

SS 2024 Solutions - Exam solution of the year 2024 summer semester

Introduction to Deep Learning (Technische Universität München)



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Chair of Visual Computing School of Computation, Information and Technology Technical University of Munich

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Note:

- During the attendance check a sticker containing a unique code will be put on this exam.
- This code contains a unique number that associates this exam with your registration number.
- This number is printed both next to the code and to the signature field in the attendance check list.

Introduction to Deep Learning

Exam: IN2346 / endterm **Date:** Friday 26th July, 2024

Examiner: Prof. Dr. Matthias Nießner **Time:** 08:30 – 10:00

	P 1	P 2	P 3	P 4	P 5	P 6	P 7	
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Working instructions

- This exam consists of 16 pages with a total of 7 problems.
 Please make sure now that you received a complete copy of the exam.
- The total amount of achievable credits in this exam is 90 credits.
- · Detaching pages from the exam is prohibited.
- Allowed resources:
 - none
- Answers are only accepted if the solution approach is documented. Give a reason for each answer unless explicitly stated otherwise in the respective subproblem.
- Do not write with red or green colors nor use pencils.
- Physically turn off all electronic devices, put them into your bag and close the bag.

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Problem 1 Multiple Choice (18 credits)

Mark correct answers with a cross

To undo a cross, completely fill out the answer option

To re-mark an option, use a human-readable marking



Please note:

- For all multiple choice questions any number of answers, i.e. either zero (!), one or multiple answers can be correct.
- For each question, you'll receive 2 points if all boxes are answered correctly (i.e. correct answers are checked, wrong answers are not checked) and 0 otherwise.

1.1 Which of the following statements on Convolutional Neural Networks are true?
Early layers typically capture high-level features.
☐ All layers in a CNN have the same receptive field size.
☑ Deep layers typically capture high-level features.
Pooling layers can be used to reduce the spatial dimension of the feature maps.
1.2 Which of the following statements on activation functions are true?
The Softmax activation function is invariant to scale, i.e. $Softmax(cx) = Softmax(x)$.
☐ The output of Leaky ReLU is always non-negative.
Skip connection adds non-linearity to the model; therefore, it is a type of activation function.
1.3 Choose layers that are used in a Transformer model.
☐ Recurrent layers
Softmax layers
Convolutional layers
1.4 Which of the following statements correctly describes the relationship between loss curves, overfitting, and underfitting?
Overfitting occurs when both training and validation loss are high.
A model is underfitting if the training loss is low and the validation loss is high.
A loss curve showing a consistently decreasing training loss and a decreasing validation loss indicates overfitting.
✓ Underfitting is indicated by high training loss and high validation loss.
1.5 Which of the following statements about Dropout are true?
☐ It can not be applied to CNN.
During evaluation, it activates all nodes and scales up the output value.
It can be seen as an ensemble of networks.
☐ It increases the gap between validation loss and training loss in general.

1.6 Your model for classifying different cat species is getting a low training error with a high validation error. Which of the following are promising things to try to improve the performance?
Add weight regularization
▼ Transfer learning from a pre-trained large model
☐ Decrease the learning rate
Add more linear layers
1.7 Which of the following propositions about a Convolutional layer are true?
The channels of the input image and the number of filters can be different.
▼ The total number of parameters depends on the width and height of the kernel.
☐ The total number of parameters depends on padding.
The output size depends on the stride.
1.8 Which of the following functions are NOT suitable as activation functions to add non-linearity to a network?
f(x) = x
The floor function $f(x) = \lfloor x \rfloor$
f(x) = x
$f(x) = \sqrt{x}$
1.9 What is true about Generative Adversarial Networks for image generation?
☐ When training the Generator, we use a frozen pre-trained Discriminator as supervision.
▼ The Generator decodes a latent vector into an image.
A reduced generator loss generally means an increased discriminator loss.
Training a GAN does not require manual "real/fake" labeling of the image.
Training a GAN does not require manual "real/fake" labeling of the image.

