

1.1

$$1. P[G_H] = 0.95 \rightarrow P[\neg G_H] = 0.05$$

$$P[S_I | G_H] = 0.02$$

$$P[S_I | \neg G_H] = 0.3$$

$$P[S_I] = P[S_I | G_H] P[G_H] + P[S_I | \neg G_H] P[\neg G_H]$$

$$= 0.02 \times 0.95 + 0.3 \times 0.05$$

$$= 0.034$$

$$P[G_H | S_I] = \frac{P[S_I | G_H] P[G_H]}{P[S_I]}$$

$$= \frac{0.02 \times 0.95}{0.034}$$

$$= 0.56$$

$$2. P[S_{IT} | G_H] = P[S_I | G_H]^2 = 0.02^2 = 0.0004$$

$$P[S_{IT} | \neg G_H] = P[S_I | \neg G_H]^2 = 0.3^2 = 0.09$$

$$P[G_H] = 0.95$$

$$P[S_{IT}] = P[S_{IT} | G_H] P[G_H] + P[S_{IT} | \neg G_H] P[\neg G_H]$$

$$= 0.0004 \times 0.95 + 0.09 \times 0.05$$

$$= 0.00488$$

$$P[G_H | S_{IT}] = \frac{P[S_{IT} | G_H] P[G_H]}{P[S_{IT}]}$$

$$= \frac{0.0004 \times 0.95}{0.00488} = 0.078$$