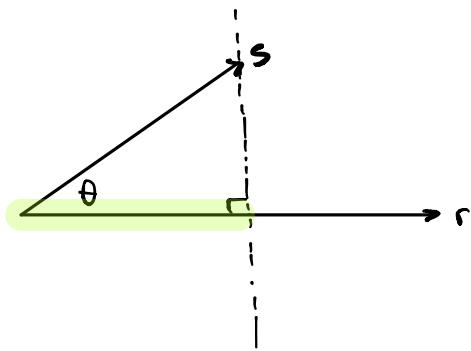


If you draw a triangle



$$\cos \theta = \frac{\text{adj}}{\text{hyp}}$$

$$= \frac{\text{adj}}{|s|}$$

$$= \frac{\left( \frac{r \cdot s}{|r|} \right)}{|s|}$$

$$= \frac{r \cdot s}{|r||s|}$$

The proof illustrates that

$$\text{adj} = |s| \cos \theta.$$

This equivalence can be found in the dot product and be understood as representing adj.

given  $\{ r \cdot s = |r||s| \cos \theta \}$   
and  $\text{adj} = \text{hyp} \cos \theta$   
 $= |s| \cos \theta$   
 $= \frac{r \cdot s}{|r|}$

The scalar projection is,

$$\frac{r \cdot s}{|r|} = |s| \cos \theta$$

and is understood as the projection of one vector onto another.

In general the dot-product is also known as the projection product.

Vector projection is the projection of a vector onto another - multiplied by the normalized unit vector of the base ("r") vector.

$$\frac{r}{|r|} \times \frac{r \cdot s}{|r|} = \frac{r(r \cdot s)}{|r||r|}, \text{ the vector projection includes the scalar projection as a scalar multiplied by the unit vector of 'r'}$$

$$= r \times \frac{(r \cdot s)}{r \cdot r}$$

Takeaways,

1. size/modulus of a vector

2. found the dot product

3. found mathematical operations we can do w- dot product

I. distributive over vector addition

II. associative over scalar multiplication

III. commutative

4. dot-product properties of dot product

I. finds the angle between two vectors

II. the relative directions of the vectors.