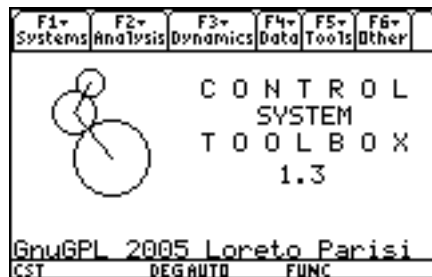


Control System Toolbox

for TI-89



release 1.3

The CST Reference Guide

First Edition October 2005

Gnu GPL 2002-2005 Loreto Parisi

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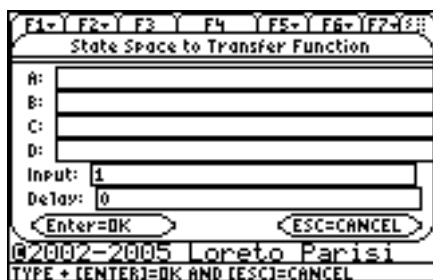
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Systems



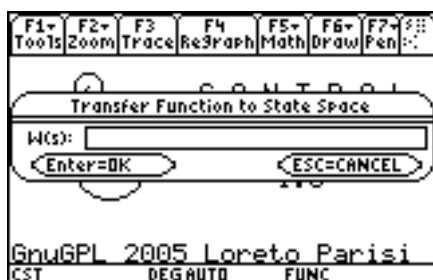
The **Systems** menu (F1) contains all the functions to build the model, using state-space or transfer function and to perform conversions from one representation to another, even from continuous time to discrete time model.



ss2tf(A,B,C,D,iu)

Gives transfer function $W(s)=C(sI-A)^{-1}B+D$ from state-space $\dot{x} = Ax + Bu$, $y = Cx + Du$, relating to input iu (it works on MIMO systems, but only one input at time).

Delay τ is the Time Delay $e^{-\tau s}$.



tf2ss(SYS)

Convert transfer function $W(s)$ in the state-space representation $\dot{x} = Ax + Bu$, $y = Cx + Du$, using the observability canonical form.

Delay τ is the Time Delay $e^{-\tau s}$.



tf(NUM,DEN)

Calculates transfer function, where NUM and DEN are LIST of coefficients of numerator's and denominator's polynomial: NUM={ b_0, b_1, \dots, b_n }, DEN={ a_0, a_1, \dots, a_n }, so

$$W(s) = \frac{b_0 s^n + b_1 s^{n-1} + \dots + b_n}{a_0 s^n + a_1 s^{n-1} + \dots + a_n}.$$

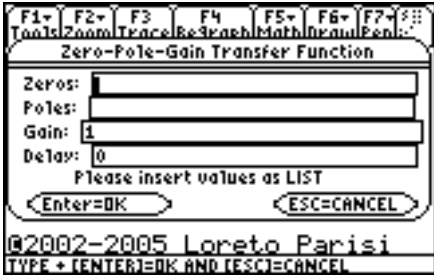
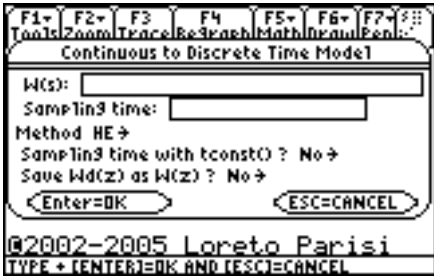
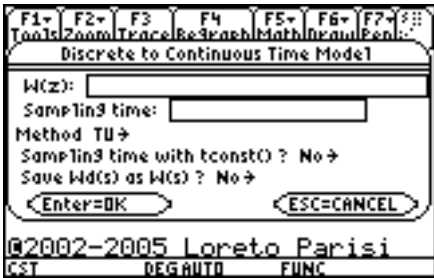
Delay τ is the Time Delay $e^{-\tau s}$.



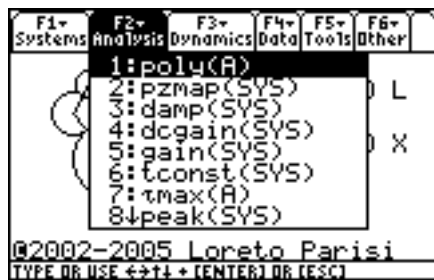
tf(SYS)

Calculates transfer function from a rational expression in s

Delay τ is the Time Delay $e^{-\tau s}$.

	<p><i>zpk(Z,P,G)</i> Calculates transfer function $W(s)$ in the zeros-poles-gain representation, where Z, P are LIST of zeros of numerator and denominator (poles), while G is NUM and represents constant gain K.</p> <p>Control's Toolbox v.1.16 author: Francesco Orabona E-mail: bremen79@infinito.it Home: http://web.genie.it/utenti/b/bremen79/</p>
	<p><i>c2d(SYS,T_c)</i> Converts continuous time model SYS to the discrete time model, using sample time T_c and different methods: HE (Linear Hold Equivalence), TU (Bilinear Tustin), BE (Bilinear Backward Eulero), FE (Bilinear Forward Eulero). Can use function <code>tconst(SYS)</code> to determinate sample time T_c. Use function <code>sampler(A,B,T_c)</code> to use ZOH method. Can save the resulting discrete time model $W_d(z)$ as current discrete transfer function $W(z)$.</p>
	<p><i>d2c(SYS,T_c)</i> Converts discrete time model SYS (in z) to the continuous time model, using sample time T_c and different methods: HE (Linear Hold Equivalence), TU (Bilinear Tustin), BE (Bilinear Backward Eulero), FE (Bilinear Forward Eulero). Can use function <code>tconst(SYS)</code> to determinate sample time T_c. Can save the resulting continuous time model $W_d(s)$ as current continuous transfer function $W(s)$.</p>

Analysis



The **Analysis** menu (F2) contains all the tools to analyze the model you have created with Systems' tools. You can also analyze different models, using different SYS at time.

This will not change current transfer function.



poly(A)

This function calculates characteristic polynomial of matrix A, as $p(s) = |sI - A|$, where $|\bullet|$ is determinat of a matrix.



pzmap(SYS)

This function calculates poles and zeros of given transfer function SYS, where poles are zeros of denominator of SYS.



damp(SYS)

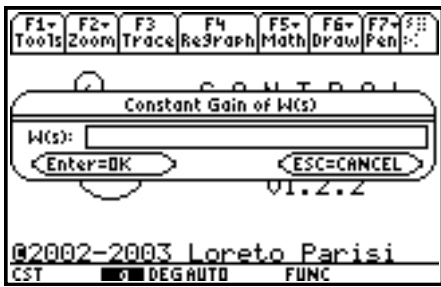
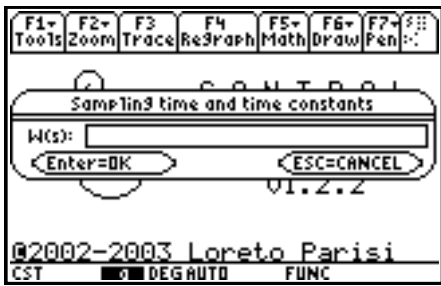
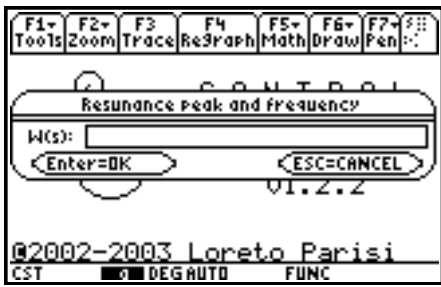

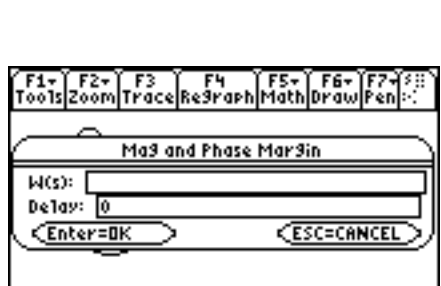
Calculate natural frequencies ω_{nh} and damping factors ζ_h for transfer function SYS, where $\omega_{nh} = \sqrt{\alpha_h^2 + \omega_h^2}$ and

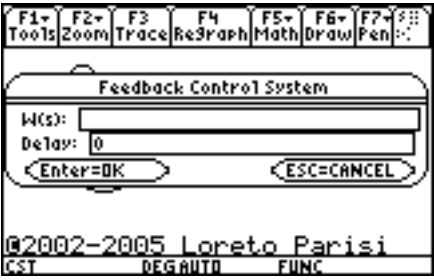
$$\zeta_h = \frac{-\alpha_h}{\omega_{nh}} \text{ for eigenvalue } \lambda_h = \alpha_h + j\omega_h.$$



dcgain(SYS)

Calculates d.c. gain G for transfer function SYS, as $G = \lim_{s \rightarrow 0} W(s)$.

