Instructive Computer Games of Chess: What we can learn from the beasts?

May 5, 2019

#### **Chapter 1**

# **Strategic Advantage**

# 1.1 LCZero v0.21.1-nT40.T6.532 – Bluefish Dev

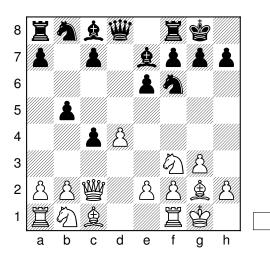
TCEC S15 Bonus: Bluefish vs Leela Jhorthos E05 Catalan, Open, Classical Line 2019-04-28

Following concepts exemplified:

1.

The engines started play from the usual start position.

1	d4	<b><b><b><u>Ø</u>f6</b></b></b>
2	c4	<b>e6</b>
3	<b>g3</b>	d5
4	<b>≜g2</b>	<b>≜e7</b>
5	<b><b>②f</b>3</b>	0-0
6	0-0	$d\times c4$
7	₩c2	b5?!



Typical play here is 7... a6, instead. Trying to hold on to c4 allows white to get quite a lot of activity.

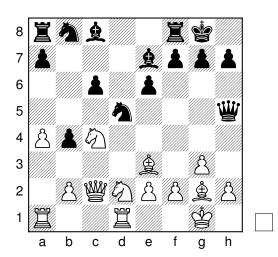
8 a4 b4 9 ⊘fd2

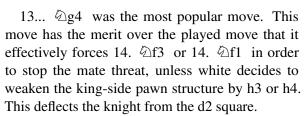
9. ②bd2 slightly more popular, but 9. ②fd2 has better statistics for white. The merit of the move in the game is that it unblocks the bishop's vision, adding pressure towards a8.

Black has here three options to protect the rook. 9... ②d5 gives up the pawn back and allows black to develop the queenside. 9... b3 10. 豐×c4 鱼a6 11. 豐×b3 and either 11... c6 and black will get one pawn back, or 11... ②d5 for trading one pawn for better development. A third and the most

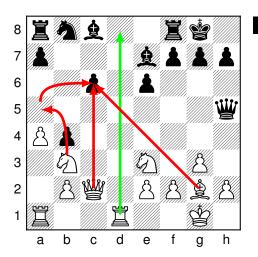
popular option was played in the game, postponing the resolution of the queenside development.

9	•••	<b>c6</b>
10	②×c4	<b>≝×d4</b>
11	<b>ℤd1</b>	₩c5
12	≜e3	<b>₩h</b> 5
13	∅bd2	ଏପ5!?N





13...  $\triangle d5$  would make more sense if the purpose was to block the g2-bishop eyeing towards the black's queen-side corner. However, the intention was to trade the knight with the bishop.

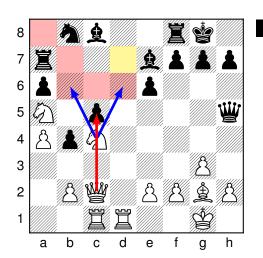


Now the small subtlety of playing 13... 2 d5 instead of 13... 2 d5 becomes obvious: black is going to have some serious questions to answer on developing the queen side, as the c6 pawn is starting to become a liability. Further, white has gained the d-file, thwarting development ideas such as 4 d7 with 4 d6 for now. So, black goes with another typical development idea in Catalan: push the apawn, play 4 d6 and then untangle with moves such as 4 d6 and c5.

15 ... a6

Now move  $\Xi a7$  is enabled. The move 15... a6 over the move 15... a5 has the following two benefits: (1) The a-pawn will not become a target for a later  $\triangle \times a5$ , and (2) the pawn controls the b5 square after c5.

			16	<b>4</b> 2c4	<b></b> a7
14	<b>②b3</b>	②×e3?!	17	<b>Zac1</b>	<b>c5</b>
15	<a>∅×e3</a>		18	∅ba5	

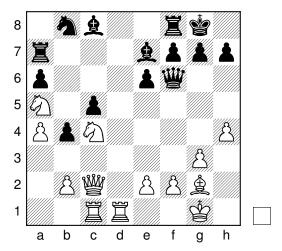


The b4-pawn is now finally protected, but black's problems are still far from over. The black queenside is a minefield due to white's control, and the d7-square is a bottleneck for black development. Further, should the e7-bishop move, white is ready to jump the c4-knight exposing the threat to take the c5-pawn.

