

To explain dot products require linear transformation

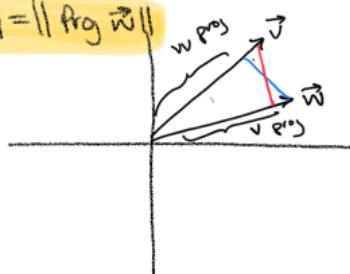
$$\begin{bmatrix} 2 \\ 4 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 0 \end{bmatrix} = 2 \cdot 1 + 4 \cdot 0 = 8$$

$$= (\text{length of projected } \vec{w}) \cdot (\text{length of } \vec{v})$$

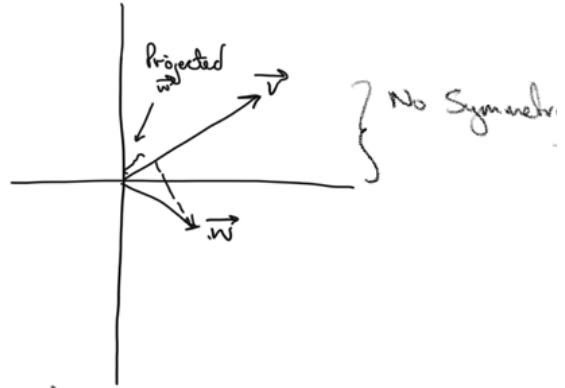
A Symmetrical approach.

$$\|\vec{v}\| = \|\vec{w}\|$$

$$\|\text{Proj } \vec{v}\| = \|\text{Proj } \vec{w}\|$$



A Projection,



Asymmetric Dot Products work because there is independence between the projection and the other asymmetric vector.

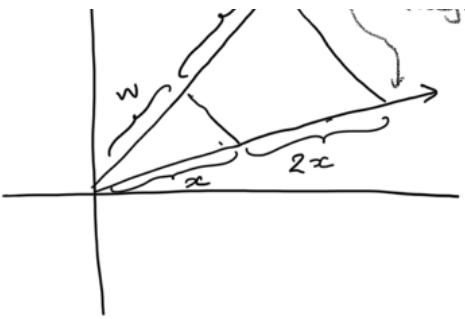
Therefore,

$$(2\vec{v}) \cdot \vec{w} = 2(\vec{v} \cdot \vec{w})$$

Asymmetry doesn't matter. You are either just scaling the projection or the vector which you are projecting on too which are equal.

Only when  
aligned,  $\vec{v} \parallel \vec{w}$   
 $2\vec{v} \parallel \vec{w}$        $\vec{v} \perp \vec{w}$   
                         $\rightarrow$  2x hypo  
                         $\rightarrow$  2x adj.

In this case the  $\vec{w}$  projection doesn't change length; although



Can do proof using perpendicular vectors because projection is 0.

the "vector" which it is projecting on to does. The effect is doubled.

Similarly, projecting a doubled vector  $\vec{v}$  onto the original vector is equal to doubling the original product.  $\rightarrow$  this is because the hypotenuse grows proportionally to the adjacent line segment.

## Reconciling Euclidean Distance Commutative Vector Projection

$$\begin{bmatrix} u_x & u_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = u_x \cdot x + u_y \cdot y$$

$$\begin{bmatrix} u_x \\ u_y \end{bmatrix} \cdot \begin{bmatrix} x \\ y \end{bmatrix} = u_x \cdot x + u_y \cdot y$$

THE DOT PRODUCT IS THE SAME AS APPLYING THE VECTOR AS A LINEAR TRANSFORMATION.

↳ The columns making up the vector are transformations of the original vector basis vectors.

## Point of Dot.

A geometric tool for

- understanding projections
- testing orientation

With more meaning, dotting is the collapse of a vector onto the real number line (of the original vector).