	<p>gain(SYS) Calculates constant gain K for transfer function SYS, as $K = \lim_{s \rightarrow 0} s^{n_0 - m_0} W(s)$, where n_0 and m_0 are multiplicity of zero roots for denominator and numerator.</p>
	<p>tconst(SYS) Calculates sample time T_c and time constants τ_i, τ_h, and T_h, where $\tau_i = -\frac{1}{\lambda_i}$, $\tau_h = -\frac{1}{\alpha_h}$ and $T_h = \frac{2\pi}{\omega_h}$, while $T_c = 0.1 \min\{\tau_i, \tau_h, T_h\}$.</p>
	<p>peak(SYS) This function uses a proprietary numerical algorithm to calculate resonance peak $M_p = \max_{\omega} M(\omega)$, where $M(\omega) = W(s) _{s=j\omega}$ and relating frequency f_r, which is $M(2\pi f_r) = M_p$.</p>
	<p>tmmax(A) Calculates maximum time constant for characteristic polynomial of matrix A, in continuous or discrete time, where $\tau_{\max} = \frac{1}{\min(-\Re \lambda_i)}$ (continuous time) and $\tau_{\max} = \frac{1}{\min(\ln \lambda_i)}$ (discrete time).</p>
	<p>margin(SYS) Calculates Mag and Phase Margins. $K_m = 1 / W(i\omega_m)$ (Mag Margin) $\omega_m: \angle W(i\omega_m) = -180^\circ$ $\phi_m = 180^\circ - \phi_c$ (Phase Margin) $\omega_c: W(i\omega_c) = 1$ $\phi_c = \angle W(i\omega_c)$ (Critical Phase) $\tau_c = \phi_m / \omega_c * \pi / 180^\circ$ (Critical Time Constant)</p>

	<p><i>feedback(sys)</i> Performs the analysis and design of the closed loop control system of process SYS. Delay τ is the Time Delay $e^{-\tau s}$. Please see <i>Feedback Control Systems</i> section.</p>
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Dynamics

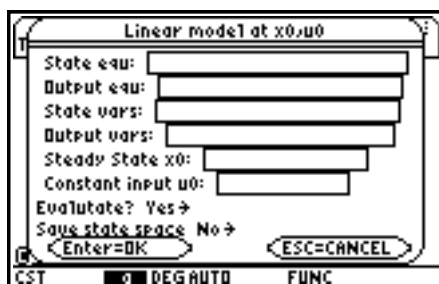


The **Dynamics** menu (F3) contains functions concerning dynamics of system for input, output and linearization of a non-linear model, frequency analysis with Bode and Nyquist diagrams and Root Locus yet.



trim(A,B,C,D,u₀)

This function calculates the steady state x_0 , relating to input u_0 for state-space $\dot{x} = Ax + Bu$, $y = Cx + Du$.



linmod(f,y,x,u,x₀,u₀)

This function calculates linear model for non-linear model assigned in terms of input equations f , such as $f=\{f_1(x,u),\dots,f_n(x,u)\}$ and output equations y , such as $y=\{y_1(x,u),\dots,y_n(x,u)\}$, relating to constant input u_0 and steady state x_0 . The jacobian matrixes can be evaluated in x_0, u_0 and the state-space can be saved, or can be calculated in a symbolic way, before being evaluated.



bodex(SYS)

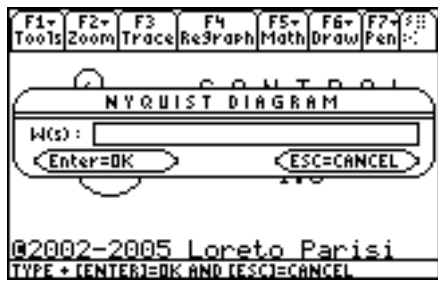
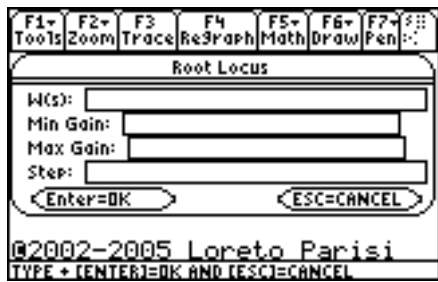


This program, made by 92BROTHERS, plots Bode diagrams of phase and magnitude and offers several tools to work with the plotted diagrams.


BodeX v.2.2.3

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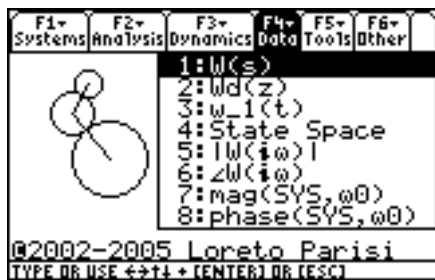
Home: <http://www.92brothers.net/>

	<p><i>nyquist(SYS)</i> Plots Nyquist diagram of SYS</p> <p>Control Toolbox v1.16 Author: Francesco Orabona E-mail: bremen79@infinito.it Home: http://web.genie.it/utenti/b/bremen79/</p>
	<p><i>rlocus(SYS)</i> Plots the Root Locus of SYS Max, min gain are the extremes of the gain list.</p> <p>Porting for CST: Loreto Parisi Control Toolbox v1.16 Author: Francesco Orabona E-mail: bremen79@infinito.it Home: http://web.genie.it/utenti/b/bremen79/</p>
	<p><i>step(SYS)</i> This tool calculates the step response for SYS, as $U * w_{-1}(t) = L^{-1}(W(s)U/s)$, with amplitude U. Needs the tool LZT to perform symbolic calculation of Laplace direct and inverse transformation.</p> <p>LZT r7 Author: Jiri Bazant Email: georger@razdva.cz Home: http://www.razdva.cz/georger/</p>
	<p><i>pstep(SYS)</i> Calculates characteristic parameter of step response for transfer function SYS, such as T_e, T_a, T_s, T_p and s. Step response $w_{-1}(t)$ can be specified or calculated with step(SYS). Needs the tool LZT to perform symbolic calculation of Laplace direct and inverse transformation.</p>

	<p><i>gstep(w_1(t))</i></p> <p>This tool plots the step response $w_1(t)$ calculated with <code>step(SYS)</code> or specified directly. Can use <code>pstep(SYS)</code> to evaluate $w_1(t)$ around its typical parameters.</p>
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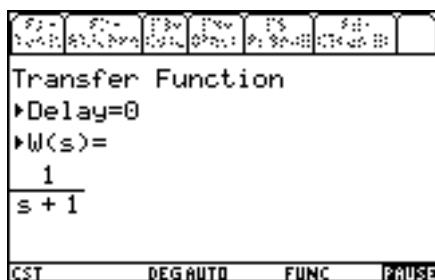
Notes.

