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 CS 102 - Data Structures
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A.1

- Runtime of $O(n^2)$ because it is a nested for loop.
- Runtime of $O(n)$ because it loops thru the list once.
- Runtime of $O(n^3)$ because there are 3 for loops.

A.2

a.

$$N = \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix}$$

$$N^1 = \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix}$$

$$N^2 = \begin{vmatrix} 2 & 1 \\ 1 & 1 \end{vmatrix}$$

$$N^4 = \begin{vmatrix} 5 & 3 \\ 3 & 2 \end{vmatrix}$$

$$N^8 = \begin{vmatrix} 34 & 21 \\ 21 & 13 \end{vmatrix}$$

b.

Base Case:

Fib(0) is 0 and Fib(1) is 1

Assuming the following is true...

$$N^n = \begin{vmatrix} F(n+1) & F(n) \\ F(n) & F(n-1) \end{vmatrix}$$

When $N = \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix}$

$$N^{2n} = N^n * N^n = \begin{vmatrix} F(n+1) & F(n) \\ F(n) & F(n-1) \end{vmatrix} * \begin{vmatrix} 1 & 1 \\ 0 & 1 \end{vmatrix} = \begin{vmatrix} F(n+1)*1 + f(n)*0 & F(n+1)*1 + f(n)*1 \\ F(n)*1 + f(n-1)*1 & F(n)*1 + f(n-1)*0 \end{vmatrix}$$

= the next term in the sequence

A.3

a.

We didn't include removeTail, and it's not included in the java libraries because it is a problematic function that could lead to various NullPointerExceptions and is a time consuming process for a singly linked list.

b.

```
int removeTail() {
    if (head == null) return Integer.MIN_VALUE;
    Node n = head.next;

    while(n.next.next != tail){
        n = n.next;
    }

    tail = n.next;
    tail.next = null;
    return tail.value;
}
```

c.

```
for(int i = 0; i < 3; i++) {
    tailList.removeTail();
    headList.removeTail();
}
tailList.show("tailList after 3 removeTail() is:");
```

```
headList.show("headList after 3 removeTail() is:");
```

A.4

Pat1 (solution):

```
"^(?!.*(r|0|H|\\-|wk)).*$"
```

Pat2 (false negative):

```
"e"
```

Pat3 (false positive):

```
".*zip"
```

Pat4

```
".*rar"
```