

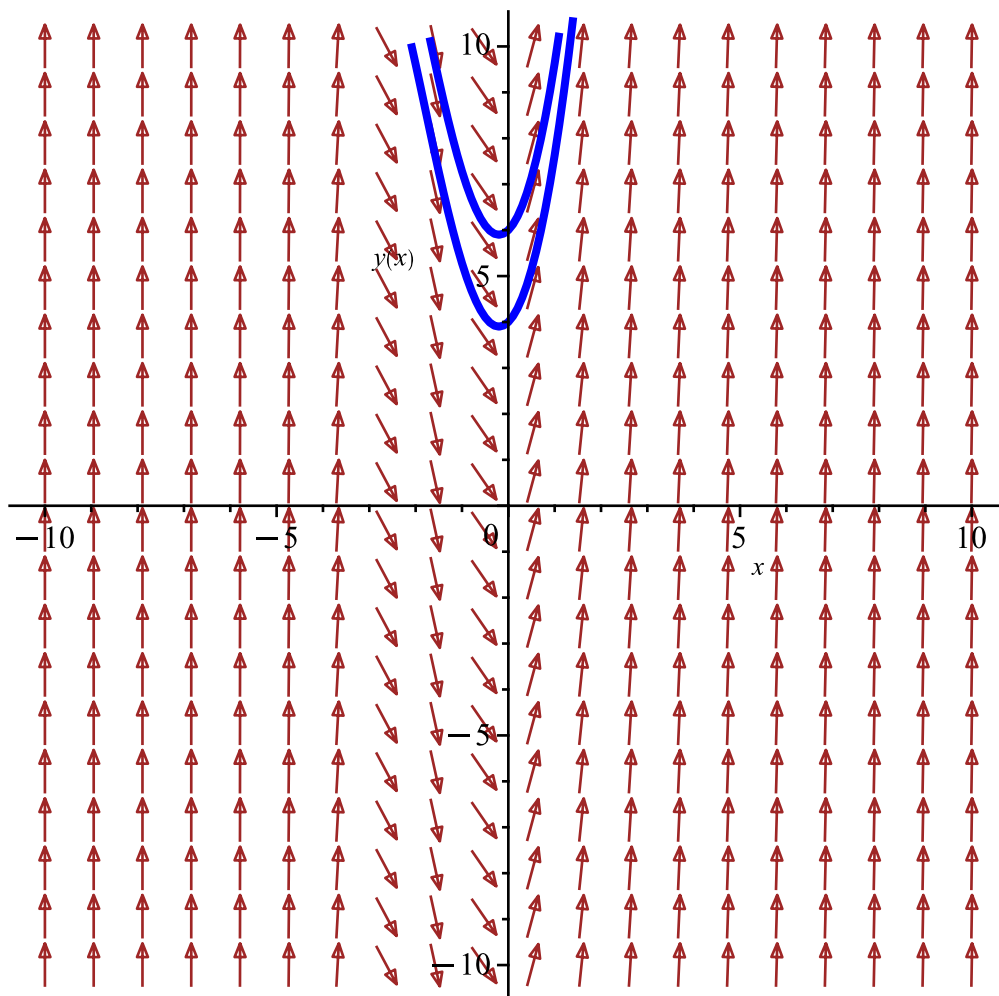
```
> #ex1:
> ec1:=diff(y(x),x)-6*x-exp(-x)=0
```

$$ec1 := \frac{d}{dx} y(x) - 6x - e^{-x} = 0 \quad (1)$$

```
> sol__1a:=dsolve(ec1,y(x))
```

$$sol_{1a} := y(x) = 3x^2 - e^{-x} + c_1 \quad (2)$$

```
> with(DEtools):
> DEplot(ec1,y(x),x=-10..10,y=-10..10,[[y(0)=4],[y(0)=6]],arrows=
medium, linecolor=blue, stepsize=0.1)
```



```
> cond_in:=y(-1)=1-exp(1)
```

$$cond_in := y(-1) = 1 - e \quad (3)$$

```
> sol__1b:=dsolve({ec1,cond_in},y(x))
```

$$sol_{1b} := y(x) = 3x^2 - e^{-x} - 2 \quad (4)$$

```
> #ex2:
> ec2:=diff(y(x),x$2)-7*diff(y(x),x)+10*y(x)-30*x-19=0
```

$$ec2 := \frac{d^2}{dx^2} y(x) - 7 \frac{d}{dx} y(x) + 10y(x) - 30x - 19 = 0 \quad (5)$$

```
> sol__2a:=dsolve(ec2,y(x))
```

$$sol_{2a} := y(x) = e^{2x} c_2 + e^{5x} c_1 + 3x + 4 \quad (6)$$

```
> cond_in2:=y(0)=6,D(y)(0)=10
```

$$cond_in2 := y(0) = 6, D(y)(0) = 10 \quad (7)$$

```
> sol__2b:=dsolve({ec2,cond_in2},y(x))
```