1. About *pstep(SYS)*. Calculates time domain parameters of the step response for transfer function `SYS`, such as T_e , T_a , T_s , T_p and s , where T_e is the Elongation Time, T_r is the Raise Time, T_s is the Delay Time and s is the elongation.

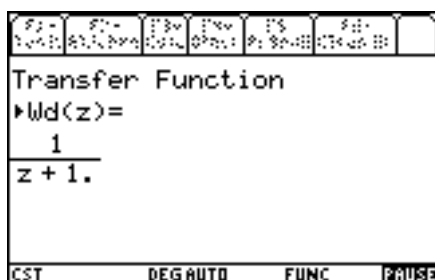
Data

The **Data** menu (F4) gives access to current transfer function $W(\bullet)$ ¹, its discrete model $Wd(\bullet)$, the step response $w_1(\bullet)$, the current state space and magnitude and phase of $W(\bullet)$.

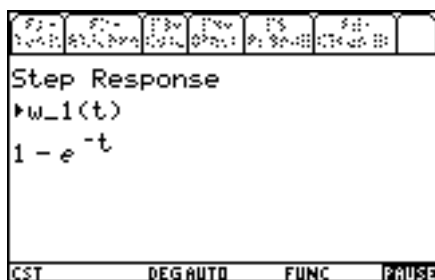
¹ According to current Time Domain Settings (see Other menu)

 **$W(s)$ [$W(z)$]**

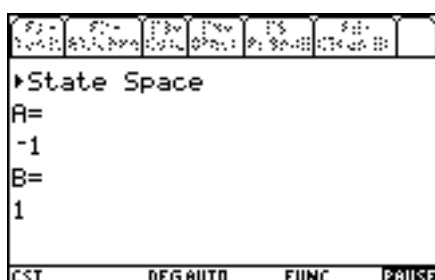
Displays the current transfer function. SYS refers to it in all calculations of current session of CST, once you've calculated it with one of the tools of Systems menu.

 **$Wd(z)$ [$Wd(s)$]**

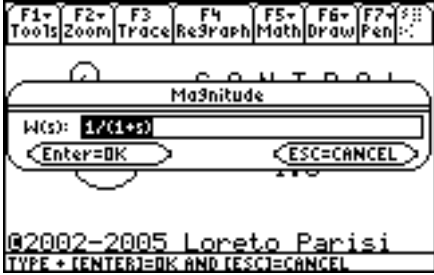
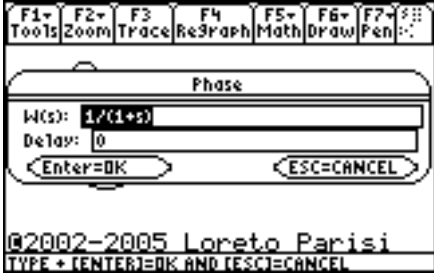


The discrete transfer function $Wd(z)$ [$Wd(s)$], obtained by $c2d(SYS,Tc)$ [$d2c(SYS,Tc)$] using the current transfer function $W(s)$ [$W(z)$] or by $sampler(A,B,Tc)$ using the current state space.

 **$w_1(t)$ [$w_1(k)$]**

Shows the current step response obtained with $step(SYS)$.

**State Space**

It displays the current state space, as defined from one of tools of System menu.

	<p>$W(\omega)$</p> <p>Displays magnitude of transfer function $W(\bullet)$ in Laplace domain (for $W(s)$) and even in domain Z (for $W(z)$).</p>
	<p>$\angle W(\omega)$</p> <p>Displays phase of transfer function $W(\bullet)$ in Laplace domain (for $W(s)$) and even in domain Z (for $W(z)$).</p>
	<p>$mag(SYS, \omega_0)$</p> <p>Calculates magnitude of SYS in Laplace domain (for $W(s)$) and even in domain Z (for $W(z)$), relating to ω_0.</p>
	<p>$phase(SYS, \omega_0)$</p> <p>Calculates phase of SYS in Laplace domain (for $W(s)$) and even in domain Z (for $W(z)$), relating to ω_0.</p>

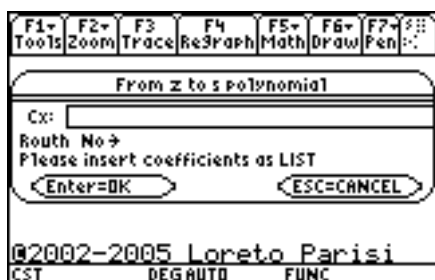
Tools



The **Tools** menu (F5) offers several useful functions to complete the analysis of the model you're working and to give more detailed information about it. Moreover presents different tools for discrete systems and finite state systems.

***cpoles(Cx)***

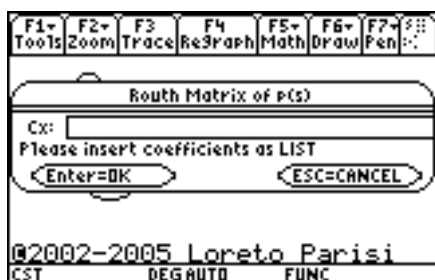
It calculates zeros of polinomyal given as LIST of coefficients, Cx.

***polyz2s(Cx)***






This tool calculates the continuous polynomial $q(s)$, relating to discrete polynomial $p(z)$, assigned in terms of its coefficients LIST, Cx, using the formula

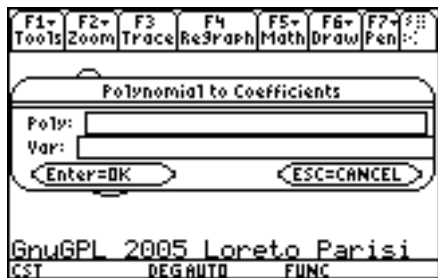




$$q(s) = (s-1)^n p(z) \Big|_{z=\frac{s+1}{s-1}}$$
***band(SYS)***


This function uses a numerical algorithm and several preexistent formulas to calculate bandwith of system with transfer function SYS. It calculates f_i , f_s , where $B=[f_i, f_s]$, f_r (resonance frequency) and M_p (resonance peak).

***routh(Cx)***

It calculates the Routh matrix for polynomial assigned with its coefficients LIST, Cx.

	<p><i>routhc(Cx)</i> Applies Routh Criterion to parametric $W(s)$ to obtain Routh conditions using the specified parameter.</p>
	<p><i>pade(n,τ)</i> Calculates the delay Padé approximation. Resulting delay transfer function can be saved as the current continuous transfer function $W(s)$.</p>
	<p><i>eigev(A)</i> It calculates eigenvalues and eigenvectors of matrix A.</p>
	<p><i>spectre(A)</i> This tool calculates the spectral decomposition of matrix A, even in the continuous (e^{At}) and in the discrete time (A^k), relating to real eigenvalues and complex eigenvalues.¹</p>
	<p><i>sampler(A,B,Tc)</i> This function performs the discrete time conversion of continuous time model with state-space $\dot{x} = Ax + Bu$ at sample time T_c, using the ZOH (Zero Order Hold) method. It permits to use sample time T_c calculated with function $tconst(SYS)$ for current transfer function SYS. It can save the resulting discrete transfer function $Wd(z)$.</p>

