ec1:=diff(x(t),t)=x(t)+4*y(t)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = x(t) + 4y(t) \tag{1}$$

> ec2:=diff(y(t),t)=x(t)+y(t)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t)$$
 (2)

sist:=ec1,ec2

$$sist := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (3)

> dsolve({sist}, {x(t),y(t)})

$$\left\{ x(t) = c_1 e^{3t} + c_2 e^{-t}, y(t) = \frac{c_1 e^{3t}}{2} - \frac{c_2 e^{-t}}{2} \right\}$$
 (4)

> restart > ec1:=diff(x(t),t)=5*x(t)+3*y(t)+1

$$ec1 := \frac{d}{dt} x(t) = 5 x(t) + 3 y(t) + 1$$
 (5)

> ec2:=diff(y(t),t)=-6*x(t)-4*y(t)+exp(-t)

$$ec2 := \frac{d}{dt} y(t) = -6 x(t) - 4 y(t) + e^{-t}$$
 (6)

> sist2:=ec1,ec2

$$sist2 := \frac{d}{dt} x(t) = 5 x(t) + 3 y(t) + 1, \frac{d}{dt} y(t) = -6 x(t) - 4 y(t) + e^{-t}$$
 (7)

> dsolve({sist2}, {x(t),y(t)})

$$\left\{ x(t) = e^{-t} c_2 + e^{2t} c_1 - 2 - t e^{-t} - \frac{e^{-t}}{3}, y(t) = -2 e^{-t} c_2 - e^{2t} c_1 + \frac{e^{-t}}{3} + 2 t e^{-t} + 3 \right\}$$
 (8)

> restart > ec1:=diff(x(t),t)=2*x(t)-y(t)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = 2 \ x(t) - y(t)$$

> ec2:=diff(y(t),t)=x(t)+2*y(t)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + 2 \ y(t)$$
 (10)

> sist3:=ec1,ec2

$$sist3 := \frac{d}{dt} x(t) = 2 x(t) - y(t), \frac{d}{dt} y(t) = x(t) + 2 y(t)$$
 (11)

> dsolve({sist3}, {x(t),y(t)})

$$\left\{ x(t) = e^{2t} \left(c_2 \cos(t) + c_1 \sin(t) \right), y(t) = -e^{2t} \left(\cos(t) c_1 - \sin(t) c_2 \right) \right\}$$
 (12)

ec1:=diff(x(t), t)=x(t)+3*y(t)+cos(t)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = x(t) + 3y(t) + \cos(t)$$
 (13)

> ec2:=diff(y(t),t)=x(t)-y(t)+2*t

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) - y(t) + 2t$$
 (14)

> sist4:=ec1,ec2

$$sist4 := \frac{d}{dt} x(t) = x(t) + 3 y(t) + \cos(t), \frac{d}{dt} y(t) = x(t) - y(t) + 2 t$$
 (15)

> dsolve({sist4}, {x(t),y(t)})

$$\left\{ x(t) = -e^{-2t} c_2 + 3 e^{2t} c_1 + \frac{\sin(t)}{5} - \frac{\cos(t)}{5} - \frac{3t}{2}, y(t) = e^{-2t} c_2 + e^{2t} c_1 - \frac{\cos(t)}{5} + \frac{t}{2} \right. \tag{16}$$

$$\left\{ -\frac{1}{2} \right\}$$

> restart > ec1:=diff(x(t),t)=x(t)-y(t)+z(t)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = x(t) - y(t) + z(t)$$
 (17)

= > ec2:=diff(y(t),t)=x(t)+y(t)-z(t)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t) - z(t)$$
 (18)

> ec3:=diff(z(t),t)=-y(t)+2*z(t)

$$ec3 := \frac{d}{dt} z(t) = -y(t) + 2 z(t)$$
 (19)