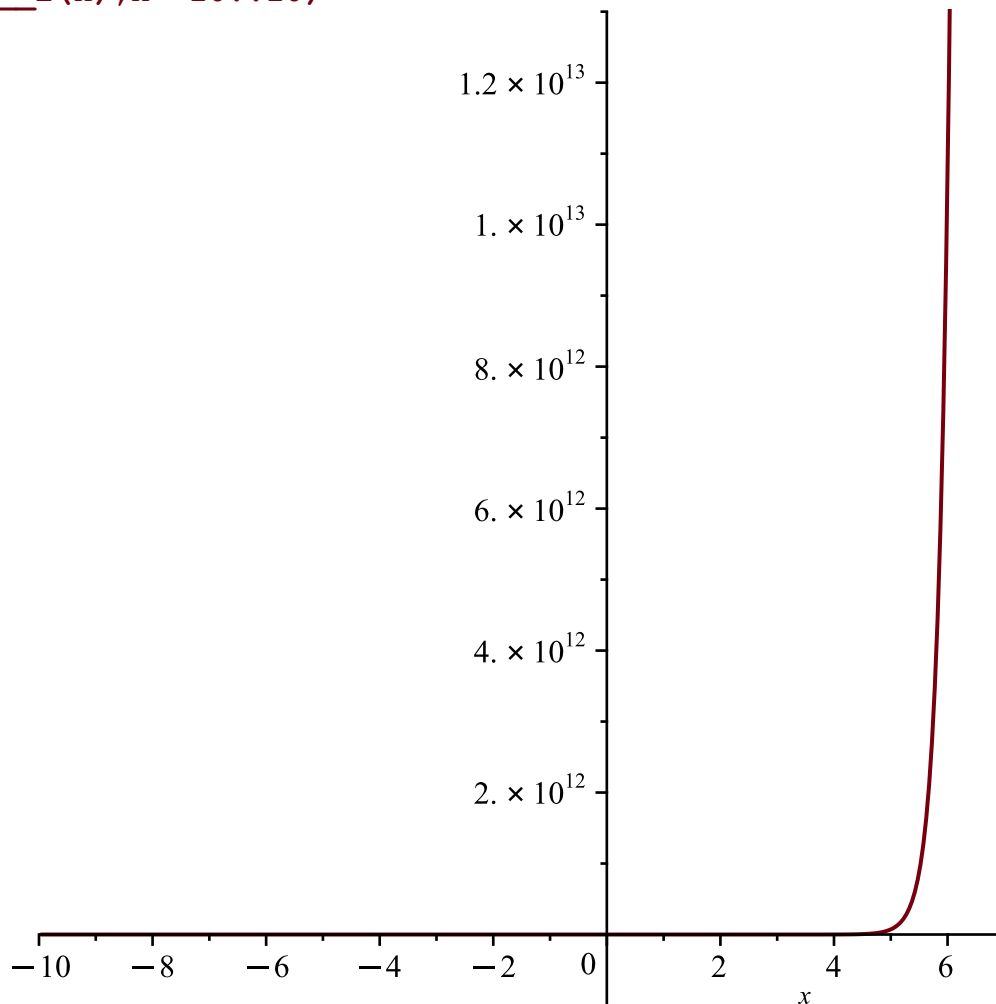
$$sol_{2b} := y(x) = e^{2x} + e^{5x} + 3x + 4 \quad (8)$$

```
> y__2:=unapply(rhs(sol__2b),x)
```

$$y_2 := x \mapsto e^{2 \cdot x} + e^{5 \cdot x} + 3 \cdot x + 4 \quad (9)$$

```
> with(plots):
```

```
> plot(y__2(x),x=-10..10)
```



```
> restart: with(DEtools):
```

```
> #ex3:
```

```
> ec1:=diff(x(t),t)=x(t)+5*y(t)
```

$$ec1 := \frac{d}{dt} x(t) = x(t) + 5 y(t) \quad (10)$$

```
> ec2:=diff(y(t),t)=-x(t)-3*y(t)
```

