

1. Use Roster notation for

$$A = \{x \mid x^2 - 1 = 0\}$$

$$\text{r.n} \rightarrow \{-1, 1\}$$

$$B = \{x \mid (x-1)^2 = 0\}$$

$$\text{r.n} \rightarrow \{1\}$$

$$C = \{x \mid x + 8 = 9\}$$

$$\text{r.n} \rightarrow \{1\}$$

$$D = \{x \mid x^3 - 2x^2 + x = 2\}$$

$$\text{r.n} \rightarrow \{2, (x-2)\}$$

$$(x-2)$$

2.  $B \subseteq A$ ,  $B \subseteq C$ ,  $C \subseteq A$ ,  $C \subseteq A$

3. Prove  $A = B$ ,  $A = \{1, 3\}$ ,  $B = \{1, 2, 3\}$

$$\textcircled{1} \forall x \in A \rightarrow x \in B$$

$$\textcircled{2} A \neq B$$

Therefore  $A \subset B$  and  $A \not\subseteq B$ .

Prove  $A \subseteq B$ , where  $A = \{1, 3\}$  and  $B = \{1, 2, 3\}$ .

$$\textcircled{1} \forall x \in A \rightarrow x \in B \quad * \text{ whenever every element of } A \text{ also belongs to } B.$$

Disprove  $A \subseteq B$ ,

$$\textcircled{1} \forall x \in B \rightarrow x \in A$$

Prove  $1 \in A$ .

$$\textcircled{1} 1 \in B.$$

$$B \subseteq A$$

Therefore  $1 \in A$ , or  $B$  could not be a subset of  $A$ .

Disprove  $1 \subseteq A$ .

$A$  is a set,  $1$  is a number.

Subsets are not possible with numbers.

7. Prove the following,

$$\text{a) } \{a, a\} = \{a\}$$

$$\text{Let } A = \{a, a\}$$

$$\text{Let } B = \{a\}$$

$$|A| = |B| = |A \cup B|.$$

Sets are equal when every element from every set can be found in every other set.

$$\text{b) } \{a, b\} = \{b, a\}$$

$$\forall x \in B \rightarrow x \in A$$

$$\forall x \in A \rightarrow x \in B$$

$$\text{c) } \{a\} = \{b, c\}$$

$$A = \{a\}$$

$$B = \{b, c\}$$

$$\forall x \in A \rightarrow \exists y \in B, x = y$$

And vice-versa.

8. Commutative Laws:  $A \cup B = B \cup A$ ,  $A \cap B = B \cap A$

•  $A \cup B$ , is the result of combining elements in  $A$ ,  $B$  or in Both.

$$C = A \cup B \rightarrow \forall x \in C, x \in A \vee x \in B$$

$$\Leftrightarrow D = B \cup A \rightarrow \forall x \in D, x \in A \vee x \in B$$

$$\Leftrightarrow \forall z \in D \& \forall z \in C$$

• Associative Laws,  $A \cup (B \cap C) = (A \cup B) \cap C$

$$\forall x \in A \rightarrow x \in A \cup (B \cap C), x \in (A \cup B) \cap C$$

$$" \quad " \quad B \rightarrow "$$

$$" \quad " \quad C \rightarrow "$$

$$\forall x \notin A \vee B \vee C \rightarrow x \in A \cup (B \cap C), x \in (A \cup B) \cap C$$

• Distributive Laws,  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

$$\forall x \in A \text{ AND } (x \in B \text{ OR } x \in C) \rightarrow (x \in B \text{ OR } x \in C) \text{ AND } x \in A$$