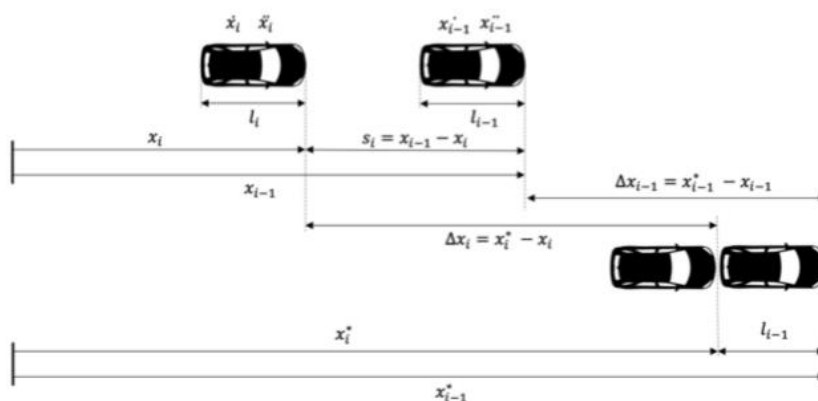


## 10.Gipps 推导

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有如下关系：

$$x_{i-1}^* - x_i \geq x_i^* - x_i + l_{i-1}$$

整理后可得

$$(x_{i-1}^* - x_{i-1}) + (x_{i-1} - x_i) \geq x_i^* - x_i + l_{i-1}$$

即：

$$\frac{v_{i-1}^2(t)}{2a_{i-1}} + s_i \geq \frac{v_i(t) + v_i(t + \tau)}{2} \tau_i + \frac{v_i^2(t + \tau)}{2a_i} + l_{i-1}$$

$$\frac{v_i^2(t + \tau)}{2a_i} + \frac{v_i(t + \tau)}{2} \tau_i - \left( \frac{v_{i-1}^2(t)}{2a_{i-1}} + s_i - l_{i-1} - \frac{v_i(t) \tau_i}{2} \right) \leq 0$$

解得

$$v_i(t + \tau_i) \leq -a_i \tau_i + \sqrt{a_i^2 \tau_i^2 + a_i (-v_i(t) \tau_i + \frac{v_{i-1}^2(t)}{2a_{i-1}} - 2l_{i-1} + 2s_i)}$$