```
#include<iostream>
#include<omp.h>
#include<bits/stdc++.h>
using namespace std;
class Graph{
  public:
    // vector<vector<int>> graph;
    // vector<bool> visited;
    // int vertices = 0;
    // int edges = 0;
    int vertices = 6;
    int edges = 5;
    vector<vector<int>> graph = {{1},{0,2,3},{1,4,5},{1,4},{2,3},{2}};
    vector<bool> visited;
    // Graph(){
    // cout << "Enter number of nodes: ";
    // cin >> vertices;
    // cout << "Enter number of edges: ";
    // cin >> edges;
    // graph.assign(vertices, vector < int > ());
    // for(int i = 0; i < edges;i++){
    //
          int a,b;
    //
           cout << "Enter adjacent nodes: ";
    //
           cin >> a >> b;
    //
           addEdge(a,b);
    // }
    //}
    void addEdge(int a, int b){
      graph[a].push_back(b);
      graph[b].push_back(a);
    }
    void printGraph(){
      for(int i = 0; i < vertices; i++){
         cout << i << " -> ";
         for(auto j = graph[i].begin(); j != graph[i].end();j++){
```

```
cout << *j << " ";
     }
     cout << endl;
  }
}
void initialize_visited(){
  visited.assign(vertices,false);
}
void dfs(int i){
  stack<int> s;
  s.push(i);
  visited[i] = true;
  while(s.empty() != true){
     int current = s.top();
     cout << current << " ";
     s.pop();
     for(auto j = graph[current].begin(); j != graph[current].end();j++){
       if(visited[*j] == false){
         s.push(*j);
         visited[*j] = true;
       }
     }
  }
}
void parallel_dfs(int i){
  stack<int> s;
  s.push(i);
  visited[i] = true;
  while(s.empty() != true){
     int current = s.top();
    cout << current << " ";</pre>
     #pragma omp critical
       s.pop();
     #pragma omp parallel for
       for(auto j = graph[current].begin(); j != graph[current].end();j++){
```

```
if(visited[*j] == false){
            #pragma omp critical
            {
              s.push(*j);
              visited[*j] = true;
           }
         }
       }
  }
}
void bfs(int i){
  queue<int> q;
  q.push(i);
  visited[i] = true;
  while(q.empty() != true){
    int current = q.front();
    q.pop();
    cout << current << " ";</pre>
    for(auto j = graph[current].begin(); j != graph[current].end();j++){
       if(visited[*j] == false){
         q.push(*j);
         visited[*j] = true;
       }
    }
  }
}
void parallel_bfs(int i){
  queue<int> q;
  q.push(i);
  visited[i] = true;
  while(q.empty() != true){
       int current = q.front();
       cout << current << " ";
       #pragma omp critical
         q.pop();
```

```
#pragma omp parallel for
           for(auto j = graph[current].begin(); j != graph[current].end();j++){
              if(visited[*j] == false){
                #pragma omp critical
                  q.push(*j);
                  visited[*j] = true;
             }
           }
      }
    }
};
int main(int argc, char const *argv[])
{
  Graph g;
  cout << "Adjacency List:\n";</pre>
  g.printGraph();
  g.initialize visited();
  cout << "Depth First Search: \n";</pre>
  auto start = chrono::high_resolution_clock::now();
  g.dfs(0);
  cout << endl;
  auto end = chrono::high resolution clock::now();
  cout << "Time taken: " << chrono::duration cast<chrono::microseconds>(end - start).count() <<
" microseconds" << endl;
  cout << "Parallel Depth First Search: \n";</pre>
  g.initialize_visited();
  start = chrono::high_resolution_clock::now();
  g.parallel dfs(0);
  cout << endl;
  end = chrono::high_resolution_clock::now();
  cout << "Time taken: "<< chrono::duration cast<chrono::microseconds>(end - start).count() << "
microseconds" << endl;
  start = chrono::high_resolution_clock::now();
  cout << "Breadth First Search: \n";</pre>
  g.initialize_visited();
  g.bfs(0);
  cout << endl;
  end = chrono::high_resolution_clock::now();
```

```
cout << "Time taken: "<< chrono::duration_cast<chrono::microseconds>(end - start).count() << "
microseconds" << endl;
start = chrono::high_resolution_clock::now();
cout << "Parallel Breadth First Search: \n";
g.initialize_visited();
g.parallel_bfs(0);
cout << endl;
end = chrono::high_resolution_clock::now();
cout << "Time taken: " << chrono::duration_cast<chrono::microseconds>(end - start).count() << "
microseconds" << endl;
return 0;
}</pre>
```

#### OUTPUT

Adjacency List:

0 -> 1

1 -> 0 2 3

2 -> 1 4 5

3 -> 1 4

4 -> 2 3

5 -> 2

Depth First Search:

013425

Time taken: 1000 microseconds

Parallel Depth First Search:

013425

Time taken: 1997 microseconds

Breadth First Search:

012345

Time taken: 999 microseconds

Parallel Breadth First Search:

 $0\,1\,3\,2\,4\,5$ 

Time taken: 1990 microseconds

# **Basic classification: Classify images of clothing**

```
In [1]: # TensorFlow and tf.keras
import tensorflow as tf

# Helper libraries
import numpy as np
import matplotlib.pyplot as plt

print(tf.__version__)
```

2.11.0

# Import the Fashion MNIST dataset

This guide uses the <u>Fashion MNIST (https://github.com/zalandoresearch/fashion-mnist)</u> dataset which contains 70,000 grayscale images in 10 categories. The images show individual articles of clothing at low resolution (28 by 28 pixels), as seen here:

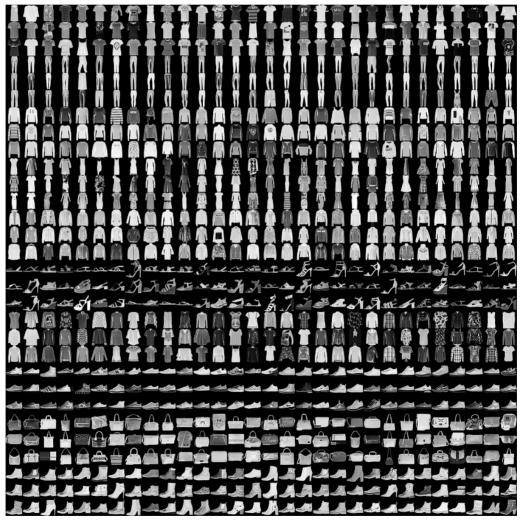


Figure 1. Fashion-MNIST samples (https://github.com/zalandoresearch/fashion-mnist) (by Zalando, MIT License).

Fashion MNIST is intended as a drop-in replacement for the classic MNIST (http://yann.lecun.com/exdb/mnist/) dataset—often used as the "Hello, World" of machine learning programs for computer vision. The MNIST dataset contains images of handwritten digits (0, 1, 2, etc.) in a format identical to that of the articles of clothing you'll use here.

This guide uses Fashion MNIST for variety, and because it's a slightly more challenging problem than regular MNIST. Both datasets are relatively small and are used to verify that an algorithm works as expected. They're good starting points to test and debug code.

Here, 60,000 images are used to train the network and 10,000 images to evaluate how accurately the network learned to

Loading the dataset returns four NumPy arrays:

- The train\_images and train\_labels arrays are the training set—the data the model uses to learn.
- The model is tested against the test set, the test\_images, and test\_labels arrays.

