./ a r; ./ a c
Rect{x:4.000000,y:3.000000,w:6.000000,h:5.000000}
Shape area: 30
Shape circumference: 22
Circle{x:7.000000,y:8.000000,r:10.000000}
Shape area: 314
Shape circumference: 62.8
```

```
#include <iostream>
Virtual functions using namespace std;
                     class Shape{public:virtual float A()=0;virtual float C()=0;virtual void S()=0;};
Public interfaces class Rect: public Shape{private:float x, y, w, h;
                     public: Rect(float xi, float yi, float wi, float hi)
                             {x=xi:v=vi:w=wi:h=hi:}
                             float A(){return w*h;} float C(){return 2*(w+h);}
                             void S(){printf("Rect{x:%f,y:%f,w:%f,h:%f}\n",x,y,w,h);}
                     class Circ: public Shape{private:float x, y, r;
                     public: Circ(float xi, float yi, float ri){x=xi;y=yi;r=ri;}
                             float A(){return 3.14*r*r;} float C(){return 6.28*r;}
                             void S()\{printf("Circle\{x:\%f,y:\%f,r:\%f\}\n",x,y,r);\}
                     int main(int argn, char* argc[]){
                             // cannot instantiate a pure virtual type, but a reference of it
                             // serves somewhat as the void* pointer in C programming language
                             Shape* a shape;
                             if (1==argn || argc[1][0]=='r'){
                                     Rect a rect(4,3,6,5); a shape = &a rect;
                             }else{ Circ a circ(7,8,10); a shape = &a circ; }
                             a shape->S();cout << "Shape area: "<<a shape->A()<<"\n";
                             cout << "Shape circumference: "<<a shape->C()<<"\n";</pre>
                             return 0:
                      "demoVirtual pure.cpp" 25L, 1017C
```



- Inheritance+Polymorphism
 - Virtual functions
 - Public interfaces

```
virtual {TYPE} {FUNC}({ARG});
```

(general i.e. non-pure) virtual

Shape circumference: 62.8

```
g++ demoVirtual_def.cpp -o _a; ./_a r; ./_a c
Rect{x:4.000000,y:3.000000,w:6.000000,h:5.000000}
Shape area: 30
Shape circumference: 22
Circle{x:7.000000,y:8.000000,r:10.000000}
Shape area: 314
```

```
#include <iostream>
using namespace std;
class Shape{public: virtual float A(){return 0;};
        virtual float C(){return 0;};virtual void S(){};};
class Rect: public Shape{private:float x, y, w, h;
public: Rect(float xi, float yi, float wi, float hi)
        {x=xi;v=vi;w=wi;h=hi;}
        float A(){return w*h;} float C(){return 2*(w+h);}
        void S()\{printf("Rect\{x:\%f,y:\%f,w:\%f,h:\%f\}\n",x,y,w,h);\}
class Circ: public Shape{private:float x, y, r;
public: Circ(float xi, float yi, float ri){x=xi;y=yi;r=ri;}
        float A(){return 3.14*r*r;} float C(){return 6.28*r;}
        void S()\{printf("Circle\{x:\%f,y:\%f,r:\%f\}\n",x,y,r);\}
int main(int argn, char* argc[]){
        Shape* a shape;
        if (1==argn || argc[1][0]=='r'){
                Rect a rect(4,3,6,5); a_shape = &a_rect;
        }else{ Circ a circ(7,8,10); a shape = &a circ; }
        a shape->S();cout << "Shape area: "<<a shape->A()<<"\n";
        cout << "Shape circumference: "<<a shape->C()<<"\n";</pre>
        return 0;
```



- Inheritance+Polymorphism
 - Virtual functions
 - Public interfaces

```
virtual {TYPE} {FUNC}({ARG});
```

(general i.e. non-pure) virtual

why pure virtual?