	<p><i>poly2cof(expr,var)</i> Gives the LIST of coefficients of the polynomial given in expr in the variable var.</p> <p>Control's Toolbox v.1.16 Author: Francesco Orabona E-mail: bremen79@infinito.it Home: http://web.genie.it/utenti/b/bremen79/</p>
	<p><i>rts2poly(roots)</i> Builds the polynomial with roots assigned as LIST.</p> <p>Author: Chadd L. Easterday Email: easterday@mindspring.com</p>
	<p><i>laplace(f(t))</i> Performs Laplace Transformation of f(t) Needs the tool LZT to perform symbolic calculation.</p> <p>LZT r7 Author: Jiri Bazant Email: georger@razdva.cz Home: http://www.razdva.cz/georger/</p>
	<p><i>ilaplace(F(s))</i> Performs Inverse Laplace Transformation of F(s). Needs the tool LZT to perform symbolic calculation.</p> <p>LZT r7 Author: Jiri Bazant Email: georger@razdva.cz Home: http://www.razdva.cz/georger/</p>
	<p><i>zeta(f(k))</i> Performs Zeta Transformation of f(k) Needs the tool LZT to perform symbolic calculation.</p> <p>LZT r7 Author: Jiri Bazant Email: georger@razdva.cz Home: http://www.razdva.cz/georger/</p>

	<p>izeta(F(z)) Performs Inverse Zeta Transformation of F(z). Needs the tool LZT to perform symbolic calculation.</p> <p>LZT r7 Author: Jiri Bazant Email: georger@razdva.cz Home: http://www.razdva.cz/georger/</p>
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Notes.¹ About *spectre(A)*

The spectral decomposition of matrix A is

$$e^{At} = \sum_{i=1}^{\mu} u_i e^{\lambda_i t} v_i^T + \sum_{h=1}^{\nu} (u_{ha} \quad u_{hb}) e^{\alpha_h t} \begin{pmatrix} \cos \omega_h t & \sin \omega_h t \\ -\sin \omega_h t & \cos \omega_h t \end{pmatrix} \begin{pmatrix} v_{ha}^T \\ v_{hb}^T \end{pmatrix} \quad (\text{continuous})$$

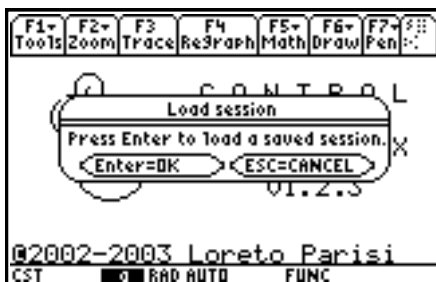
$$A^k = \sum_{i=1}^{\mu} u_i \lambda_i^k v_i^T + \sum_{h=1}^{\nu} (u_{ha} \quad u_{hb}) \rho_h^k \begin{pmatrix} \cos \theta_h k & \sin \theta_h k \\ -\sin \theta_h k & \cos \theta_h k \end{pmatrix} \begin{pmatrix} v_{ha}^T \\ v_{hb}^T \end{pmatrix} \quad (\text{discrete})$$

relating to real μ eigenvalues λ_i and 2ν complex eigenvalues $\lambda_h = \alpha_h \pm j\omega_h = \rho_h e^{\pm j\theta_h}$ and the relating eigenvector u_i and $u_h = u_{ha} \pm u_{hb}$.

Other

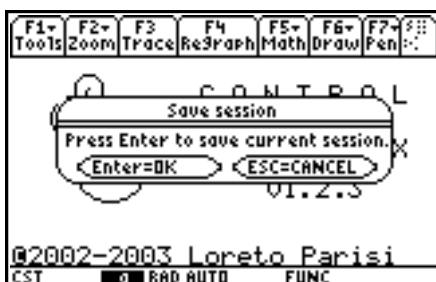


The **Other** menu (F6) gives tools to manage files, the current working session, the Settings, to access to on-line help tool with help(), some information about CST, and the way to exit CST.



Quick Load

Loads the current working session (i.e. transfer functions $W(s)$ and $W(z)$, State space, $w_1(t)$, T_c , step response parameters, etc.) previously saved. It overwrites all the existing values for the current session. Be careful.



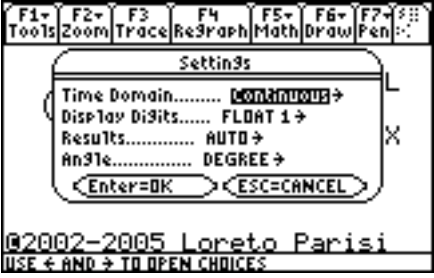
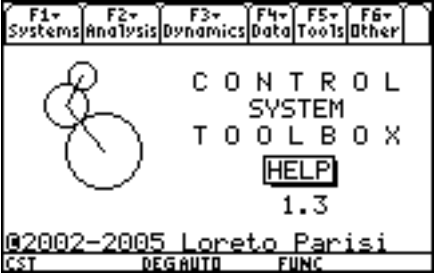


Quick Save

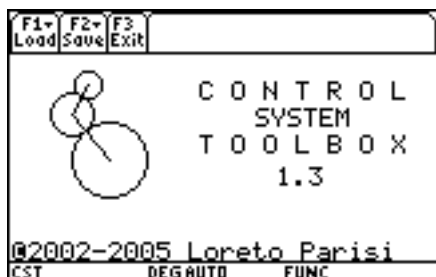
Saves the current working session (i.e. transfer functions $W(s)$ and $W(z)$, State space, $w_1(t)$, T_c , step response parameters, etc.).



File...

The File toolbox gives access to the File & Session Management. Here you can load and save the current working session, the State Space, the Transfer Function, the Step Response and bode diagram obtained with bode(SYS). There are three menus Load, Save and Exit. Exit menu (F3) brings to the previous toolbox.

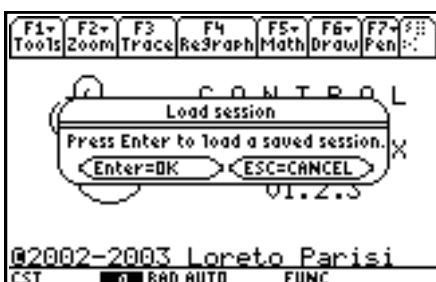
	<p>Settings</p> <p>It permits to modify some settings of the calculator, such as the display digits, the angle, the format of results and to switch the current Time Domain: Continuous to work with continuous time model $W(s)$ or Discrete to work with discrete time model $W(z)$ in the same working session.</p>
	<p>help()</p> <p>Starts the help tool. To get help, simply choose a function from one of the menus and you'll get some information about it.</p>
	<p>About</p> <p>Gives the current version of CST for TI-89, the way to contact the author and to obtain support and upgrades.</p>
	<p>Exit</p> <p>To close Control System Toolbox for TI-89. All previous settings of the calculator will be restored. Prompts for non-saved working session.</p>

File

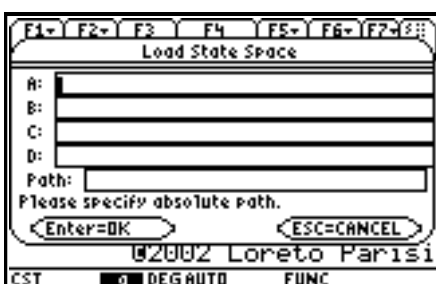
The **File** toolbox gives access to the File & Session Management. Here you can load and save the current working session, the State Space, the Transfer Function, the Step Response and bode diagram obtained with `bodex(SYS)`. There are three menus Load, Save and Exit. Exit menu (F3) brings to the previous toolbox.

**Load**

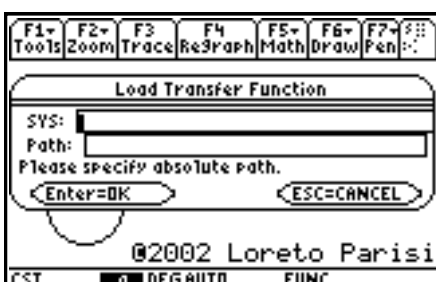
The Load menu (F1) permits to load the current working session, the State Space, Transfer Function, Step Response and bode diagrams from the specified path.

