

# THE NEAR-INFRARED NUMBER COUNTS AND LUMINOSITY FUNCTIONS OF LOCAL GALAXIES

GYULA P. SZOKOLY, MARK U. SUBBARAO, AND ANDREW J. CONNOLLY  
 Department of Physics and Astronomy, The Johns Hopkins University, Baltimore, MD 21218

AND

BAHRAM MOBASHER

Astrophysics Group, Blackett Laboratory, Imperial College, Prince Consort Road, London SW7 2BZ, England, UK

Received 1997 June 6; accepted 1997 August 22

## ABSTRACT

This study presents a wide-field near-infrared ( $K$ -band) survey in two fields: SA 68 and Lynx 2. The survey covers an area of  $0.6 \text{ deg}^2$ , complete to  $K = 16.5$ . A total of 867 galaxies are detected in this survey of which 175 have available redshifts. The near-infrared number counts to  $K = 16.5 \text{ mag}$  are estimated from the complete photometric survey and are found to be in close agreement with other available studies. The sample is corrected for incompleteness in redshift space, using selection function in the form of a Fermi-Dirac distribution. This is then used to estimate the local near-infrared luminosity function (IRLF) of galaxies. A Schechter fit to the infrared data gives  $M_K^* = -25.1 \pm 0.3$ ,  $\alpha = -1.3 \pm 0.2$ , and  $\phi^* = (1.5 \pm 0.5) \times 10^{-3} \text{ Mpc}^{-3}$  (for  $H_0 = 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$  and  $q_0 = 0.5$ ). When reduced to  $\alpha = -1$ , this agrees with other available estimates of the local IRLF. We find a steeper slope for the faint end of the infrared luminosity function when compared to previous studies. This is interpreted as being due to the presence of a population of faint but evolved (metal-rich) galaxies in the local universe. However, it is not from the same population as the faint blue galaxies found in the optical surveys. The characteristic magnitude ( $M_K^*$ ) of the local IRLF indicates that the bright red galaxies ( $M_K \sim -27 \text{ mag}$ ) have a space density of  $\leq 5 \times 10^{-5} \text{ Mpc}^{-3}$  and, hence, are not likely to be local objects.

*Subject headings:* cosmology: observations — galaxies: luminosity function, mass function — galaxies: photometry — galaxies: statistics — infrared: galaxies — surveys

## 1. INTRODUCTION

The change in the intrinsic properties of galaxies as a function of lookback time provides a sensitive probe of the theories of formation of galaxies. A detailed knowledge of this is also required for interpreting the deep counts of galaxies and, hence, exploring the underlying geometry of the universe. At the optical, far-infrared and radio wavelengths, however, the observed properties of galaxies are sensitive to the morphological types, star formation history, and dust content, which makes it difficult to disentangle the effects of evolution and cosmology at these passbands. The exception is the near-infrared wavelength ( $2.2 \mu\text{m}$ ), which is less affected by the evolutionary processes (owing to the dominance of the near-infrared light by old, near-solar mass stars) and can be more securely modeled. Also, at these wavelengths, the galaxy spectral energy distributions are similar for all galaxy types, which leads to similar  $K$ -corrections for all galaxies. Therefore, the near-infrared number-magnitude counts of galaxies are less affected by the mix of galaxy types or uncertainties due to evolution, compared to other wavelengths. However, the interpretation of the infrared counts requires knowledge of the faint-end slope of the local infrared luminosity function (IRLF).

There are other independent studies, also requiring knowledge of the IRLF of galaxies. Owing to type dependence of the optical LF (Efsthathiou, Ellis, & Peterson 1988) and existence of a density-morphological type relation for galaxies, the optical LF is expected to be environmental dependent. Indeed, recent spectroscopic studies of field galaxies have shown the existence of a population of massive, star-forming galaxies (Cowie, Hu, & Songaila 1995; Cowie et al. 1996) in the field, not present in clusters (Trentham

1997). The IRLF is not sensitive to such star-forming galaxies, which affect the bright end of the optical LF and, hence, is likely to have a universal form. Further, this also gives the integrated star formation in the local universe.

Previous studies of the IRLFs of galaxies either depend on surveys selected at optical wavelengths (Mobasher, Sharples, & Ellis 1993; Mobasher, Ellis, & Sharples 1986) or are mainly pencil-beam surveys, covering only small solid angles (Cowie et al. 1996; Glazebrook et al. 1994). Also, the only study of the morphological type dependence of the IRLF (Mobasher et al. 1993) is biased against early-type galaxies (owing to the optical selection of galaxies) and has too few objects of a given type. Moreover, since this sample is optically selected, it is not possible to convert it to an infrared-limited survey because of the changes in type mix (i.e., color) with redshift. Therefore, it can constrain only the bright end of the IRLF. Recently, a wide-angle near-infrared survey was performed (Gardner et al. 1997) to a limiting magnitude of  $K = 15$ . This is, however, too shallow to constrain the faint-end slope of the local IRLF with the statistics becoming very poor fainter than  $M_K = -23.5 + 5 \log (H_0/50) \text{ mag}$  (i.e., 1 mag below  $M_K^*$ ), where the disagreement between different measurements of the IRLFs becomes the largest.

To overcome these problems, we have carried out a medium-deep near-infrared survey, covering a large area and complete to  $K \sim 16 \text{ mag}$ . The fields were selected to have optical multicolor data, with redshifts available for a subsample of galaxies. In this first paper of a series, we introduce this near-infrared-selected survey. Using published redshifts, we then construct the local IRLF of galaxies and compare it with other, independent measurements. A study of the morphological type-dependence of

the IRLF, color-magnitude relations for field galaxies, and the bivariate optical/infrared LF will be presented in following papers.

In § 2 we present the observations and data reduction. Section 3 explains source detection and photometry. The astrometry and construction of the infrared catalog are discussed in § 4. The number-magnitude counts are presented in § 5. Section 6 explores the completeness of the sample. The infrared luminosity function is constructed in § 7. Finally, our conclusions are summarized in § 8.

## 2. OBSERVATIONS AND DATA REDUCTION

The near-infrared observations presented here were performed using the IRIM camera on the 1.3 m telescope at KPNO. This instrument is a NICMOS 3 array (HgCdTe) with  $256 \times 256$  pixels. The pixel scale of  $1''.96$  corresponds to a field of view of  $8.3 \times 8.3$ . This configuration enables us to undertake a wide field survey with relatively little cost in observation time. The observations were carried out in  $K_s$  filter ( $\lambda = 2.15 \mu\text{m}$ ;  $\Delta\lambda = 0.33 \mu\text{m}$ ). This filter is *not* the  $K'$  filter described by Wainscoat & Cowie (1992) but rather the  $K$ -short filter also used by the 2MASS survey—unfortunately the IRIM instrument manual refers to it as  $K'$ . The filter cuts off about  $0.1 \mu\text{m}$  bluer than the standard  $K$  filter. This significantly reduces the thermal emission resulting in a decrease of approximately 25% in the sky background over the standard  $K$  filter.

