

There are a huge number of solvers for non-linear least squares problems.

### ④ using Hessian

By doing a Taylor Series expansion of the Chi Squared test and finding the second term—the Hessian; that term could be used to evaluate the gradient of the gradient—that is the curvature of the Jacobian.

The Hessian would detect when the gradient of the function is zero—since the gradient of the gradient would near zero in those same locations. Could use Newton-Raphson to do this.

⇒ This approach would be faster than taking steps with the Jacobian (via steepest descent). Where the size of the step is proportional to the Hessian's gradient.

⚠ The problem with this method is that the Hessian as a proportionality constant for step size is too variadic/unstable when not in the vicinity of an extrema.

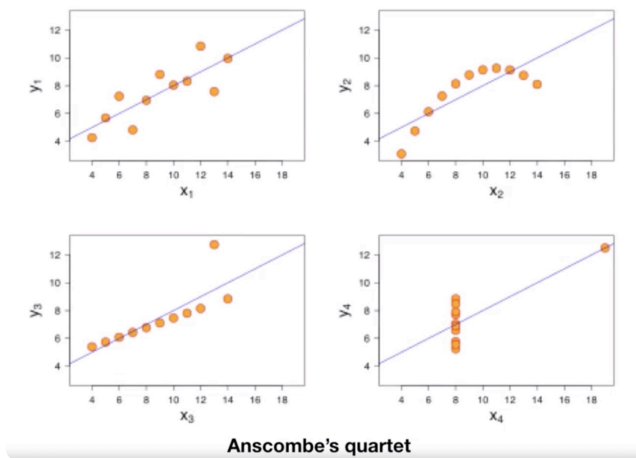
### ② Levenberg-Marquardt

- Uses steepest descent when far from the extrema
- then use Hessian closer to the extrema.  
if Chi Squared is getting better

### ③ Gauss-Newton, BFGS

- use Hessian's directly
- or - build up info about the Hessian iteratively
- ↳ depending on the convergence different methods are better

## Robust Fitting



Fitting methods which place less significance on outliers/flyer data points are called "robust".

One method more robust than Least Squares is taking the Absolute of the squared deviations.

(\*) Numerical Methods book.