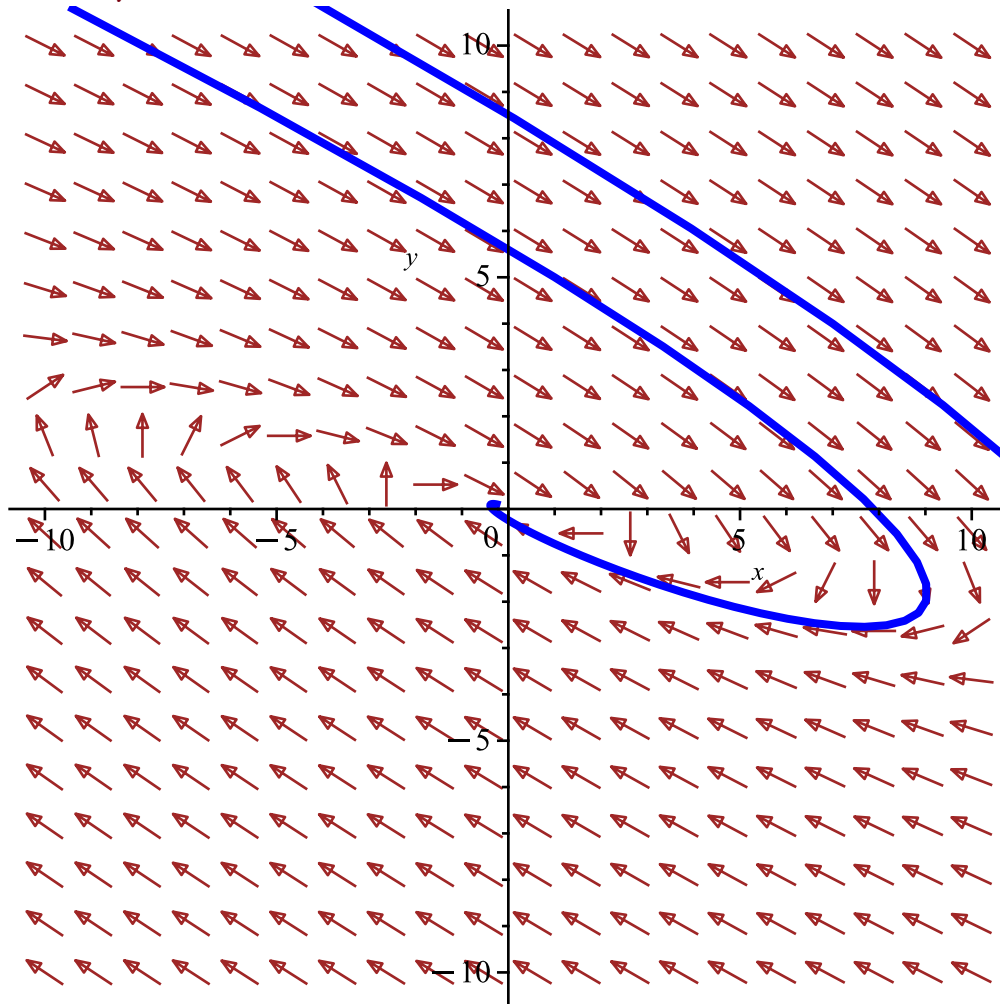
$$ec2 := \frac{d}{dt} y(t) = -x(t) - 3 y(t) \quad (11)$$

```
> sol__a:=dsolve({ec1,ec2},{x(t),y(t)})
```

$$sol_a := \left\{ x(t) = e^{-t} (\sin(t) c_1 + \cos(t) c_2), y(t) = \right. \quad (12)$$

$$\left\{ -\frac{e^{-t} (2 \sin(t) c_1 + \sin(t) c_2 - \cos(t) c_1 + 2 \cos(t) c_2)}{5} \right\}$$

```
> DEplot([ec1,ec2],[x(t),y(t)],t=-5..5,x=-10..10,y=-10..10,[[x(0)=
1,y(0)=5],[x(0)=7,y(0)=4]],arrows=medium, linecolor=blue,
stepsize=0.1)
```



```
> #se observa din directia campului de directii ca ambele limite
tind la 0 => lim(x(t))=lim(y(t)), cand t -> infinnit
```

```
> cond_in__d:=x(0)=1,y(0)=4
```

$$cond_in_d := x(0) = 1, y(0) = 4$$

(13)

```
> sol__d:=dsolve({ec1,ec2,cond_in__d},{x(t),y(t)})
```

$$sol_d := \left\{ x(t) = e^{-t} (22 \sin(t) + \cos(t)), y(t) = -\frac{e^{-t} (45 \sin(t) - 20 \cos(t))}{5} \right\}$$