The images are 28x28 NumPy arrays, with pixel values ranging from 0 to 255. The *labels* are an array of integers, ranging from 0 to 9. These correspond to the *class* of clothing the image represents:

Class	Label		
T-shirt/top	0		
Trouse	1		
Pullove	2		
Dress	3		
Coa	4		
Sanda	5		
Shir	6		
Sneake	7		
Вад	8		
Ankle boo	9		

Each image is mapped to a single label. Since the *class names* are not included with the dataset, store them here to use later when plotting the images:

# **Explore the data**

Let's explore the format of the dataset before training the model. The following shows there are 60,000 images in the training set, with each image represented as 28 x 28 pixels:

```
In [4]: train_images.shape
Out[4]: (60000, 28, 28)

Likewise, there are 60,000 labels in the training set:
```

```
In [5]: len(train_labels)
Out[5]: 60000
```

Each label is an integer between 0 and 9:

```
In [6]: train_labels
Out[6]: array([9, 0, 0, ..., 3, 0, 5], dtype=uint8)
```

There are 10,000 images in the test set. Again, each image is represented as 28 x 28 pixels:

```
In [7]: test_images.shape
Out[7]: (10000, 28, 28)
```

And the test set contains 10,000 images labels:

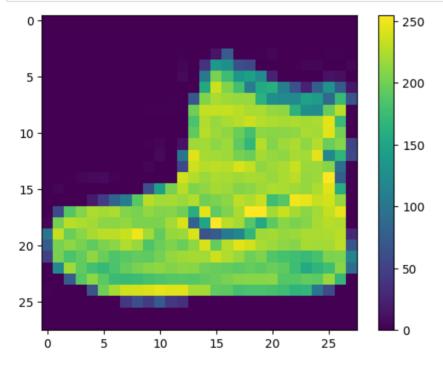
```
In [8]: len(test_labels)
```

Out[8]: 10000

# Preprocess the data

The data must be preprocessed before training the network. If you inspect the first image in the training set, you will see that the pixel values fall in the range of 0 to 255:

```
In [9]: plt.figure()
   plt.imshow(train_images[0])
   plt.colorbar()
   plt.grid(False)
   plt.show()
```



Scale these values to a range of 0 to 1 before feeding them to the neural network model. To do so, divide the values by 255. It's important that the *training set* and the *testing set* be preprocessed in the same way:

```
In [10]: train_images = train_images / 255.0
test_images = test_images / 255.0
```

To verify that the data is in the correct format and that you're ready to build and train the network, let's display the first 25 images from the *training set* and display the class name below each image.

```
In [11]: plt.figure(figsize=(10,10))
    for i in range(25):
        plt.subplot(5,5,i+1)
        plt.xticks([])
        plt.yticks([])
        plt.grid(False)
        plt.imshow(train_images[i], cmap=plt.cm.binary)
        plt.xlabel(class_names[train_labels[i]])
    plt.show()
```



## **Build the model**

Building the neural network requires configuring the layers of the model, then compiling the model.

## Set up the layers

The basic building block of a neural network is the <u>layer (https://www.tensorflow.org/api\_docs/python/tf/keras/layers)</u>. Layers extract representations from the data fed into them. Hopefully, these representations are meaningful for the problem at hand.

 $Most\ of\ deep\ learning\ consists\ of\ chaining\ together\ simple\ layers.\ Most\ layers,\ such\ as\ tf.keras.layers.Dense\ ,$ 

```
In [12]: model = tf.keras.Sequential([
    tf.keras.layers.Flatten(input_shape=(28, 28)),
    tf.keras.layers.Dense(128, activation='relu'),
    tf.keras.layers.Dense(10)
])
```

The first layer in this network, tf.keras.layers.Flatten, transforms the format of the images from a two-dimensional array (of 28 by 28 pixels) to a one-dimensional array (of 28 \* 28 = 784 pixels). Think of this layer as unstacking rows of pixels in the image and lining them up. This layer has no parameters to learn; it only reformats the data.

After the pixels are flattened, the network consists of a sequence of two tf.keras.layers.Dense layers. These are densely connected, or fully connected, neural layers. The first Dense layer has 128 nodes (or neurons). The second (and last) layer returns a logits array with length of 10. Each node contains a score that indicates the current image belongs to one of the 10 classes.

#### Compile the model

Before the model is ready for training, it needs a few more settings. These are added during the model's <u>compile</u> (<a href="https://www.tensorflow.org/api\_docs/python/tf/keras/Model#compile">https://www.tensorflow.org/api\_docs/python/tf/keras/Model#compile</a>) step:

- <u>Loss function (https://www.tensorflow.org/api\_docs/python/tf/keras/losses)</u>.—This measures how accurate the model is during training. You want to minimize this function to "steer" the model in the right direction.
- Optimizer (https://www.tensorflow.org/api\_docs/python/tf/keras/optimizers) —This is how the model is updated based on the data it sees and its loss function.
- <u>Metrics (https://www.tensorflow.org/api\_docs/python/tf/keras/metrics)</u> —Used to monitor the training and testing steps. The following example uses *accuracy*, the fraction of the images that are correctly classified.

## Train the model

Training the neural network model requires the following steps:

- 1. Feed the training data to the model. In this example, the training data is in the train\_images and train\_labels arrays.
- 2. The model learns to associate images and labels.
- 3. You ask the model to make predictions about a test set—in this example, the test\_images array.
- 4. Verify that the predictions match the labels from the test\_labels array.

#### Feed the model

To start training, call the <a href="model.fit\_(https://www.tensorflow.org/api\_docs/python/tf/keras/Model#fit">model.fit\_(https://www.tensorflow.org/api\_docs/python/tf/keras/Model#fit)</a> method—so called because it "fits" the model to the training data:

Out[14]: <keras.callbacks.History at 0x7f326fff3370>

As the model trains, the loss and accuracy metrics are displayed. This model reaches an accuracy of about 0.91 (or 91%) on the training data.

#### **Evaluate accuracy**

Next, compare how the model performs on the test dataset:

It turns out that the accuracy on the test dataset is a little less than the accuracy on the training dataset. This gap between training accuracy and test accuracy represents *overfitting*. Overfitting happens when a machine learning model performs worse on new, previously unseen inputs than it does on the training data. An overfitted model "memorizes" the noise and details in the training dataset to a point where it negatively impacts the performance of the model on the new data. For more information, see the following:

- Demonstrate overfitting (https://www.tensorflow.org/tutorials/keras/overfit\_and\_underfit#demonstrate\_overfitting)
- <u>Strategies to prevent overfitting</u> (<a href="https://www.tensorflow.org/tutorials/keras/overfit\_and\_underfit#strategies\_to\_prevent\_overfitting">https://www.tensorflow.org/tutorials/keras/overfit\_and\_underfit#strategies\_to\_prevent\_overfitting</a>)

#### Make predictions

With the model trained, you can use it to make predictions about some images. Attach a softmax layer to convert the model's linear outputs—<u>logits (https://developers.google.com/machine-learning/glossary#logits)</u>—to probabilities, which should be easier to interpret.

Here, the model has predicted the label for each image in the testing set. Let's take a look at the first prediction:

A prediction is an array of 10 numbers. They represent the model's "confidence" that the image corresponds to each of the 10 different articles of clothing. You can see which label has the highest confidence value:

```
In [19]: np.argmax(predictions[0])
Out[19]: 9
```

So, the model is most confident that this image is an ankle boot, or class\_names[9]. Examining the test label shows that this classification is correct:

```
In [20]: test_labels[0]
Out[20]: 9
```

Graph this to look at the full set of 10 class predictions.

```
In [21]: | def plot_image(i, predictions_array, true_label, img):
           true_label, img = true_label[i], img[i]
           plt.grid(False)
           plt.xticks([])
           plt.yticks([])
           plt.imshow(img, cmap=plt.cm.binary)
           predicted_label = np.argmax(predictions_array)
           if predicted_label == true_label:
             color = 'blue'
           else:
             color = 'red'
           plt.xlabel("{} {:2.0f}% ({})".format(class_names[predicted_label],
                                          100*np.max(predictions_array),
                                          class_names[true_label]),
                                          color=color)
         def plot_value_array(i, predictions_array, true_label):
           true_label = true_label[i]
           plt.grid(False)
           plt.xticks(range(10))
           plt.yticks([])
           thisplot = plt.bar(range(10), predictions_array, color="#777777")
           plt.ylim([0, 1])
           predicted_label = np.argmax(predictions_array)
           thisplot[predicted_label].set_color('red')
           thisplot[true_label].set_color('blue')
```

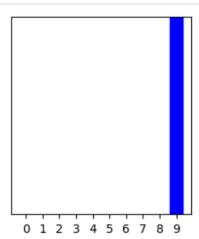
## **Verify predictions**

With the model trained, you can use it to make predictions about some images.

Let's look at the 0th image, predictions, and prediction array. Correct prediction labels are blue and incorrect prediction labels are red. The number gives the percentage (out of 100) for the predicted label.

