# Vision 1 - Intro + Camera models + Calibration

## 1. Projection

- 1.1. What size if the projection matrix P?
- 1.2. If we have a 3D point M and a projection matrix P, how do we compute the corresponding pixel location where the camera will see the 3D point? Give steps.
- 1.3. Given the projection matrix (P) and a 3D point compute where that point will be seen in the camera.

1.3.1. 
$$P = \begin{pmatrix} 1000 & 0 & 500 & 0 \\ 0 & 1000 & 500 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}; M = \begin{bmatrix} -400 \\ 300 \\ 1000 \end{bmatrix}$$
  
1.3.2.  $P = \begin{pmatrix} 0 & -500 & -1000 & -190000 \\ 1000 & -500 & 0 & -120000 \\ 0 & 0 & 0 & -300 \end{pmatrix}; M = \begin{bmatrix} 60 \\ -900 \\ -200 \end{bmatrix}$   
1. If we have m (2D point on image plane), can we compute M (3D p

- 1.4. If we have m (2D point on image plane), can we compute M (3D point)? (If yes: How?, if no: Why not?)
- 1.5. What is the meaning/use of the individual intrinsic parameters  $(f, \alpha_u, \alpha_v, s, u_0, v_0)$ ?

$$\mathsf{K*A} = \begin{pmatrix} f * \alpha_u & f * s & u_0 & 0 \\ 0 & f * \alpha_v & v_0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

1.6. What are a camera's extrinsic parameters? What do they model?

#### 2. Distortion

- 2.1. What is the name of the two distortion models we discussed?
- 2.2. Why can the distortion models not be integrated into the projection matrix? (Why do these two components (distortion, projection) need to be handled separately?)

## 3. Calibration

3.1. How does one of the three discussed camera calibration methods work (choose which one you want to describe)?

### 4. Projective space

4.1. What is the inhomogeneous version of

$$\begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}, \begin{bmatrix} 4 \\ 2 \\ 2 \end{bmatrix}, \begin{bmatrix} 6 \\ 4 \\ -1 \end{bmatrix}, \begin{bmatrix} 5 \\ 3 \\ 0.5 \end{bmatrix}, \begin{bmatrix} 1 \\ 10 \\ -3 \\ 1 \end{bmatrix}, \begin{bmatrix} 2 \\ -4 \\ 1.1 \\ 2 \end{bmatrix}, \begin{bmatrix} 0 \\ 0 \\ -1 \\ 10 \end{bmatrix}, \begin{bmatrix} -15 \\ 3 \\ 6 \\ 3 \end{bmatrix}$$

4.2. Which of the points (p) lie on the line (l) (points and line are described in projective 2 space (P2))?

$$l = \begin{bmatrix} 1 \\ 2 \\ -3 \end{bmatrix}, \ p = \left\{ \begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 6 \\ 0 \\ 2 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix} \quad \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \quad \begin{bmatrix} 110 \\ -40 \\ 10 \end{bmatrix} \right\}$$

4.3. What is the geometric interpretation of a projective space point with a zero as last entry? (e.g.,  $\begin{bmatrix} a & b & 0 \end{bmatrix}^T$ ,  $\begin{bmatrix} c & d & e & 0 \end{bmatrix}^T$ )