What is the motivation/reason behind using sigma algebra? What properties does it lend that other types of algebra of sets do not lend?

Why is this applicable to probability spaces and measurable spaces?

What _is_ a random variable??