Problem 2 Short Questions (16 credits) 2.1 Explain the role of 1x1 convolutions in CNN. Reduce the number of channels. 2.2 Explain the concept of receptive field. What happens if the receptive field of the output layer is too small? Receptive field refers to the region in the input that affects a particular feature in the output. If the receptive field is too small, the output won't capture the information of the entire input, causing the prediction to be inaccurate. 2.3 Consider two different models for image classification of the MNIST dataset. The models are (i) a fully connected network with three hidden layers of size 16, (ii) VGGNet. Which of the two models is more robust to the translation of the digits in the images? Give a short explanation of why. VGGNet is more robust to translation of the digits in the images because it uses convolutions, which are translation equivariant and has a larger capacity for capturing complex patterns. 2.4 Alexnet is using an 11 x 11 convolutional filter in the first layer. Name 1 disadvantage of using such a large filter. 11 x 11 is very expensive in both parameters and calculations. It captures more global features than specific local features. 2.5 You are trying to solve a binary classification problem, but the positive class is very underrepresented (e.g., 8 negatives for every positive). Describe a technique that you can use during training to help alleviate the class imbalance problem. Would you apply this technique at test time as well? Why or why not? Oversample the positive class so that it is more evenly distributed during training. You wouldn't apply this technique at test time because it would result in an inaccurate model performance metric (accuracy). Or apply different weights to the losses of images from different classes. This does not affect the accuracy, so it doesn't matter if you apply it on test time.

Or apply different weights to the losses of images from different classes.

This does not affect the accuracy, so it doesn't matter if you apply it on test time.

2.6 Give one situation where it would make sense to overfit the model on purpose.

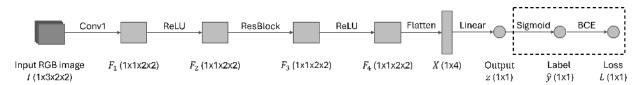
To test the functionality and capability of the model on a small subset of data before the normal training.

To fine-tune a model on a dataset to be tested.

8 If your input batch of images is 10×20×30×40 (N×C×H×W), how many parameters are there 3 convolution filter operating on this input with stride 2, including bias?	in a single
3x3x20+1=181	
.9 The Adam optimizer is described with the following formulae:	
$\begin{split} m_k &= \beta_1 m_{k-1} + (1-\beta_1) \nabla L(x,\theta), v_k &= \beta_2 v_{k-1} + (1-\beta_2) [\nabla L(x,\theta) \circ \nabla L(x,\theta)], \\ \hat{m}_k &= \frac{m_k}{1-\beta_1^k}, \hat{v}_k &= \frac{v_k}{1-\beta_2^k}, \end{split}$	(1) (2)
$\theta_k = \theta_{k-1} - \frac{\eta}{\sqrt{\hat{v}_k} + \epsilon} \hat{m}_k.$ lease explain why we need the operations in (2).	(3)
Initially, the first and second moment are zero; without the operations, the accumulated grad bias towards zero, making the early updates less effective.	lient will
.10 Assume the input of batch normalization in a CNN has shape [BxCxHxW], where B, C, H, Watch size, number of channels, height, and width, respectively. Please:	V represent
1. Write down the cached variables after training and mark the variables with their shapes.	
2. Explain why these variables need to be cached and the purpose of using them.	
mean and variance of shape [C], During testing, we use the cached variables to do normalization to prevent bias in the data discaused by batch sampling. This gives us consistent results.	tribution

Problem 3 Back Propagation (14 credits)

Consider the following network for the task of Binary Classification:





3.1 Let's focus on the fully connected layer (Linear), z = XW + b. Note that X is the output of a ReLU function.

$$X_{1\times 4} = \begin{bmatrix} 1 & 2 & 0 & 1 \end{bmatrix}, W_{4\times 1} = \begin{bmatrix} 1 \\ -2 \\ 3 \\ 3 \end{bmatrix}, b_{1\times 1} = [0]$$

We've calculated the forward pass for you. Our RGB image's ground-truth label is y = 1.

•
$$z = XW + b = 1 * 1 + 2 * (-2) + 0 * 3 + 1 * 3 + 0 = 0$$

•
$$\hat{y} = \sigma(z) = \frac{1}{1+e^{-z}} = 0.5$$

•
$$L = BCE(y, \hat{y}) = -\frac{1}{1} \sum_{i=1}^{1} 1 \cdot \ln(0.5) = 0.693$$

Calculate the following gradients using the chain rule:

1.
$$\frac{\partial L}{\partial \hat{y}}$$
, Hint: $\frac{\partial \ln(x)}{\partial x} = \frac{1}{x}$