Therefore, it is no wonder that it is already getting difficult to find any useful moves for black:

- (a) 18... \(\beta\)c7 does not help development, since the c6 square is already attacked twice by white. Similarly, a natural move 18... \(\beta\)g7 cannot be played.
- (c) 18... 罩d1 allows white to practically force 19. 罩×d8+ 魚×d8 20. 罩d1 魚×a5 21. ②×a5 豐g5 22. 罩d6 罩c7 23. 豐d1 ②d7 24. 罩c6 罩×c6 25. ②×c6. The 26... c4 move here would be met with 27. 豐d6 threatening to either win a piece by ②e7+ or a pawn by 豐×b4 while still keeping black's queenside development cumbersome.
- (d) 18... 单d7 with a possible continuation 19. b3 罩c7 20. 豐d3 罩d8 21. 豐e3 彙e8 22. 豐f4 罩cd7 23. 罩xd7 彙xd7 24. e3 threatening 豐c7, for instance.

Black simply does not seem to be able to find any useful counterplay, so black decided to play a semi-waiting queen move, reinforcing the d8 square.

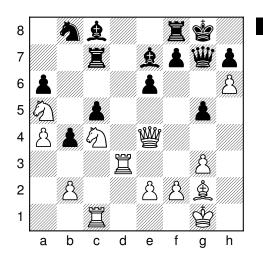


As black is unable to make progress, white is now starting to improve her position. The move h4 not only restricts the queen, but it also signals white's intention to shift the play in the king-side. Often such ideas are useful when one side has better access to squares.

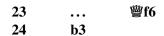
20 響e4 罩c7 21 罩d3 g5

Black was soon forced to do something. If black would continue to play waiting moves, then white would soon break black's position. An example line 21... 會h8 22 b3 會g8 23 罩cd1 會h8 24 罩f3 豐h6 25 豐e5 with unparriable threats. For example: 25... 罩d7 26. 罩fd3 罩×d3 27. 罩×d3 豐c1+ 28. 負f1 ②d7 29. 豐c7 負f6 30. ②c6 a5 31. ②a7 負a6 32. 罩×d7 with no hope for black.

22 h5! 響g7 23 h6!!

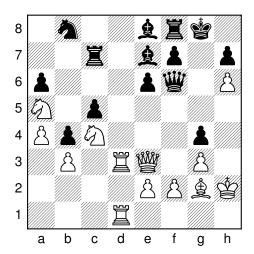


With the h-pawn moves, white continues to strangle black's position, and begins to threaten a king-side attack. Note that the h6-pawn cannot be taken as black queen must be ready to stop 豐e5, as that would win a piece due to the skewer (23... 豐×h6?? 24. 豐e5 罩d7 25. 豐×b8).



Solidifying move by white and preventing potential tactics by ...b3. Note that often with such moves, white needs to pay attention not to trap pieces, as b3 was the natural escape square for the a5-knight. However, here white could simply move the c4-knight somewhere to provide another escape square, should the need arise.

24	•••	奠d7
25	₩e3	<b>g4</b>
26	<b>ℤcd1</b>	≜e8
27	∯h2	



The king move is a subtle move in this complex position. Black is now almost in a Zugswang where it would be preferable not to make a move at all. The king move is also preparatory to avoid tempo loss by  $\frac{1}{2}$ h8/ $\frac{1}{2}$ g8+ in some variations after both the g-pawns have moved to other files, as well as to prepare Rh1 to protect the h6-pawn with possible rook lift ideas. Finally,  $\frac{1}{2}$ h2 prepares  $\frac{1}{2}$ g3 to attack the g4-pawn should the opportunity arise. Let us review some of black's choices:

- (a) 27... **§**f5 would essentially transpose to the game continuation after 28. **§**f4
- (b) 27... 曾h8 28. ②e5 豐f5 29. 豐f4 豐×f4 30. g×f4 and white maintains the advantage with a continuation such as 30... f6 31. ②ec4 鱼g6 32. 罩3d2 罩g8 33. 曾g3 鱼f8 34. e3 鱼×h6 35. 罩d8 罩e7 36. ②b7 罩×d8 37. 罩×d8+ 罩e8 38. 罩×e8+ 鱼×e8 39. ②×c5. Note that a move 29... 豐h5+ would not save the day, since 30. 曾g1 豐f5 31. 豐×f5 e×f5 would just leave white with a better pawn structure with otherwise similar prospects.
- (c) 27... 单d7 28. ②e5 单e8 29. ②×g4 and white simply wins a free pawn.
- (d) 27... \( \mathbb{Z}\)a7 followed by, e.g., 28. \( \mathbb{W}\)e4 \( \mathbb{W}\)×h6+ 29. \( \mathbb{C}\)g1 \( \mathbb{Z}\)c7 30. \( \mathbb{W}\)×g4+ \( \mathbb{W}\)g5 31. \( \mathbb{W}\)×g5+ \( \mathbb{L}\)×g5 32. \( \mathbb{Z}\)d6 and white gets a strong