Two fields were selected for near-infrared observations: Lynx 2 ( $8^{\text{h}}41^{\text{m}}43^{\text{s}}.7$ ,  $44^{\circ}46'42''$  [1950]) and SA 68 ( $0^{\text{h}}14^{\text{m}}53^{\text{s}}$ ,  $15^{\circ}36'48''$  [1950]). The fields were selected to have existing multicolor photometric ( $UB_J R_F I_N$ ) and spectroscopic data (Munn et al. 1997). The near-infrared observations were carried out by dithering around each pointing position. Using an offset of  $20''$  and an exposure time of 1 minute (20 s with 3 co-adds), a total of five exposures were taken, corresponding to an integration time of 5 minutes per pointing. This scheme was chosen to avoid cosmic rays and bad pixels. The dithered pointings were used to estimate the sky background and to construct flat fields. This dithering pattern was repeated a total of 36 times to produce a mosaic of each field. Small overlaps between the mosaic elements were incorporated into the dither pattern in order to check the internal consistency of the photometry and astrometry. Using an integration time of 5 minutes, we reach a formal magnitude limit of  $K_s = 17$  for a  $5 \sigma$  detection in a  $5''$  aperture. A total area of about  $0.8 \text{ deg}^2$  was covered in both fields to a depth of  $K_s = 17$ . The overlap between the optical and near-infrared survey is about  $0.6 \text{ deg}^2$ .

The data were reduced using standard IRAF routines. After dark subtraction, each exposure was flat-fielded using the following three steps: Initially the dome flat was used to correct the data frames for the large-scale sensitivity variance of the detector. The flat-fielded data frames were then corrected for changes in the instrument response (which was found to vary slightly over a timescale of a few minutes) by dividing them by the sky flats, constructed by median filtering five to 10 successive data frames. Finally, the small background gradients present on the images were estimated and removed by creating a median-filtered image with a very large box size and subtracting this from the original data frames.

Bad pixels were removed by deriving the average signal and variance for each pixel over the whole night and identifying those pixels that were greater than (hot pixels) or less

than (nonresponding pixels)  $5 \sigma$  above or below the mean. Those pixels with a large variance were identified as having variable sensitivity (i.e., noisy pixels) and were excluded.

The final frames were registered to a common coordinate system using bright stars, not affected by bad pixels, in the frame. The measured uncertainties of the centroiding of the bright stars was  $0.1\text{--}0.2$  pixels. Owing to the undersampling of our data and the large number of bad pixels, image shifts were done using linear interpolation after excluding each of the identified bad pixels. This procedure conserves the flux (which was our main goal) and maximizes the signal-to-noise ratio. However, it does increase the intrinsic PSF of the resultant images by about 40%. The five exposures, covering the same area, were then averaged and trimmed to construct the final images. Standard photometric calibrations were derived using the UKIRT faint standards (Casali & Hawarden 1992). The observations are estimated to have an intrinsic photometric uncertainty of approximately  $0.06 \text{ mag}$  in the zero point.

## 3. SOURCE DETECTION AND PHOTOMETRY

The source detection was performed using the SExtractor package (Bertin & Arnouts 1996). Objects were identified using a Gaussian detection kernel with FWHM of  $3''$ . A detection limit was set such that the objects have a minimum of 5 pixels  $1.5 \sigma$  above the level of the sky background (after convolution). This corresponds to a surface brightness of  $19.7 \text{ mag arcsec}^{-2}$ . For all detected objects, two sets of magnitudes were measured: an aperture magnitude over a radius of  $5''$  and a Kron magnitude with a Kron parameter of 2.5 (Kron 1980). Owing to the large pixel scale and the relatively small intrinsic sizes of the galaxies at  $K_s = 15$ , the difference between the aperture and Kron magnitudes were found to be negligible for the majority of our sample. At the brightest magnitude limit considered in our survey,  $K_s = 13$ , the galaxy sizes exceed the aperture size and, hence, are better represented by the Kron magnitudes. For the subsequent analysis in this study, we use the Kron magnitudes. For the adopted Kron parameter, these roughly correspond to the total magnitudes of galaxies. No shape parameters (e.g., second moments) were estimated from the near-infrared images because of the poor spatial resolution and the existence of higher resolution optical data.

From the selection function derived for the near-infrared data, we estimate that our  $5 \sigma$  detection limit is  $17.0 \text{ mag}$ , and our completeness limit is  $K_s = 16.5$ . To determine the internal accuracy of our photometry, those sources detected in the overlapping regions are compared in Figure 1. The rms dispersion of the one-to-one correlation is  $0.15 \text{ mag}$  at the completeness limit and  $0.3 \text{ mag}$  at the detection limit. These are taken as the internal uncertainties in our infrared photometry. The external photometric accuracy is estimated by comparing, in Figure 1, the  $K_s$  band magnitudes for those galaxies in common between the present study and those by Bershadsky et al. (1994). This gives a larger rms scatter of  $0.2 \text{ mag}$ , which is, in part, due to the fact that we are comparing our Kron magnitudes with the aperture magnitudes measured by Bershadsky (with associated aperture corrections). The spatial resolution of our data prevents an analysis of the Bershadsky data using matched apertures. It is encouraging, however, that we detect no significant zero-point offset or correlation that could suggest systematic errors in either study. For the rest of this