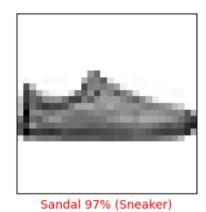
```
In [22]: i = 0
plt.figure(figsize=(6,3))
plt.subplot(1,2,1)
plot_image(i, predictions[i], test_labels, test_images)
plt.subplot(1,2,2)
plot_value_array(i, predictions[i], test_labels)
plt.show()
```

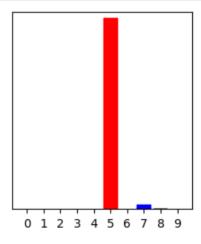




Ankle boot 100% (Ankle boot)

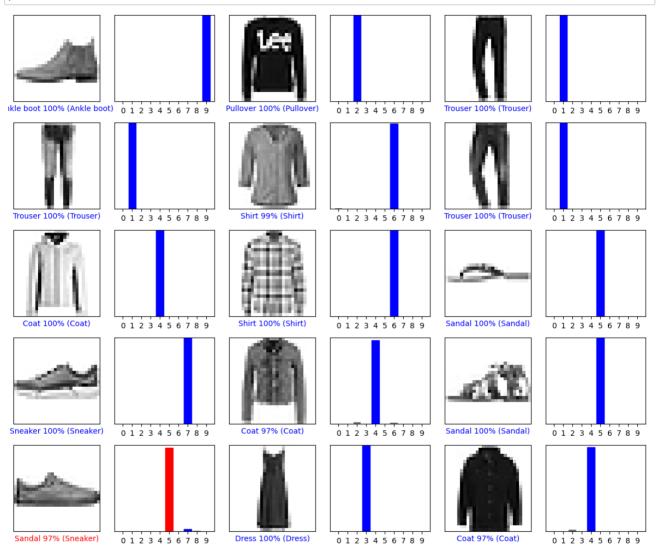
```
In [23]: i = 12
    plt.figure(figsize=(6,3))
    plt.subplot(1,2,1)
    plot_image(i, predictions[i], test_labels, test_images)
    plt.subplot(1,2,2)
    plot_value_array(i, predictions[i], test_labels)
    plt.show()
```





Let's plot several images with their predictions. Note that the model can be wrong even when very confident.

```
In [24]: # Plot the first X test images, their predicted labels, and the true labels.
# Color correct predictions in blue and incorrect predictions in red.
num_rows = 5
num_cols = 3
num_images = num_rows*num_cols
plt.figure(figsize=(2*2*num_cols, 2*num_rows))
for i in range(num_images):
    plt.subplot(num_rows, 2*num_cols, 2*i+1)
    plot_image(i, predictions[i], test_labels, test_images)
    plt.subplot(num_rows, 2*num_cols, 2*i+2)
    plot_value_array(i, predictions[i], test_labels)
plt.tight_layout()
plt.show()
```



#### Use the trained model

Finally, use the trained model to make a prediction about a single image.

```
In [25]: # Grab an image from the test dataset.
img = test_images[1]
print(img.shape)

(28, 28)
```

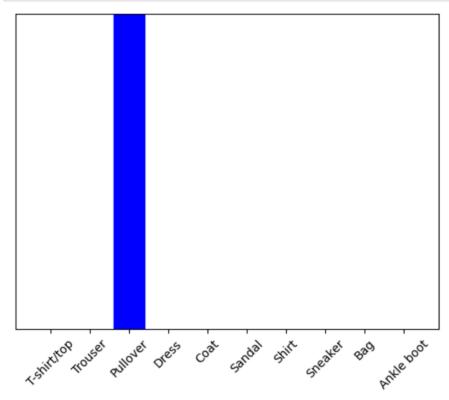
tf.keras models are optimized to make predictions on a *batch*, or collection, of examples at once. Accordingly, even though you're using a single image, you need to add it to a list:

```
In [26]: # Add the image to a batch where it's the only member.
img = (np.expand_dims(img,0))
print(img.shape)

(1, 28, 28)
```

Now predict the correct label for this image:

```
In [28]: plot_value_array(1, predictions_single[0], test_labels)
    _ = plt.xticks(range(10), class_names, rotation=45)
    plt.show()
```



tf.keras.Model.predict returns a list of lists—one list for each image in the batch of data. Grab the predictions for our (only) image in the batch:

```
In [29]: np.argmax(predictions_single[0])
```

Out[29]: 2

And the model predicts a label as expected.

# 1. Problem statement

**Recurrent neural network (RNN)** Use the Google stock prices dataset and design a time series analysis and prediction system using RNN.

- We are given Google stock price from 01/2012 to 12/2017.
- The task is to predict the trend of the stock price for 01-06 2018.

# 2. Import library

```
In [1]: import numpy as np
    import matplotlib.pyplot as plt
    import pandas as pd
    from sklearn.preprocessing import MinMaxScaler
    from tensorflow.keras.models import Sequential
    from tensorflow.keras.layers import LSTM
    from tensorflow.keras.layers import Dense
    from tensorflow.keras.layers import Dropout
```

# 3. Data Collection

## 3.0 import the data

```
In [2]: dataset_train = pd.read_csv('Google_Stock_Price_Train.csv')
In [3]: dataset_train.head()
                Date Open
                              High
                                    Low Close
                                                     Volume
Out[3]:
        0 01/03/2012 325.25 332.83 324.97 663.59
                                                   7,380,500
        1 01/04/2012 331.27 333.87 329.08 666.45
                                                    5,749,400
        2 01/05/2012 329.83 330.75 326.89 657.21
                                                   6,590,300
        3 01/06/2012 328.34 328.77 323.68 648.24
                                                    5,405,900
        4 01/09/2012 322.04 322.29 309.46 620.76 11,688,800
In [4]: #keras only takes numpy array
        training_set = dataset_train.iloc[:, 1: 2].values
In [5]: training_set.shape
Out[5]: (1509, 1)
        3.1 Feature scaling
```

```
In [6]: sc = MinMaxScaler(feature_range = (0, 1))
#fit: get min/max of train data
training_set_scaled = sc.fit_transform(training_set)
```

# 3.2 Data structure creation

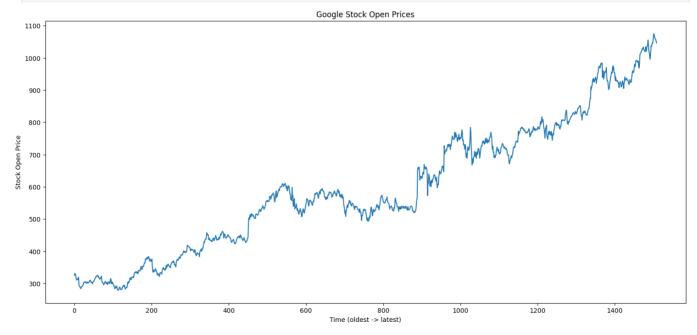
- taking the reference of past 60 days of data to predict the future stock price.
- It is observed that taking 60 days of past data gives us best results.
- In this data set 60 days of data means 3 months of data.
- · Every month as 20 days of Stock price.
- X train will have data of 60 days prior to our date and y train will have data of one day after our date

- 1. Number of stock prices 1449
- 2. Number of time steps 60
- 3. Number of Indicator 1

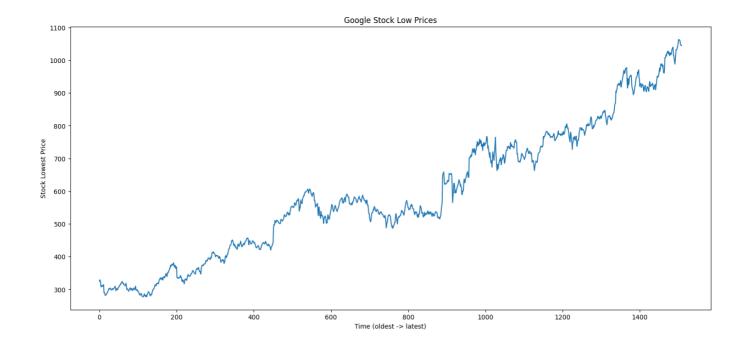
```
In [11]: X_train.shape
Out[11]: (1449, 60, 1)
```

# 4. Exploratory Data Analysis

```
In [12]:
    plt.figure(figsize=(18, 8))
    plt.plot(dataset_train['Open'])
    plt.title("Google Stock Open Prices")
    plt.xlabel("Time (oldest -> latest)")
    plt.ylabel("Stock Open Price")
    plt.show()
```



```
In [13]: plt.figure(figsize=(18, 8))
    plt.plot(dataset_train['Low'])
    plt.title("Google Stock Low Prices")
    plt.xlabel("Time (oldest -> latest)")
    plt.ylabel("Stock Lowest Price")
    plt.show()
```



