

The variance of a dataset will increase when each element is multiplied by the same constant. The variance will increase proportionate to the square of that constant.

$$\mu = \frac{1}{N} \sum_{n=0}^N x_n$$

$$\mu_1 = \frac{1}{N} \sum_{n=0}^N c \cdot x_n$$

$$= \frac{c}{N} \sum_{n=0}^N (x_n - \mu)$$

$$\text{var}_1(x) = \frac{1}{N} \sum_{n=0}^N (cx_n - \mu_1)^2$$

$$= \frac{1}{N} \sum_{n=0}^N (cx_n - c \cdot \mu)^2$$

$$= \frac{1}{N} \sum_{n=0}^N [c \cdot (x_n - \mu)]^2$$

$$= \frac{1}{N} \sum_{n=0}^N [c^2 \cdot (x_n - \mu)^2]$$

$$= \frac{c^2}{N} \sum_{n=0}^N (x_n - \mu)^2$$

$$= c^2 \text{ var } X.$$