2.
$$\frac{\partial L}{\partial z}$$
,

3.
$$\frac{\partial L}{\partial W}$$

4.
$$\frac{\partial L}{\partial b}$$

$$\frac{\partial L}{\partial \hat{y}} = -\frac{1}{\hat{y}} = -\frac{1}{0.5} = -2$$

$$\frac{\partial L}{\partial z} = \frac{\partial L}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} = (-2) * (0.5 * (1 - 0.5)) = -0.5$$

$$\frac{\partial L}{\partial W} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial W} = X^{\top} \cdot \frac{\partial L}{\partial z} = [1, 2, 0, 1]^{\top} \cdot [-0.5] = [-0.5, -1, 0, -0.5]^{\top}$$

$$\frac{\partial L}{\partial b} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial b} = [1]^{\top} \cdot \frac{\partial L}{\partial z} = [-0.5]$$

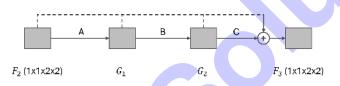


3.2 With the same context of 3.1, write down the variables that should be cached during the forward pass in order to compute the backward pass efficiently.

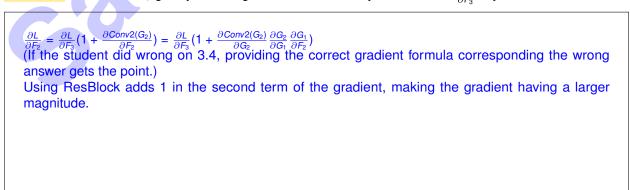
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The gradient is $\frac{\partial L}{\partial W} = \frac{\partial L}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z} \frac{\partial z}{\partial W}$.		┨
The Sigmoid function's gradient $\frac{\partial \hat{y}}{\partial z}$ is always positive.	 	٦ ;
The BCE's gradient $\frac{\partial L}{\partial \hat{y}}$ in the range of [0, 1] is always negative.	-	
$\frac{\partial z}{\partial W} = X^{\top}$ where X is obtained after a ReLU function, which is non-negative.		
Therefore, according to the formula $\frac{\partial L}{\partial W}$ is always non-positive.		
3.4 The structure of the ResBlock is shown below. Please:		(

- - 1. Assign layers ReLu, Conv1, and Conv2 to A, B, and C. Each layer can be assigned only once.
 - 2. Choose one from F_2 , G_1 , and G_2 that connects to the addition operator.
 - 3. Conv1 has kernel size 1, stride 1, and padding 0. Conv2 has kernel size 3, stride 1. Write down the padding of Conv2.



- 1. A: Conv1, B: ReLU, C: Conv2
- 2. F₂
- 3. padding: 1
- 3.5 With the same context (**including your solution**) of 3.4, write down the gradient $\frac{\partial L}{\partial F_2}$ and explain why ResBlock introduces a "highway" for the gradient flow. You may use the term $\frac{\partial L}{\partial F_3}$ in your answer.



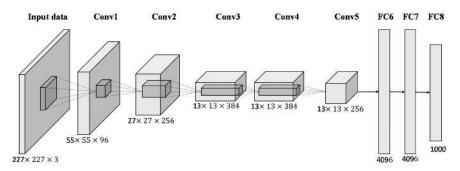
Problem 4 Dataset and Transfer Learning (10 credits)

the Internet with various resolutions and start labeling them by hand. After a while, you have collected a dataset with 1000 images of dogs, cats, and birds. 4.1 To train and test the model, you first split your dataset into train, validation, and test subsets. Write down a meaningful percentage of data you would assign to each subset. training > 50% validation 10-20% test 10-20% 4.2 Before training, you apply normalization to the images. Explain the benefit of doing this. Normalization makes the pixel value zero-centered and has a variance of 1, which makes it easier for the model to capture features and prevents numerical instabilities. 4.3 After splitting, you realize that the train set only contains pictures taken during the day, whereas the others only have pictures taken at night. What will happen if you continue with these splits? How can you correct it? Bad generalization Correction: Mix the subsets, reshuffle, and split again 4.4 With the same context of 4.1, you trained your model from scratch with the train set, then ran the model to predict images in both the train and validation set. What result do you expect? (Note: the dataset contains 1000 images.) Write down two approaches (besides transfer learning) to further improve your model. High accuracy on train set but low accuracy on validation set. label more data, data augmentation, other regularization methods. 4.5 You decide to use transfer learning. First, you need a model as the backbone of your classifier. Instead of downloading a pre-trained model from the Internet, you can train the backbone yourself. Explain how you can do it.

You want to train a classifier to classify images of dogs, cats, and birds. You downloaded 1M images from

Build an autoencoder and train with the 1M unlabeled images.

Other self-supervised learning methods using the 1M images also work.