# 5. Create & Fit Model

## 5.1 Create model

```
In [14]: regressor = Sequential()
         #add 1st lstm layer
         regressor.add(LSTM(units = 50, return_sequences = True, input_shape = (X_train.shape[1], 1)))
         regressor.add(Dropout(rate = 0.2))
         ##add 2nd lstm layer: 50 neurons
         regressor.add(LSTM(units = 50, return_sequences = True))
         regressor.add(Dropout(rate = 0.2))
         ##add 3rd Lstm Layer
         regressor.add(LSTM(units = 50, return_sequences = True))
         regressor.add(Dropout(rate = 0.2))
         ##add 4th Lstm Layer
         regressor.add(LSTM(units = 50, return_sequences = False))
         regressor.add(Dropout(rate = 0.2))
         ##add output Layer
         regressor.add(Dense(units = 1))
In [15]: regressor.compile(optimizer = 'adam', loss = 'mean_squared_error')
```

# 5.2 Model fit

# 6. Model evaluation

#### 6.1 Read and convert

```
In [17]: dataset_test = pd.read_csv('Google_Stock_Price_Test.csv')
In [18]: dataset_test.head()
Out[18]:
                 Date
                                                                 Close
                                                                         Volume
                             Open
                                          High
                                                      Low
         0 02/01/2018 1048.339966
                                   1066.939941 1045.229980
                                                           1065.000000
                                                                        1237600
         1 03/01/2018 1064.310059
                                   1086.290039
                                               1063.209961
                                                            1082.479980
                                                                        1430200
         2 04/01/2018 1088.000000
                                   1093.569946
                                               1084.001953 1086.400024 1004600
         3 05/01/2018 1094.000000
                                   1104.250000
                                               1092.000000
                                                           1102.229980 1279100
         4 08/01/2018 1102.229980
                                   1111.270020 1101.619995 1106.939941 1047600
In [19]: #keras only takes numpy array
         real_stock_price = dataset_test.iloc[:, 1: 2].values
         real stock price.shape
Out[19]: (125, 1)
         6.2 Concat and convert
In [20]: #vertical concat use 0, horizontal uses 1
         dataset_total = pd.concat((dataset_train['Open'], dataset_test['Open']),
                                   axis = 0
         ##use .values to make numpy array
         inputs = dataset_total[len(dataset_total) - len(dataset_test) - 60:].values
         6.3 Reshape and scale
In [21]: #reshape data to only have 1 col
         inputs = inputs.reshape(-1, 1)
         #scale input
         inputs = sc.transform(inputs)
```

#### 6.4 Create test data strucutre

In [22]: len(inputs)

Out[22]: 185

# 7. Model prediction

```
In [25]: predicted_stock_price = regressor.predict(X_test)

4/4 [=========] - 1s 26ms/step

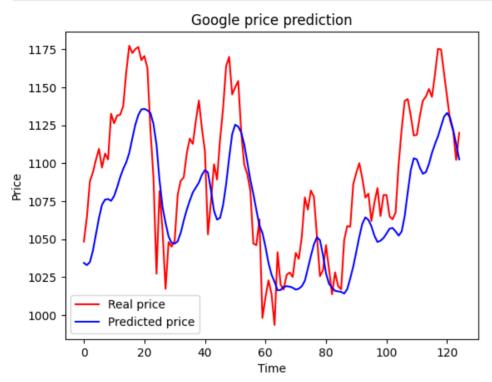
In [26]: #inverse the scaled value
    predicted_stock_price = sc.inverse_transform(predicted_stock_price)
```

## 7.1 Result visualization

```
In [27]: ##visualize the prediction and real price
plt.plot(real_stock_price, color = 'red', label = 'Real price')
```

```
plt.plot(predicted_stock_price, color = 'blue', label = 'Predicted price')

plt.title('Google price prediction')
plt.xlabel('Time')
plt.ylabel('Price')
plt.legend()
plt.show()
```



# **Import Library**

```
In [1]: # Data analysis and visualization
   import tensorflow as tf
   import numpy as np
   import pandas as pd
   import matplotlib.pyplot as plt
   %matplotlib inline

# Preprocessing and evaluation
   from sklearn.model_selection import train_test_split
   from sklearn.compose import make_column_transformer
   from sklearn.preprocessing import MinMaxScaler
```

# Load Data

# **Exploratory Data Analysis**

## Initial Observation

# View summary of datasets

X\_train\_df.info()

```
In [3]: # Checking the data shape and type
         (X_train.shape, type(X_train)), (X_test.shape, type(X_test)), (y_train.shape, type(y_train)), (y_test.shape, type(X_test))
Out[3]: (((404, 13), numpy.ndarray),
          ((102, 13), numpy.ndarray),
          ((404,), numpy.ndarray),
          ((102,), numpy.ndarray))
In [4]: # Converting Data to DataFrame
         X_train_df = pd.DataFrame(X_train)
         y_train_df = pd.DataFrame(y_train)
         # Preview the training data
         X_train_df.head(10)
                            2
                                                                         10
                                                                                       12
Out[4]:
         0 0.09178
                     0.0
                          4.05 0.0 0.510 6.416 84.1 2.6463
                                                             5.0 296.0 16.6
                                                                             395.50
                                                                                     9.04
         1 0.05644 40.0
                          6.41 1.0 0.447 6.758 32.9 4.0776
                                                             4.0
                                                                  254.0 17.6
                                                                             396.90
         2 0.10574
                     0.0
                        27.74 0.0
                                  0.609 5.983 98.8
                                                    1.8681
                                                              4.0 711.0 20.1
                                                                             390.11
                                                                                    18.07
         3 0.09164
                     0.0
                        10.81 0.0
                                   0.413 6.065
                                                 7.8 5.2873
                                                              4.0
                                                                  305.0 19.2 390.91
                                                                                     5.52
         4 5 09017
                     0.0
                        18.10 0.0 0.713 6.297 91.8 2.3682 24.0 666.0 20.2 385.09 17.27
                                  0.437 6.279 74.5 4.0522
         5 0.10153
                     0.0
                        12.83 0.0
                                                             5.0 398.0 18.7 373.66
                                                                                   11 97
         6 0.31827
                     0.0
                          9.90 0.0 0.544 5.914 83.2 3.9986
                                                             4.0 304.0 18.4
                                                                             390.70 18.33
         7 0.29090
                     0.0
                        21.89 0.0
                                  0.624 6.174
                                                93.6
                                                     1.6119
                                                             4.0 437.0 21.2
                                                                             388.08 24.16
         8 4.03841
                        18.10 0.0 0.532 6.229 90.7 3.0993
                                                                  666.0 20.2
                                                                             395.33
                                                            24.0
         9 0.22438
                     0.0
                          9.69 0.0 0.585 6.027 79.7 2.4982
                                                              6.0 391.0 19.2 396.90 14.33
```

```
print('_'*40)
        y_train_df.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 404 entries, 0 to 403
         Data columns (total 13 columns):
            Column Non-Null Count Dtype
         0
                      404 non-null
                                      float64
         1
             1
                     404 non-null
                                      float64
                     404 non-null
                                      float64
         2
             2
                     404 non-null
         3
                                      float64
                     404 non-null float64
         5
                    404 non-null float64
         6
            6
                    404 non-null float64
         7
             7
                     404 non-null float64
         8
             8
                     404 non-null float64
                      404 non-null
         9
             9
                                      float64
         10 10
                      404 non-null
                                      float64
         11
             11
                      404 non-null
                                      float64
         12 12
                      404 non-null
                                      float64
         dtypes: float64(13)
        memory usage: 41.2 KB
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 404 entries, 0 to 403
         Data columns (total 1 columns):
         # Column Non-Null Count Dtype
         0 0
                     404 non-null float64
         dtypes: float64(1)
         memory usage: 3.3 KB
In [6]: # distribution of numerical feature values across the samples
         X_train_df.describe()
                                                                              5
                                                                                                   7
                       0
                                                        3
                                                                   4
Out[6]:
                                  1
         count 404.000000 404.000000 404.000000 404.000000 404.000000 404.000000 404.000000 404.000000 404.000000 404.000000
                 3.789989
                           11.568069
                                      11.214059
                                                  0.069307
                                                             0.554524
                                                                       6.284824
                                                                                  69.119307
                                                                                             3.792258
                                                                                                        9.660891 408.960396
         mean
                 9.132761
                           24.269648
           std
                                       6.925462
                                                  0.254290
                                                             0.116408
                                                                       0.723759
                                                                                  28.034606
                                                                                             2.142651
                                                                                                        8.736073 169.685166
                 0.006320
                            0.000000
                                       0.460000
                                                  0.000000
                                                             0.385000
                                                                       3.561000
                                                                                  2.900000
                                                                                             1.137000
                                                                                                        1.000000 187.000000
          min
          25%
                 0.081960
                            0.000000
                                       5.190000
                                                  0.000000
                                                             0.452000
                                                                       5.878750
                                                                                 45.475000
                                                                                             2.097050
                                                                                                        4.000000 281.000000
          50%
                 0.262660
                            0.000000
                                       9.690000
                                                  0.000000
                                                             0.538000
                                                                       6.210000
                                                                                  77.500000
                                                                                             3.167500
                                                                                                        5.000000 330.000000
                 3 717875
                           12 500000
                                      18 100000
                                                  0.000000
                                                             0.624000
                                                                       6 620500
                                                                                             5 118000
                                                                                                       24 000000 666 000000
          75%
                                                                                  94.425000
                88.976200 100.000000
                                      27.740000
                                                             0.871000
                                                                       8.780000 100.000000
                                                                                             12.126500
                                                                                                       24.000000 711.000000
          max
                                                  1.000000
```

