

Matrices these are objects that rotate and stretch vectors.

Imagine buying apples and bananas,

a: apples b: bananas

$$2a + 3b = 8$$

$$10a + 1b = 13$$

} each equation represents the cost of buying the respective amount of apples and bananas from independent stores.

Which price is more competitive?

↳ form of price discovery.

These linear equations can be represented by using a matrix,

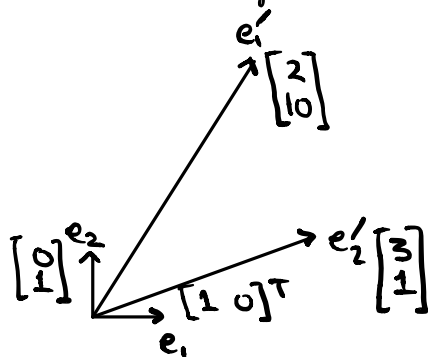
$$\begin{bmatrix} 2 & 3 \\ 10 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 8 \\ 13 \end{bmatrix}$$

2x2 matrix.

2x1 Column Matrix

Matrices transform vectors, for example  $e_1$ .

$$\begin{bmatrix} 2 & 3 \\ 10 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 \\ 10 \end{bmatrix}$$



The question is what vector is required to get  $\begin{bmatrix} 8 \\ 13 \end{bmatrix}$ ?

(\*) Matrices transform the basis vectors.

With the understanding of matrices, can see why Linear Algebra is named so,

- linear: takes input - then multiplies by constant values.
- algebra: a notation describing mathematical objects and a system of manipulating those notations.

- manipulating vectors in a space described by vectors

- relationship between simultaneous eq.s, matrices and vectors  
the key to solving simultaneous eq. is by how matrices transform vectors.