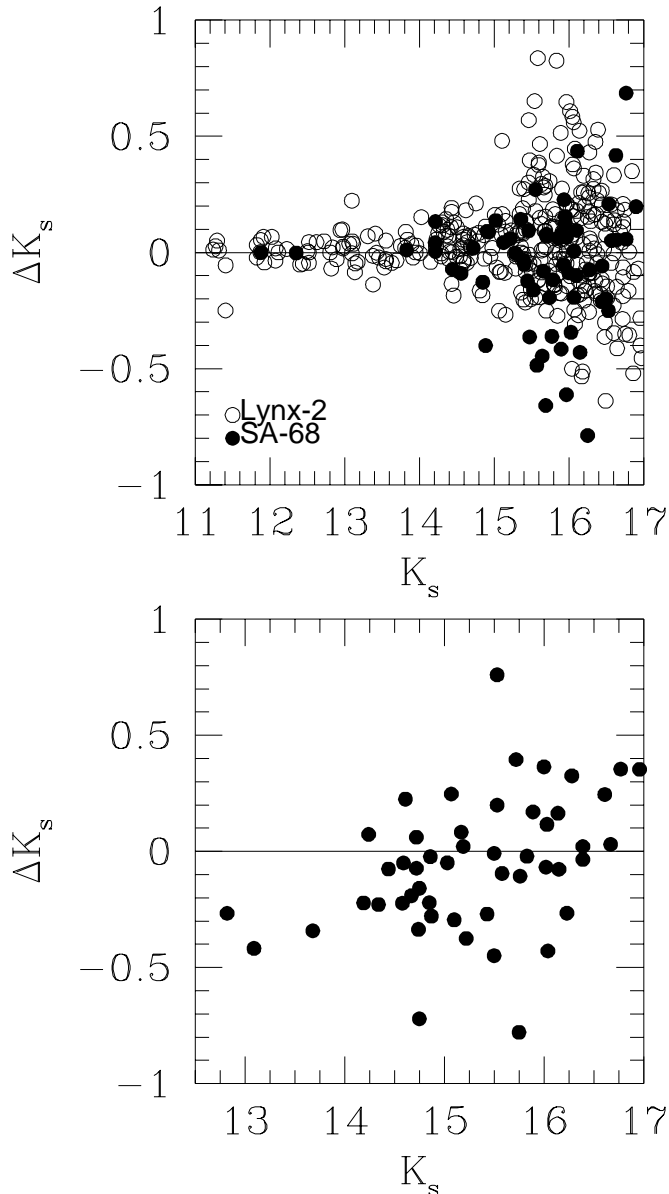


FIG. 1.—Photometric uncertainties within our data are estimated internally from a comparison between repeated observations and externally using published  $K$ -band photometry. The top panel shows the dispersion about a one-to-one correlation for those sources detected in overlap IRIM frames. At the completeness limit ( $K_s = 16.5$ ) the rms dispersion is 0.15 mag. The lower panel shows a comparison between our photometry and that of Bershadsky (Bershadsky et al. 1994),  $K_s^{(1)}$ . There is no significant offset between our photometric system, but owing to the use of different magnitudes, the rms dispersion increases to 0.2 mag.

paper, we assume an internal photometric accuracy of 0.15 mag.

#### 4. ASTROMETRY AND COMPARISON WITH THE OPTICAL CATALOG

As noted above, the large pixel scale of the near-infrared detector here limits our ability to perform accurate star galaxy separation (essentially all but the largest objects detected are pointlike). However, for each of the survey fields, deep independent multicolor surveys exist, which can be used to classify the near-infrared detections (Koo 1986; Kron 1980). This requires accurate astrometric calibration of our detected sources.

The astrometry was carried out in two steps. Initially, approximate astrometric offsets were determined by identifying stars on each frame from the Guide Star Catalog (GSC; Lasker et al. 1990; Russell et al. 1990; Jenkner et al. 1990). This resulted in two to six stars per frame. Averaging over all the frames, we found the overall deviation from a zero-distortion focal plane negligible. An astrometric zero point for each frame was determined from the GSC stars. Using this crude calibration, the near-infrared data were paired up with the optical catalogs by searching within a  $10''$  radius around each detected object. From the paired data, we extract isolated sources (i.e., those near-infrared objects with only one optical counterpart within the search radius) and rederive a more accurate astrometric solution. While the astrometric solution for each frame can be established rather accurately ( $0.1''$ – $0.2''$ ), the uncertainty in astrometry for individual objects remains large ( $\sim 1.8''$ ), owing to the large PSF.

We construct an optical–near-infrared catalog of all the detected objects in the overlapping region, by extending the technique of Sutherland & Saunders (1992) to use both positional and magnitude information. The simplest method for identifying the same object in different catalogs is to estimate the maximum positional uncertainty and to pair up the detected objects with separations smaller than this threshold. This technique works well for surveys in which the average astrometric uncertainty is much smaller than the typical separation between the objects. However, for moderately dense fields, this method does not produce reliable catalogs as shown for our data set in Figure 3a. The dashed line is the number of near-infrared detections without an optical counterpart and indicates that a tolerance level of  $\sim 2$  normalized distance units is required (normalized distance is  $[(d_1/\sigma_1)^2 + (d_2/\sigma_2)^2]^{1/2}$ , where  $d_1$  and  $d_2$  are the angular positional differences along the two axes with  $\sigma_1$  and  $\sigma_2$  as their mean respective uncertainties). At this level, about 25% of the detections have multiple optical counterparts (dotted line). The solid line shows the number of cases in which this simple method results in unique matches. This cuts off rather sharply, indicating that this identification is not too reliable.

To eliminate multiple hits within the matched catalogs, the usual practice is to pick the closest object from the optical catalog. One can assign a *likelihood* to this identification:

$$L = \frac{q(m)f(x, y)}{n(m)}, \quad (1)$$

where  $q(m)$  is the probability distribution in magnitude,  $f(x, y)$  describes the distribution of positional uncertainties, and  $n(m)$  is the surface density of objects of magnitude  $m$ . This method does not take into account the local information. For isolated objects, the match is likely to be genuine even if the positional uncertainty is large, while in a crowded area, multiple objects can be very close, which makes the identification unreliable (even though the likelihood is high). Following Sutherland & Saunders (1992), we address this problem by defining a new local quantity, the *reliability*, as

$$R = \frac{L_i}{\sum_j L_j + (1 - Q)}, \quad (2)$$

where  $L_i$  is the likelihood of an identification, as defined

above,  $L_j$  are the likelihoods of other candidates, and  $Q$  is the probability that the identification is possible (i.e., both catalogs contain the object). This formalism properly takes into account the existence of other identified candidates.

In the present study, we extend this technique to include positional and magnitude information. First, we identify isolated objects (sources with no other detection within a  $10''$  radius) present in both the catalogs. Since the infrared survey is not as deep as its optical counterpart, this subset, in practice, contains only genuine identifications. From these data we then derive a correlation between the near-infrared ( $K_s$ -band) and optical detections by fitting the function  $K^*(U, B_J, R_F, I_N)$  to a second-degree polynomial (Connolly et al. 1995). To allow for differences in optical photometry between the two fields, this procedure was done independently for each field. The correlation between the predicted and measured  $K$ -band magnitudes is shown in Figure 2. The mean residual uncertainty for both fields is 0.45 mag, and the error distribution is Gaussian with no outlying points. Since about 40% of the galaxies are isolated, we do not expect more than a few (at most five) galaxies with unusual  $K$  magnitude in the full survey.

Using the fit  $K^*(U, B_J, R_F, I_N)$ , a normalized distance metric is then defined as

$$\rho = \sqrt{\frac{(\alpha_K - \alpha_0)^2}{\sigma_\alpha^2} + \frac{(\delta_K - \delta_0)^2}{\sigma_\delta^2} + \frac{(K - K^*)^2}{\sigma_K^2}}, \quad (3)$$

where  $\sigma_\alpha$ ,  $\sigma_\delta$ ,  $\sigma_K$  are the uncertainties in the spatial and color dimensions. Since the distributions in all three directions are Gaussian and independent, the likelihood functions are then calculated as

$$L = \frac{f(\alpha, \delta, K)}{n(K)} \approx Q(<K) \frac{e^{-\rho^2/2}}{2\pi\sigma_\alpha\sigma_\delta\sigma_K}, \quad (4)$$

where  $n(K)$  is the density of optical detections and  $Q(<K)$  the probability that an object of magnitude  $K$  has an optical counterpart [in this case  $Q(<K) \approx 1$  for the infrared catalog]. Finally, the reliability of the match is defined as

$$R_j = \frac{L_j}{\sum_i L_i + (1 - Q)} \approx \frac{L_j}{\sum_i L_i}. \quad (5)$$

This technique is used to cross-compare the near-infrared and optical catalogs, and as demonstrated in Figure 3b, it considerably improves the match between the two surveys. The ratio of number of objects uniquely matched to the number of objects with multiple matches is, at all distances, greater than that derived when using only the positional information. Therefore, including color information greatly reduces the number of spurious pairs, which results in a much more reliable catalog.