# Preprocessing

Out[7]:		0	1	2	3	4	5	6	7	8	9
	count	404.000000	404.000000	404.000000	404.000000	404.000000	404.000000	404.000000	404.000000	404.000000	404.000000
	mean	0.042528	0.115681	0.394210	0.348815	0.521905	0.681970	0.241618	0.376560	0.423589	0.625737
	std	0.102650	0.242696	0.253866	0.239522	0.138678	0.288719	0.194973	0.379829	0.323827	0.229502
	min	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
	25%	0.000850	0.000000	0.173387	0.137860	0.444098	0.438466	0.087361	0.130435	0.179389	0.510638
	50%	0.002881	0.000000	0.338343	0.314815	0.507569	0.768280	0.184767	0.173913	0.272901	0.691489
	75%	0.041717	0.125000	0.646628	0.491770	0.586223	0.942585	0.362255	1.000000	0.914122	0.808511
	max	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000

# Model, Predict, Evaluation

```
In [8]: # Reserve data for validation
X_train, X_val, y_train, y_val = train_test_split(X_train, y_train, test_size=0.1, random_state=42)
X_train.shape, X_val.shape, y_train.shape, y_val.shape
Out[8]: ((363, 12), (41, 12), (363,), (41,))
```

# Creating the Model and Optimizing the Learning Rate

learning rate = 0.01, batch\_size = 32, dense\_layers = 2, hidden\_units for Dense\_1 layer= 10, hidden\_units for Dense\_2 layer = 100

```
In [9]: # Set random seed
        tf.random.set_seed(42)
        # Building the model
        model = tf.keras.Sequential([
          tf.keras.layers.Dense(units=10, activation='relu', input_shape=(X_train.shape[1],), name='Dense_1'),
          tf.keras.layers.Dense(units=100, activation='relu', name='Dense_2'),
          tf.keras.layers.Dense(units=1, name='Prediction')
        # Compiling the model
        model.compile(
            loss = tf.keras.losses.mean_squared_error,
            optimizer = tf.keras.optimizers.RMSprop(learning_rate=0.01),
            metrics = ['mse']
        # Training the model
        history = model.fit(
           X_train,
            y_train,
            batch_size=32,
            epochs=50,
            validation_data=(X_val, y_val)
```

```
12/12 [==========] - 0s 3ms/step - loss: 13.7454 - mse: 13.7454 - val_loss: 15.7261 - val_mse: 15.7261

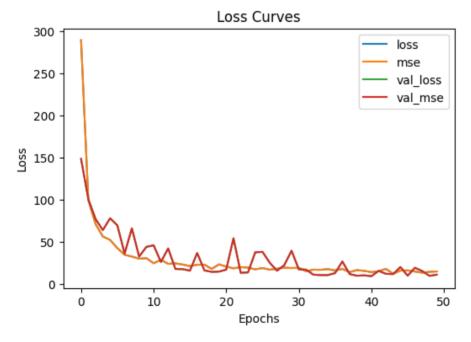
Epoch 49/50

12/12 [=========] - 0s 4ms/step - loss: 14.7645 - mse: 14.7645 - val_loss: 9.9898 - val_m se: 9.9898

Epoch 50/50

12/12 [=========] - 0s 3ms/step - loss: 15.1951 - mse: 15.1951 - val_loss: 11.3679 - val_mse: 11.3679
```

# Model Evaluation



## Model Prediction

# Classifying movie reviews: a binary classification example

Design a neural network to perform two-class classification or *binary classification*, of reviews form IMDB movie reviews dataset, to determine wether the reviews are positive or negative. We will use the Python library Keras to perform the classification

#### The IMDB Dataset

The IMDB dataset is a set of 50,000 highly polarized reviews from the Internet Movie Database. They are split into 25000 reviews each for training and testing. Each set contains equal number (50%) of positive and negative reviews.

The IMDB dataset comes packaged with Keras. It consists of reviews and their corresponding labels (0 for *negative* and 1 for *positive* review). The reviews are a sequence of words. They come preprocessed as sequence of integers, where each integer stands for a specific word in the dictionary.

The IMDB datset can be loaded directly from Keras and will usually download about 80 MB on your machine.

# **Import Packages**

```
In [1]:
import numpy as np
from keras.datasets import imdb
from keras import models
from keras import layers
from keras import optimizers
from keras import losses
from keras import metrics

import matplotlib.pyplot as plt
%matplotlib inline
```

```
Loading the Data
In [2]:
        # Load the data, keeping only 10,000 of the most frequently occuring words
        (train data, train labels), (test data, test labels) = imdb.load data(num words = 10000)
In [3]: # Check the first label
        train_labels[0]
Out[3]: 1
In [4]:
        # Since we restricted ourselves to the top 10000 frequent words, no word index should exceed
        # we'll verify this below
        # Here is a list of maximum indexes in every review --- we search the maximum index in this
        print(type([max(sequence) for sequence in train_data]))
        # Find the maximum of all max indexes
        max([max(sequence) for sequence in train_data])
        <class 'list'>
Out[4]: 9999
```

```
In [5]: # Let's quickly decode a review
    # step 1: load the dictionary mappings from word to integer index
    word_index = imdb.get_word_index()

# step 2: reverse word index to map integer indexes to their respective words
    reverse_word_index = dict([(value, key) for (key, value) in word_index.items()])

# Step 3: decode the review, mapping integer indices to words

#
# indices are off by 3 because 0, 1, and 2 are reserverd indices for "padding", "Start of sedecoded_review = ' '.join([reverse_word_index.get(i-3, '?') for i in train_data[0]])

decoded_review
```

Out[5]: "? this film was just brilliant casting location scenery story direction everyone's really suited the part they played and you could just imagine being there robert? is an amazing a ctor and now the same being director? father came from the same scottish island as myself so i loved the fact there was a real connection with this film the witty remarks throughout the film were great it was just brilliant so much that i bought the film as soon as it was released for? and would recommend it to everyone to watch and the fly fishing was amazing really cried at the end it was so sad and you know what they say if you cry at a film it mu st have been good and this definitely was also? to the two little boy's that played the? of norman and paul they were just brilliant children are often left out of the? list i think because the stars that play them all grown up are such a big profile for the whole film but these children are amazing and should be praised for what they have done don't you think the whole story was so lovely because it was true and was someone's life after all that was shared with us all"

```
In [6]: len(reverse_word_index)
```

Out[6]: 88584

# Preparing the data

#### Vectorize input data

We cannot feed list of integers into our deep neural network. We will need to convert them into tensors.