- Resize input image
- Replace the last dense layer with a new layer that matches the number of classes (here: 3)
- For efficiency: Freeze the weights of the pre-trained model part
- Train the model on the new data

4.7 One of your classmates found a classifier trained to classify brands from car images with high accuracy. Would you use this model for your task? Why?

No. The model is likely trained with car images only, so it doesn't learn to capture features of animals. Therefore it doesn't generalize to our task.

Or Yes, the model learns to capture low-level features in early layers, so we could reuse only the early layers.



Problem 5 Activation and Regularization (10 credits)

After you told your friend about what you learned in I2DL, he is excited to try those Neural Networks himself. Because he didn't attend I2DL, he made some mistakes.

He tries the following model architecture on a 10-class classification problem:

- Linear(784 to 400) ightarrow ReLU ightarrow Linear(400 to 200) ightarrow ReLU ightarrow Linear(200 to 10) ightarrow output \emph{z}
- The loss function is Categorical cross entropy $CCE(\hat{y}, y) = -\sum_{i} y_{i} \log(\hat{y}_{i})$, where $\hat{y} = Sigmoid(z)$
- The weights are initialized using Xavier initialization.
- He additionally applies a regularization loss $reg = \sum_{w \in \theta} \exp(-w)$ where θ contains all weights of the network excluding biases.

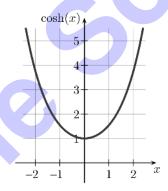


5.1 What weights does the used regularization encourage? Name two problems the resulting weights can cause.

Large positive weights: exploding gradients, poor performance, numerical instability



5.2 After you explained the problem to your friend, he wants to try $reg = \sum_{w \in \theta} \cosh(w) - 1$. He insists that the "-1" is necessary so 0 weights are not punished. Will the "-1" change the weights resulting from training? Explain why.



No, the gradient is not changed by -1.



5.3 After training, the network achieves a CCE loss close to zero but only around 10% accuracy. Explain how this could happen.

 \hat{y} is 1 for all classes. Because CCE does not punish false positives.

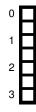
5.4 Your friend has read that shuffling the data during training can be beneficial. He uses the following code to generate training and validation sets in each epoch.	\mathbf{H}°
<pre>def generate_data_for_epoch(data): np.random.shuffle(data) # inplace shuffling of data split_index = int(0.8 * len(data)) train = data[:split_index] val = data[split_index:] return train, val</pre>	
Indicate the problem with his approach and explain what is the consequence of using this code.	
The data in the validation set is leaked to the train set. Therefore the validation accuracy does not show how good the model generalizes.	
5.5 You noticed that the Xavier initialization is not the best choice, why? What do you recommend to use instead?	
Xavier initialization does not work well with ReLU. Could use Kaiming initialization instead.	
5.6 You had a debate with your friend about Linear and Convolutional layers. He made the following statement:	H
A convolutional layer with fixed input and output sizes can be replaced by three layers (Flatten \rightarrow Linear \rightarrow Reshape). By carefully setting the hyperparameters and parameters (input and output sizes of Linear, output shape of Reshape, weights and biases of Linear), these three layers can fully replicate the convolutional layer's output.	
Do you agree with his statement? Explain why.	
Agree. Linear can be used to work with fixed input and output size. Each output value of convolution attends to partial of input while each output value of Linear attends to the whole input. By setting the parameters, we could let the Linear attend to the same parameters with the same weights as in convolution, thus providing the same output.	

Problem 6 Recurrent Neural Networks (12 credits)

You are a big fan of *The Lord of the Rings* and want to build a model to translate English into Elvish (a constructed language used in the novel).

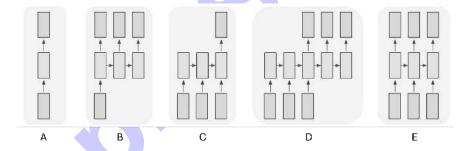


- 6.1 You first collected the vocabulary of Elvish and built an embedding dictionary. Please answer:
 - 1. What is an embedding dictionary?
 - 2. Is an embedding dictionary of Elvish enough for your project? If not, what else do you need?
 - 3. Besides the words, what else do you need as embeddings?
 - 1. Embedding dictionary is a mapping that maps words or word ids to n-dimentional vectors.
 - 2. No, in addition an English embedding dictionary is needed.
 - 3. Control tokens such as the end token and the empty token. Or punctuations such as the question mark.



