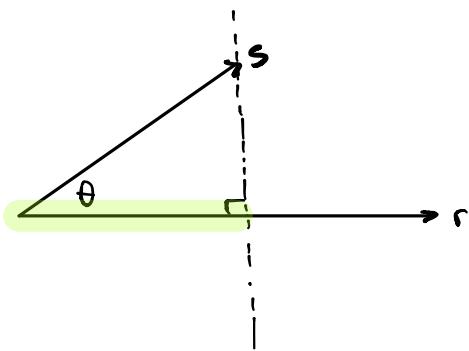


If you draw a triangle



$$\begin{aligned}\cos\theta &= \frac{\text{adj}}{\text{hyp}} \\ &= \frac{\text{adj}}{|s|} \\ &= \frac{(r \cdot s)}{|r|} \\ &= \frac{r \cdot s}{|r||s|}\end{aligned}$$

The proof illustrates that

$$adj = ls \cos\theta,$$

This equivalence can be found in the dot product; and be understood as representing adj.

• given $r \cdot s = |r||s| \cos \theta$

$$\text{and } \text{adj} = \text{hyp} \cos \theta \\ = 15 \cos 60^\circ \\ = \frac{r \cdot s}{|r|}$$

The scalar projection is,

$$\frac{r \cdot s}{|r|} = |s| \cos \theta$$

and is understood as the projection of one vector onto another.

In general the dot-product is also known as the projection product.

Vector projection is the projection of a vector onto another - multiplied by the normalized unit vector of the base ("r") vector.

$$\frac{\mathbf{r}}{|\mathbf{r}|} \times \frac{\mathbf{r} \cdot \mathbf{s}}{|\mathbf{r}|} = \frac{\mathbf{r}(\mathbf{r} \cdot \mathbf{s})}{|\mathbf{r}| |\mathbf{r}|}, \text{ the vector projection includes the scalar projection as a scalar multiplied by the unit vector of 'r'.$$

Takeaways,

1. size/modulus of a vector
 2. found the dot product
 3. found mathematical operations we can do
 - w - dot product
 - I. distributive over vector addition
 - II. associative over scalar multiplication
 - III. commutative

4. dot-product
Properties of dot product

 - I. finds the angle between two vectors
 - II. the relative directions of the vectors.