Counting			
Combinatorics			
Definition of Probability			
Equally Likely Outcomes			
Axioms of Probability			
Stories			
Enigma Machine			
Rectangles in a Grid			
Serendipity			
Birthday Paradox			
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Counting Graphs			
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Part 2: Core Probability			
Probability of or			
Probability of or			
Probability of or Conditional Probability			
Probability of or Conditional Probability Independence			
Probability of or Conditional Probability Independence Probability of and			
Probability of or Conditional Probability Independence Probability of and De Morgan's Law			
Probability of or Conditional Probability Independence Probability of and De Morgan's Law Law of Total Probability Bayes' Theorem Log Probabilities			
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Probability of or Conditional Probability Independence Probability of and De Morgan's Law Law of Total Probability Bayes' Theorem Log Probabilities Many Coin Flips			
Probability of or Conditional Probability Independence Probability of and De Morgan's Law Law of Total Probability Bayes' Theorem Log Probabilities Many Coin Flips Stories			
Probability of or Conditional Probability Independence Probability of and De Morgan's Law Law of Total Probability Bayes' Theorem Log Probabilities Many Coin Flips Stories Bacteria Evolution			

	X=0	X = 1
Y = Frosh	0.01	0.13
$Y = \mathrm{Soph}$	0.05	0.33
Y = Junior	0.04	0.21
Y = Senior	0.03	0.12
Y=5+	0.02	0.06

What is the probability that a student's favorite digit is 0, P(X = 0)? We can use the LOTP to compute this probability:

$$P(X = 0) = \sum_{y} P(X = 0, Y = y)$$
 $= P(X = 0, Y = Frosh)$
 $+ P(X = 0, Y = Soph)$
 $+ P(X = 0, Y = Junior)$
 $+ P(X = 0, Y = Senior)$
 $+ P(X = 0, Y = 5+)$
 $= 0.01 + 0.05 + 0.04 + 0.03 + 0.02 = 0.15$

Marginalization with More Variables

The idea of marginalization can be extended to joint distributions with more than two random variables. Consider having three random variables X, Y, and Z, we could marginalize out any of the variables:

$$P(X=x) = \sum_{y,z} \mathrm{P}(X=x,Y=y,Z=z)$$
 $P(Y=y) = \sum_{x,z} \mathrm{P}(X=x,Y=y,Z=z)$ $P(Z=z) = \sum_{x,z} \mathrm{P}(X=x,Y=y,Z=z)$