**Load Session**




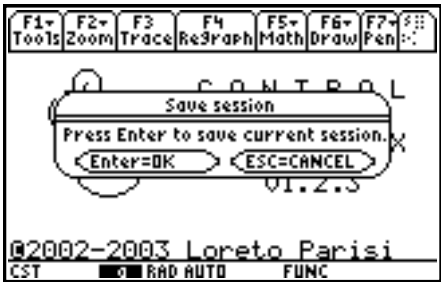
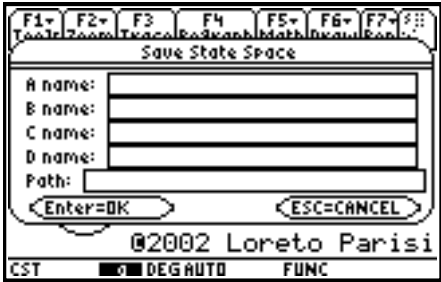
Loads the current working session (i.e. transfer functions $W(s)$ and $W(z)$, State space, $w_1(t)$, T_c , step response parameters, etc.) previously saved. It overwrites all the existing values for the current session. Be careful.

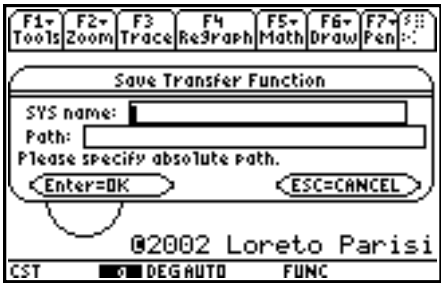

**Load State Space**

To load state space matrixes A,B,C,D from specified path. Please use absolute path. For example, if your dynamic matrix A is stored in main as dyn, you have to input dyn in A input field and main as path. All matrixes should be in the same path.

**Load Transfer Function**

Permits to load Transfer Function from specified path.

	<p>Load Step Response</p> <p>Permits to load the Step Response from specified path.</p>
	<p>Load Bode diagram</p> <p>This tools permits to load a picture stored in CST folder. It's aid is in displaying Bode plots, created with bodex() first, and estimating the diagrams in a assigned frequency ω_0.</p>
	<p>Save</p> <p>The Save menu (F2) permits to save the current working session, the State Space, Transfer Function, Step Response into a specified path.</p>
	<p>Save session</p> <p>Saves the current working session (i.e. transfer functions $W(s)$ and $W(z)$, State space, $w_1(t)$, T_c, step response parameters, etc.).</p>
	<p>Save State Space.</p> <p>Permits to save current State Space into the specified path, using given names.</p>

	<p><i>Save Transfer Function.</i></p> <p>To save current transfer function into the specified path, using given name. The current SYS results from Data menu (F4).</p>
	<p><i>Save Step Response.</i></p> <p>To save current step response into the specified path, using give name. The current step results from Data menu (F4).</p>

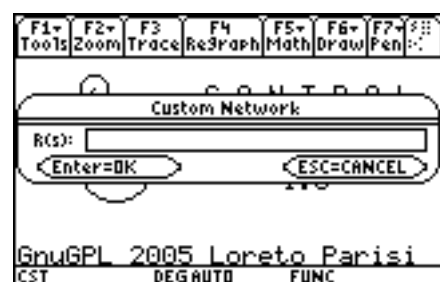
Controller



The **Controller** menu (F1) is intended to design and tuning the control system.



The **Controller Design** wizard will guide you through the full design of the network's controller. First step is to choose the *network structure* from the following types: Custom (i.e. user defined), P, PI, PD, PID, Lead, Lag and Lead-Lag networks.



Custom Network

Defines your own custom network's controller R(s).



P Controller

Defines a proportional controller $R(s) = K_p$.

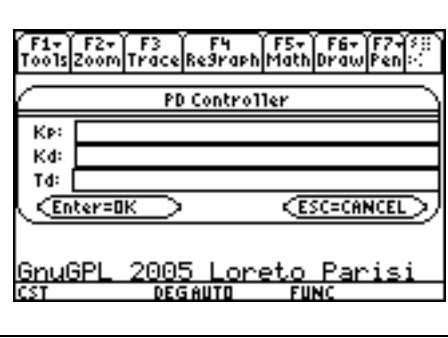
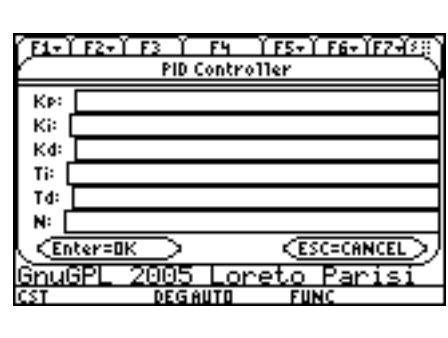
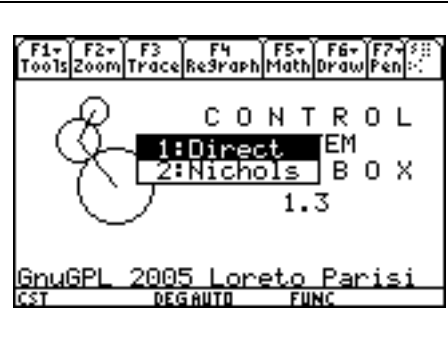
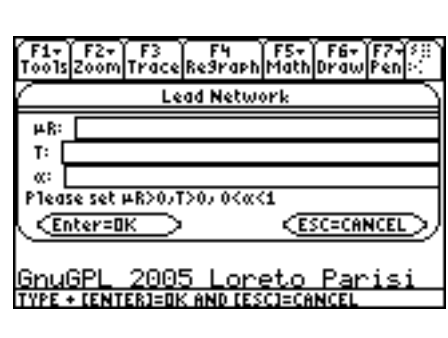
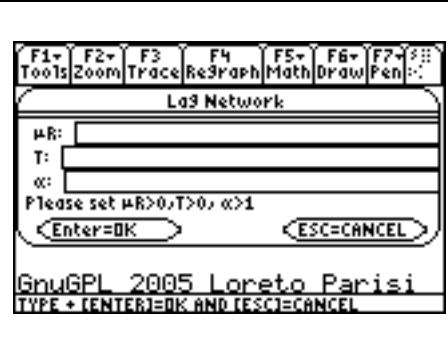


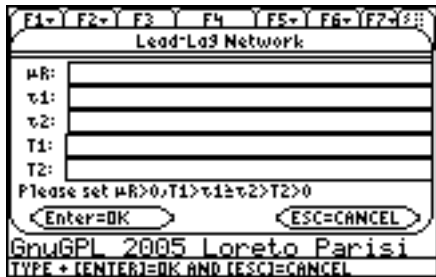
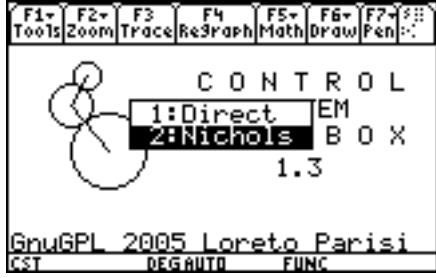
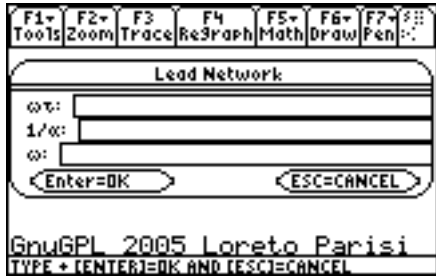
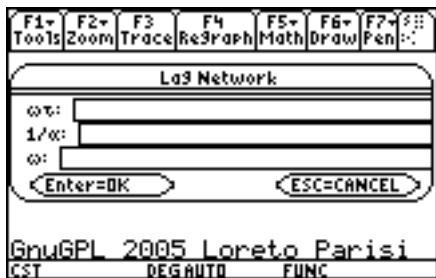