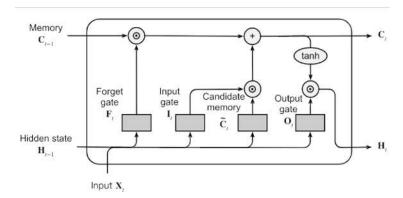
6.2 You started with a simple Recurrent Neural Network (RNN). Please explain:

- 1. What are the input and the output of the RNN block?
- 2. Which of the following pipelines is best for your task? Why?



- input: word embedding and the previous state output: the current state
- 2. D fits best, because the input and output are all sequences, and you need to first process all input to start outputting.

6.3 The RNN works good on short sentences but not as good on long sentences. You learned that LSTM is a solution to long sentences. Here is an illustration of LSTM. Please answer:

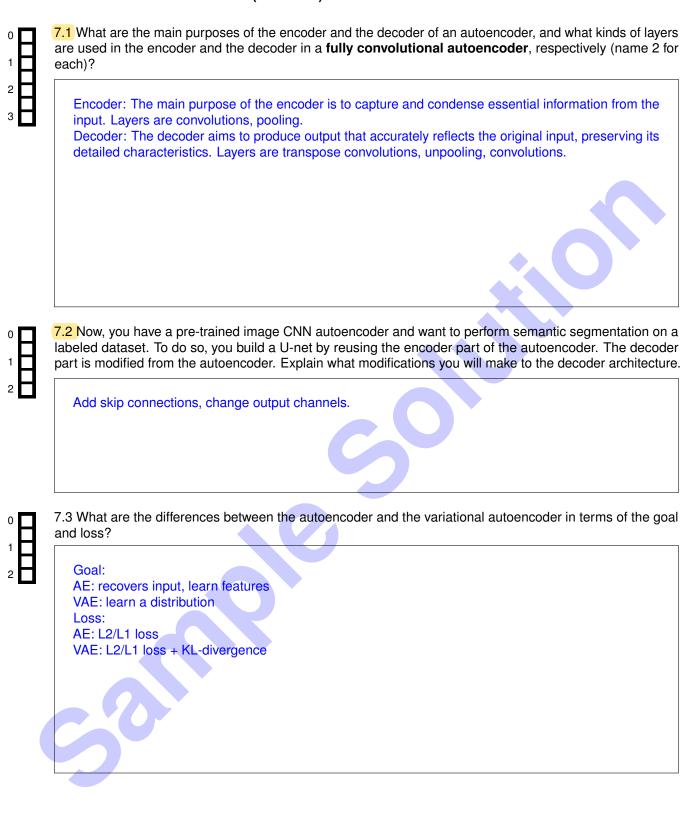


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- 1. What are the activation functions for the Forget gate, Input gate, Candidate memory, and the Output gate?
- 2. Is it a good idea to use ReLU for the Forget gate? Why?
- 3. Why is LSTM better at processing long sequences?
 - 1. sigmoid for gates, tanh for memory.
 - 2. No, because the output of ReLU can be larger than 1, which could make the long term memory larger and larger.
 - 3. It provides a highway for long-term dependency.
- 6.4 Recently, many large language models use Transformers instead of LSTM. Please answer:
 - 1. Different from RNN and LSTM, which take one element in the sequence for each time, Transformers takes all elements in the sequence as input at once. How to inform the Transformer about the ordering of the words in a sentence?
 - 2. The attention layer takes Key K, Query Q, and Value V as inputs. How are the attention weights computed (in formula or words), and what are their characteristics?
 - 3. How is the output of attention layers computed (in formula or words)? Why is this process called "attention"?
 - 1. Positional encoding
 - 2. The weight is computed by a dot product between K and Q and then softmax. The closer the query is to the key, the larger the weight is.
 - 3. The output is given by summing the values using the weight. The output is mostly affected by values with large weights, that's why it's called "attention".

Problem 7 Autoencoders (10 credits)



7.4 The diffusion model learns a denoising process to generate samples in a distribution. It has been shown to be able to learn complicated distributions such as images. The latent diffusion model, on the other hand, learns the distribution of the latent feature encoded by VAE. With your knowledge of VAE in mind, write down two advantages in terms of speed and image quality of the latent diffusion model compared to the diffusion model that operates directly on the RGB domain and explain why.
Latent diffusion model runs faster because the latent feature is smaller than the image. Latent diffusion generates image with better context because the feature it learns are high level abstractions of the image that contain more context.

Additional space for solutions-clearly mark the (sub)problem your answers are related to and strike out invalid solutions.