For all the matched objects, the most reliable optical detection was entered into the final catalog. The calculated reliabilities, in most cases, were found to be close to 1. For each object with an optical counterpart, we adopt the classification (star or galaxy) as defined in the optical catalog. An area of  $0.8 \text{ deg}^2$  was surveyed in the near-infrared, of which  $0.6 \text{ deg}^2$  overlaps with the multicolor optical surveys. Over this area, a total of 871 objects were detected in the near-infrared survey, of which 867 have optically identified counterparts. The four objects without an optical counterpart are likely to correspond to faint spurious detections.

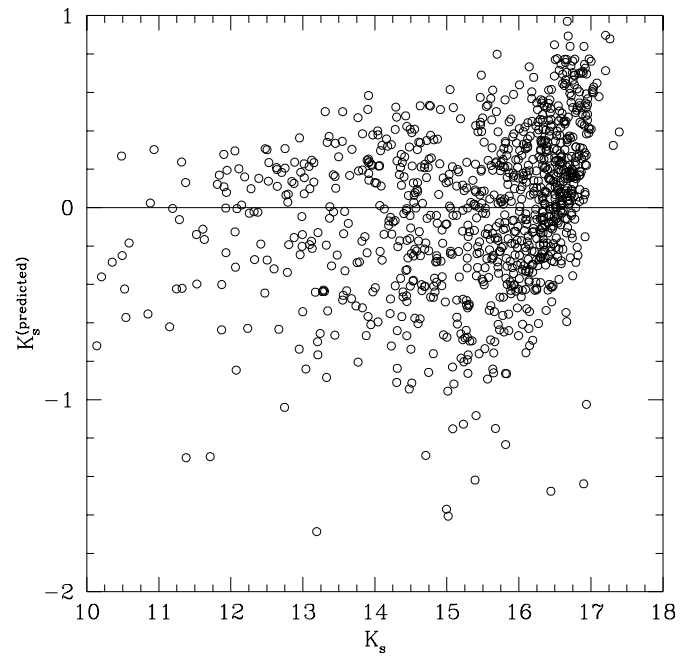


FIG. 2.—Correlation between predicted and measured  $K_s$  magnitudes. The estimated magnitude is derived by fitting a second-degree polynomial function to the optical  $U, J, F, N$  photometry. The rms dispersion about this relation is 0.4 mag. Using this correlation, the optical and near-infrared data were using a combined angular and magnitude distance metric.

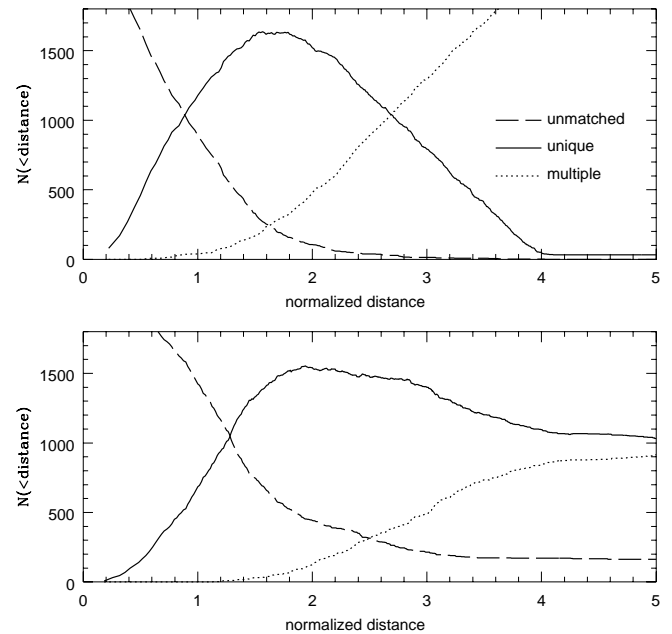


FIG. 3.—Effect of using color information to cross-identification catalogs. When one uses angular distance only (top), the acceptance criteria is very critical. Setting the limit too low will result in the rejection of valid pairs (dashed curve). Relaxing the criteria too much results in too many ambiguous pairs (dotted line). Including the color information eliminates most of the accidental coincidences (dashed line) and drastically reduces the number of ambiguous matches. At all distances, the ratio of unique to multiple matchups is larger when we incorporate color information. Further, the choice of tolerance for the metric is much less important (solid line; the number of unique identifications dies off gently). In both cases we used the dimensionless normalized distance,  $\rho = \{[(\alpha_K - \alpha_0)^2/\sigma_\alpha^2] + [(\delta_K - \delta_0)^2/\sigma_\delta^2]\}^{1/2}$  and  $\rho = \{[(\alpha_K - \alpha_0)^2/\sigma_\alpha^2] + [(\delta_K - \delta_0)^2/\sigma_\delta^2] + [(K - K^*)^2/\sigma_K^2]\}^{1/2}$  as defined in § 4.

The final infrared catalog contains 867 galaxies to  $K_s = 17$  mag. All these objects have optical data. The redshifts are compiled from literature for a subset of galaxies in the infrared catalog, giving a total of 175 galaxies with measured redshifts (Munn et al. 1997). This sample will be used in the following sections to construct the number counts and near-infrared luminosity function of local galaxies.

Using the estimated  $K$ -band magnitudes, we verify that our survey is shallow enough that blending of close pairs of galaxies does not significantly affect the catalog. We calculate the expected infrared magnitude for every optical galaxy around each infrared detection. We individually examine all infrared detections that have multiple optical counterparts within  $10''$  and with  $K_{\text{predicted}} < 16.5$  (i.e., sufficiently bright that they would make it into the  $K$ -selected sample). Within the complete photometric survey, there were 10 such candidates, each of which was handled correctly by the photometry package.

5. THE NEAR-INFRARED NUMBER COUNTS

The near-infrared number counts, estimated from this study, are presented in Table 1. These are compared in Figure 4 and Table 2 with the counts from other independent studies as compiled by Gardner, Cowie, & Wainscoat (1993). The comparison between the various studies is made over the magnitude range covered in this study ( $K_s = 13\text{--}16.5$  mag). In all the counts in Figure 4, the uncertainties are estimated using the technique developed by Gehrels (1986).