> sist5:=ec1,ec2,ec3

$$sist5 := \frac{d}{dt} x(t) = x(t) - y(t) + z(t), \frac{d}{dt} y(t) = x(t) + y(t) - z(t), \frac{d}{dt} z(t) = -y(t) + 2z(t)$$
 (20)

> restart > ec1:=diff(x(t),t)=x(t)-2*y(t)-2*z(t)+exp(-t)

$$ec1 := \frac{d}{dt} x(t) = x(t) - 2y(t) - 2z(t) + e^{-t}$$
 (22)

> ec2:=diff(y(t),t)=-2*x(t)+y(t)+2*z(t)

$$ec2 := \frac{d}{dt} y(t) = -2 x(t) + y(t) + 2 z(t)$$
 (23)

> ec3:=diff(z(t),t)=2*x(t)-y(t)-3*z(t)+exp(-t)

$$ec3 := \frac{d}{dt} z(t) = 2 x(t) - y(t) - 3 z(t) + e^{-t}$$
 (24)

> sist6:=ec1,ec2,ec3

$$sist6 := \frac{d}{dt} x(t) = x(t) - 2y(t) - 2z(t) + e^{-t}, \frac{d}{dt} y(t) = -2x(t) + y(t) + 2z(t), \frac{d}{dt} z(t)$$
 (25)

$$=2x(t)-y(t)-3z(t)+e^{-t}$$

= > dsolve({sist6},{x(t),y(t),z(t)})

$$\begin{cases}
x(t) = -c_2 e^{\sqrt{3}t} - c_3 e^{-\sqrt{3}t} + e^{-t} c_1 + e^{-t} t, y(t) = c_2 e^{\sqrt{3}t} + c_3 e^{-\sqrt{3}t}, z(t) = \frac{c_2 \sqrt{3} e^{\sqrt{3}t}}{2} \\
- \frac{c_3 \sqrt{3} e^{-\sqrt{3}t}}{2} - \frac{3 c_2 e^{\sqrt{3}t}}{2} - \frac{3 c_3 e^{-\sqrt{3}t}}{2} + e^{-t} c_1 + e^{-t} t
\end{cases}$$
(26)

ec1:=diff(x(t),t)=x(t)+4*y(t)

$$ec1 := \frac{d}{dt} x(t) = x(t) + 4 y(t)$$
 (27)

 $\stackrel{=}{>}$ ec2:=diff(y(t),t)=x(t)+y(t)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + y(t)$$
 (28)

> sist:=ec1,ec2

$$sist := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (29)

 $> cond_in:=x(0)=1,y(0)=2$

cond in :=
$$x(0) = 1, y(0) = 2$$
 (30)

> sol:=dsolve({sist,cond_in},{x(t),y(t)})

$$sol := \left\{ x(t) = -\frac{3e^{-t}}{2} + \frac{5e^{3t}}{2}, y(t) = \frac{3e^{-t}}{4} + \frac{5e^{3t}}{4} \right\}$$
(31)

> with(plots):

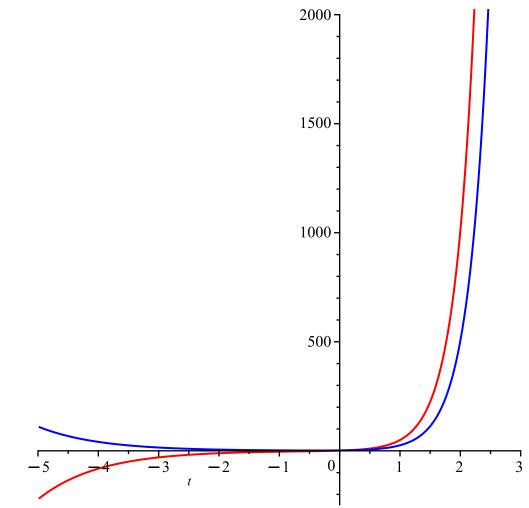
> xx:=unapply(rhs(sol[1]),t);

$$xx := t \mapsto -\frac{3 \cdot e^{-t}}{2} + \frac{5 \cdot e^{3 \cdot t}}{2}$$
 (32)

