

There are a huge number of solvers for non-linear least squares problems.

### ① Using Hessian

By doing a Taylor Series expansion of the Chi Squared test and finding the second term - the Hessian; that term could be used to evaluate the gradient of the gradient - that is the curvature of the Jacobian.

The Hessian would detect when the gradient of the function is zero - since the gradient of the gradient would near zero in those same locations. Could use Newton-Raphson to do this.

- ⇒ This approach would be faster than taking steps with the Jacobian (viz steepest descent). Where the size of the step is proportional to the Hessian's gradient.
- ⇒ The problem with this method is that the Hessian as a proportionality constant for step size is too variadic/unstable when not in the vicinity of an extrema.

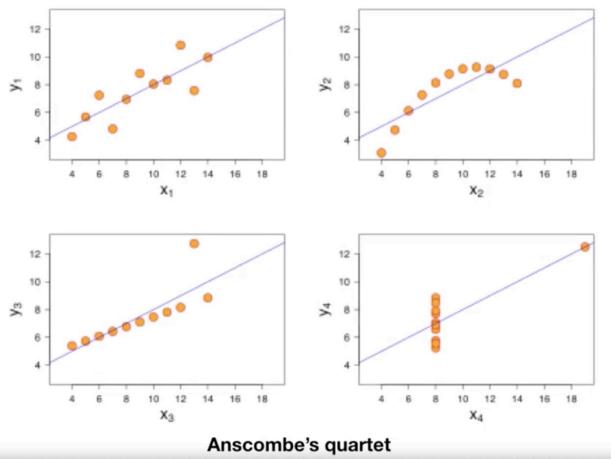
### ② Levenberg-Marguardt

- Uses steepest descent when far from the extrema
- then use Hessian closer to the extrema.  
if Chi Squared is getting better

### ③ Gauss-Newton, BFGS

- use Hessian's directly
- or - build up info about the Hessian iteratively
- depending on the convergence different methods are better

## Robust Fitting



Fitting methods which place less significance on outliers/flyer data points are called "robust".

One method more robust than Least Squares is taking the Absolute of the squared deviations.

(\*) Numerical Methods book.