```
g++ demoVirtual_ndef.cpp -o _a; ./_a r; ./_a c
Rect{x:4.000000,y:3.000000,w:6.000000,h:5.000000}
Shape area: 30
Shape circumference: 22
Circle{x:7.000000,y:8.000000,r:10.000000}
Shape area: 0
Shape circumference: 0
```

```
#include <iostream>
using namespace std;
class Shape{public: virtual float A(){return 0;};
        virtual float C(){return 0;};virtual void S(){};};
class Rect: public Shape{private:float x, y, w, h;
public: Rect(float xi, float yi, float wi, float hi)
        {x=xi;v=vi;w=wi;h=hi;}
        float A(){return w*h;} float C(){return 2*(w+h);}
        void S(){printf("Rect{x:%f,y:%f,w:%f,h:%f}\n",x,y,w,h);}
class Circ: public Shape{private:float x, y, r;
public: Circ(float xi, float yi, float ri){x=xi;y=yi;r=ri;}
        // if definition of virtual functions is forgotten
        //float A(){return 3.14*r*r;} float C(){return 6.28*r;}
        void S(){printf("Circle{x:%f,y:%f,r:%f}\n",x,y,r);}
int main(int argn, char* argc[]){
        Shape* a shape;
        if (1==argn || argc[1][0]=='r'){
                Rect a rect(4,3,6,5); a shape = &a rect;
        else{Circ a circ(7,8,10); a shape = &a circ; }
        a shape->S();cout << "Shape area: "<<a shape->A()<<"\n";
        cout << "Shape circumference: "<<a shape->C()<<"\n";</pre>
        return 0;
```



- Inheritance+Polymorphism
 - Virtual functions
 - Public interfaces

```
\{TYPE\} \{FUNC\}(\{ARG\});
```

non-virtual

why virtual?

Shape circumference: 0

```
g++ demoVirtual_non.cpp -o _a; ./_a r; ./_a c
Rect{x:4.000000,y:3.000000,w:6.000000,h:5.000000}
Shape area: 0
Shape circumference: 0
Circle{x:7.000000,y:8.000000,r:10.000000}
Shape area: 0
```

```
#include <iostream>
using namespace std;
class Shape{public: float A(){return 0;}; float C(){return 0;};
        virtual void S(){};};
class Rect: public Shape{private:float x, y, w, h;
public: Rect(float xi, float yi, float wi, float hi)
        {x=xi;y=yi;w=wi;h=hi;}
        float A(){return w*h;} float C(){return 2*(w+h);}
        void S(){printf("Rect{x:%f,y:%f,w:%f,h:%f}\n",x,y,w,h);}
class Circ: public Shape{private:float x, y, r;
public: Circ(float xi, float yi, float ri){x=xi;y=yi;r=ri;}
        float A(){return 3.14*r*r;} float C(){return 6.28*r;}
        void S()\{printf("Circle\{x:\%f,y:\%f,r:\%f\}\n",x,y,r);\}
int main(int argn, char* argc[]){
        Shape* a shape;
        if (1==argn || argc[1][0]=='r'){
                Rect a rect(4,3,6,5); a shape = &a rect;
        }else{ Circ a circ(7,8,10); a shape = &a circ; }
        a shape->S();cout << "Shape area: "<<a shape->A()<<"\n";
        cout << "Shape circumference: "<<a shape->C()<<"\n";</pre>
        return 0;
```



- Inheritance+Polymorphism
 - Virtual functions
 - Public interfaces
- Non-virtual
 - If F() of base class is not virtual, base pointer->F() in main always executes F() of base class, be F() redefined or not in derived class.
- Virtual (general i.e. non-pure)
 - If F() of base class is virtual but without =0, base pointer->F() in main executes F() of derived class if F() is refined in derived class; otherwise, executes F() of base class.
- Pure virtual
 - If A() of base class is pure virtual i.e. with =0, F() must be redefined in derived class, so base pointer->A() in main definitely executes F() of derived class.



- Inheritance+Polymorphism
 - Virtual functions
 - Public interfaces

non-virtual



virtual



virtual {TYPE} {FUNCTION}({ARGUMENTS});

virtual means "may be redefined later in a class derived from this one"

virtual {TYPE} {FUNCTION}({ARGUMENTS}) =0;

=0 says the **virtual** function is **pure virtual**, which means "not defined in this one, but *must* be defined later in any class derived from this one"



THANK YOU

