

What happens to summary statistics like the mean when the dataset is transformed - by scale or by shifting; how does our description of the dataset change when the dataset is linearly transformed?

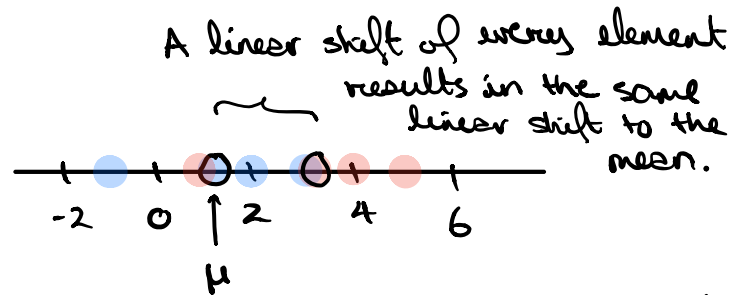
Example:

$$D = \{-1, 2, 3\}$$

$$E[D] = \frac{-1 + 2 + 3}{3} = 4/3$$

$$D' = \{-1+2, 2+2, 3+2\} = \{1, 4, 5\}$$

$$E[D'] = \frac{1 + 4 + 5}{3} = 10/3 = \frac{6}{3} + 4/3 = 2 + 4/3$$



- ◊ Blue is the original dataset
- ◊ Red is the shifted dataset

Generalized Expression of Mean with Shift.

$$E[D+a] = E[D] + E[a] = E[D] + a, \text{ where } a \text{ is a shift and } D \text{ is a dataset.}$$

Generalized Expression of Mean with Scaling

$$D'' = \{-1(2), 2(2), 3(2)\} = \{-2, 4, 6\}$$

$$E[D''] = \frac{-2 + 4 + 6}{3} = 8/3 = (4/3)2$$

$$E[\alpha D] = \alpha E[D].$$

□

Generalized Expression of Mean with Linear Transformations

$$E[\alpha D + a] = E[\alpha D] + E[a] = \alpha E[D] + a$$

Where α is the scale and a is the shift.