PI Controller

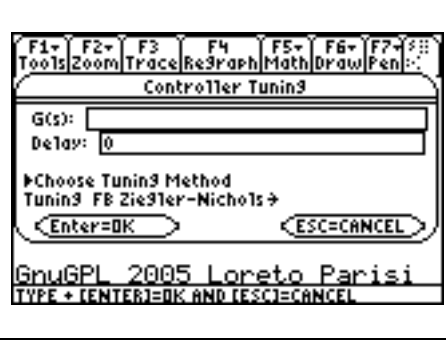
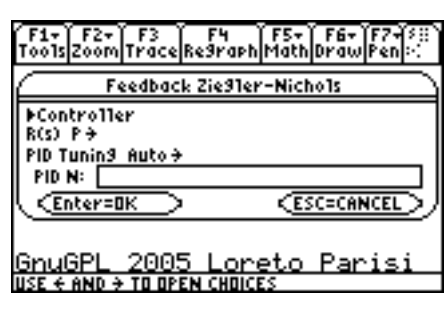
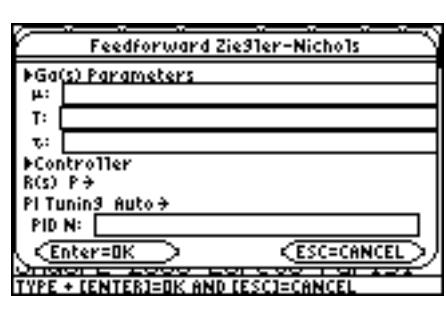
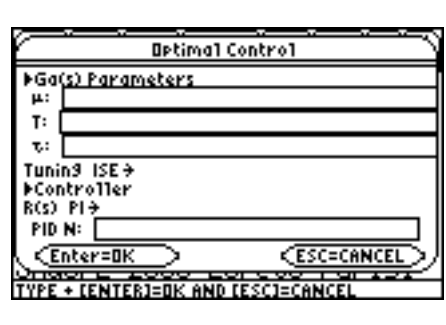
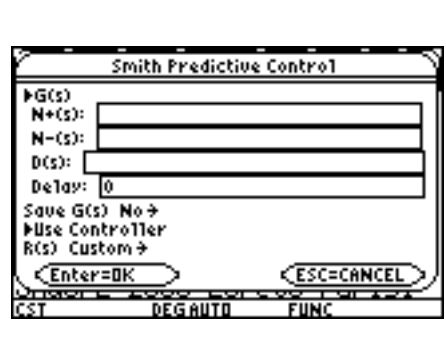
Defines a PI controller R(s) as you give K_p and K_i or K_p and T_i :

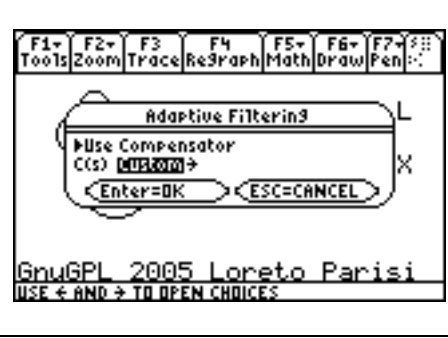
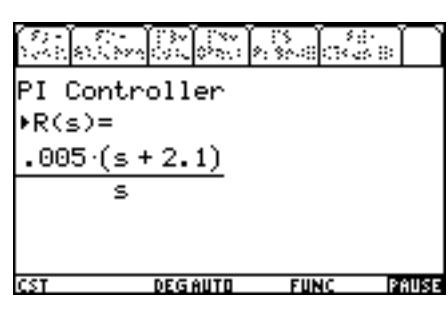
$$R_{PI}(s) = \frac{K_p s + K_i}{s} = K_p \frac{1 + T_i s}{T_i s}$$

$$\text{where } T_i = \frac{K_p}{K_i}$$

	<p>PD Controller Defines a PD controller $R(s)$ as you give K_p and K_d or K_p and T_d:</p> $R_{PD}(s) = K_p + K_D s = K_p (1 + T_D s)$ <p>where $T_D = \frac{K_D}{K_p}$</p>
	<p>PID Controller Defines a standard PID controller as you give K_p, K_i, K_d or K_p, T_i, T_d:</p> $R_{PID}(s) = \frac{K_D s^2 + K_p s + K_I}{s} = K_p \frac{T_I T_D s^2 + T_I s + 1}{T_I s}$ <p>or a real PID controller specifying N:</p> $R_{PID}(s) = K_p + \frac{K_I}{s} + \frac{K_D s}{1 + \frac{K_D}{K_p N} s} = K_p \left(1 + \frac{1}{T_I s} + \frac{T_D}{1 + \frac{T_D}{N} s} s \right)$
	<p>Direct Design Defines a Lead, Lag or Lead-lag network directly from transfer function's gain μ_R, time constant T and α parameter.</p>
	<p>Lead Network Defines a lead network $R(s)$ as you give the gain μ_R, time constant T and parameter α:</p> $R(s) = \mu_R \frac{1 + Ts}{1 + \alpha Ts}$ <p>Must be: $\mu_R > 0, T > 0, 0 < \alpha < 1$</p> <p>Usually, $\alpha = 0.1$ and $T = \frac{1}{\omega_c}$</p>
	<p>Lag Network Defines a lag network $R(s)$ as you give the gain μ_R, time constant T and parameter α:</p> $R(s) = \mu_R \frac{1 + Ts}{1 + \alpha Ts}$ <p>Must be: $\mu_R > 0, T > 0, \alpha > 1$</p> <p>Usually, $T > \frac{1}{\omega_c}$ ($T = \frac{10}{\omega_c}$)</p>

	<p>Lead-Lag Network</p> <p>Defines a lead-lag network $R(s)$ as you give the gain μ_R, and time constants τ_1, τ_2, T_1, T_2:</p> $R(s) = \mu_R \frac{(1 + \tau_1 s)(1 + \tau_2 s)}{(1 + T_1 s)(1 + T_2 s)}$ <p>Must be:</p> $\mu_R > 0, T_1 > \tau_1 \geq \tau_2 > T_2 > 0$ <p>Usually, $T_1 T_2 = \tau_1 \tau_2, \tau_2 > \frac{1}{\omega_c} > T_2$</p>
	<p>Nichols Design</p> <p>Defines a Lead, Lag or Lead-lag network using Nichols's standard networks parameters $\omega\tau, 1/\alpha$ at ω_0. In most cases ω_0 will be the critical frequency ω_c.</p>
	<p>Lead Network</p> <p>Defines a Lead network using Nichols's standard networks parameters $\omega\tau, 1/\alpha$ at ω_0.</p> $R(s) = \frac{1 + s\tau}{1 + s\alpha\tau}$
	<p>Lag Network</p> <p>Defines a Lag network using Nichols's standard networks parameters $\omega\tau, 1/\alpha$ at ω_0.</p> $R(s) = \frac{1 + s\alpha\tau}{1 + s\tau}$
	<p>Lead-Lag Network</p> <p>Defines a Lead-Lag network using Nichols's standard networks parameters $\omega\tau_1, 1/\alpha_1$ for the lead and $\omega\tau_2, 1/\alpha_2$ for the lag network at frequency ω_0.</p> $R(s) = \frac{1 + s\tau_1}{1 + s\alpha_1\tau_1} \frac{1 + s\alpha_2\tau_2}{1 + s\tau_2}$

