Homework 5

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1 Expression for Gaussian Elimination

We have Ax = b with a tridiagonal matrix A of dimension $N \times N$, so we can start directly without having to reorder the rows. The first row of A will stay the same, so we do an iteration over N-1 other rows:

```
for i := 1 to N-1:
    factor = A_{i+1,i} / A_{i,i}

# calculate the factor with which we have to
    multiply the previous row and add it to the
    next row to eleminate the left off-diagonal
    element

b_{i+1} = b_{i+1} - factor * b_i

# update the vector b so the solution stays the same

for k := 1 to N:
    A_{i+1,k} = A_{i+1,k} - factor * A_{i,k}

# update the row i+1
```

With this algorithm, we get an upper right triangular matrix A and an updated vector b. By doing backward substitution, we can get the solution of the linear equation system.

2 Backward Substitution

We have Ax = b with an upper right triangular matrix A of dimension $N \times N$. We have to start with:

with this algorithm, we get the solution vector x.