> yy:=unapply(rhs(sol[2]),t);

$$yy := t \mapsto \frac{3 \cdot e^{-t}}{4} + \frac{5 \cdot e^{3 \cdot t}}{4}$$
 (33)

> plot([xx(t),yy(t)],t=-5..5,color=[red,blue])



$$ec3 := \frac{d}{dt} x(t) = x(t) - y(t) + t - 1$$
 (34)

> ec4:=diff(y(t),t)=-2*x(t)+4*y(t)+cos(t)

$$ec4 := \frac{d}{dt} y(t) = -2 x(t) + 4 y(t) + \cos(t)$$
 (35)

> sist2:=ec1,ec2

$$sist2 := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (36)

> cond in2:=x(0)=0, y(0)=1

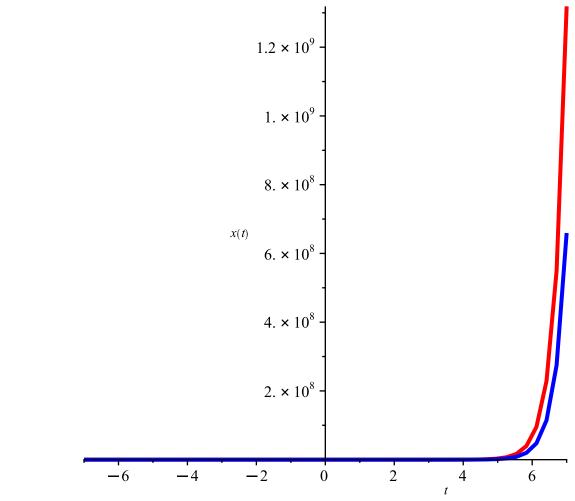
$$cond_in2 := x(0) = 0, y(0) = 1$$
 (37)

= > sol2:=dsolve({sist2,cond_in2},{x(t),y(t)})

$$sol2 := \left\{ x(t) = -e^{-t} + e^{3t}, y(t) = \frac{e^{-t}}{2} + \frac{e^{3t}}{2} \right\}$$
 (38)

> with(DEtools):

- > xx2:=DEplot([sist2],[x,y],t=-7..7,[[cond_in2]], linecolor=red, scene=[t,x(t)]):
- > yy2:=DEplot([sist2],[x,y],t=-7..7,[[cond_in2]], linecolor=blue,
 scene=[t,y(t)]):
- > display([xx2,yy2])



> ec5:=diff(x(t),t)=x(t)+2*y(t)+exp(-t)

$$ec5 := \frac{d}{dt} x(t) = x(t) + 2 y(t) + e^{-t}$$
 (39)

> ec6:=diff(y(t),t)=-2*x(t)+y(t)+1

$$ec6 := \frac{d}{dt} y(t) = -2 x(t) + y(t) + 1$$
 (40)

> sist3:=ec1,ec2

$$sist3 := \frac{d}{dt} x(t) = x(t) + 4 y(t), \frac{d}{dt} y(t) = x(t) + y(t)$$
 (41)

> cond_in3:=x(0), y(0)=1

$$cond_in3 := x(0), y(0) = 1$$
 (42)

> sol3:=dsolve({sist3,cond_in3},{x(t),y(t)})