To prepare our data we will One-hot Encode our lists and turn them into vectors of 0's and 1's. This would blow up all of our sequences into 10,000 dimensional vectors containing 1 at all indices corresponding to integers present in that sequence. This vector will have the element 0 at all indices which are not present in integer sequence.

Simply put, the 10,000 dimensional vector corresponding to each review, will have

- · Every index corresponding to a word
- Every index vith value 1, is a word which is present in the review and is denoted by its integer counterpart
- Every index containing 0, is a word not present in the review

We will vectorize our data manually for maximum clarity. This will result in a tensors of shape (25000, 10000).

```
In [7]: def vectorize_sequences(sequences, dimension=10000):
    results = np.zeros((len(sequences), dimension))  # Creates an all zero matrix of shape
    for i,sequence in enumerate(sequences):
        results[i,sequence] = 1  # Sets specific indices of results[i]
    return results

# Vectorize training Data
X_train = vectorize_sequences(train_data)

# Vectorize testing Data
X_test = vectorize_sequences(test_data)
```

```
In [8]: X_train[0]
Out[8]: array([0., 1., 1., ..., 0., 0., 0.])
In [9]: X_train.shape
Out[9]: (25000, 10000)
```

#### Vectorize labels

```
In [10]: y_train = np.asarray(train_labels).astype('float32')
y_test = np.asarray(test_labels).astype('float32')
```

# **Building the network**

Our input data is vectors which needs to be mapped to scaler labels (0s and 1s). This is one of the easiest setups and a simple stack of *fully-connected*, *Dense* layers with *relu* activation perform quite well.

## **Hidden layers**

In this network we will leverage hidden layers. we will define our layers as such.

```
Dense(16, activation='relu')
```

The argument being passed to each Dense layer, (16) is the number of hidden units of a layer.

The output from a *Dense* layer with *relu* activation is genrated after a chain of *tensor* operations. This chain of operations is implemented as

```
output = relu(dot(W, input) + b)
```

Where, W is the Weight matrix and b is the bias (tensor).

Having 16 hidden units means that the matrix W will be of the shape ( *input\_Dimension* , 16 ). In this case where the dimension of input vector is 10,000; the shape of Weight matrix will be (10000, 16). If you were to represent this network as graph you would see 16 neurons in this hidden layer.

To put in in laymans terms, there will be 16 balls in this layer.

Each of these balls, or *hidden units* is a dimension in the representation space of the layer. Representation space is the set of all viable representations for the data. Every *hidden layer* composed of its *hidden units* aims to learns one specific transformation of the data, or one feature/pattern from the data.

Hidden layers, simply put, are layers of mathematical functions each designed to produce an output specific to an intended result. Hidden layers allow for the function of a neural network to be broken down into specific transformations of the data. Each hidden layer function is specialized to produce a defined output. For example, a hidden layer functions that are used to identify human eyes and ears may be used in conjunction by subsequent layers to identify faces in images. While the functions to identify eyes alone are not enough to independently recognize objects, they can function jointly within a neural network.

#### **Model Architecture**

- 1. For our model we will use
  - two intermediate layers with 16 hidden units each
  - Third layer that will output the scalar sentiment prediction
- 2. Intermediate layers will use *relu* activation function. *relu* or Rectified linear unit function will zero out the negative values
- 3. Sigmoid activation for the final layer or output layer. A sigmoid function "squashes" arbitary values into the [0,1] range.

#### Model defination

```
In [11]: model = models.Sequential()
    model.add(layers.Dense(16, activation='relu', input_shape=(10000,)))
    model.add(layers.Dense(16, activation='relu'))
    model.add(layers.Dense(1, activation='sigmoid'))
```

# Compiling the model

In this step we will choose an optimizer, a loss function, and metrics to observe. We will go forward with

- · binary crossentropy loss function, commonlu used for Binary Classification
- · rmsprop optimizer and
- · accuracy as a measure of performance

We can pass our choices for optimizer, loss function and metrics as *strings* to the compile function because rmsprop, binary\_crossentropy and accuracy come packaged with Keras.

```
model.complie(
    optimizer='rmsprop',
    loss = 'binary_crossentropy',
    metrics = ['accuracy']
)
```

One could use a customized loss function or ortimizer by passing the custom *class instance* as argument to the loss , optimizer or mertics fields.

In this example, we will implement our default choices, but, we will do so by passing class instances. This is exactly how we would do it, if we had customized parameters.

```
In [12]: model.compile(
    optimizer=optimizers.RMSprop(learning_rate=0.001),
    loss = losses.binary_crossentropy,
    metrics = [metrics.binary_accuracy]
)
```

# **Setting up Validation**

We will set aside a part of our training data for *validation* of the accuracy of the model as it trains. A *validation set* enables us to monitor the progress of our model on previously unseen data as it goes throug epochs during training.

Validation steps help us fine tune the training parameters of the model.fit function so as to avoid overfitting and under fitting of data.

```
In [13]: # Input for Validation
X_val = X_train[:10000]
partial_X_train = X_train[10000:]

# Labels for validation
y_val = y_train[:10000]
partial_y_train = y_train[10000:]
```

# **Training our model**

Initially, we will train our models for 20 epochs in mini-batches of 512 samples. We will aslo pass our *validation set* to the fit method.

```
In [14]: history = model.fit(
       partial X train,
       partial_y_train,
       epochs=20,
       batch_size=512,
       validation_data=(X_val, y_val)
     949 - val_loss: 0.3994 - val_binary_accuracy: 0.8627
     Epoch 2/20
     993 - val loss: 0.3088 - val binary accuracy: 0.8886
     Epoch 3/20
     267 - val_loss: 0.2881 - val_binary_accuracy: 0.8869
     Epoch 4/20
     411 - val loss: 0.2792 - val binary accuracy: 0.8897
     Epoch 5/20
     501 - val_loss: 0.2767 - val_binary_accuracy: 0.8884
     Epoch 6/20
     642 - val_loss: 0.3112 - val_binary_accuracy: 0.8781
     Epoch 7/20
     694 - val_loss: 0.3267 - val_binary_accuracy: 0.8804
     Epoch 8/20
     30/30 [=================== ] - 0s 14ms/step - loss: 0.0830 - binary accuracy: 0.9
     779 - val_loss: 0.3235 - val_binary_accuracy: 0.8807
     Epoch 9/20
     798 - val_loss: 0.3542 - val_binary_accuracy: 0.8775
     Epoch 10/20
     858 - val_loss: 0.3724 - val_binary_accuracy: 0.8774
     Epoch 11/20
     889 - val loss: 0.4186 - val binary accuracy: 0.8712
     Epoch 12/20
     915 - val_loss: 0.4310 - val_binary_accuracy: 0.8773
     Epoch 13/20
     941 - val_loss: 0.4663 - val_binary_accuracy: 0.8751
     Epoch 14/20
     953 - val_loss: 0.5045 - val_binary_accuracy: 0.8726
     Epoch 15/20
     966 - val_loss: 0.5289 - val_binary_accuracy: 0.8713
     Epoch 16/20
     971 - val_loss: 0.5600 - val_binary_accuracy: 0.8704
     Epoch 17/20
     987 - val_loss: 0.6111 - val_binary_accuracy: 0.8679
     Epoch 18/20
     995 - val_loss: 0.6720 - val_binary_accuracy: 0.8633
     Epoch 19/20
     978 - val_loss: 0.6709 - val_binary_accuracy: 0.8653
     Epoch 20/20
     Loading [MathJax]/extensions/Saft/all_loss: 0.6942 - val_binary_accuracy: 0.8653
```

At the end of training we have attained a training accuracy of 99.85% and validation accuracy of 86.57%

Now that we have trained our network, we will observe its performance metrics stored in the History object.

Calling the fit method returns a History object. This object has an stribute history which is a dictionary containing four enteries: one per monitored metric.

```
In [15]: history_dict = history.history
history_dict.keys()
Out[15]: dict_keys(['loss', 'binary_accuracy', 'val_loss', 'val_binary_accuracy'])
```

history\_dict contains values of

- -
- · Trainining Accuracy
- · Validation Loss

· Training loss

· Validation Accuracy

at the end of each epoch.

Let's use Matplotlib to plot Training and validation losses and Traing and Validation Accuracy side by side.