The counts derived from our two independent fields, SA 68 and Lynx 2, agree within their uncertainties over the

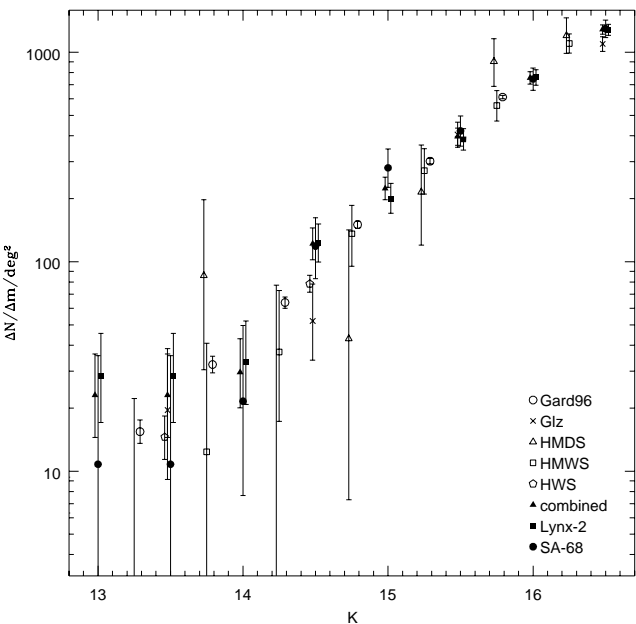


FIG. 4.— $K$ -band differential number counts in the  $K = 13\text{--}16.5$  range. The data are a compilation from Gardner et al. (1993) (HWS, HMWS, HMDS), Glazebrook et al. (1994) (Glz), Gardner (1996) (Gard96), our SA 68 and Lynx 2 fields, and our two fields combined (combined). Errors are  $1\sigma$  estimates from the raw counts.

entire magnitude range covered here. They are also in good agreement with the counts in Gardner (1996) and Huang & Cowie (1998), each covering a larger area ( $9.8\text{ deg}^2$ ) but to a shallower depth ( $K < 16$ ). These results confirm that the

TABLE 1  
K-BAND DIFFERENTIAL NUMBER COUNTS

Survey	$K$	Raw $N$	Low	High	Area (arcmin <sup>2</sup> )	$N$ (mag <sup>-1</sup> deg <sup>-2</sup> )
SA 68 field .....	13.0	1	0.17	3.3	667	10.8
	13.5	1	0.17	3.3		10.8
	14.0	2	0.71	4.6		21.6
	14.5	11	7.7	15		119
	15.0	26	21	32		281
	15.5	39	33	46		421
	16.0	69	61	78		745
	16.5	120	109	132		1295
Lynx 2 field .....	10.5	1	0.17	3.3	1519	4.7
	11.0	0	0	1.8		0
	11.5	1	0.17	3.3		4.7
	12.0	5	2.8	8.4		24
	12.5	1	0.17	3.3		4.7
	13.0	6	3.6	9.6		28
	13.5	6	3.6	9.6		28
	14.0	7	4.4	11		33
	14.5	26	21	32		123
	15.0	42	36	50		199
	15.5	81	72	91		384
	16.0	160	147	174		758
	16.5	270	254	287		1279
Combined fields .....	13.0	7	4.4	11	2185	23
	13.5	7	4.4	11		23
	14.0	9	6.1	13		30
	14.5	37	31	44		122
	15.0	68	60	77		224
	15.5	120	109	132		395
	16.0	229	214	245		755
	16.5	390	370	410		1285

NOTE.—Listed are the field, the  $K$ -magnitude (center of the bin), the raw number of galaxies, the upper and lower  $1\sigma$  limits for the raw counts (Gehrels 1986), the survey area, and the number per magnitude per square degree.

TABLE 2  
K-BAND DIFFERENTIAL NUMBER COUNTS

Survey	K	Raw N	Low	High	Area (arcmin <sup>2</sup> )	N (mag <sup>-1</sup> deg <sup>-2</sup> )
Gardner 93 (HWS) .....	12.5	5	2.8	8.4	5690	0.0009
	13.5	23	18	29		0.004
	14.5	124	113	136		0.02
Gardner 93 (HMWS) .....	12.75	2	0.71	4.6	582.03	24.7
	13.25	0	0	1.8		0
	13.75	1	0.17	3.3		12.4
	14.25	3	1.4	5.9		37.1
	14.75	11	7.7	15		136
	15.25	22	17	28		272
	15.75	45	38	53		557
	16.25	89	80	99		1100
Gardner 93 (HMDS) .....	16.75	158	145	172	167.68	1900
	13.75	2	0.71	4.6		86
	14.25	0	0	1.8		0
	14.75	1	0.17	3.3		43
	15.25	5	2.8	8.4		215
	15.75	21	16	27		902
	16.25	28	23	34		1200
	16.75	48	41	56		2060
Glazebrook 93 .....	13.5	3	1.4	5.9	551.9	0.005
	14.5	8	5.2	12	551.9	0.0145
	15.5	62	54	71	551.9	0.112
	16.5	168	155	182	551.9	0.304
Gardner 96 .....	10.25	1	0.17	3.3	30750	$6 \times 10^{-5}$
	10.75	1	0.17	3.3		$6 \times 10^{-5}$
	11.25	4	1.4	7.1		$2.6 \times 10^{-4}$
	11.75	13	9.4	18		$8.4 \times 10^{-4}$
	12.25	22	17	28		0.0014
	12.75	33	27	40		0.0021
	13.25	66	58	75		0.0043
	13.75	138	126	151		0.0090
	14.25	273	256	290		0.0177
	14.75	642	617	668		0.0418
	15.25	1290	1250	1330		0.0839
	15.75	2609	2560	2660		0.1697

NOTE.—Listed are the survey, the K-magnitude (center of the bin), the raw number of galaxies, the upper and lower 1  $\sigma$  limits for the raw counts, the survey area, and the number per magnitude per square degree.

present near-infrared survey is complete to  $K_s = 16.5$  mag. Moreover, it indicates that there is no anomaly, due to density enhancement in our fields or photometric zero points, affecting the near-infrared distribution of galaxies in this study.

Fitting a linear relation to the number-magnitude counts for  $14.5 < K_s < 16.5$ , we derive a slope of  $0.46 \pm 0.06$ ,  $0.53 \pm 0.04$ , and  $0.50 \pm 0.03$  for the SA 68, Lynx 2, and combined samples, respectively. These values are lower than those derived by Huang & Cowie (1998) and Gardner et al. (1993) from their wide-field survey. They are also lower than the predictions by Huang et al. (1997) for a no-evolutionary model. The shallower slope may be indicative of an overdensity of low-redshift galaxies in our two fields (which is clearly seen in the redshift distribution of the Lynx 2 field but not in SA 68). It is more likely, however, that the variation among the measured slopes is an artifact of fitting linear relations over a narrow range of magnitudes.

## 6. SELECTION FUNCTIONS

As the spectroscopic observations in this study are based on an optically selected sample, it is likely that at fainter  $K_s$  magnitudes, the survey becomes incomplete in redshift space. Therefore, it is instructive to estimate the incompleteness in redshift as a function of  $K_s$ . Assuming a Fermi-Dirac distribution for the selection function (Sandage, Tammann,

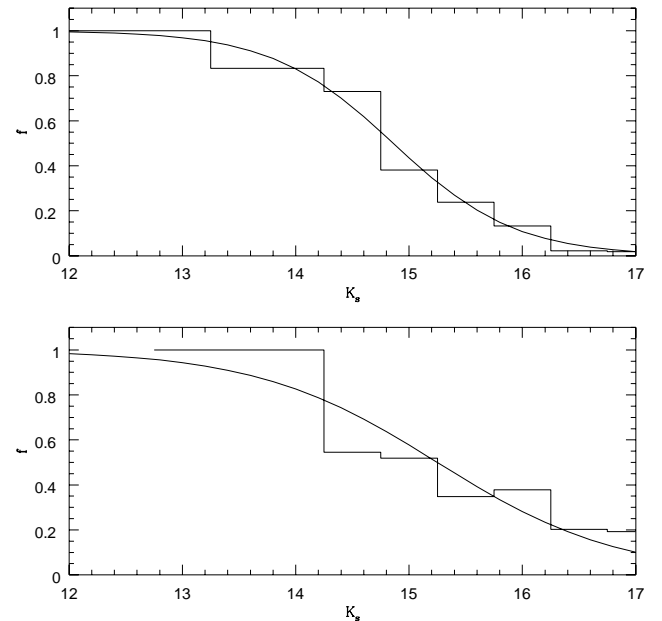


FIG. 5.—Redshift completeness,  $f$ , in each of the fields. The sample used in the luminosity function is cut at  $K_s = 16$  in SA 68 and  $K_s = 15.25$  in Lynx 2. Sandage functions are fitted to the incompleteness with parameters,  $m_i = 15.25$ ,  $\Delta m_i = 0.80$  in SA 68, and  $m_i = 14.86$ ,  $\Delta m_i = 0.54$  in Lynx 2 (see text).