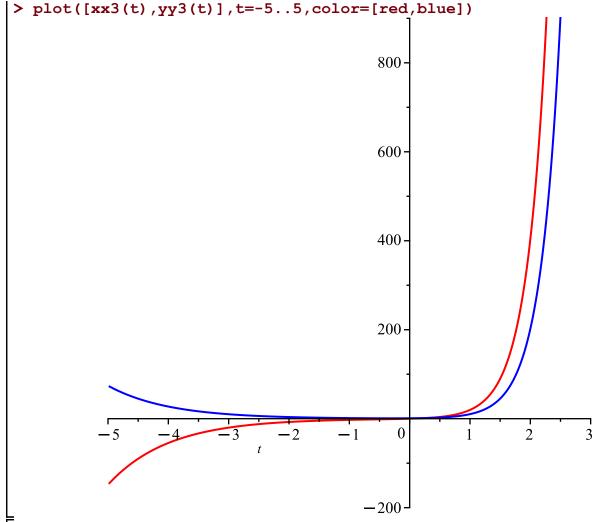
$$sol3 := \left\{ x(t) = -e^{-t} + e^{3t}, y(t) = \frac{e^{-t}}{2} + \frac{e^{3t}}{2} \right\}$$
 (43)

> xx3:=unapply(rhs(sol3[1]),t)

$$xx3 := t \mapsto -e^{-t} + e^{3 \cdot t} \tag{44}$$

> yy3:=unapply(rhs(sol3[2]),t)

$$yy3 := t \mapsto \frac{e^{-t}}{2} + \frac{e^{3 \cdot t}}{2}$$
 (45)



> ec7:=diff(x(t),t)=-x(t)+3*y(t)+3*z(t)+27*t^2

$$ec7 := \frac{d}{dt} x(t) = -x(t) + 3 y(t) + 3 z(t) + 27 t^2$$
(46)

> ec8:=diff(y(t),t)=2*x(t)-2*y(t)-5*z(t)+3*t

$$ec8 := \frac{d}{dt} y(t) = 2 x(t) - 2 y(t) - 5 z(t) + 3 t$$
 (47)

> ec9:=diff(z(t),t)=-2*x(t)+3*y(t)+6*z(t)+3

$$ec9 := \frac{d}{dt} z(t) = -2 x(t) + 3 y(t) + 6 z(t) + 3$$
 (48)

= > sist4:=ec7,ec8,ec9

$$sist4 := \frac{d}{dt} x(t) = -x(t) + 3 y(t) + 3 z(t) + 27 t^2, \frac{d}{dt} y(t) = 2 x(t) - 2 y(t) - 5 z(t) + 3 t, \quad \textbf{(49)}$$

$$\frac{d}{dt} z(t) = -2 x(t) + 3 y(t) + 6 z(t) + 3$$

> cond_in4:=x(0)=50, y(0)=-30, z(0)=26

$$cond_in4 := x(0) = 50, y(0) = -30, z(0) = 26$$
(50)