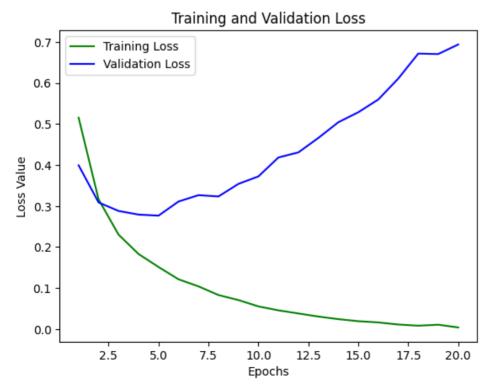
```
In [16]: # Plotting losses
loss_values = history_dict['loss']
val_loss_values = history_dict['val_loss']

epochs = range(1, len(loss_values) + 1)

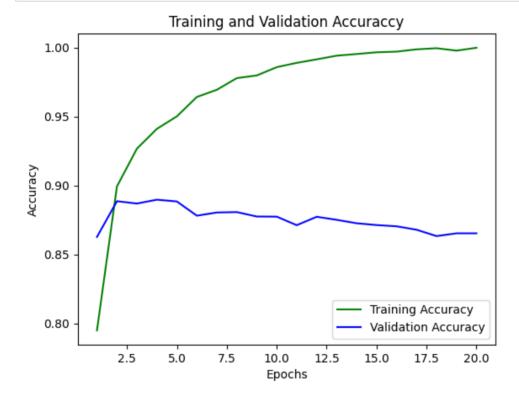
plt.plot(epochs, loss_values, 'g', label="Training Loss")
plt.plot(epochs, val_loss_values, 'b', label="Validation Loss")

plt.title('Training and Validation Loss')
plt.xlabel('Epochs')
plt.ylabel('Loss Value')
plt.legend()

plt.show()
```



# In [17]: # Training and Validation Accuracy acc\_values = history\_dict['binary\_accuracy'] val\_acc\_values = history\_dict['val\_binary\_accuracy'] epochs = range(1, len(loss\_values) + 1) plt.plot(epochs, acc\_values, 'g', label="Training Accuracy") plt.plot(epochs, val\_acc\_values, 'b', label="Validation Accuracy") plt.title('Training and Validation Accuraccy') plt.xlabel('Epochs') plt.ylabel('Accuracy') plt.legend() plt.show()



We observe that *minimum validation loss* and *maximum validation Accuracy* is achived at around 3-5 epochs. After that we observe 2 trends:

- · increase in validation loss and decrese in training loss
- · decrease in validation accuracy and increase in training accuracy

This implies that the model is getting better at classifying the sentiment of the training data, but making consistently worse predictions when it encounters new, previously unseed data. This is the hallmark of *Overfitting*. After the 5th epoch the model begins to fit too closely to the training data.

To address overfitting, we will reduce the number of epochs to somewhere between 3 and 5. These results may vary depending on your machine and due to the very nature of the random assignment of weights that may vary from model to mode.

In our case we will stop training after 3 epochs.

## Retraining our model

```
In [18]: model.fit(
         partial_X_train,
         partial_y_train,
         epochs=3,
         batch_size=512,
         validation_data=(X_val, y_val)
      Epoch 1/3
      996 - val_loss: 0.7299 - val_binary_accuracy: 0.8648
      Epoch 2/3
      30/30 [============= - 0s 15ms/step - loss: 0.0040 - binary accuracy: 0.9
      993 - val_loss: 0.7694 - val_binary_accuracy: 0.8659
      Epoch 3/3
      999 - val_loss: 0.8005 - val_binary_accuracy: 0.8638
Out[18]: <keras.callbacks.History at 0x7f1e00ba11e0>
```

In the end we achive a training accuracy of 99% and a validation accuray of 86%

#### **Model Evaluation**

```
# Making Predictions for testing data
In [19]:
         np.set_printoptions(suppress=True)
         result = model.predict(X_test)
         782/782 [=========== ] - 1s 1ms/step
In [20]: result
Out[20]: array([[0.00426335],
                [0.9999999],
                [0.99748594],
                [0.000199],
                [0.02019035],
                [0.5236855 ]], dtype=float32)
In [21]: y_pred = np.zeros(len(result))
         for i, score in enumerate(result):
            y_pred[i] = np.round(score)
In [22]: mae = metrics.mean_absolute_error(y_pred, y_test)
         mae
Out[22]: <tf.Tensor: shape=(), dtype=float32, numpy=0.15012>
```

