

# INS\_Mechanization class

## member function

construct function

sensor update

velocity update  $\mathbf{v}_k^n = \mathbf{v}_{k-1}^n + \Delta \mathbf{v}_{f,k}^n + \Delta \mathbf{v}_{g/cor,k}^n$

position update

$$\mathbf{q}_{n(k)}^{e(k-1)} = \mathbf{q}_{n(k-1)}^{e(k-1)} \star \mathbf{q}_{n(k)}^{n(k-1)} \quad \mathbf{q}_{n(k)}^{n(k-1)} = \begin{bmatrix} \cos \|0.5 \boldsymbol{\zeta}_k\| \\ \frac{\sin \|0.5 \boldsymbol{\zeta}_k\|}{\|0.5 \boldsymbol{\zeta}_k\|} 0.5 \boldsymbol{\zeta}_k \end{bmatrix} \quad \mathbf{v}_{k-1/2}^n = \frac{1}{2}(\mathbf{v}_{k-1}^n + \mathbf{v}_k^n)$$

$$\mathbf{q}_{n(k)}^{e(k)} = \mathbf{q}_{e(k-1)}^{e(k)} \star \mathbf{q}_{n(k)}^{e(k-1)} \quad \mathbf{q}_{e(k-1)}^{e(k)} = \begin{bmatrix} \cos \|0.5 \boldsymbol{\xi}_k\| \\ -\frac{\sin \|0.5 \boldsymbol{\xi}_k\|}{\|0.5 \boldsymbol{\xi}_k\|} 0.5 \boldsymbol{\xi}_k \end{bmatrix} \quad \boldsymbol{\xi}_k = \boldsymbol{\omega}_{ie}^e \Delta t_k$$

$$h_k = h_{k-1} - v_{D,k-1/2} \Delta t_k$$

attitude update

$$\mathbf{q}_{n(k)}^{n(k)} = \mathbf{q}_{n(k-1)}^{n(k)} \circ \mathbf{q}_{b(k-1)}^{n(k-1)} \circ \mathbf{q}_{b(k)}^{b(k-1)} \quad \mathbf{q}_{b(k)}^{b(k-1)} = \begin{bmatrix} \cos \|0.5 \boldsymbol{\phi}_k\| \\ \frac{\sin \|0.5 \boldsymbol{\phi}_k\|}{\|0.5 \boldsymbol{\phi}_k\|} 0.5 \boldsymbol{\phi}_k \end{bmatrix} \quad \boldsymbol{\phi}_k = \int_{t_{k-1}}^{t_k} \left[ \boldsymbol{\omega}_{ib}^b + \frac{1}{2} \Delta \boldsymbol{\theta}(t) \times \boldsymbol{\omega}_{ib}^b \right] dt$$

$$\approx \Delta \boldsymbol{\theta}_k + \frac{1}{12} \Delta \boldsymbol{\theta}_{k-1} \times \Delta \boldsymbol{\theta}_k,$$

$$\mathbf{q}_{n(k-1)}^{n(k)} = \begin{bmatrix} \cos \|0.5 \boldsymbol{\zeta}_k\| \\ -\frac{\sin \|0.5 \boldsymbol{\zeta}_k\|}{\|0.5 \boldsymbol{\zeta}_k\|} 0.5 \boldsymbol{\zeta}_k \end{bmatrix} \quad \boldsymbol{\zeta}_k = \int_{t_{k-1}}^{t_k} [\boldsymbol{\omega}_{in}^n(t) + \boldsymbol{\omega}_{en}^n(t)] dt \approx [\boldsymbol{\omega}_{in}^n(t_{k-1}) + \boldsymbol{\omega}_{en}^n(t_{k-1})] \Delta t$$

$$\boldsymbol{\omega}_{ie}^n = \begin{bmatrix} \omega_e \cos \varphi & 0 & -\omega_e \sin \varphi \end{bmatrix}$$

$$\boldsymbol{\omega}_{en}^n = \begin{bmatrix} v_E / (R_N + h) \\ -v_N / (R_M + h) \\ -v_E \tan \varphi / (R_N + h) \end{bmatrix}$$

$$R_M = \frac{a(1-e^2)}{\sqrt{(1-e^2 \sin^2 \varphi)^3}}$$

$$R_N = \frac{a}{\sqrt{1-e^2 \sin^2 \varphi}}$$

$$a = 6378137.0$$

$$e = 0.08181919104$$

$$\mathbf{q}_{\delta \theta} = \left( \mathbf{q}_{n(k-1)}^{e(k-1)} \right)^{-1} \star \mathbf{q}_{n(k)}^{e(k)} \quad \mathbf{q}_{n(k-1/2)}^{e(k-1/2)} = \mathbf{q}_{n(k-1)}^{e(k-1)} \star \mathbf{q}_{0.5 \delta \theta}$$

data record

Mechanization output

to skew symmetric matrix

## member variable

IMU output

Vector3d delta\_theta\_, last\_delta\_theta\_  
Vector3d delta\_v\_, last\_delta\_v\_  
double time\_, last\_time\_, delta\_time\_  
Quaternion<double> q\_b\_to\_n\_, q\_b\_last\_to\_n\_last\_  
Vector3d v\_proj\_n\_, last\_v\_proj\_n\_, before\_last\_v\_proj\_n\_  
Quaterniond q\_n\_to\_e, q\_n\_last\_to\_e\_last\_  
double h\_, h\_last\_  
Vector3d omega\_in\_proj\_n\_, last\_omega\_in\_proj\_n\_  
Quaterniond q\_n\_midway\_to\_e\_midway\_  
double h\_midway\_  
Vector3d v\_midway\_proj\_n\_

constant

double a\_ = 6378137.0  
double e\_ = 0.08181919104  
double omega\_e\_  
Vector3d omega\_ie\_proj\_e\_