## Scrap

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## 1 Identities

Here are some identities that (maybe) can be shown by the WZ-method.

$$1. \sum_{k=0}^{n} \binom{n}{k} = 2^n$$

2. 
$$\sum_{k=0}^{n} (-1)^k \binom{n}{k} \binom{2k}{k} 4^{n-k} = \binom{2n}{n}$$

$$3. \sum_{k=0}^{n} \binom{n}{k}^2 = \binom{2n}{n}$$

4. 
$$\sum_{k=-n}^{n} (-1)^k {2n \choose n+k}^3 = \frac{(3n)!}{n!}$$

5. 
$$\sum_{k=0}^{n} 2^k \binom{n}{k} = 3^n$$

6. 
$$\sum_{k=0}^{n} k \binom{n}{k} = n2^{n-1}$$

7. 
$$\sum_{k=1}^{n} \frac{1}{k(k-1)} = 1 - \frac{1}{n}$$

8. 
$$\sum_{k=0}^{n} {k \choose c} = {n+1 \choose c+1}$$

9. 
$$\sum_{k=0}^{n} {r+k \choose k} = {r+n+1 \choose n}$$

$$10. \sum_{k=0}^{n} {m-k \choose n-k} = {m+1 \choose n}$$