> sol4:=dsolve({sist4,cond_in4}, {x(t),y(t),z(t)})
sol4:= {
$$x(t) = 3 e^{t} + 2 e^{-t} + 27 t^{2} - 63 t + 45, y(t) = e^{3 t} + 2 e^{t} - 18 t^{2} + 24 t - 32 - e^{-t}, z(t)$$
 (51)

```
= xx4:=unapply(rhs(sol4[1]),t)

xx4 := t \mapsto 3 \cdot e^{t} + 2 \cdot e^{-t} + 27 \cdot t^{2} - 63 \cdot t + 45
                                                                                                                        (52)
> yy4:=unapply (rhs (sol4[2]),t)

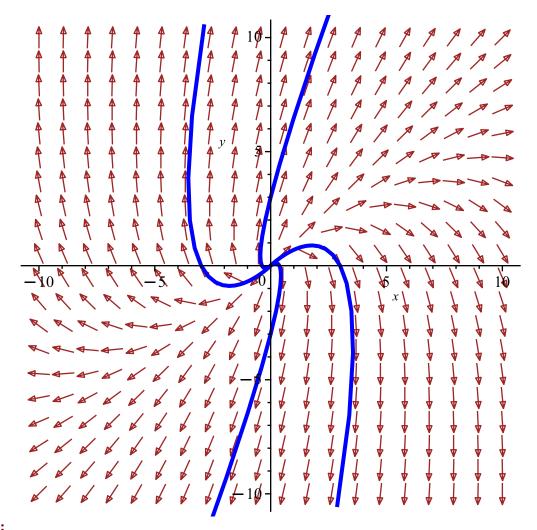
yy4 := t \mapsto e^{3 \cdot t} + 2 \cdot e^{t} - 18 \cdot t^{2} + 24 \cdot t - 32 - e^{-t}
                                                                                                                        (53)
= > plot([xx4(t),yy4(t)],t=-10..10,color=[red,blue])
                                                    7. \times 10^6 -
                                                    5. \times 10^6 -
                                                    3. \times 10^6 -
                                                    2. \times 10^6
                                                    1. \times 10^6
                -10
                                                             0
                                                                                                          10
> with(DEtools): with(plots):
> ec1:=diff(x(t),t)=x(t)+y(t)
                                          ec1 := \frac{\mathrm{d}}{\mathrm{d}t} x(t) = x(t) + y(t)
                                                                                                                        (54)
> ec2:=diff(y(t),t)=-2*x(t)+4*y(t)
                                      ec2 := \frac{\mathrm{d}}{\mathrm{d}t} y(t) = -2 x(t) + 4 y(t)
                                                                                                                        (55)
> sist:=ec1,ec2
                       sist := \frac{d}{dt} x(t) = x(t) + y(t), \frac{d}{dt} y(t) = -2 x(t) + 4 y(t)
                                                                                                                        (56)
```

(27)

 $= -e^{3t} - 27t + 18t^2 + 26 + e^{-t}$

 $cond_in1:=x(0)=3, y(0)=0$

```
cond in 1 := x(0) = 3, y(0) = 0
                                                                                             (57)
> cond in2:=x(0)=0, y(0)=3
                                cond in 2 := x(0) = 0, y(0) = 3
                                                                                             (58)
> cond in3:=x(0)=-3, y(0)=0
                              cond in3 := x(0) = -3, y(0) = 0
                                                                                             (59)
> cond in4:=x(0)=0, y(0)=-3
                              cond in4 := x(0) = 0, y(0) = -3
                                                                                             (60)
> sol1:=dsolve({sist,cond in1},{x(t),y(t)})
                      sol1 := \{x(t) = 6 e^{2t} - 3 e^{3t}, y(t) = 6 e^{2t} - 6 e^{3t} \}
                                                                                             (61)
> limit(sol1[1],t=infinity)
                                                                                             (62)
                                       \lim_{t \to \infty} x(t) = -\infty
> limit(sol1[2],t=infinity)
                                                                                             (63)
                                       \lim y(t) = -\infty
> sol2:=dsolve({sist,cond in2},{x(t),y(t)})
                    sol2 := \{x(t) = -3 e^{2t} + 3 e^{3t}, y(t) = -3 e^{2t} + 6 e^{3t}\}\
                                                                                             (64)
> limit(sol2[1],t=infinity)
                                        \lim_{t\to\infty} x(t) = \infty
                                                                                             (65)
> limit(sol2[2],t=infinity)
                                                                                             (66)
                                        \lim_{t \to \infty} y(t) = \infty
> sol3:=dsolve({sist,cond in3},{x(t),y(t)})
                    sol3 := \{x(t) = -6 e^{2t} + 3 e^{3t}, y(t) = -6 e^{2t} + 6 e^{3t}\}\
                                                                                             (67)
> limit(sol3[1],t=infinity)
                                        \lim_{t \to \infty} x(t) = \infty
                                                                                             (68)
> limit(sol3[2],t=infinity)
                                        \lim_{t \to \infty} y(t) = \infty
                                                                                             (69)
> sol4:=dsolve({sist,cond_in4},{x(t),y(t)})
                      sol 4 := \{x(t) = 3 e^{2t} - 3 e^{3t}, y(t) = 3 e^{2t} - 6 e^{3t}\}
                                                                                             (70)
> limit(sol4[1],t=infinity)
                                                                                             (71)
                                       \lim_{t\to\infty} x(t) = -\infty
> limit(sol4[2],t=infinity)
                                       \lim_{t \to \infty} y(t) = -\infty
                                                                                             (72)
> cond in:=[x(0)=3, y(0)=0],[x(0)=0, y(0)=3],[x(0)=-3, y(0)=0],[x
   (0) = \overline{0}, y(0) = -3
cond in := [x(0) = 3, y(0) = 0], [x(0) = 0, y(0) = 3], [x(0) = -3, y(0) = 0], [x(0) = 0, y(0) = 0]
                                                                                             (73)
    = -31
> DEplot([sist],[x(t),y(t)],t=-5..5,x=-10..10,y=-10..10,[cond in],
   arrows=medium, linecolor=blue, stepsize=0.1)
```