	<p>Controller Tuning</p> <p>The Controller Tuning wizard will guide you through the tuning of the network's controller $R(s)$ for the given process $G(s)$ and its delay. First choose the tuning method from ones available: <i>Feedback Ziegler-Nichols</i>, <i>Feedforward Ziegler-Nichols</i>, <i>Optimal Control</i>, <i>Predictive Control</i> and <i>Adaptive Filtering</i>.</p>
	<p>Feedback Ziegler-Nichols</p> <p>Uses the <i>Closed Loop Ziegler-Nichols</i> method to tune the controller for the feedback network. Choose the desired structure for $R(s)$ – P, PI or PID. Only for PIDs, choose the assignment method for gain and phase margins (Auto, assign Gain Margin or assign Phase Margin) and the parameter N if you wish to use a real PID controller, instead of a standard PID controller.</p>
	<p>Feedforward Ziegler-Nichols</p> <p>Uses the <i>Open Loop Ziegler-Nichols</i> method to tune the controller for the approximate process (obtained from the step response using the <i>areas method</i>)</p> $G_a(s) = \frac{\mu}{1 + Ts} e^{-\tau s}$ <p>Choose the structure (P, PI or PID) for $R(s)$ and for PIs only the assignment method for the phase margin (Auto, assign Phase Margin).</p>
	<p>Optimal Control</p> <p>Uses optimization methods to tune the controller $R(s)$: ISE (<i>Integral Square Error</i>), ISTE (<i>Integral Square Time Error</i>) and IST²E (<i>Integral Square Time² Error</i>). K_p, T_i and T_d are defined by a table as follows:</p> $K_p = \frac{a_1}{\mu} \theta^{b_1}, T_i = \frac{T}{a_2 + b_2 \theta}, T_d = a_3 T \theta^{b_3}$
	<p>Smith Predictive Control</p> <p>Used to tune network's controllers for processes with positive real zeros or time delays. The process $G(s)$ is given as $G(s) = \frac{N^-(s)N^+(s)}{D(s)} e^{-\tau s}$. The predictor $P(s)$ and the network transfer function $L'(s)$ for the given controller $R(s)$ are $P(s) = \left(1 - \frac{N^+(s)}{N^+(-s)} e^{-\tau s}\right) \frac{N^-(s)N^+(-s)}{D(s)}$ and $L'(s) = (G(s) + P(s))R(s)$.</p>

	<p>Adaptive Filtering</p> <p>Uses a pre-filtering technique (compensation of input signal) to improve static and dynamic behaviour. You have to choose the structure for the compensator $C(s)$. We suppose you have defined it as a controller (custom, lead, lag or lead-lag) yet.</p>
	<p>Custom, P, PI, PD, PID, Lead, Lag, Lead-Lag</p> <p>Shows the controller defined for that structure. Note that you have to choose the controller first to perform the analysis, but it's possible to define (design or tuning) more controllers, then choose one of them as the current $R(s)$.</p>

Network



The **Network** menu (F2) permits to design and analyse the control system, calculating gain and phase margins, and the network transfer functions.



Network Design

Define the process $G(s)$ and its delay, the controllers $R_0(s)$ and $R(s)$.



Network Design

Use the inner loop transfer function $F(s)$ as $G(s)$ in the unstable processes control systems. Now you can tune the controller against the inner closed loop transfer function. See notes for more informations.



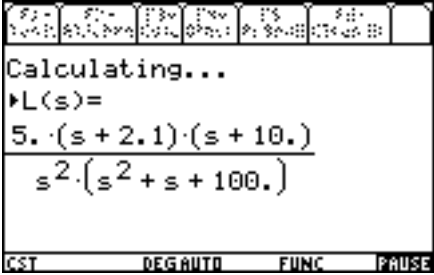
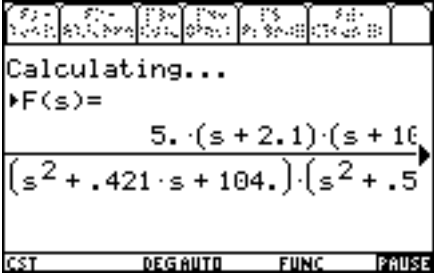
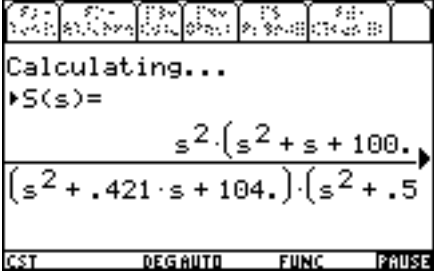
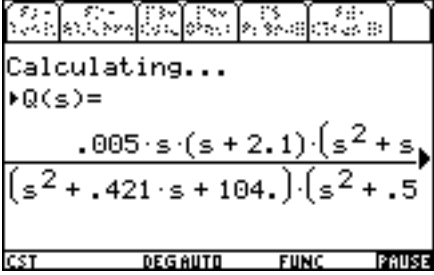
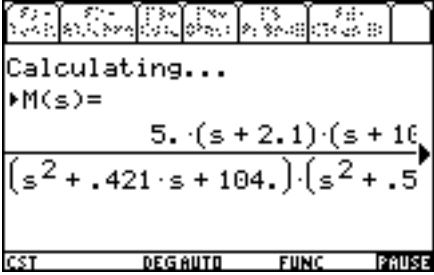
Network Design

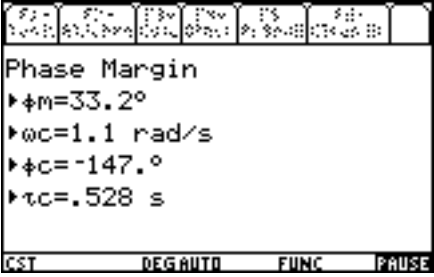
Choose the controller $R_0(s)$ between custom, proportional, lead or lag structures. Generally, use it to satisfy static requirements.



Network Design

Choose the controller $R(s)$ between all structures available to satisfy dynamic requirements.

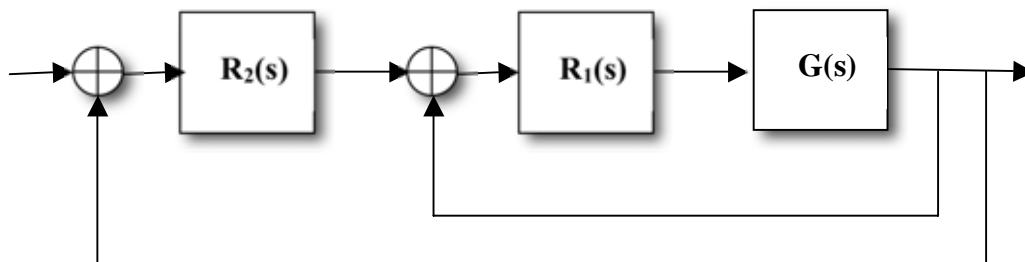
	<p>$L(s)$ The network transfer function</p> $L(s) = R(s)G(s)$
	<p>$F(s)$ The network transfer function</p> $F(s) = \frac{R(s)G(s)}{1 + R(s)G(s)}$
	<p>$S(s)$ The network transfer function</p> $S(s) = \frac{1}{1 + R(s)G(s)}$
	<p>$Q(s)$ The network transfer function</p> $Q(s) = \frac{R(s)}{1 + R(s)G(s)} = F(s)G(s)^{-1} = R(s)S(s)$
	<p>$M(s)$ The network transfer function</p> $M(s) = G(s)S(s)$

	<p>Analysis</p> <p>Performs an analysis of the defined control system, calculating the Gain and the Phase margins.</p>
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Notes.

About *Network Design*.

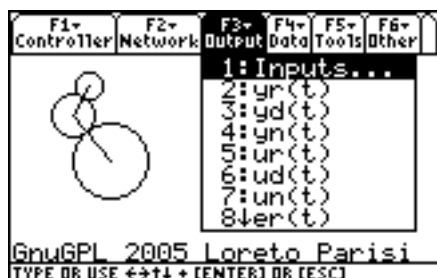
1. When $G(s)$ is such an unstable process, we'll use a block model with a inner control loop, like the block diagram below.