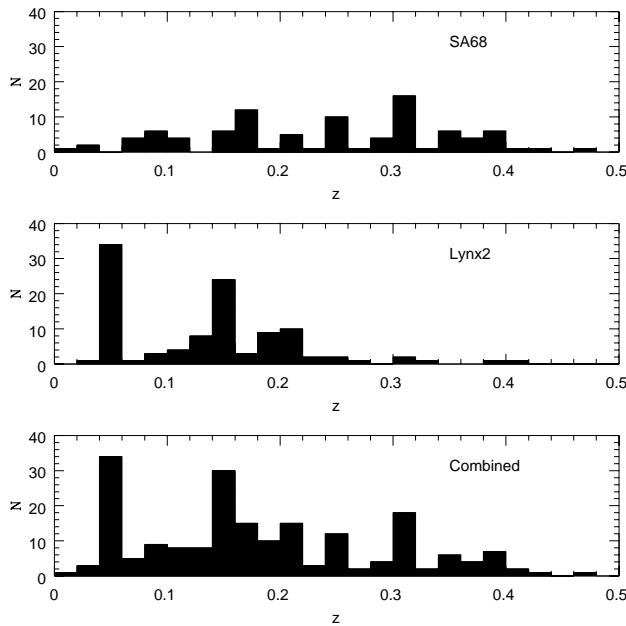


FIG. 6.—Redshift distribution of each sample of galaxies that were used in the luminosity function derivation. Two points are evident from these distributions. The majority of galaxies have redshifts  $z < 0.4$ , and the Lynx 2 field contains a low-redshift cluster at  $z = 0.05$ . The presence of significant structure in the redshift distribution requires the use of an estimator of the luminosity function that is not dependent on the clustering.

& Yahil 1979),  $[\exp(m - m_l/\Delta m) + 1]^{-1}$ , the incompleteness (defined as the change with magnitude of the ratio of the number of galaxies with measured redshift to the total number of galaxies to a given  $K_s$  limit), is calculated and fitted to this parametric form in Figure 5. We find  $m_l = 15.25$ ,  $\Delta m_l = 0.80$  for SA 68 and  $m_l = 14.86$ ,  $\Delta m_l = 0.54$  for Lynx 2. For the luminosity function analysis in this study, we select a redshift completeness limit of 30% in Figure 5. This corresponds to a limiting magnitude of  $K_s = 16$  and  $K_s = 15.25$  in the SA 68 and Lynx 2 fields, respectively. These will be used as the completeness limits in the following section to construct the near-infrared luminosity function. The redshift distributions for the complete sample, containing both the fields, are presented in Figure 6. There are a total of 110 galaxies in the two fields brighter than the above  $K_s$ -band magnitude limits in this survey. Assuming the estimated magnitude limits, a  $V/V_m$  test (Schmidt 1968) gives  $\langle V/V_m \rangle = 0.50 \pm 0.02$  and  $\langle V/V_m \rangle = 0.35 \pm 0.02$  for the SA 68 and Lynx 2 fields, respectively. The smaller than expected  $\langle V/V_m \rangle$  for the Lynx 2 field is likely to be due to a cluster at  $z \sim 0.05$  in this field (Fig. 6). The effect of this density enhancement on the IRLF will be explored in the next section. The redshift distribution in Figure 6 also shows that the galaxies in the infrared survey here are mainly local ( $z < 0.4$ ) objects.

## 7. LOCAL NEAR-INFRARED LUMINOSITY FUNCTION

Most determinations of the luminosity function assume a parametric form (normally a Schechter form) to fit to the observed data. The shape of the luminosity function is, however, likely to be type dependent or to be affected by density enhancements or its local environment. For these reasons, and because of the presence of a cluster at  $z = 0.05$  in the Lynx 2 field, we first use the nonparametric C-method (Lynden-Bell 1971) to assess the shape of the local near-ir

luminosity function. A parametric maximum likelihood method (Sandage et al. 1979), insensitive to density enhancement, will then be used to find the best fit to the data.

Using the near-infrared  $K$ -corrections from Glazebrook et al. (1995), the  $K$ -band luminosity function, estimated from the C-method, is shown in Figure 7. The uncertainties are estimated using bootstrap resampling simulations. Clearly, the shape of the local infrared luminosity function here is consistent with a Schechter form (Schechter 1976). A parametric fit to the data, using the cluster-free maximum likelihood method, gives  $M_{K_s}^* = -25.05 + 5 \log(H_0/50)$  and  $\alpha = -1.27$ . The correlated uncertainty contours at 68%, 90%, and 95% levels are estimated for  $M_{K_s}^*$  and  $\alpha$  and are presented in Figure 8. From these, we estimate  $3\sigma$  uncertainties corresponding to 0.3 mag and 0.2 in  $M_{K_s}^*$  and  $\alpha$ , respectively.

To explore the sensitivity of this result to the density enhancement in the Lynx 2 field, we also find the luminosity function using the “conventional” technique. This calculates the contribution from each galaxy to the volume covered by that galaxy at the apparent magnitude limit of the survey ( $1/V_{\max}$ ). The total contribution of galaxies in absolute magnitude intervals ( $\sum_{i=1}^n 1/V_{\max}^{(i)}$ ) is then estimated and compared with the result from the cluster-free C-method in Figure 7. A Schechter function fit to these data, also shown in Figure 7, gives  $M_{K_s}^* = -24.90$  mag,  $\alpha = -1.42$ , and  $\phi^* = 9.5 \times 10^{-4} \text{ Mpc}^{-3}$ . Within the uncertainties, this is similar to the parameters estimated from the cluster-free maximum likelihood method, which indicates that the presence of nonhomogeneities in our sample does not significantly affect the resulting luminosity function. Therefore, the parameters from the C-method/cluster-free fit here will be taken as the values for the local near-infrared luminosity function in this study.