> #ex4: > resta

> with (DEtools): with (plots):

> ec1:=diff(x(t),t)=y(t)

$$ec1 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = y(t) \tag{74}$$

> ec2:=diff(y(t),t)=-x(t)-2*y(t)

$$ec2 := \frac{d}{dt} y(t) = -x(t) - 2y(t)$$
 (75)

> sist:=ec1,ec2

$$sist := \frac{d}{dt} x(t) = y(t), \frac{d}{dt} y(t) = -x(t) - 2y(t)$$
 (76)

> sol:=dsolve({sist}, {x(t),y(t)})
sol :=
$$\{x(t) = e^{-t} (c_2 t + c_1), y(t) = -e^{-t} (c_2 t + c_1 - c_2)\}$$
 (77)

> limit(sol[1],t=infinity)

$$\lim_{t \to \infty} x(t) = 0 \tag{78}$$

> limit(sol[2],t=infinity)

$$\lim_{t \to \infty} y(t) = 0 \tag{79}$$

> DEplot([sist],[x(t),y(t)],t=-5..5,x=-10..10,y=-10..10,[[x(0)=1,y(0)=-2],[x(0)=2,y(0)=-5]],arrows=medium, linecolor=blue)

> #ex5:

> restart

> with (DEtools): with (plots):

> ec1:=diff(x(t),t)=2*x(t)+y(t)

$$ec1 := \frac{d}{dt} x(t) = 2x(t) + y(t)$$
 (80)

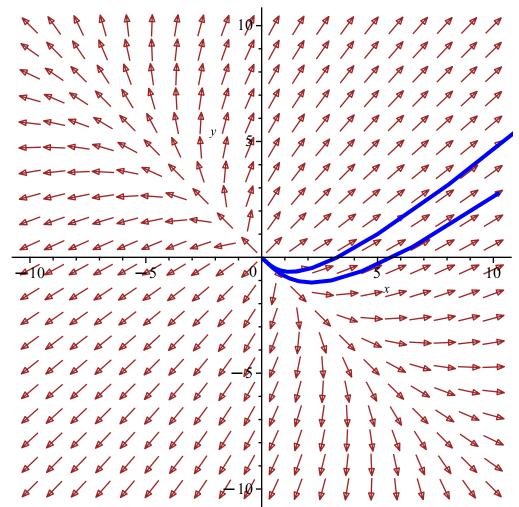
> ec2:=diff(y(t),t)=x(t)+2*y(t)

$$ec2 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) + 2 \ y(t)$$
 (81)

> sist:=ec1,ec2

$$sist := \frac{d}{dt} x(t) = 2 x(t) + y(t), \frac{d}{dt} y(t) = x(t) + 2 y(t)$$
 (82)

> DEplot([sist], [x(t),y(t)], t=-5..5, x=-10..10, y=-10..10, [[x(0)=5,y(0)=1], [x(0)=3,y(0)=-1]], arrows=medium, linecolor=blue)