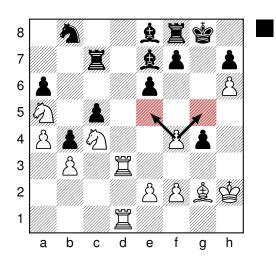
foothold into black's territory, renewing the question on the queen-side weaknesses. Also, the exchange sacrifice after 28. 罩d6 鱼×d6 29. 罩×d6 罩d8 30. 罩×d8 豐×d8 31. 豐e5 f6 32. 豐×e6+ looks interesting with good compensation, although probably not necessary to take a risk.

(e) 27... 罩a7 28. ②b7 豐g5 29. 豐×g5+ 遼×g5 30. ②×c5 罩c7 31. ②e4 遼×h6 32. ②f6+ 鸷g7 33. ②×e8+ 罩×e8 34. 罩d4 does not look very attractive, either.

None of the options look particularly good, so black went with the straightforward queen exchange.

White does not exchange the queen immediately, but forces better terms. The exchange on f4 square prevents black to get into the game, which 28 豐×g5+ 魚×g5 29 罩d6 魚×h6 30 罩b6 魚d7 31 氫e5 魚g7 would have allowed.

Black is forced to exchange the queens on white's terms. Note that curiously, black cannot make a waiting move 28... 宣c8 asking again to exchange the queens on the g5 square. The sequence after 29. 豐×g5 no longer works because the move 鱼d7 is no longer possible because the rook had moved. Also, the intermediate queen check is no good either, because after 28...豐h5+29 曾g1 e5 30 ②×e5 鱼g5 31 豐f5 豐×h6 32 ②×g4 豐g6 33 豐e5 black simply drops a piece under white's threats.

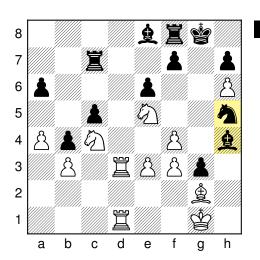


The pawn now controls two important squares: e5 provides an anchor point for a knight, and g5 protects indirectly the h6-pawn by preventing \(\delta g5\).

The threat was more important than the execution. Now its time to get back and protect the f2-pawn.

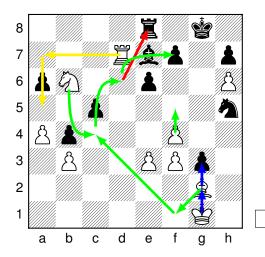
Black is trying to create counterplay by trying to open the g-file and repositioning minor pieces in the h-file. However, white has a simple answer:

29 g×f4 34 f3!



White simply makes black's own pawn a shield for the potential attack on the g-file, claiming that the pawn is rather weak. Now the black minor pieces on the h-file are irreparably mispositioned, and white can concentrate again on the queen-side. This time black has no answer to prevent white's penetration with the rooks.

34	•••	<b>≜e7</b>
35	ઈd7!	≜×d7
36	≅×d7	<b>ℤfc8</b>
<b>37</b>	<b>ᡚb6!</b>	≅×d7
38	۳×d7	Ξe8



White has now multiple pieces for the plan to finish the game:

- (a) The rook can claim the a5-pawn, creating a passed pawn for white. The cost is some time. (Yellow arrows)
- (b) The king can march to g2 after the bishop has moved. Then, if the black knight moves, the g3 pawn can be taken. (Blue arrows)
- (c) The knight can move to d6 driving \( \frac{\textsf{Z}}{2} \) away, allowing the white rook to add additional pressure on f7. The bishop can reposition to c4, and the pawn can move to f5 adding even more pressure to the e6/f7 squares. This should allow white to create passed connected passers on e/f-files. (Green arrows)

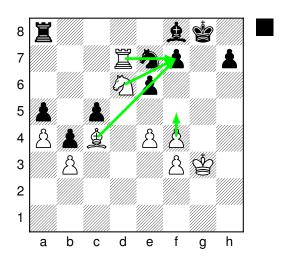
Meanwhile, white's h6-pawn has now become weak and cannot be protected. Some precision is still required.

