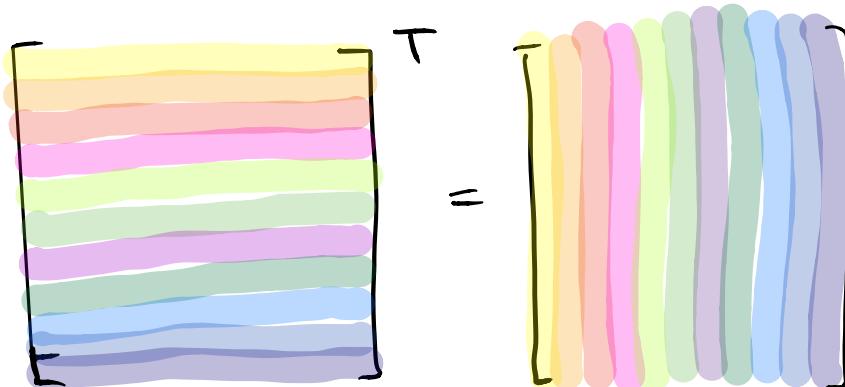


Whenever possible we want to use an orthonormal basis vector set when we transform our data.

- ↳ That is transformation matrix to be an orthogonal matrix.
- inverse is easy to compute.
- transformation is reversible; it doesn't collapse space.
- projection is just the dot product.

The transpose of a matrix is the interchange of columns for rows.

$$A_{ij}^T = A_{ji}$$



$$A^T A = \begin{matrix} & \text{[Diagonal entries 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 0]} \\ \text{[0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1]} \end{matrix} = I. \quad \left. \begin{array}{l} \text{When all vectors are perpendicular called orthonormal.} \\ a_i \cdot a_j = 0, \quad i \neq j \\ a_i \cdot a_i = 1, \quad i = j \end{array} \right\}$$

$$|A^T A| = \pm 1. \text{ (if inversion).}$$