> ec3:=diff(x(t),t)=-x(t)-y(t)

$$ec3 := \frac{d}{dt} x(t) = -x(t) - y(t)$$
 (83)

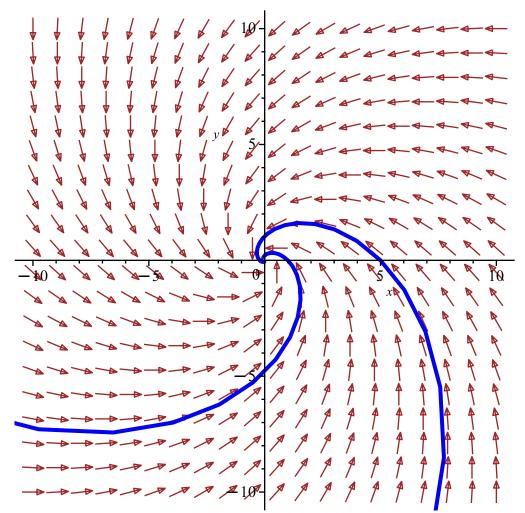
> ec4:=diff(y(t),t)=x(t)-y(t)

$$ec4 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = x(t) - y(t)$$
 (84)

> sist2:=ec3,ec4

$$sist2 := \frac{d}{dt} x(t) = -x(t) - y(t), \frac{d}{dt} y(t) = x(t) - y(t)$$
 (85)

> DEplot([sist2], [x(t),y(t)], t=-5..5, x=-10..10, y=-10..10, [[x(0)=1,y(0)=0], [x(0)=5,y(0)=0]], arrows=medium, linecolor=blue)



> #limitele la infinit sunt 0

$$sol := \left\{ x(t) = e^{-t} \left(c_2 \cos(t) + c_1 \sin(t) \right), y(t) = -e^{-t} \left(\cos(t) c_1 - \sin(t) c_2 \right) \right\}$$
 (86)

> ec5:=diff(x(t),t)=y(t)

$$ec5 := \frac{\mathrm{d}}{\mathrm{d}t} \ x(t) = y(t) \tag{87}$$

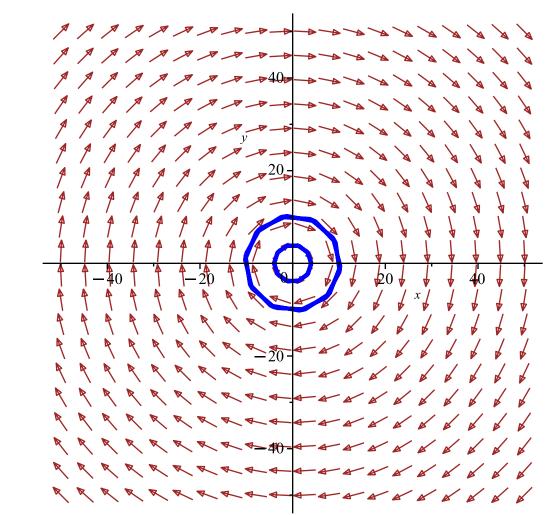
> ec6:=diff(y(t),t)=-x(t)

$$ec6 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = -x(t) \tag{88}$$

> sist3:=ec5,ec6

$$sist3 := \frac{d}{dt} x(t) = y(t), \frac{d}{dt} y(t) = -x(t)$$
 (89)

> DEplot([sist3], [x(t),y(t)], t=-15..15, x=-50..50, y=-50..50, [[x(0) = 9,y(0)=5], [x(0)=4,y(0)=0]], arrows=medium, linecolor=blue)



> ec7:=diff(x(t),t)=-2*x(t)

$$ec7 := \frac{d}{dt} x(t) = -2 x(t)$$
 (90)