# HPC/3/statistics.cpp

```
1 #include <limits.h>
    #include <omp.h>
 2
   #include <stdlib.h>
 3
 5
   #include <arrav>
   #include <chrono>
 7
    #include <functional>
 8
   #include <iostream>
    #include <string>
 9
10
   #include <vector>
11
    using std::chrono::duration_cast;
12
13
    using std::chrono::high_resolution_clock;
14
    using std::chrono::milliseconds;
    using namespace std;
15
16
17
    void s_avg(int arr[], int n) {
18
        long sum = \theta L;
19
        int i;
20
        for (i = 0; i < n; i++) {
21
            sum = sum + arr[i];
22
        cout << sum / long(n);</pre>
23
24
    }
25
    void p_avg(int arr[], int n) {
26
27
        long sum = 0L;
28
        int i;
    #pragma omp parallel for reduction(+ : sum) num_threads(16)
29
        for (i = 0; i < n; i++) {
30
31
            sum = sum + arr[i];
32
        }
33
        cout << sum / long(n);</pre>
34
    }
35
    void s_sum(int arr[], int n) {
36
37
        long sum = 0L;
        int i;
38
39
        for (i = 0; i < n; i++) {
40
            sum = sum + arr[i];
41
42
        cout << sum;
43
44
    void p_sum(int arr[], int n) {
45
        long sum = \theta L;
46
47
        int i;
    #pragma omp parallel for reduction(+ : sum) num_threads(16)
48
        for (i = 0; i < n; i++) {</pre>
49
50
            sum = sum + arr[i];
51
52
        cout << sum;
53
    }
54
55
    void s_max(int arr[], int n) {
        int max_val = INT_MIN;
56
        int i;
57
58
        for (i = 0; i < n; i++) {
59
            if (arr[i] > max_val) {
60
                max_val = arr[i];
61
62
63
        cout << max_val;</pre>
64
65
    void p_max(int arr[], int n) {
66
67
        int max_val = INT_MIN;
68
        int i;
69
    #pragma omp parallel for reduction(max : max_val) num_threads(16)
        for (i = 0; i < n; i++) {
70
```

```
71
             if (arr[i] > max_val) {
 72
                 max_val = arr[i];
 73
 74
75
         cout << max_val;</pre>
    }
76
77
    void s_min(int arr[], int n) {
 78
 79
         int min_val = INT_MAX;
         int i;
 80
         for (i = 0; i < n; i++) {
81
             if (arr[i] < min_val) {</pre>
 82
                 min_val = arr[i];
 83
 84
             }
 85
 86
         cout << min_val;</pre>
 87
88
 89
    void p_min(int arr[], int n) {
 90
         int min_val = INT_MAX;
 91
         int i:
 92
     #pragma omp parallel for reduction(min : min_val) num_threads(16)
 93
         for (i = 0; i < n; i+) {
 94
             if (arr[i] < min_val) {</pre>
 95
                 min_val = arr[i];
96
             3
97
98
         cout << min_val;</pre>
99
    }
100
    std::string bench_traverse(std::function<void()> traverse_fn) {
101
         auto start = high_resolution_clock::now();
102
103
         traverse_fn();
         cout << " ("
104
         auto stop = high_resolution_clock::now();
105
106
107
         // Subtract stop and start timepoints and cast it to required unit.
108
         // Predefined units are nanoseconds, microseconds, milliseconds, seconds,
109
         // minutes, hours. Use duration_cast() function.
110
         auto duration = duration_cast<milliseconds>(stop - start);
111
112
         // To get the value of duration use the count() member function on the
113
         // duration object
114
         return std::to_string(duration.count());
115
116
    int main(int argc, const char **argv) {
117
118
         if (argc < 3) {
             std::cout << "Specify array length and maximum random value\n";</pre>
119
120
             return 1:
121
122
         int *a, n, rand_max;
123
124
         n = stoi(argv[1]);
125
         rand_max = stoi(argv[2]);
         a = new int[n];
126
127
         for (int i = 0; i < n; i++) {
128
129
             a[i] = rand() % rand_max;
130
131
132
         cout << "Generated random array of length " << n << " with elements between 0 to " << rand_max
              << "\n\n";
133
         cout << "Given array is \Rightarrow \n";
134
         for (int i = 0; i < n; i++) {</pre>
135
136
             cout << a[i] << ", ";
137
138
         cout << "\n\n";</pre>
139
140
         omp_set_num_threads(16);
141
         std::cout << "Sequential Min: " << bench_traverse([&] { s_min(a, n); }) << "ms)\n";
142
143
         <<< "Parallel (16) Min: " << bench_traverse([&] { p_min(a, n); }) << "ms)\n\n";
144
```

```
145
146
         std::cout << "Sequential Max: " << bench_traverse([&] { s_max(a, n); }) << "ms)\n";</pre>
147
        std::cout << "Parallel (16) Max: " << bench_traverse([&] { p_max(a, n); }) << "ms)\n\n";
148
149
        std::cout << "Sequential Sum: " << bench_traverse([&] { s_sum(a, n); }) << "ms)\n";</pre>
150
151
        std::cout << "Parallel (16) Sum: " << bench_traverse([&] { p_sum(a, n); }) << "ms)\n\n";
152
153
        std::cout << "Sequential Average: " << bench_traverse([&] { s_avg(a, n); }) << "ms)\n";</pre>
154
155
156
        std::cout << "Parallel (16) Average: " << bench_traverse([&] { p_avg(a, n); }) << "ms)\n";</pre>
157
        return 0;
158
159
160
161
    OUTPUT:
162
163
    Generated random array of length 100 with elements between 0 to 200
164
165
    Given array is ⇒
166
167 183, 86, 177, 115, 193, 135, 186, 92, 49, 21, 162, 27, 90, 59, 163, 126, 140, 26, 172, 136, 11, 168,
168 167, 29, 182, 130, 62, 123, 67, 135, 129, 2, 22, 58, 69, 167, 193, 56, 11, 42, 29, 173, 21, 119,
    184, 137, 198, 124, 115, 170, 13, 126, 91, 180, 156, 73, 62, 170, 196, 81, 105, 125, 84, 127, 136,
169
170 105, 46, 129, 113, 57, 124, 95, 182, 145, 14, 167, 34, 164, 43, 150, 87, 8, 76, 178, 188, 184, 3,
    51, 154, 199, 132, 60, 76, 168, 139, 12, 26, 186, 94, 139,
171
172
173
    Sequential Min: 2 (0ms)
174
    Parallel (16) Min: 2 (0ms)
175
    Sequential Max: 199 (0ms)
176
177
    Parallel (16) Max: 199 (0ms)
178
179
    Sequential Sum: 10884 (0ms)
180
    Parallel (16) Sum: 10884 (1ms)
181
182
    Sequential Average: 108 (0ms)
    Parallel (16) Average: 108 (0ms)
183
184
185
    OUTPUT:
186
187
    Generated random array of length 100000000 with elements between 0 to 100000000
188
189
190
    Sequential Min: 0 (185ms)
191
    Parallel (16) Min: 0 (19ms)
192
193
    Sequential Max: 99999999 (187ms)
194
    Parallel (16) Max: 99999999 (18ms)
195
196
    Sequential Sum: 4942469835882961 (191ms)
197
    Parallel (16) Sum: 4942469835882961 (14ms)
198
199
    Sequential Average: 49424698 (190ms)
200
    Parallel (16) Average: 49424698 (14ms)
201
202
203
```

```
#include<iostream>
#include<omp.h>
#include<bits/stdc++.h>
using namespace std;
void sequential_bubble_sort(int arr[],int size){
  int array[size];
  for(int i = 0; i < size; i++){
    array[i] = arr[i];
  }
  double start = omp_get_wtime();
  for(int i = 0; i < size - 1; i + +){
    for(int j = 0; j < size - i - 1; j++){
       if(array[j] > array[j+1]){
         swap(array[j],array[j+1]);
       }
    }
  }
  double end = omp_get_wtime();
  cout << "Sequential Bubble Sort:\n";</pre>
  // for(int i = 0 ; i < size; i++){
  // cout << array[i] << " ";
  //}
  cout << endl;
  cout << "Time Required: " << end - start << endl;</pre>
}
void parallel_bubble_sort(int arr[],int size){
  int array[size];
  for(int i = 0; i < size; i++){
    array[i] = arr[i];
  }
```

```
double start = omp_get_wtime();
  for(int k = 0; k < size; k ++){
    if(k \% 2 == 0){
       #pragma omp parallel for
         for(int i = 1; i < size - 1; i += 2){
            if(array[i] > array[i+1]){
              swap(array[i],array[i+1]);
            }
         }
    }
     else{
       #pragma omp parallel for
         for(int i = 0; i < size - 1; i += 2){
            if(array[i] > array[i+1]){
              swap(array[i],array[i+1]);
            }
         }
    }
  }
  double end = omp_get_wtime();
  cout << "Parallel Bubble Sort:\n";</pre>
  // for(int i = 0 ; i < size; i++){
  // cout << array[i] << " ";
  //}
  cout << endl;
  cout << "Time Required: " << end - start << endl;</pre>
void merge(int array[],int low, int mid, int high,int size){
  int temp[size];
  int i = low;
  int j = mid + 1;
  int k = 0;
  while((i <= mid) && (j <= high)){
```

}

```
if(array[i] >= array[j]){
       temp[k] = array[j];
       k++;
      j++;
    }
    else{
       temp[k] = array[i];
       k++;
       i++;
    }
  }
  while(i \le mid){
    temp[k] = array[i];
    k++;
    i++;
  }
  while(j <= high){
    temp[k] = array[j];
    k++;
    j++;
  }
  k = 0;
  for(int i = low; i \le high; i++){
    array[i] = temp[k];
    k++;
  }
void mergesort(int array[],int low,int high,int size){
  if(low < high){
    int mid = (low + high) / 2;
    mergesort(array,low,mid,size);
    mergesort(array,mid+1,high,size);
```

}

```
merge(array,low,mid,high,size);
  }
}
void perform_merge_sort(int arr[],int size){
  int array[size];
  for(int i = 0; i < size; i++){
    array[i] = arr[i];
  }
  double start = omp_get_wtime();
  mergesort(array,0,size-1,size);
  double end = omp_get_wtime();
  cout << "Merge Sort:\n";</pre>
  // for(int i = 0 ; i < size; i++){
  // cout << array[i] << " ";
  //}
  cout << endl;
  cout << "Time Required: " << end - start << endl;</pre>
}
void p_mergesort(int array[],int low,int high,int size){
  if(low < high){
    int mid = (low + high) / 2;
    #pragma omp parallel sections
    {
       #pragma omp section
         p_mergesort(array,low,mid,size);
       #pragma omp section
         p_mergesort(array,mid+1,high,size);
    }
    merge(array,low,mid,high,size);
  }
}
```

```
void perform_p_merge_sort(int arr[],int size){
  int array[size];
  for(int i = 0; i < size; i++){
    array[i] = arr[i];
  }
  double start = omp_get_wtime();
  p_mergesort(array,0,size-1,size);
  double end = omp_get_wtime();
  cout << "Parallel Merge Sort:\n";</pre>
  // for(int i = 0 ; i < size; i++){
  // cout << array[i] << " ";
  //}
  cout << endl;
  cout << "Time Required: " << end - start << endl;</pre>
}
int main(int argc, char const *argv[])
{
  int SIZE;
  int MAX = 1000;
  cout << "Enter size of array: ";</pre>
  cin >> SIZE;
  int array[SIZE];
  for(int i = 0; i < SIZE; i ++){
    array[i] = rand() % MAX;
  }
  // cout << "Initial Array:\n";
  // for(int i = 0 ; i < SIZE; i++){
  // cout << array[i] << " ";
  //}
  cout << endl;
  sequential_bubble_sort(array,SIZE);
```

```
parallel_bubble_sort(array,SIZE);
perform_merge_sort(array,SIZE);
perform_p_merge_sort(array,SIZE);
return 0;
}

OUTPUT

Enter size of array: 10

Sequential Bubble Sort:

Time Required: 0

Parallel Bubble Sort:

Time Required: 0.0320001

Merge Sort:

Time Required: 0

Parallel Merge Sort:
```

Time Required: 0