The normalization of the luminosity function ( $\phi^*$  in the Schechter formalism), not given by the cluster-free

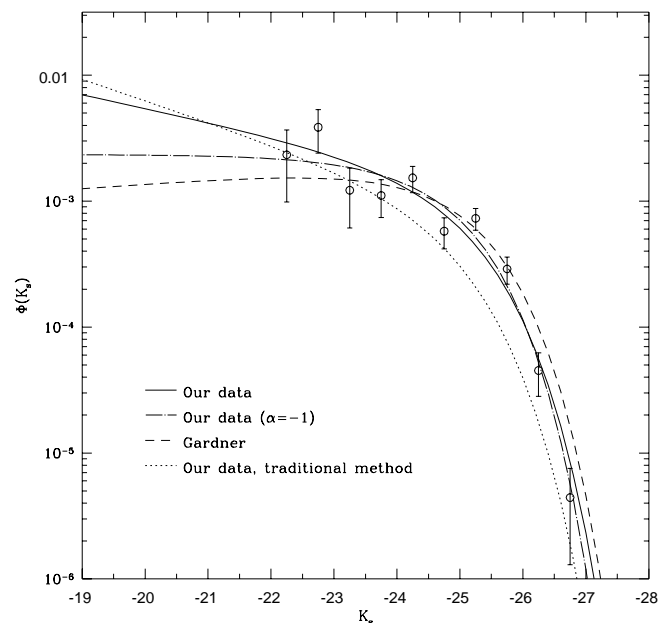


FIG. 7.—Differential luminosity function from our redshift sample. Error bars are calculated from the number of galaxies in each absolute magnitude bin, assuming Poisson statistics. The lines shown are for the Schechter functions fits (both with and without setting the parameter  $\alpha$  to  $-1$ ) as well as for previous determinations of the luminosity function.

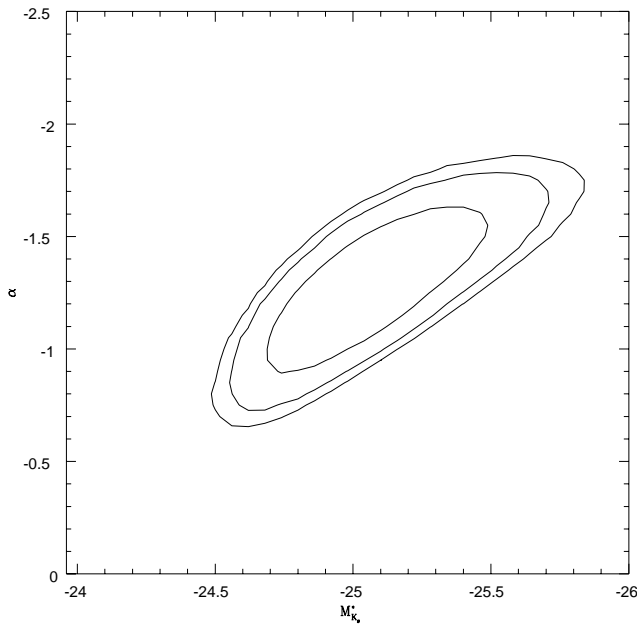


FIG. 8.—Confidence intervals for the Schechter parameters. The 68, 90, and 95 percentile confidence interval regions are shown derived from the maximum likelihood fitting techniques.

maximum likelihood technique, is estimated using three different methods. The first one is performing a  $\chi^2$  minimization of the Schechter function to the results from the C-method in Figure 7. The second method is using the  $\phi^*$  value estimated from the “conventional” technique, as presented above. The third method is employing our estimate of  $M_K^*$  and  $\alpha$  to establish a model of the  $K$ -band number counts and normalizing this to the observed counts in Figure 4. We adopt the normalization given by the C-method and estimate the uncertainty based on the variation in  $\phi^*$  derived by the three methods:  $\phi^* = (0.15 \pm 0.05) \times 10^{-2} (H_0/50)^3 \text{ Mpc}^{-3}$ .

The IRLFs in Figure 7 are compared with a similar study by Gardner et al. (1997). Their measured IRLF is based on a larger sample ( $\sim 500$  galaxies) but is less deep than the present survey (it is complete to only  $K \sim 15$  mag). Although both the bright end and normalizations agree fairly closely, the faint end of the IRLF in this study is significantly steeper. The reality of the steep faint-end slope for the local IRLF, found here, will be further investigated by measuring redshifts for the fainter galaxies in our sample, extending the completeness of our survey to  $K_s \sim 17$  mag.

In order to avoid the correlation between  $M_K^*$  and  $\alpha$  affecting the fit and to compare the present luminosity function with other independent studies, we fix  $\alpha = -1$  and estimate  $M_K^*$ . The local IRLFs, estimated by different

groups, are presented in Table 3. The characteristic magnitude ( $M_K^*$ ) here, is transformed from  $K_s$  to  $K$ , using the relation in § 5. Following Glazebrook et al. (1995), we apply a correction of  $+0.22$  mag to Mobasher et al. (1993)’s measurement to account for differences in  $K$ -corrections. Also, an aperture correction of  $-0.3$  mag is applied to Glazebrook et al. (1995) to convert it to the same scale as other measurements. All the estimates are corrected to  $H_0 = 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$ . It is clear from Table 3 that, at a given  $\alpha$ , the  $M_K^*$  values from different methods are in close agreement. The space density of local galaxies ( $\phi^*$ ) in this study is slightly smaller than other similar measurements ( $\sim 1.5$ ). This will be further explored by increasing the size of our sample, extending its completeness in redshift space.

The steep faint-end slope of the local IRLF, if confirmed, will have important implications toward constraining the models for formation of nearby, low-luminosity field galaxies (i.e., the mergers scenarios) since the IRLF is mainly sensitive to the mass function and not the star formation (young population) in galaxies. Also, this implies the existence of a large population of evolved, metal-rich galaxies in the local universe. The color distribution of the  $K$ -selected surveys shows that the faint blue galaxies start to contribute to the galaxy counts at about  $K \sim 18$  mag (Gardner 1995a, 1995b). Such near-infrared surveys will then reveal if the faint blue galaxies have an underlying population of old stars. The surveys selected in the  $K$  band are mainly dominated by normal massive galaxies. Therefore, the characteristic magnitude ( $M_K^*$ ) found for the IRLF here implies that the very red galaxies with  $M_K \sim -27$  mag (Egami, Hu, & Cowie 1996; Graham & Day 1996) have a space density of  $\leq 5 \times 10^{-5} \text{ Mpc}^{-3}$  and hence, are not likely to be local objects ( $z < 0.4$ ).

We are currently completing the redshift measurements for the fainter galaxies ( $K_s > 16$ ) in the present survey. This will be used to constrain further the faint-end slope of the “local” infrared luminosity function by improving the statistical significance of the sample and to explore its morphological type dependence.

## 8. CONCLUSIONS

In this study we carried out a wide-angle near-infrared galaxy survey in two fields, SA 68 and Lynx 2. The survey is complete to  $K_s = 16$  (SA 68) and  $K_s = 15.25$  (Lynx 2) and covers a total area of  $0.6 \text{ deg}^2$ . When we match the near-infrared detections with existing optical multicolor surveys, we derive a catalog of 867 galaxies. Of these, 175 have available redshifts. Employing the complete photometric survey, the near-infrared number-magnitude counts are estimated to  $K \sim 16.5$  mag and are found to be in agreement with other independent measurements.

