

Work 1

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TEST!

Problem 5.2

From example 5.2 we know that our equations of motion are

$$\begin{aligned}y(t) &= C_1 \cos(\omega t) + C_2 \sin(\omega t) + \frac{E}{B}t + C_3 \\z(t) &= C_2 \cos(\omega t) - C_1 \sin(\omega t) + C_4\end{aligned}$$

where

$$\omega = \frac{QB}{m}$$

Part b

We then know

$$\mathbf{x}_0 = 0 \text{ and } \mathbf{v}_0 = \frac{E}{2B}\hat{y}$$

We can put in our initial conditions to get

$$\begin{aligned}0 &= C_1 \cos(\omega t) + C_2 \sin(\omega t) + \frac{E}{B}t + C_3 \\0 &= C_2 \cos(\omega t) - C_1 \sin(\omega t) + C_4 \\\frac{E}{2B} &= -C_1 \omega \sin(\omega t) + C_2 \omega \cos(\omega t) + \frac{E}{B} \\0 &= -C_1 \omega \cos(\omega t) - C_2 \omega \sin(\omega t)\end{aligned}$$

Back to my favourite program to find the constants

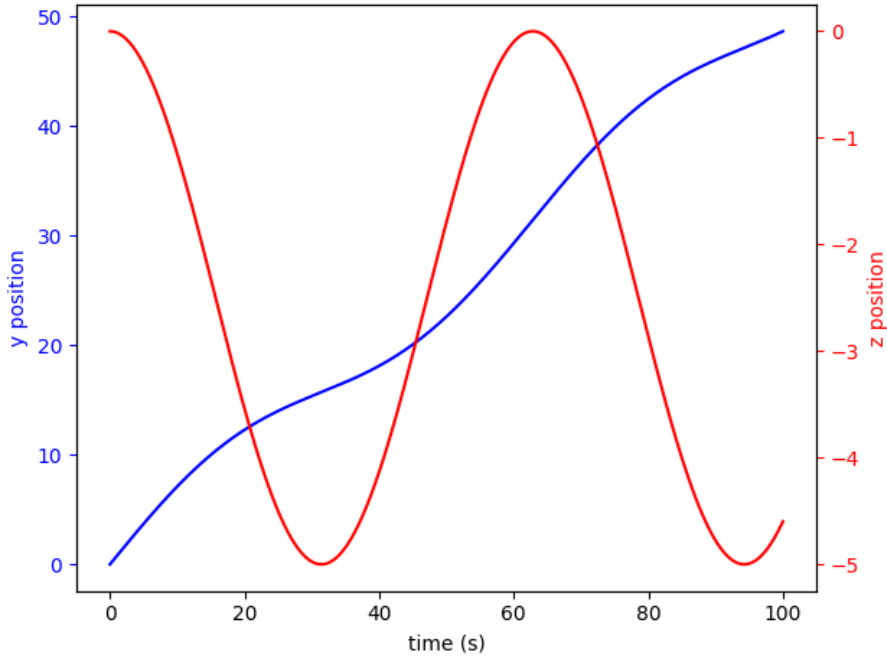
$$\begin{aligned}\text{Input: FullSimplify} & \left[\text{RowReduce} \left[\left(\begin{array}{ccccc} \cos(0) & \sin(0) & 1 & 0 & 0 \\ -\sin(0) & \cos(0) & 0 & 1 & 0 \\ -\omega \sin(0) & \omega \cos(0) & 0 & 0 & \frac{e}{2B} \\ -\omega \cos(0) & -\omega \sin(0) & 0 & 0 & 0 \end{array} \right) \right] \right] \\ \text{Output:} & \left(\begin{array}{ccccc} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & \frac{e}{2B\omega} \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & -\frac{e}{2B\omega} \end{array} \right)\end{aligned}$$

After simplifying, it turns out that our equations of motion are

$$y(t) = \frac{E(2t\omega + \sin(t\omega))}{2B\omega}$$

$$z(t) = \frac{E(\cos(t\omega) - 1)}{2B\omega}$$

Using some sample numbers and running these equations in python, we get the following behaviour



From this we can conclude that there is no motion in the x direction, that the particle follows an almost linear path in the y direction, and that it spins in a circle in the z direction

Part c