<b>39</b>	<b>鱼f1</b>	<b>€</b> 2f6
40	<b>≌b7</b>	<b><b>②d</b>5</b>
41	<b>②c4</b>	<b>≜f8</b>
42	<b>⊈g2</b>	≜×h6
43	⋭×g3	

The king has now claimed the g3 pawn. Note that 40. 罩a7 would probably have been slightly more precise, although it does not matter.

43	•••	<b>≜f8</b>
44	<b>e4</b>	<b>©e7</b>
45	<b>Ød6</b>	≌a8
46	<b>ℤd7</b>	

A waiting move to ask black to move again, and to prevent the black to move ... \( \begin{aligned} \begin{aligned} \dd & \text{with tempo on the knight.} \end{aligned} \)

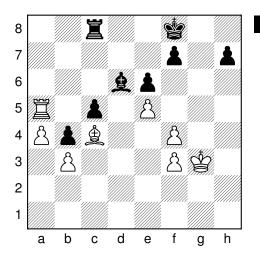


Now focusing on the f7 pawn with f4 pawn waiting to be moved.

The pawn move f5 is now temporarily discouraged due to tactics: 49 f5 \( \begin{align\*} \frac{1}{2} \text{c7} \\ \begin{align\*} \delta \delta \delta \text{c7}.\\ \delta \

However, white did not go into such complications, and simply switched to taking the a5-pawn first and then resolving the pin by moving the e4pawn before pushing the f-pawn.

49	<b>ℤa7</b>	≜d6
50	≅×a5	<b>∲f8</b>
51	<b>e</b> 5	

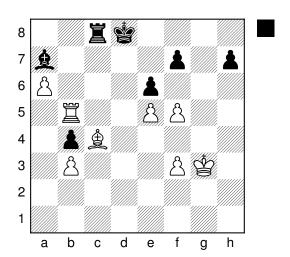


Black has no good squares for the bishop. 鱼b8 would lose quickly to 罩a8 pinning, and then white pushing the a-pawn.

51... 全 7 would postpone the game by some moves with the following possible continuation: 52. 全 7 52. 温 7 堂 8 53. 全 6! 温 b 8 54. 全 b 5 + 堂 f 8 55. 全 c 4. Note the move 53. 全 a 6! . It drives the rook away from the c 8-square, forcing ... 堂 f 8 after the check. The king cannot come to d 8-square after ... 温 d 8 since it's already occupied, or after ... 温 b 8 since then white would play 温 b 7 + with reveal check, winning the rook.

So, black sacrificed the c5-pawn in order to be able to block the a-pawn with a bishop.

51	•••	奠c7
52	≅×c5	<b>∲e7</b>
53	a5	<b>∲d8</b>
54	a6	<b>≜b6</b>
55	<b>≝b</b> 5	≜a7
56	f5	



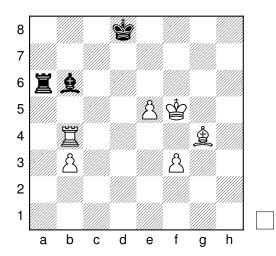
White is now finally going after the f7-pawn. In opposite-color bishop endings, it is important to have two passed pawns with some distance to make it impossible for the bishop to stop both.

White could have also exchanged the rooks. The rest is simple technique.

57	•••	e×f5
58	<b>≜</b> ×f7	<b>≜b</b> 6
59	≌a2	

The final pitfall was the natural-looking 罩b5. This would have blundered the win away to simple tactics: 59 罩b5 食f2+ 60 常×f2 罩×b5 with a disappointing draw. But now the rest is simple technique.

<b>59</b>	•••	<b>ℤc8</b>
60	<b>∲f4</b>	h5
61	<b>∲</b> ×f5	≌c7
62	≜×h5	<b>≌h7</b>
63	≜g4	≌c7
64	<b>Za</b> 4	<b>ℤa</b> 7
65	≅×b4	≅×a6



However, in this game, Leela did not have the distance-to-zero (DTZ) tablebase files available and was on her own after reaching the winning position as per the win-draw-loss (WDL) files. As is characteristic to the current neural network (NN) engines, the endgame was not concluded quickly. The NN engines are simply interested in winning the game, not winning the game quickly.