(14)

```
> restart
```

```
> ec1:=diff(x(t),t)=-k*x(t)
```

$$ec1 := \frac{d}{dt} x(t) = -kx(t)$$

(15)

```
> cond_in:=x(0)=x__0
```

$$cond_in := x(0) = x_0$$

(16)

$$\begin{aligned} &> \text{sol_a} := \text{dsolve}(\{\text{ec1}, \text{cond_in}\}, \mathbf{x}(t)) \\ &\quad \text{sol}_a := x(t) = x_0 e^{-kt} \end{aligned} \quad (17)$$

$$\begin{aligned} &> \mathbf{xx} := \text{unapply}(\text{rhs}(\text{sol_a}), t, \mathbf{x_0}, k) \\ &\quad \mathbf{xx} := (t, x_0, k) \mapsto x_0 \cdot e^{-kt} \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{ec_d} := \mathbf{xx}(6, 100, k) = 30 \\ &\quad \text{ec}_d := 100 e^{-6k} = 30 \end{aligned} \quad (19)$$

$$\begin{aligned} &> \mathbf{k_d} := \text{solve}(\text{ec_d}, k) \\ &\quad k_d := -\frac{\ln\left(\frac{3}{10}\right)}{6} \end{aligned} \quad (20)$$

$$\begin{aligned} &> \text{restart: with(DEtools): with(linalg):} \\ &> \text{\#ex5:} \\ &> \mathbf{f_1} := (\mathbf{x}, \mathbf{y}) \rightarrow \mathbf{x} \cdot \mathbf{y} \\ &\quad f_1 := (x, y) \mapsto x \cdot y \end{aligned} \quad (21)$$

$$\begin{aligned} &> \mathbf{f_2} := (\mathbf{x}, \mathbf{y}) \rightarrow \mathbf{x} - \mathbf{y}^2 + 1 \\ &\quad f_2 := (x, y) \mapsto x - y^2 + 1 \end{aligned} \quad (22)$$

$$\begin{aligned} &> \text{ec1} := \text{diff}(\mathbf{x}(t), t) = \mathbf{f_1}(\mathbf{x}(t), \mathbf{y}(t)) \\ &\quad \text{ec1} := \frac{d}{dt} x(t) = x(t) y(t) \end{aligned} \quad (23)$$

$$\begin{aligned} &> \text{ec2} := \text{diff}(\mathbf{y}(t), t) = \mathbf{f_2}(\mathbf{x}(t), \mathbf{y}(t)) \\ &\quad \text{ec2} := \frac{d}{dt} y(t) = x(t) - y(t)^2 + 1 \end{aligned} \quad (24)$$

$$\begin{aligned} &> \mathbf{sist} := \text{ec1}, \text{ec2} \\ &\quad \text{sist} := \frac{d}{dt} x(t) = x(t) y(t), \frac{d}{dt} y(t) = x(t) - y(t)^2 + 1 \end{aligned} \quad (25)$$

$$\begin{aligned} &> \mathbf{PctEch} := \text{solve}(\{\mathbf{f_1}(\mathbf{x}, \mathbf{y}) = 0, \mathbf{f_2}(\mathbf{x}, \mathbf{y}) = 0\}, \{\mathbf{x}, \mathbf{y}\}) \\ &\quad \text{PctEch} := \{x = -1, y = 0\}, \{x = 0, y = 1\}, \{x = 0, y = -1\} \end{aligned} \quad (26)$$

$$\begin{aligned} &> \mathbf{J} := \text{jacobian}([\mathbf{f_1}(\mathbf{x}, \mathbf{y}), \mathbf{f_2}(\mathbf{x}, \mathbf{y})], [\mathbf{x}, \mathbf{y}]) \\ &\quad J := \begin{bmatrix} y & x \\ 1 & -2y \end{bmatrix} \end{aligned} \quad (27)$$

$$\begin{aligned} &> \mathbf{A} := \text{subs}(\text{PctEch}[1, 1], \text{PctEch}[1, 2], \text{eval}(\mathbf{J})) \\ &\quad A := \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \end{aligned} \quad (28)$$

$$\begin{aligned} &> \text{eigenvals}(\mathbf{A}) \\ &\quad I, -I \end{aligned} \quad (29)$$

$$\begin{aligned} &> \text{\#instabil, de tip centru} \\ &> \mathbf{B} := \text{subs}(\text{PctEch}[2, 1], \text{PctEch}[2, 2], \text{eval}(\mathbf{J})) \\ &\quad B := \begin{bmatrix} 1 & 0 \\ 1 & -2 \end{bmatrix} \end{aligned} \quad (30)$$

```
> eigenvals(B)
```

1, -2

(31)

```
> #instabil, de tip sa
```

```
> C:=subs(PctEch[3,1],PctEch[3,2],eval(J))
```

$$C := \begin{bmatrix} -1 & 0 \\ 1 & 2 \end{bmatrix}$$

(32)

```
> eigenvals(C)
```

-1, 2

(33)

```
> #instabil, de tip sa
```

```
> DEplot([sist],[x(t),y(t)],t=-5..5,x=-3..3,y=-3..3,[[x(0)=-1,y(0)=1],[x(0)=-1/2,y(0)=1],[x(0)=1,y(0)=1],[x(0)=1,y(0)=2],[x(0)=2,y(0)=1/2],[x(0)=-1,y(0)=-1]])
```