Correcting the spectroscopic samples for incompleteness in redshift space, using selection functions in the form of

TABLE 3  
SCHECHTER PARAMETERS FOR NEAR-INFRARED LUMINOSITY FUNCTION

Study	$M_K^*$	$\alpha$	$\Phi^*$	$n$
This study (C-method) .....	-25.09	-1.27	$0.15 \times 10^{-2}$	110
This study (conventional method) .....	-24.94	-1.42	$0.95 \times 10^{-3}$	110
This study $\alpha = -1$ .....	-24.84	-1	$0.15 \times 10^{-2}$	110
Gardner et al. 1997 .....	-24.87	-1.03	$0.22 \times 10^{-2}$	532
Glazebrook et al. 1995 .....	-24.55	-1.04	$0.33 \times 10^{-2}$	98
Mobasher et al. 1993 .....	-24.88	-1	$0.14 \times 10^{-2}$	95



Fermi-Dirac distribution, the luminosity function has been derived for local galaxies. Applying a parametric Schechter fit, we find  $M_K^* = -25.09 \pm 0.3$ ,  $\alpha = -1.27 \pm 0.2$ , and  $\phi^* = (0.15 \pm 0.05) \times 10^{-2} \text{ Mpc}^{-3}$  (for  $H_0 = 50 \text{ km s}^{-1} \text{ Mpc}^{-1}$  and  $q_0 = 0.5$ ). When reduced to  $\alpha = -1$ , this agrees with other available estimates of the local IRLF.

The most important limitation of our survey is that the redshift survey is optically selected. Indeed, we see a systematic, color-dependent incompleteness at  $K_s > 14.5$  in the Lynx 2 field and  $K_s > 15$  in the SA 68. To estimate the effect of this approximation, we used the simulated catalogs produced by Gronwall & Koo (1993). We calculate the  $K$ -band luminosity function for an ideal, 100% complete,  $K$ -selected catalog and for an optically selected redshift catalog with a selection function somewhat more conservative than that of the KPGRS data ( $R < 18.5$ ). We found that the two calculated luminosity functions are identical, within the uncertainties, up to  $M_{K_s} = -22.5$ . For  $M_{K_s} > -21.5$ , the optically selected sample systematically overestimates the

amplitude of the luminosity function. We therefore limit our analysis to  $M_{K_s} = -22.5$  for the current data set.

The faint-end slope of the IRLF here is steeper than previous studies. This implies the presence of a population of faint but evolved (metal-rich) galaxies in the local universe. Comparison with the flat faint-end slope of the optical luminosity function reveals that this is unlikely to be the same population as the faint blue galaxies found in the optical surveys. The characteristic magnitude ( $M_K^*$ ) of the local IRLF indicates that the bright red galaxies ( $M_K \sim -27 \text{ mag}$ ) have a space density of  $\leq 5 \times 10^{-5} \text{ Mpc}^{-3}$  and, hence, are not likely to be local objects.

We thank Mark Dickinson and Alex Szalay for useful discussions about the analysis and interpretation of the near-infrared data. We are grateful to David Koo, Richard Kron, Jeffrey Munn, Steven Majewski, Matthew Bershad, and John Smetanka for prepublication access to the KPGRS catalogs.

#### REFERENCES

- Bershad, M. A. 1995, *AJ*, 109, 87  
 Bershad, M. A., Hereld, M., Kron, R. G., Koo, D. C., Munn, J. A., & Majewski, S. R. 1994, *AJ*, 108, 870  
 Bertin, E., & Arnouts, S. 1996, *A&AS*, 117, 393  
 Casali, M. M., & Hawarden, T. G. 1992, *JCMT-UKIRT Newsletter*, 4, 33  
 Connolly, A. J., Csabai, I., Szalay, A. S., Koo, D. C., Kron, R. G., & Munn, J. A. 1995, *AJ*, 110, 2655  
 Cowie, L. L., Hu, E. M., & Songaila, A. 1995, *Nature*, 377, 603  
 Cowie, L. L., Songaila, A., Hu, E. M., & Cohen, J. G. 1996, *AJ*, 112, 839  
 Efstathiou, G., Ellis, R. S., & Peterson, B. A. 1988, *MNRAS*, 232, 431  
 Egami, E., Hu, E., & Cowie, L. L. 1996, *ApJ*, 112, 73  
 Gardner, J. P. 1995a, *ApJ*, 452, 538  
 ———. 1995b, *ApJS*, 98, 441  
 ———. 1996, *MNRAS*, 279, 1157  
 Gardner, J. P., Cowie, L. L., & Wainscoat, R. J. 1993, *ApJ*, 415, L9  
 Gardner, J. P., Sharples, R. M., Carrasco, B. E., & Frenk, C. S. 1996, *MNRAS*, in press  
 Gardner, J. P., Sharples, R. M., Frenk, C. S., & Carrasco, B. E. 1997, *ApJ*, 480, L99  
 Gehrels, N. 1986, *ApJ*, 303, 336  
 Glazebrook, K., Peacock, J. A., Collins, C. A., & Miller, L. 1994, *MNRAS*, 266, 65  
 Glazebrook, K., Peacock, J. A., Miller, J. A., & Collins, C. A. 1995, *MNRAS*, 275, 169  
 Graham, J. R., & Day, A. 1996, *ApJ*, 471, 720  
 Gronwall, C., & Koo, D. C. 1993, *BAAS*, 182, 3002  
 Huang, J. S., & Cowie, L. L. 1998, in preparation  
 Huang, J. S., Cowie, L. L., Gardner, J. P., Hu, E. M., Songaila, A., & Wainscoat, R. J. 1997, *ApJ*, 476, 12  
 Jenker, H., Lasker, B. M., Sturch, C. R., McLean, B. J., Shara, M. M., & Russell, J. L. 1990, *AJ*, 99, 2082  
 Koo, D. C. 1986, *ApJ*, 311, 651  
 Kron, R. G. 1980, *ApJS*, 43, 305  
 Lasker, B. M., Sturch, C. R., McLean, B. J., Russell, J. L., Jenker, H., & Shara, M. M. 1990, *AJ*, 99, 2019  
 Lynden-Bell, D. 1971, *MNRAS*, 155, 95  
 Mobasher, B., Ellis, R. S., & Sharples, R. M. 1986, *MNRAS*, 223, 11  
 Mobasher, B., Sharples, R. M., & Ellis, R. S. 1993, *MNRAS*, 263, 560  
 Munn, J. A., Koo, D. C., Kron, R. G., Majewski, S. R., Bershad, M. A., & Smetanka, J. J. 1997, *ApJS*, 109, 45  
 Russell, J. L., Lasker, B. M., McLean, B. J., Sturch, C. R., & Jenker, H. 1990, *AJ*, 99, 2059  
 Sandage, A., Tammann, G. A., & Yahil, A. 1979, *ApJ*, 232, 352  
 Schechter, P. 1976, *ApJ*, 203, 297  
 Schmidt, M. 1968, *ApJ*, 151, 393  
 Sutherland, W., & Saunders, W. 1992, *MNRAS*, 259, 413  
 Trentham, N. 1997, *MNRAS*, 286, 133  
 Wainscoat, R. J., & Cowie, L. L. 1992, *AJ*, 103, 332.