66 f4 兔c5 67 罩c4 兔f2 68 宫e4 罩g6 69 宫f3 兔h4 70 b4 罩a6 71 兔f5 兔e1 72 b5 罩a3+ 73 宫g4 罩g3+ 74 宫h5 兔a5 75 罩a4 兔b6 76 兔g4 宫e8 77 宫g5 兔d8+ 78 宫f5 兔b6 79 罩a6 兔f2 80 兔h5+ 宫e7 81 罩e6+ 宫d7 82 兔e8+ 宫c7 83 罩c6+ 宫b8 84 罩c4 宫a7 85 e6 罩g7 86 宫e5 兔h4 87 f5 兔e7 88 兔g6 兔f8 89 罩c6 罩b7 90 宫f6 兔e7+ 91 宫g7 兔a3+ 92 宫h6 罩xb5 93 f6 兔f8+ 94 宫h7 罩b7+ 95 兔f7 兔a3 96 罩c2 宫b6 97 宫g6 宫b5 98 兔e8+ 宫b6 99 兔d7 罩c7 100 罩xc7 宫xc7 101 宫f7 兔c5 102 e7 宫xd7 103 e8豐+ 宫d6 104 宫g8 宫d5 105 豐a8+ 宫d4 106 豐c8 兔b4 107 豐d7+ 宫c3 108 豐e8 宫d4 109 豐f7 宫c3 110 豐g7 兔c5 111 豐h8 宫c4 112 豐h7 宫c3 113 豐g7 宫c4 114 豐h8 兔d4

115 豐h7 魚c5 116 豐g6 曾c3 117 豐f7 魚d6 118 빨e8 호c5 119 항g7 항d3 120 항g6 항d4 121 항f5 125 營b8+ 含c4 126 營a8 食b4 127 營a7 含d3 128 豐a6+ 曾d4 129 豐a8 曾c4 130 f8公 曾d3 131 ②g6 曾d4 132 ②f4 奠e1 133 豐a7+ 曾c4 134 豐b7 &c3 135 豐c8+ 曾b3 136 豐d7 &h8 137 豐e8 &c3 138 豐f7+ 含b4 139 豐g8 &e1 140 豐h7 魚d2 141 豐g6 含c5 142 豐e8 含d4 143 豐f7 當c3 144 豐g8 &e1 145 豐h7 &d2 146 豐g6 當d4 147 響e8 會c5 148 響a8 魚e1 149 響a7+ 會b5 150 豐b7+ 曾c4 151 豐c7+ 曾b5 152 豐d7+ 曾b4 153 豐e7+ 曾b3 154 豐×e1 曾c4 155 豐e8 曾c5 156 豐d8 曾c4 157 豐f8 曾b5 158 豐c8 曾b6 159 豐d8+ 含c5 160 豐e8 含c4 161 豐f7+ 含b5 162 豐g7 曾c6 163 豐h7 曾b5 164 豐h6 曾c5 165 豐h5 曾d4 166 豐h4 曾c3 167 豐h3+ 曾c2 168 豐h8 曾b3 169 曾b8+ 曾c4 170 曾a8 曾c3 171 曾b7 曾d4 172 빨a7+ 함c3 173 빨a6 함b4 174 빨b6+ 할c4 175 빨c7+ 할b4 176 빨d7 할c5 177 빨e7+ 曾c4 178 曾d8 曾c3 179 曾d7 曾c4 180 曾e7 曾c3 181 曾e5 曾c4 182 曾d6 曾d4 183 豐d8 曾e4 184 豐f8 曾d4 185 豐c8 曾e4 186 豐d7 曾×f4 187 豐c8 ġe4 188 빨d8 ġf4 189 빨b8 ġe4 190 빨a7 ġf4 191 營a6 含e4 192 營a5 含f4 193 營a4+ 含e3 194 豐a8 曾f4 195 曾d5 曾f5 196 豐a7 曾f6 197 豐b7 曾f5 198 曾b8 曾f6 199 曾d6 曾f5 200 曾a8 曾f4 201 曾e6 曾e3 202 曾e5 曾d3 203 豐a7 曾c3 204 豐b8 曾c4 205 曾d6 曾d4 206 豐e8 曾c3 207 曾c5 할c2 208 할c4 할d2 209 빨e7 할c1 210 할c3 할d1 211 **營e8 含c1 212 營e1**#. White wins.

### **Chapter 2**

## **Endgame techniques**

#### 2.1 Ethereal 10.88 – Lc0 17.11089

CCCC 1: Rapid Rumble (15|5) Stage 1 Round 35 B90 NAJDORF, BYRNE (ENGLISH) ATTACK 2018-09-10

Following concepts exemplified:

- 1. Prying lines open with pawn-and-piece attacking pawn moves
- 2. The triangle of interception for pawn and king races
- 3. Blocking two pawns with a knight

The engines started play from the usual start position.

1	e4	<b>c5</b>
2	<b><b>②f</b>3</b>	<b>d6</b>
3	<b>d4</b>	c×d4
4	②×d4	<b><b>②f6</b></b>
5	Ø)c3	a6

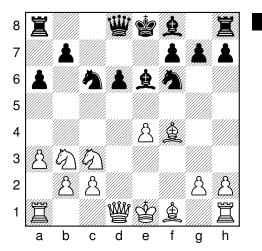
The popular Najdorf variation of the Sicilian defence.

6 **≜e3** 

The Byrne (English) attack.

The first move to diverge from the mainlines. The move is not bad at all, but makes the game sharper than the most popular move, 8. f3.

8	•••	e×f4
9	≜×f4	<b>Øc6</b>
10	a3?!N	



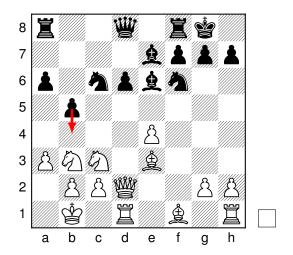
This is a novelty. The main moves here are 10. we2 and 10. wd2, preparing for long castling. This seemingly unnecessary move has some potential issues:

1. Black can play Bxb3 and white has to take with the c-pawn, instead of having the additional option to take with the a-pawn.

<sup>&</sup>lt;sup>1</sup>Lichess masters database, accessed Apr 2019.

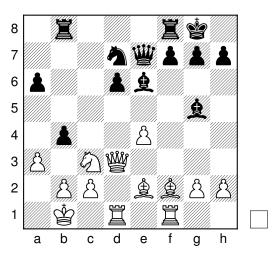
2. Black has later additional options to open Q-side files by pushing the b-pawn.

10	•••	≜e7
11	<b>豐d2</b>	ଏ) h5
12	≜e3	<b>②f6</b>
13	O-O-O	0-0
14	<b>ģ</b> b1	<b>b</b> 5



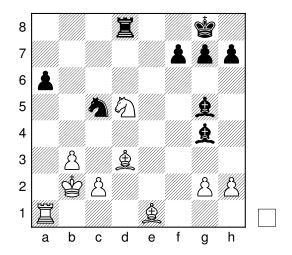
Now exercising black's typical Najdorf plan after opposite-side castling. The threat is now to push b4 and force a×b4.

15	<b><b>②d4</b></b>	ઈ√d4
16	≜×d4	<b>≝b8</b>
<b>17</b>	≜e2	ହ <b>ିd</b> 7
18	<b>ℤhf1</b>	<b>≜g</b> 5
19	₩d3	₩e7
20	<b>≜f2</b>	b4



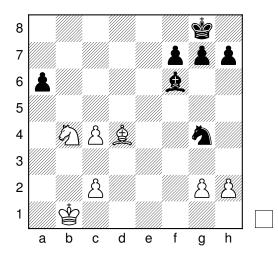
Now finally pushing b4. This is a typical attacking move to pry open files. If the knight moves,  $b \times a3$  will be played.

21	a×b4	罩×b4
22	豐×d6	罩fb8
23	<b>b3</b>	₩d8
24	<b><b>②d5</b></b>	≅×e4
25	<b>≝fe1</b>	<b>≜f5</b>
26	<b>∲b2</b>	<b>ℤc8</b>
27	≜d3	≅×e1
28	≜×e1	≜g4
29	<b>ℤa1</b>	<b>②c5</b>
30	₩× <b>d8</b> +	≅×d8



White has managed to temper black's attack. The position is still somewhat complicated, but should be objectively a draw.

31	≜c4	≜e6
32	<b>ℤd1</b>	≌d7
33	<b>≜b4</b>	<b>©e4</b>
34	<b>∲b1</b>	≜d8
35	<b>ℤd4</b>	<b>包f2</b>
36	<b>≜c5</b>	<b>∮</b> )g4
37	<b>⊘b4</b>	罩×d4
38	≜×d4	≜×c4
39	b×c4	<b>≜f6?!</b>



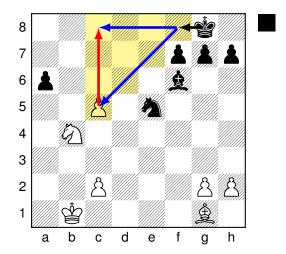
This is a dubious-looking move, offering extra options for white to drive the endgame into a desireable direction. The game should still be a draw. Black had a number of other options, such as 39...  $\triangle \times h2$  taking the pawn, 39... f5 hastening the pawn push, or 39... \$f8 bringing the king to play. But since black played 39... \$f6?!, white has at least three options to choose from:

Option 1 — Deflect the knight from attacking h2, gaining a bit of time. 40  $\& \times f6$ .

Option 2 — Exchange the bishop for the knight, simplifying the position. 40 h3 &×d4 41 h×g4. While this position may look a bit weird at first, white's pawns are all in the light squares, untouchable by the black bishop, and white has double passed c-pawns while black's a-passer is weak.

But white decided to go with the third option: \( \frac{1}{2}g1. \) This move has multiple purposes: (1) it protects h2; (2) it protects the next square for the c4-pawn; and (3) it avoids exchanging pieces. The dark-square bishop alone cannot support the advancement of the c-pawn, and the knight alone is clumsy. But the bishop and the knight generally work well together to control squares on the way of the pawn. This was also the best choice for white.

Now is the time for black to play \$\delta\$f8. The black king needs to move in time to stop the c5 pawn. Highlighted is the triangle of interception where the king needs to be after black's move in order to win the race.

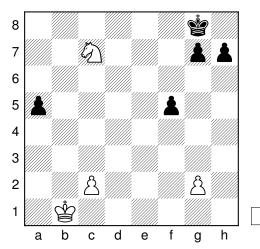


However, black did not play \$\delta\$f8 and black pieces alone cannot block or win the passed pawn. Preventing c8\$\delta\$ will now cost a piece.

41	•••	a5??
42	<b>c6</b>	≜d8
43	<b>≜d4</b>	<b>≜c7</b>

Black at least gets now two pawns for the piece. Note that 43...a×b4 44  $\triangleq$ xe5  $\triangleq$ f8 45 c7  $\triangleq$ xc7 46  $\triangleq$ xc7 would have been even worse for black.

44	≜×e5	≜×e5
45	<b>②a6</b>	奠×h2
46	<b>c</b> 7	≜×c7
47	②×c7	f5



Here Leela thinks she is somewhat better with black, and this misevaluation was probably the reason why Leela played the losing ...41...a5?? move earlier. A beginning player might make a similar evaluation mistake.

The king-side black pawns surely look intimidating, but this is only superficial. If one does not calculate and/or spot the pattern to stop the king-side pawns, it is plausible to think that black has time to march the king to support the a5-pawn, block white's passed c-pawn, and overrun the king-side with the pawn wall. If white king intercepts this plan, surely the white knight and a pawn cannot stop the black pawn wall?

However, white has an easy plan. The g2 pawn guarantees that at least one black pawn will be exchanged when the black pawns march forward. If the knight is in time, it can stop two black pawns with ease with the L-shaped defensive pattern. In fact, white even has the time to take a small detour with the knight and take the a5, and then to blockade the king-side pawns.

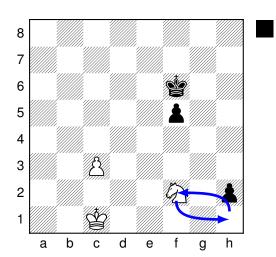
When choosing the blockading squares for the knight, it is here beneficial to block the black pawns

as late as possible, because that would require the black king to move beyond the c4 pawn for support, and then c4 pawn would have easy time to march forward and queen.

This plan is a forced win for white with the best but not difficult play.

<b>②e6</b>	<b>∲f7</b>
<b>⊘d8</b> +	<b>∲f6</b>
<b>⊘b7</b>	<b>a4</b>
<b>②c5</b>	<b>g</b> 5
②×a4	h5
<b>②c5</b>	h4
<b>Ġc1</b>	<b>g4</b>
2d3	h3
$g \times h3$	g×h3
	②d8+ ②b7 ②c5 ②×a4 ②c5 ঔc1 ②d3

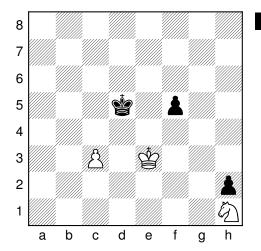
As promised, the g2 pawn was able to take one black pawn from the wall. Two pawns left for black.



Now the knight controls the h1 and f2 squares and the black pawns cannot advance through those squares without support. However, the king cannot offer assistance, since the c4-pawn would run.

Further, it is important to note that the knight can jump freely between the h1 and f2 squares to lose tempi if necessary. Losing (or gaining) tempi is often important in king-pawn endings, and this ending is not an exception. With only the white king and pawn versus black king, this would be an easy draw.

58	•••	<b>∳e5</b>
<b>59</b>	<b>Ġd2</b>	<b>∲d5</b>
60	<b>Ġd3</b>	<b>∲e5</b>
61	<b>∲e3</b>	<b>∲d5</b>
62	<b>②h1</b>	

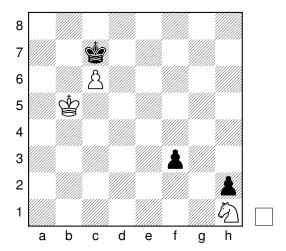


The first tempo loss, basically asking black to make another move. However, 62.  $\dot{g}$ d3 and losing the tempo later was equally good.

Black has here one last attempt to trick a draw, although this variant was not played: 62... f4+ 63  $^{\circ}\times$ f4??  $^{\circ}$ c4 64  $^{\circ}$ g3  $^{\circ}\times$ c3 65  $^{\circ}\times$ h2 draw. The correct move for white was 63.  $^{\circ}$ d3! letting the knight to stop the f-pawn, and not allowing the king to stray away from the all-important c-pawn.

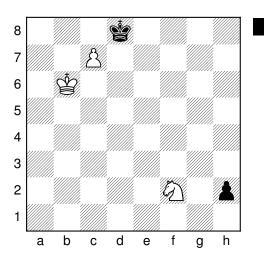
62	•••	<b>⋭c4</b>
63	<b>Ġd2</b>	<b>ġd5</b>
64	<b>Ġd3</b>	f4
65	c4+	<b>堂c5</b>
66	<b>Ġc3</b>	<b>ġd6</b>
<b>67</b>	<b>Ġd4</b>	<b>∲d7</b>
68	<b>c5</b>	<b>∲d8</b>
69	<b>c6</b>	<b>∲c8</b>
70	<b>∲c5</b>	<b>∲c7</b>





Black does not want to move the king, as this allows white to push forward with \$\&\circ\$c6. But after the pawn moves are exhausted, black is out of options.

72	<b>堂c5</b>	f2
73	②×f2	<b>Ġc8</b>
74	<b>∲b6</b>	<b>ġd8</b>
75	c7+	



Without the knight and black pawn, \$\ddots c8\$ would be a draw, since the only way (\$\ddots c6\$) white can protect the pawn would lead in a stalemate. But here white can always lose a tempo with a knight

move, and ask black to make another move. So, black simply gives up.

<b>75</b>	• • •	<b>∲d7</b>
<b>76</b>	<b>∲b7</b>	<b>ģe6</b>
77	c8 <b></b> +	<b>⊉e5</b>
<b>78</b>	<b>豐h3</b>	<b>∲f4</b>
<b>79</b>	豐×h2+	<b>∲f3</b>
80	<b>₩h3</b> +	

Final note. Ethereal follows the quickest distance to zero in tablebase win positions. 80. \$\displace{c}\$ c6 would have delivered the mate one move earlier.

80	•••	<b>⋭</b> ×f2
81	<b>Ġ</b> b6	<b>⊈</b> e2
82	<b>堂</b> c5	<b>∲</b> f2
83	<b>Ġ</b> d4	<b>ģg1</b>
84	<b>Ġd3</b>	<b>∲</b> f2
85	₩g4	<b>∲f1</b>
86	<b>∲e3</b>	<b>ģe1</b>
87	<b>₩g1</b> #	

White wins.