And we'll tune $R_1(s)$ to stabilize $G(s)$ and $R_2(s)$ against $F(s) = \frac{R_1(s)G(s)}{1 + R_1(s)G(s)}$ to satisfy

given requirements. To do so, first design $R_1(s)$ as usual. When the inner closed loop is stable, you can design $R_2(s)$ choosing in *Network Design* **Use F(s)** as new $G(s)$ from the drop down menu.

Output



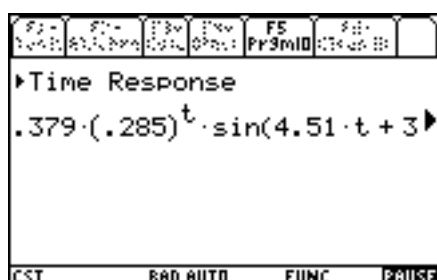
The **Output** menu (F3) permits to perform a time domain analysis of the closed loop system against inputs, noises and measure noise.



Inputs

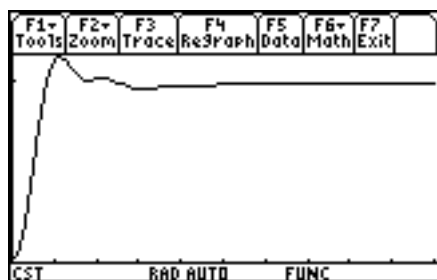
To set the input $r(t)$, noise inputs $d(t)$ and $d^*(t)$, and measure noise input $n(t)$.

To set a step input of amplitude K use K for $r(t)$. To set a sinusoidal measure noise, use $\sin(\omega t)$ as $n(t)$.



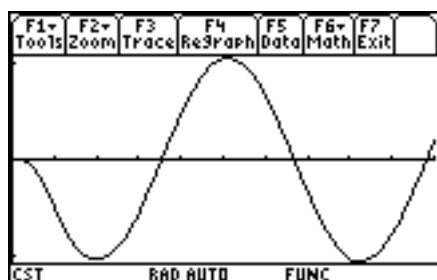
yr(t), yd(t), yn(t)

The output y time response against input $r(t)$, noise input $d(t)$ and measure noise input $n(t)$.



ur(t), ud(t), un(t)

The control variable u time response against input $r(t)$, noise input $d(t)$ and measure noise input $n(t)$.



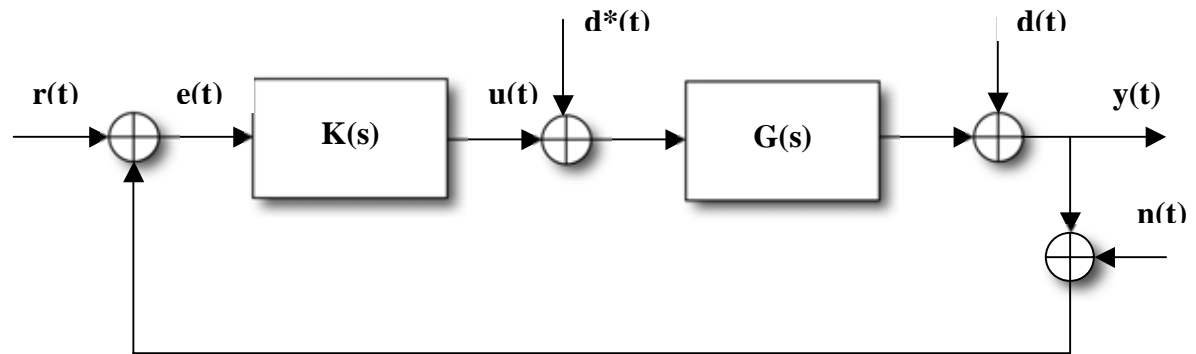
er(t), ed(t), en(t)

The error $e=r-y$ time response against input $r(t)$, noise input $d(t)$ and measure noise input $n(t)$.

Notes.

About *Output* menu.

1. We assume a Closed Loop Control System block model like that below.



2. We assume the following transfer functions.

$$\begin{bmatrix} Y(s) \\ U(s) \\ E(s) \end{bmatrix} = \begin{bmatrix} F(s) & S(s) & -F(s) \\ Q(s) & -Q(s) & -Q(s) \\ S(s) & -S(s) & F(s) \end{bmatrix} \cdot \begin{bmatrix} R(s) \\ D(s) \\ N(s) \end{bmatrix}$$

where

$$F(s) = \frac{K(s)G(s)}{1 + K(s)G(s)},$$

$$S(s) = \frac{1}{1 + K(s)G(s)},$$

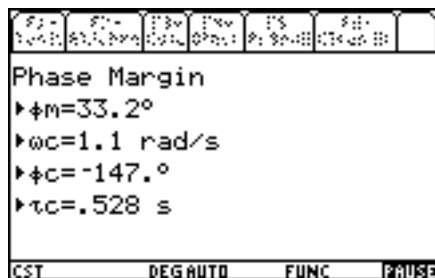
$$Q(s) = \frac{K(s)}{1 + K(s)G(s)},$$

and $Y^*(s) = M(s)D^*(s)$ where $M(s) = G(s) S(s)$.

Data



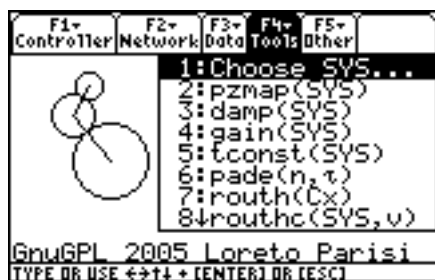
The **Data** menu (F3) shows detailed informations about the control system.



Margins

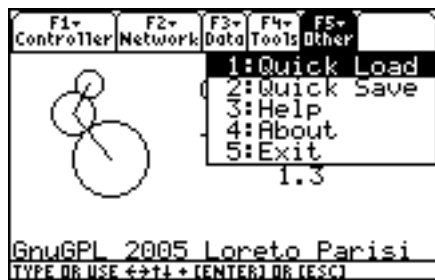
Shows the Gain and Phase margins of the control system.

Tools



The **Tools** menu (F4) permits you to perform a detailed analysis of transfer function SYS. You need to choose the current transfer function SYS first.

Other



The **Other** menu (F3) shows some help, info and permits to exit the program.



Quick Load

Loads the current working session (i.e. transfer functions of process, network and controllers, calculated margins, etc.) previously saved. It overwrites all the existing values for the current session. Be careful.



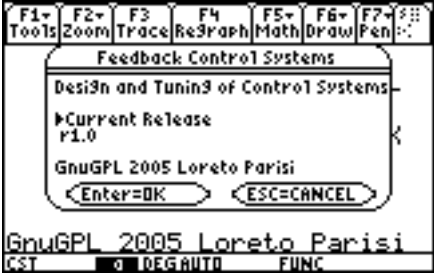
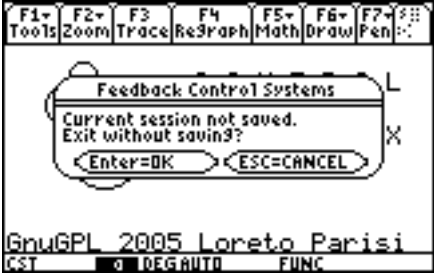
Quick Save

Saves the current working session (i.e. transfer functions of process, network and controllers, calculated margins, etc.).



Help

Shows some help.

	<p>About</p> <p>Shows some info.</p>
	<p>Exit</p> <p>Exit the program. Unsaved session will be lost.</p>