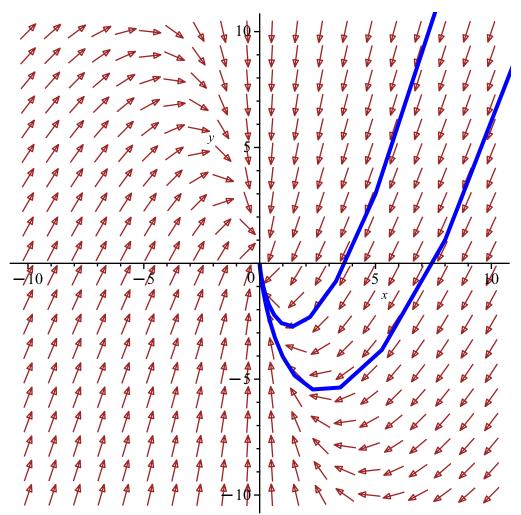
> ec8:=diff(y(t),t)=-4*x(t)-2*y(t)

$$ec8 := \frac{d}{dt} y(t) = -4 x(t) - 2 y(t)$$
 (91)

> sist4:=ec7,ec8

$$sist4 := \frac{d}{dt} x(t) = -2 x(t), \frac{d}{dt} y(t) = -4 x(t) - 2 y(t)$$
 (92)

> DEplot([sist4],[x(t),y(t)],t=-5..5,x=-10..10,y=-10..10,[[x(0)=8,y(0)=1],[x(0)=5,y(0)=3]],arrows=medium,linecolor=blue)



> #limitele la infinit sunt 0
> ec9:=diff(x(t),t)=x(t)-4*y(t)

$$ec9 := \frac{d}{dt} x(t) = x(t) - 4 y(t)$$
 (93)

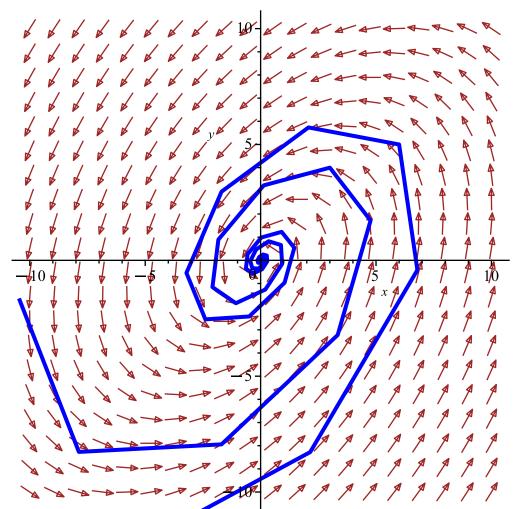
> ec10:=diff(y(t),t)=5*x(t)-3*y(t)

$$ec10 := \frac{d}{dt} y(t) = 5 x(t) - 3 y(t)$$
 (94)

> sist5:=ec9,ec10

$$sist5 := \frac{d}{dt} x(t) = x(t) - 4 y(t), \frac{d}{dt} y(t) = 5 x(t) - 3 y(t)$$
 (95)

DEplot([sist5],[x(t),y(t)],t=-5..5,x=-10..10,y=-10..10,[[x(0)=6,y(0)=5],[x(0)=3,y(0)=4]],arrows=medium,linecolor=blue)



> #limitele la infinit sunt 0
ec11:=diff(x(t),t)=3*x(t)-y(t)

$$ec11 := \frac{d}{dt} x(t) = 3 x(t) - y(t)$$
 (96)

> ec12:=diff(y(t),t)=y(t)

$$ec12 := \frac{\mathrm{d}}{\mathrm{d}t} \ y(t) = y(t) \tag{97}$$

> sist6:=ec11,ec12

$$sist6 := \frac{d}{dt} x(t) = 3 x(t) - y(t), \frac{d}{dt} y(t) = y(t)$$
 (98)

> DEplot([sist6], [x(t),y(t)], t=-5..5, x=-10..10, y=-10..10, [[x(0)=3,y(0)=5], [x(0)=8,y(0)=4]], arrows=medium, linecolor=blue)

