

In [1]:

```
from sympy import Symbol, sin, cos, sqrt, pi
from sympy.plotting.plot import plot_parametric as plotp
```

In [2]:

```
theta = Symbol('theta')
```

In [3]:

```
def r_hor_m(Q, M):
    return 0.5 * (M - sqrt(M ** 2 - 4 * Q ** 2))
```

In [4]:

```
def r_hor_p(Q, M):
    return 0.5 * (M + sqrt(M ** 2 - 4 * Q ** 2))
```

In [5]:

```
m = 8.2
Q = 2
```

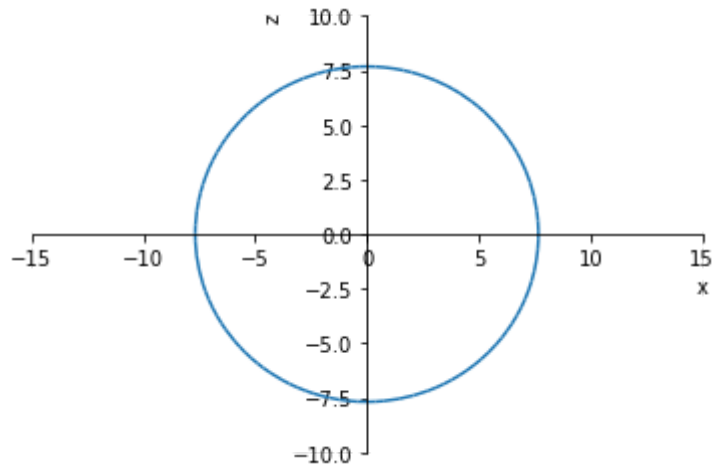
In [6]:

```
inner_event_horizon = plotp(
    (
        r_hor_m(Q, m) * sin(theta),
        r_hor_m(Q, m) * cos(theta)
    ),
    (theta, 0, 2 * pi),
    xlim=[-15, 15], ylim=[-10, 10],
    xlabel="x", ylabel="z"
)
```

<Figure size 640x480 with 1 Axes>

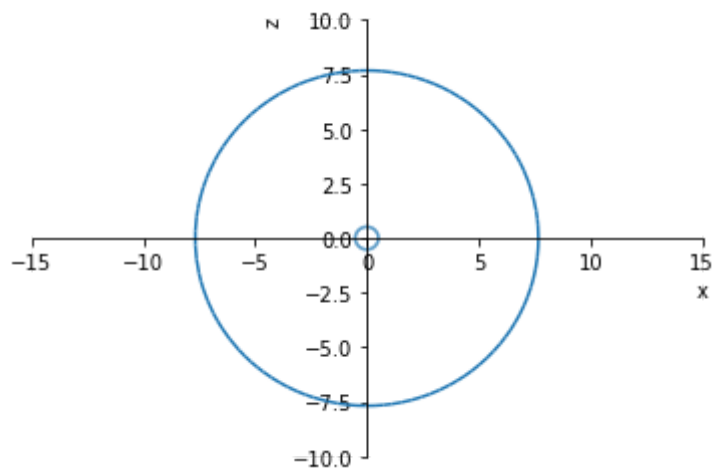
In [7]:

```
outer_event_horizon = plotp(  
    (  
        r_hor_p(Q, m) * sin(theta),  
        r_hor_p(Q, m) * cos(theta)  
    ),  
    (theta, 0, 2 * pi),  
    xlim=[-15, 15], ylim=[-10, 10],  
    xlabel="x", ylabel="z"  
)
```



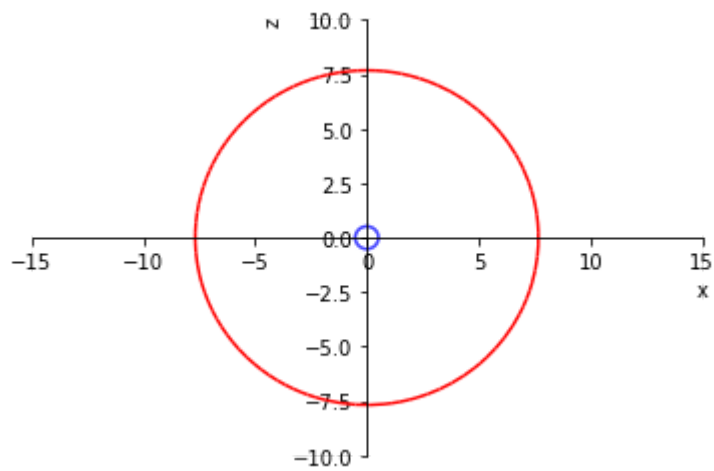
In [8]:

```
black_hole = plotp(  
    (  
        r_hor_m(Q, m) * sin(theta),  
        r_hor_m(Q, m) * cos(theta)  
    ),  
    (  
        r_hor_p(Q, m) * sin(theta),  
        r_hor_p(Q, m) * cos(theta)  
    ),  
    (theta, 0, 2 * pi), aspect_ratio=(1,1),  
    xlim=[-15, 15], ylim=[-10, 10],  
    xlabel="x", ylabel="z"  
)
```



In [9]:

```
black_hole[0].line_color = 'blue'  
black_hole[1].line_color = 'red'  
  
black_hole.show()
```



In []: