

The 1090 Megahertz Riddle

A Guide to Decoding and Interpreting ADS-B and
Other Mode S Signals

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This book is dedicated to my sons: William and Vincent

Contents

I	Getting started	8
1	Introduction	9
1.1	Background: the “death ray” that saves lives	9
1.2	The primary radar	10
1.3	The secondary radar	10
1.4	Mode S	12
1.5	ADS-B	16
1.6	Other Mode S services	16
1.7	Summary	17
2	Quick Start: Hardware and Software to Receive Mode S Data	19
2.1	Range	19
2.2	Antenna	20
2.3	Receiver	22
2.4	Software tools	22
II	Fundamental ADS-B Decoding	28
3	ADS-B Basics	29
3.1	Message structure	29
3.2	Capability	30
3.3	ICAO address	30
3.4	ADS-B message types	30
3.5	Example of ADS-B message structure	31
3.6	Availability and transmission rate	32
3.7	ADS-B versions	32
4	Aircraft Identification and Category	35
4.1	Identification (Call Sign)	35
4.2	Wake vortex category	36
4.3	Example	36
5	Airborne Position	38
5.1	A over-simplified example	39
5.2	Compact Position Reporting	41
5.3	Globally unambiguous position decoding	44
5.4	Locally unambiguous position decoding	48
5.5	Altitude decoding	51
5.6	Verification of decoded positions	52

6	Surface Position	53
6.1	Movement	53
6.2	Ground track	54
6.3	Position	54
6.4	Example	55
7	Airborne Velocity	61
7.1	Example messages	61
7.2	Vertical Rate	63
7.3	Difference between GNSS and barometric altitudes	64
7.4	Sub-type 1 and 2: Ground Speed decoding	65
7.5	Subtype 3 and 4: Airspeed decoding	67
8	Aircraft Operation Status	69
8.1	Version 0	69
8.2	Version 1	70
8.3	Version 2	71
9	Uncertainties in ADS-B	72
9.1	Terminology	72
9.2	Version 0	73
9.3	Version 1	75
9.4	Version 2	78
10	Error control in ADS-B	80
10.1	CRC error control	80
10.2	ADS-B parity	82
III	Advanced Mode S Decoding	84
11	Basics of Mode S services	85
11.1	Mode S message structures	85
11.2	Parity	86
11.3	ICAO address recovery	87
11.4	Two's complement coding	88
12	All-call reply	90
13	Surveillance replies	92
13.1	Message structure	92
13.2	Altitude code	93
13.3	Identity code	93
14	Airborne Collision Avoidance System	95
14.1	Background	95
14.2	ACAS with Mode C Transponders	95
14.3	ACAS with Mode S Transponders	96

14.4 Message fields of ACAS coordination messages	99
15 Comm-B replies	104
15.1 Structure	104
15.2 BDS	105
16 Mode S Elementary Surveillance	106
16.1 Data link capability report (BDS 1,0)	106
16.2 Common usage GICB capability report (BDS 1,7)	108
16.3 Aircraft identification (BDS 2,0)	110
16.4 ACAS active resolution advisory (BDS 3,0)	112
17 Mode S Enhanced Surveillance	115
17.1 Selected vertical intention (BDS 4,0)	115
17.2 Track and turn report (BDS 5,0)	118
17.3 Heading and speed report (BDS 6,0)	120
18 Mode S meteorological services	123
18.1 Meteorological routine air report (BDS 4,4)	123
18.2 Meteorological hazard report (BDS 4,5)	126
19 Inferencing of BDS codes	128
19.1 BDS codes identification logics	128
19.2 Identification of BSD 5,0 and 6,0	128
19.3 Examples	130
References	133

Preface

This book provides a practical guide to decoding ADS-B and other types of common Mode S messages. Firstly, it consolidates the information from various ICAO documentation to provide readers easy access to key knowledge of Mode S and ADS-B and related topics. Secondly, examples and sample Python code are used extensively in the book to explain the decoding process.

Back in 2015, I joined Delft University of Technology to undertake PhD research on analyzing and modeling aircraft performance using open aircraft surveillance data. ADS-B data served as my primary data source.

Frustrated with the lack of open literature on ADS-B and Mode S, I created a live online project to document my experience in decoding ADS-B data, the *ADS-B Decoding Guide*. As the guide grew in popularity, I started to receive questions, feedback, suggestions from the research community all over the world. These inputs greatly helped me to fix and improve the content of the decoding guide.

At the same time, I also started to incorporate Mode S Enhanced Surveillance data into my research, which required me to further develop tools for inferring and decoding new types of messages. At the same time, I created more content for the *ADS-B Decoding Guide*. Due to the increasing interest expressed and demand from readers, I started writing a more comprehensive book focused on the decoding practice of the data, which was the starting point of this book.

Alongside the book, I also created a Python library, pyModeS, which welcomed contributions from GitHub users from all over the world. The evolution of pyModeS proceeded more quickly than the updating of the book.

In 2019, I completed my PhD and continued as a faculty member in the aerospace engineering faculty of TU Delft. By then, I had time to reflect on aircraft surveillance data from a new perspective and determined that much of the book content could be updated.

The result is this text, which is both the second edition of *the 1090 Megahertz Riddle* and one of the first books published under the TU Delft's OPEN publishing initiative. The book is published as open access book, under the CC-BY-NC-SA 4.0 license. The \LaTeX source of the book is also shared on GitHub, where comments and pull requests are greatly appreciated.

Junzi Sun
Delft, the Netherlands
18th of August, 2020

Part I

Getting started

1 | Introduction

1.1 Background: the “death ray” that saves lives

Like many modern technologies such as computers, the internet, and GPS whose origins can be traced back to the military, aviation radar is no exception.

The fundamental theory of radar started long before the application. Since the 1860s, when the electromagnetic theory was discovered by James Clerk Maxwell, the foundation for many science and technology fields was laid out. In the late 19th century, Heinrich Hertz, who proved the existence of electromagnetic waves, also confirmed that metals could reflect radio waves. In the first decades of the 20th century, several systems for using radio waves to provide short-range directional information of objects were developed. German inventor Christian Hulsmeier is often considered as the first person to use radio waves to detect metal objects in 1904.

However, not until the Second World War, was the concept of *RA*dio *DE*tectio*N* And *R*ang*ing* (RADAR) developed. The technology was simultaneously researched by both major Allies and Axis countries. However, the United Kingdom led the race to in developing a functional radar system.

Originally, British Air Ministry officials, who were concerned about falling behind the technology race with the Germans, advised the physicist Robert Watson Watt to propose a set of abstract technical challenges to his colleague Skip Wilkins:

"Suppose, just suppose, that you had eight pints [17kg] of water, 3,000ft [1km] above the ground. And suppose that water was at 98°F [37°C], and you wanted to heat it to 105°F [41°C]. How much radio frequency power would you require, from a distance of 5km?"

Both scientists understood very well that the average adult human has 17 kg blood and a critical body temperature of 41°C. This represented an idea of the *death ray* that could be used to disable enemy aircraft pilots.

Without even developing such a system, they figured out that the power requirement was far beyond practice at that time. However, they realized an opportunity for funding a different project. Given the amount of power that can be transmitted, it was possible to detect the reflection of aircraft, and, thus calculate the position of aircraft. This proposal was approved by the air ministry. Later on, this technology was developed and shared with Americans during the war. After that, the widespread usage of RADAR (later became radar) had begun.

After the war ended, radar became more and more important for civil aviation. With the rapid growth of commercial flights, it developed into a prominent technology for aircraft surveillance in the aviation industry.

1.2 The primary radar

Aircraft surveillance in the early days relied only on, what is known today as the primary surveillance radar (PSR). The concept of PSR is fairly simple. It is a rotating radio transponder with an omnidirectional antenna. Commonly, the radar transmits a one-microsecond pulse for every one millisecond and listens to the reflections from the airplanes. The position of the aircraft is measured by distance and angle to the radar. The distance is known as slant distance, which is the line-of-sight distance between an aircraft and the radar. It can be calculated by measuring the time difference between the original signal and the reflection received, since the speed of the radio wave (speed of light) is known. The azimuth angle¹ of the aircraft is determined by the rotation angle of the radar. By processing radar signals, technologies like phase filter and Doppler filter can be used to filter out moving targets like aircraft and remove static objects, such as mountains, buildings, and other obstacles.

The slant distance of an aircraft does not always correspond to the horizontal distance to the radar. This is because all points having the same slant distance are located on a sphere that has the radius equal to the distance. Since the civil radar usually does not provide elevation information on the target, it is not possible to accurately convert the slant distance to the horizontal distance. Historically, it is sufficient to use primary radar for separating airplanes without considering this altitude differences. However, other systems have to be in place to provide air traffic controllers more accurate positions of the aircraft.

1.3 The secondary radar

The secondary surveillance radar (SSR), also known as air traffic control radar beacon system (ATCRBS), was designed to provide air traffic controllers more information than that provided by the primary radar. The secondary radar can be installed separately or installed on top of the primary radar. It uses a different radio frequency to actively interrogate the aircraft and receive information transmitted by the aircraft.

The SSR transmits interrogations using the 1030 MHz radio frequency and the aircraft transponder transmits replies using 1090MHz radio frequency. In the early design of SSR, two civilian communication protocols (Mode A and Mode C) were introduced. Mode A and Mode C allow the SSR to continuously interrogate the identity (squawk code) and the barometric altitude of an aircraft respectively.

Although Mode A and Mode C provide additional information to air traffic controllers, they present several design challenges [8]. The secondary surveillance radar initiates Mode A and C interrogations with two different pulse patterns, which are shown in Figure 1.1.

The pulses are about 0.8 microseconds wide. P1 and P3 are the two main pulses

¹ Azimuth angle is the horizontal angle measured clockwise with to the north of the observer.

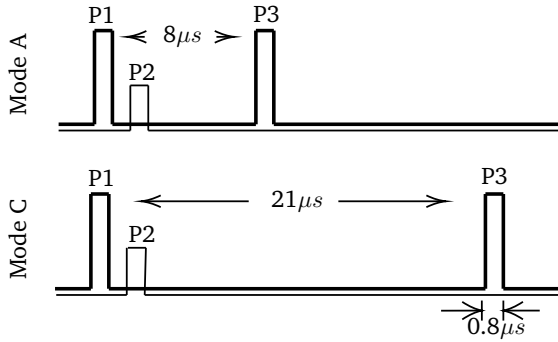


Figure 1.1: Mode A/C interrogation pulses

sent by the directional antenna. They are separated by 8 microseconds and 21 microseconds respectively for Mode A and C. P2 is a pulse sent by the omnidirectional antenna right after P1. Pulse P2 is introduced for sidelobe suppression. When the aircraft is close to the radar, the power of P2 can be higher than P1. In this case, the interrogation is likely generated by the side lobes of the directional antenna and should be ignored by the aircraft.

In Figure 1.2, an example of a Mode A/C reply is shown. Each reply consists of two persistent pulses separated by 20.3 microseconds (F1 and F2). Within this period, either the identity code or the altitude code is encoded using 13 0.45 microseconds pulses. The pulses are separated by gaps of one microsecond. The pulse at the center serves as a verification pulse and is always absent. The presence or absence of any other 12 pulses represents a 1 or 0 bit. When required by air traffic controllers for identification purposes, a special purpose identification (SPI) may follow F2 after two absent pulses.

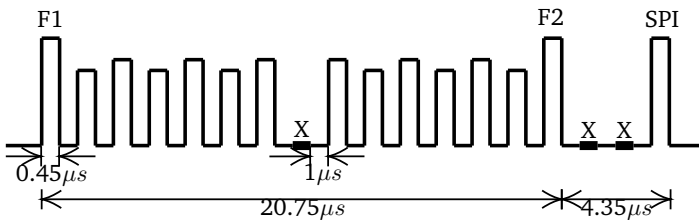


Figure 1.2: Mode A/C reply pulses

The response type (A or C) cannot be identified based on the reply signal itself. The SSR determines the content based on the synchronization with interrogations. This design of ATCRBS works sufficiently well with low-density air traffic, but it cannot efficiently cope with higher flight densities. Since all aircraft replies are transmitted on the same frequency, when several aircraft are in the same direction of the radar beam, reply signals can overlap and introduce errors for decoding. This is known as synchronous garbling.

When there are multiply secondary radars in the vicinity, replies originated by other radars may be considered as valid responses of one radar, which in turn, causes errors and confusion. This syndrome is called FRUIT (False Replies Unsynchronized In Time).

Though some of the garbling and the FRUIT problem can be mitigated with the reduction of interrogation frequency and improvements in signal processing ability, the information transmitted in Mode A and Mode C is still very limited. The number of identity codes available in Mode A communication is limited to a maximum of 4096 unique codes, which poses another clear limitation.

Hence, more advanced communication protocols needed to be developed to acquire more information from a large number of aircraft.

1.4 Mode S

Mode S (Mode Select Beacon System) was designed by Lincoln Laboratory at Massachusetts Institute of Technology in the 1970s. Based on different iterations of hardware and software design in the 1980s, the implementation of Mode S in air traffic control began in the 1990s. Since then, Mode S has become one of the main sources for aircraft surveillance.

The main characteristic of Mode S is its selective interrogation, which allows the SSR to interrogate different information from different aircraft separately. By using selective interrogation, it largely mitigated the problem of garbling in Mode A/C and thus greatly improved the capacity of the communication channel.

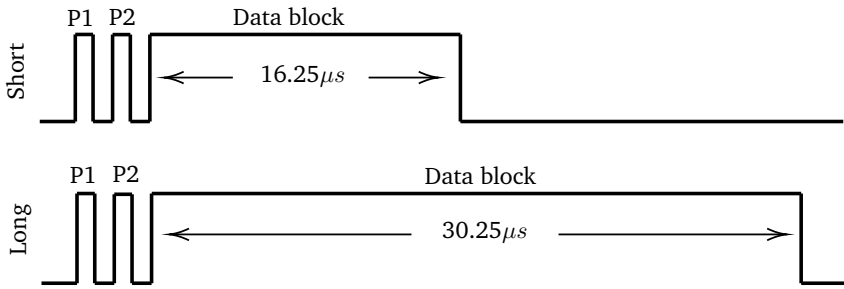
Unlike the limited number (4096) of unique identification codes in Mode A communication, the Mode S transponder is identified by a 24-bit transponder code, which can support up to 16,777,216 (2^{24}) unique addresses. In addition to these two major advantages, the Mode S protocol introduced many different types of information that could be interrogated and downlinked.

1.4.1 Mode S interrogations

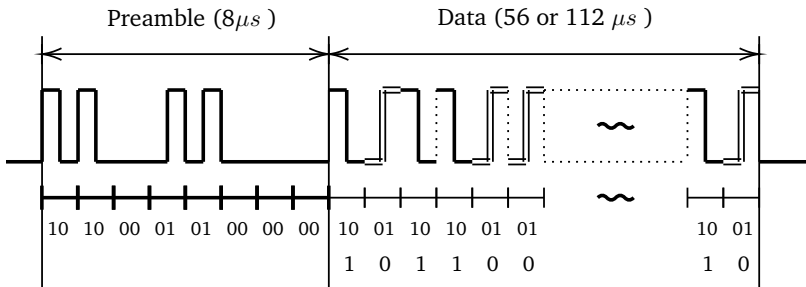
The Mode S uplink signal contains parameters that indicate which information is desired by the air traffic controller. There are two types of Mode S interrogations, which are shown in Figure 1.3. The short interrogation has 56 bits of information contained in the data block, while the long interrogation contains 112 bits of information. The P2 pulse acts as the sidelobe suppression for Mode A/C transponders so that they will ignore the rest of the interrogation pulses. Information in the Mode S interrogation data block is uses the Differential Phase-Shift Keying (DPSK) modulaion [12].

1.4.2 Mode S replies

There two types of Mode S downlink signals, short reply and long reply, which correspond to the short and long interrogations from the SSR. For each microsec-



ond, two bits are transmitted. All Mode S replies start with an 8-microsecond fixed preamble and continue with 56 or 122 microseconds of the data block. The structure of the downlink message is shown in Figure 1.4.



The 16-bit fix preamble can be represented as 1010000101000000 in binary. The information contained in the data block is modulated using the Pulse Position Modulation (PPM), which is a type of amplitude modulation. In PPM, the 1 bit is represented by a 0.5-microsecond of pulse followed by a 0.5-microsecond flat signal. The 0 bit is reversed compared to the 1 bit. It is represented by a 0.5-microsecond flat signal and followed by a 0.5-microsecond pulse.

Note

Mode S uplink and downlink signals use different modulation methods. The uplink uses phase modulation, while the downlink uses amplitude modulation. Phase modulation requires slightly more complicated hardware implementation but has a better performance in terms of error tolerance.

1.4.3 Compatibility with Mode A/C

Similar to Mode A/C, Mode S SSR can send *All-Call* interrogations to all aircraft in the vicinity. The All-Call interrogations are designed to be compatible with Mode A/C transponders. In Figure 1.5, the All-Call interrogation is shown. There would

be 8 or 21 microseconds between P1 and P3, which is the same as Mode A/C. P4 is a wider pulse lasting for 1.6 microseconds.

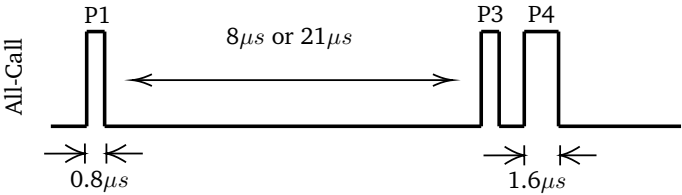


Figure 1.5: Mode A/C/S All-Call interrogation

When a Mode A/C transponder receives this interrogation, the last pulse P4 is ignored. Hence, a normal Mode A or Mode C reply is replied. A Mode S transponder would detect P4, and thus, produce a Mode S All-Call reply. The Mode A/C/S All-Call reply is designed for SSR to identify which aircraft are in the vicinity, including Mode A/C only aircraft.

This is one of the several different interrogation pulse patterns from a Mode A/C compatible Mode S radar. Most current SSRs can perform both Mode A/C and Mode S interrogations. In Figure 1.6, the interrogation pulses and replies from aircraft transponders are summarized.

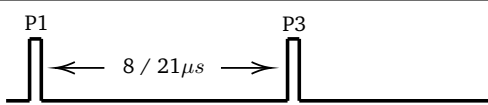
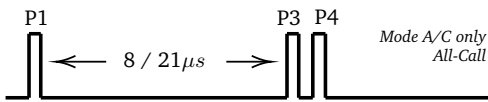
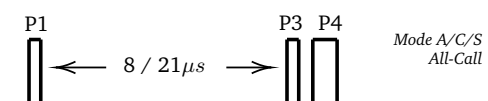
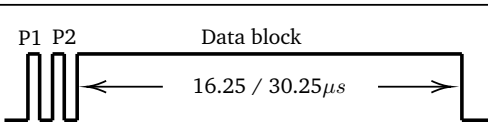
SSR Interrogations	Mode A/C Transponder	Mode S Transponder
	Mode A/C Reply	Ignore
	Mode A/C Reply	Ignore
	Mode A/C Reply	All-Call Reply
	Ignore	Mode S Reply

Figure 1.6: SSR interrogations pulses and transponder replies

We can see that:

- Mode A/C transponders respond to all interrogations with P1 and P3.

- When P4 is not present or a shorter P4 is used (as shown in the first and second patterns), Mode S transponders will ignore the interrogations.
- Mode S transponders will produce an All-Call reply to interrogations with a long P4. This interrogation is used to acquire all aircraft with either Mode A/C or Mode S capability.
- Finally, all Mode S interrogation is designed to be ignored by Mode A/C transponders due to the presence of P2 (as shown in the last pattern), which is considered as a side lobe suppression mechanism for Mode A/C transponders.

Note

Mode S SSR is also able to produce a Mode S only All-Call interrogation using the standard Mode S uplink (with uplink format 11).

1.4.4 Mode S format

The Mode S communication protocol is designed to handle different types of uplink and downlink message formats. The first 5 bits of the uplink or downlink message define the uplink format (UF) or downlink format (DF) number of the message. Based on the UF/DF number, different structures of the data block are defined. In Table 1.1, all available Mode S formats are shown. Currently, 11 Mode S formats are being used. Numbers not in this table are reserved for future use.

Table 1.1: Mode S uplink and downlink formats

UF/DF	Bits	Uplink type	Downlink type
0	56	Short air-air surveillance (ACAS)	Short air-air surveillance (ACAS)
4	56	Surveillance, altitude request	Surveillance, altitude reply
5	56	Surveillance, identity request	Surveillance, identity reply
11	56	Mode S All-Call	All-Call reply
16	112	Long air-air surveillance (ACAS)	Long air-air surveillance (ACAS)
17	112	-	Extended squitter
18	112	-	Extended squitter / non transponder
19	112	-	Military extended squitter
20	112	Comm-A, altitude request	Comm-B, altitude reply
21	112	Comm-A, identity request	Comm-B, identity reply
24	112	Comm-C (ELM)	Comm-D (ELM)

Note

Format number 24 is an exception. It is identified using only the first two bits, which must be 11. All following bits are used for encoding other information.

We can see that the short 56-bit data block is used to encode messages with format numbers from 0 to 11. Messages with format numbers above 16 are encoded with

the long 112-bit data block. Among all uplink formats, UF 17, 18, and 19 are not used. This is because the corresponding downlink messages (extended squitter messages) are designed to be broadcast automatically without the need for SSR interrogations.

One of the most common applications for the extended squitter is the Automatic Dependent Surveillance-Broadcast service, which is also commonly known as ADS-B.

1.5 ADS-B

Automatic Dependent Surveillance-Broadcast (ADS-B) is a surveillance technology designed to allow aircraft to broadcast their flight state periodically without the need for interrogation. The word *automatic* refers to the fact that no inputs from controllers or pilots are required. The word *dependent* indicates this technology depends on information from other onboard systems, such as air data systems and navigation systems.

Common aircraft state parameters included in ADS-B are position, altitude, and speed. The position is determined by Global Navigation Satellite Systems (GNSS). The velocity is derived from the GNSS position and the inertial measurement system. The altitude information includes both barometric altitude and GNSS altitude. The barometric altitude is provided by the air data system.

In addition to these primary state parameters, ADS-B also allows other information to be broadcast, for example, aircraft call-sign, accuracy indicators, integrity indicators, and operational status.

Different types of ADS-B messages are identified by Type Codes. The structures of these messages are all defined in ICAO documents, such as in [9] and [13]. In Part I of this book, we will explain how these different types of ADS-B messages can be decoded.

Note

Originally, there were three candidates to build ADS-B: Mode S Extended Squitter, VHF Data Link - Mode 4 (VDL4)), and Universal Access Transceiver (UAT). Different specifications are designed for these frequency channels [13, 14]. However, the Mode S extended squitter implementation of ADS-B is the most adopted one among all candidates. UAT is only partially implemented in some countries like the USA, while VDL4 did not go beyond the test phase.

1.6 Other Mode S services

The most common data format number used in Mode S for information downlink are 4, 5, 20, and 21. Format 4 and 5 are short messages designed to acquire aircraft altitude and identity (similar to Mode A/C messages). Downlink messages

with format 20 or 21, as known as Comm-B messages, contain other information desired by air traffic controllers, in addition to altitude and identity.

In theory, up to 255 different message types are supported by the Mode S Comm-B. A new parameter, Comm-B Data Selector (BDS), is designed to identify which additional information is included in Mode S messages. It functions similarly to the Type Code of ADS-B message. In practice, not all 255 BDS codes are defined or used.

A subgroup of these codes is commonly interrogated by air traffic controllers. By combining different BDS codes into groups, several Mode S services are defined. The two most used services are Mode S Elementary Surveillance (ELS) and Mode S Enhanced Surveillance (EHS) [5]. For example, in the European airspace, aircraft above certain takeoff weight category are required to have these capabilities enabled.

The Mode S Elementary Surveillance (ELS) consists of four BDS codes (10, 17, 20, and 30). It provides basic information such as Mode S capabilities, identification (callsign), and ACAS resolution advisory, in addition to the altitude or identity (squawk code) information.

The Mode S Enhanced Surveillance consists of three BDS codes (40, 50, and 60). It provides much more additional information on aircraft states, such as selected altitudes, true airspeed, indicated airspeed, Mach number, bank angle, and turn rate.

In addition to the common ELS and EHS, the meteorological routine air report (MRAR), and the meteorological hazard report (MHR) are also interrogated in some controlled airspaces. These reports provide weather-related information such as wind and temperature that are measured by the aircraft sensors.

1.7 Summary

In Figure 1.7, all aforementioned Mode S services and their relationships with Mode S downlink formats are illustrated.

In the rest of this book, the details of these services are discussed in different chapters. In chapter 2 (the rest of Part I), common hardware and software setups are shown. In chapter 3 to 10 (Part II), the focus is on ADS-B messages. Detailed guides on how to decode different types of messages are presented. In chapter 11 to 19 (Part III), the focus is on Mode S ELS, EHS, and meteorological services. Accordingly, the decoding and inference of the messages are provided.

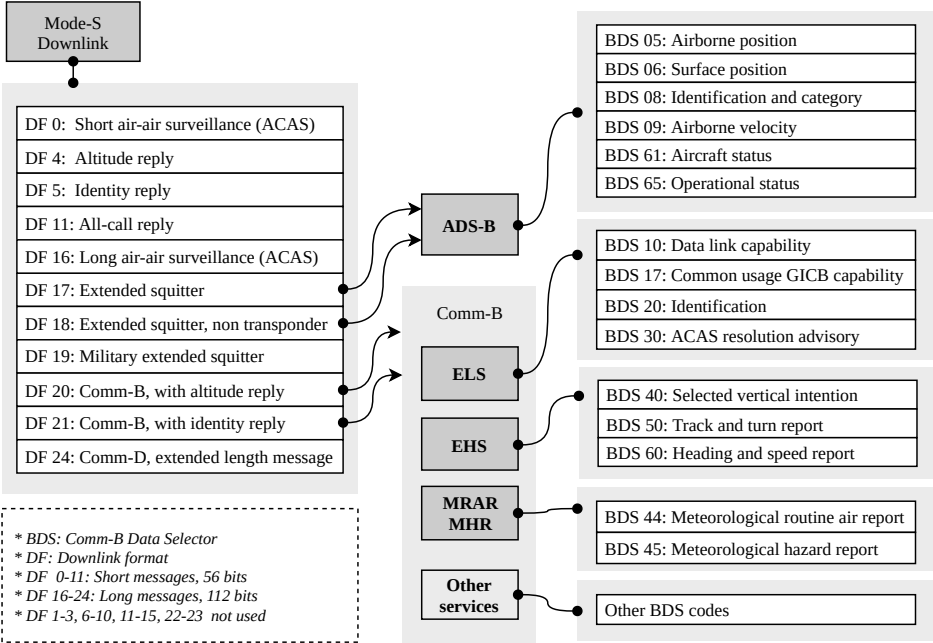


Figure 1.7: Relationship between Mode S downlink formats and different services

2 | Quick Start: Hardware and Software to Receive Mode S Data

Chapter 1 introduced several fundamental concepts about Mode S communication. This chapter focuses on the practical aspects of Mode S data, specifically, how to receive and obtain information that is transmitted in Mode S downlink communications. Mode S signals are transmitted using 1090 megahertz radio waves. Hence, the receiver and antenna have to be designed to work with this frequency. Nowadays, all necessary components required to obtain the Mode S data can be easily made with low-cost off-the-shelf components. Several open-source software tools are available to support the extraction and decoding of data from Mode S signals. In this chapter, we explain how to step up a functional hardware and software system to receive Mode S data.

2.1 Range

Since Mode S uses L band high-frequency signals that follow the line-of-sight propagation, any obstructions between the transmitter and receiver can cause a significant amount of signals to be blocked. Assuming no obstacles between an aircraft and receiver and the transmitter has a sufficient amount of power, the maximum range of the receiver is determined by the curvature of the earth. Figure 2.1 illustrates how the maximum range of the receiver can be obtained.

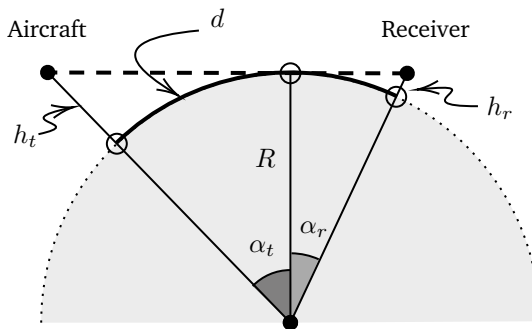


Figure 2.1: Maximum receiver range

Knowing the altitude of the receiver antenna, it is possible to determine the maximum range (d) of a Mode S receiver as:

$$d = (\alpha_r + \alpha_t)R \quad (2.1)$$

$$= \left(\arccos \frac{R}{R + h_r} + \arccos \frac{R}{R + h_t} \right) R \quad (2.2)$$

where R is the radius of the earth, while h_t and h_r are the height of the aircraft and receiver above the sea level. Using this equation, we can calculate the maximum receiving range for aircraft flying at different altitudes. In Figure 2.2, the maximum range curves calculated using several receiver heights are shown.

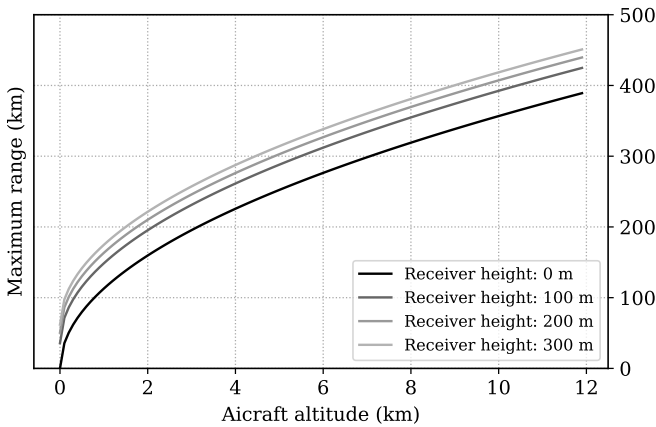


Figure 2.2: Maximum receiver range curve

It should be noted that this figure shows the maximum radio range due to the curvature of the Earth. However, in real-life applications, Mode S signal follows the Friis transmission model, which states that the maximum distance also depends on the power of the transmitter, as well as the directivities of the transmission and receiving antennas. When considering these factors, the actual radio range for the receiver might be more limited than the theoretical values shown in the previous figure.

2.2 Antenna

A large variety of commercial off-the-shelf antennas can be deployed to receive Mode S signals. In principle, any antenna designed for the radio frequency around 1 GHz can be used for receiving Mode S signals.

However, it is not difficult to design your own antenna. The carrier frequency of Mode S is 1090 MHz, which corresponds to the wavelength of 27.5 centimeters. In order to have an antenna that is tuned to this specific frequency, one can design the antenna simply using a piece of a conductor (metal wire) and a coaxial feeder cable. In Figure 2.3, a few common antenna designs are shown.

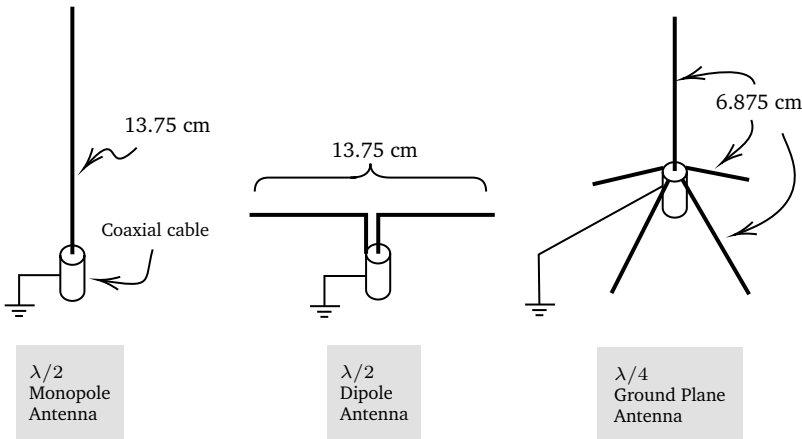


Figure 2.3: Common antenna designs

The monopole antenna and the dipole antenna both are half-wavelength ($\lambda/2$) antennas with a total conductor length of 13.75 cm. The ground plan antenna is a quarter-wavelength ($\lambda/4$) antenna, where the main pole is 6.875 cm.

For a remote installation where the antenna is far from the receiver (i.e. long coaxial cable between the antenna and receiver), the high-frequency signal of Mode S can attenuate quickly. When the signal has arrived at the receiver end, the signal to noise ratio can become quite high. To overcome this limitation, an active antenna may be used.

The active antenna has a low-noise amplifier integrated at the antenna side. Sometimes, it also includes a band-pass filter that is designed for 1090 MHz. The active antenna requires additional powering. Power is commonly supplied through a bias-tee device (Figure 2.4) connected at the receiver end, which is on the left-hand side of the diagram. On the right-hand side, the radio frequency is mixed with the DC component, which allows the electronic circuit to be powered close to the receiver end.

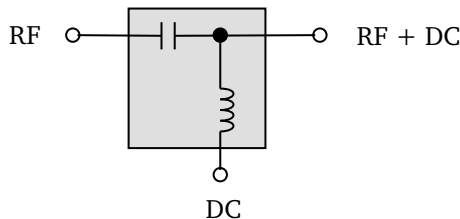


Figure 2.4: Bias-tee diagram

2.3 Receiver

Many modern Mode S receivers are built using software-defined radio (SDR). An SDR usually can be tuned to a wide range of radio frequencies. The user can conveniently select the center frequency of the receiver and the sampling rate, as well as defined the bandwidth of the onboard low-pass filter if it is supported.

For receiving ADS-B (and other types of Mode S message), a RTL-SDR is the most common type of low-cost receiver to choose. Many different brands of RTL-SDR receivers exist; they are often built with the Realtek RTL2832U chipset. It can work with radio frequencies from 24 to 1766 MHz. The maximum sampling rate is 2.8 million samples per second (MSPS). Given that a Mode S bit consists of a pulse cycle of 2 microseconds (see Figure 1.3), the minimum SDR sampling rate required for Mode S is 2 MSPS. RLT-SDR devices just barely manage to meet this requirement.

Note

The maximum frequency range of RTL-SDR can be from 0 to 2220 MHz. However, the sensitivity drops off significantly outside the 24 - 1766 MHz range. The sampling rate can actually go up to a maximum of 3.2 million samples per second, but some samples may be dropped at this sampling rate. Hence, it is not stable.

SDRs that offer a higher performance also exist. They often support a larger frequency range with higher sampling rates. Some offer multiple transmitting (TX) and receiving (RX) channels. In Table 2.1, a few examples of common SDR devices are given. The performance of RTL-SDR is listed as a comparison.

Table 2.1: Examples of common software defined radio devices

	RTL-SDR	AirSpy R2	HackRF 1	LimeSDR	BladeRF 2
Frequency (from)	24 MHz	24 MHz	1 MHz	100 KHz	47 MHz
Frequency (to)	1766 MHz	1700 MHz	6000 MHz	3800 MHz	6000 MHz
Max sample rate	2.8 MSPS	10 MSPS	20 MSPS	61.44 MSPS	61.44 MSPS
RX channels	1	1	1	2	2
TX channels	0	1	1	2	2
Open hardware	No	Firmware	Full	Full	Firmware, Schematics

2.4 Software tools

Several software tools are also available to work with some of these SDR devices and decode Mode S and ADS-B signals directly. In this section, we explain how to use two open-source tools, which are `dump1090` and `pyModeS`.

2.4.1 dump1090

`dump1090` is the most well-known open-source Mode S decoder currently available. The software is written in C programming language and was originally developed by Salvatore Sanfilippo ¹ under the BSD three clause license.

Since its release in 2013, the repository has been forked and extended intensively on GitHub, creating more than 900 forks so far. Many of the branched versions contain different variations, such as support for additional hardware, additional decoded Mode S messages, and additional output format. Currently, one of the most comprehensive forks is the repository maintained by FlightAware.² The following examples will be based on the FlightAware version of `dump1090`, using a Debian based Linux system.

2.4.1.1 Installation of dump1090

The latest version of `dump1090` source code can download as follows:

```
$ git checkout https://github.com/flightaware/dump1090.git
```

Before compiling the code, following dependencies must be installed:

```
sudo apt-get install build-essential debhelper librtlsdr-dev \  
pkg-config dh-systemd libncurses5-dev libbladerf-dev
```

Next, we can compile the source code as:

```
$ cd dump1090  
$ make
```

It is worth noting that the FlightAware version of `dump1090` supports both RTL-SDR and BladeRF devices by default.

2.4.1.2 Default usage of dump1090

Once it is compiled and the RTL-SDR receiver is connected, we can run the following command to start receiving and decoding signals:

```
$ ./dump1090
```

With the default option, Mode S messages and decoded information are displayed in the terminal. For example:

¹ <https://github.com/antirez/dump1090>

² <https://github.com/flightaware/dump1090>

```
*8d451dbd9905b5018004005979c5;
CRC: 000000
RSSI: -20.6 dBFS
Score: 1800
Time: 9214131.08us
DF:17 AA:451DBD CA:5 ME:9905B501800400
Extended Squitter Airborne velocity over ground, subsonic (19/1)
  ICAO Address: 451DBD (Mode S / ADS-B)
  Air/Ground:   airborne
  Ground track 271.4
  Groundspeed: 436.1 kt
  Geom rate:    0 ft/min
  NACv:         0
```

2.4.1.3 Raw Mode S messages

If we only want to display the raw messages, the `-raw` option can be provided, as follows:

```
$ ./dump1090 --raw
```

In this case, the terminal output will only contain the raw messages:

```
*5d4074358ad00c;
*8d407435990dbd01900484f66c3c;
*8d40743558af828cd326fe0c2fe9;
*a00015b8c2680030a80000318667;
*a80011b1e0da112fe0140060939f;
*a00015b8c2680030a80000318667;
*5d4074358ad030;
*5d4074358ad030;
```

2.4.1.4 Interactive mode

`dump1090` can also provide a live view of all aircraft seen by the receiver through the use of the `-interactive` option:

```
$ ./dump1090 --interactive
```

An example of the terminal output is shown in Figure 2.5.

Hex	Mode	Sqwk	Flight	Alt	Spd	Hdg	Lat	Long	RSSI	Msgs	Ti
40750D	S	3573	WUK2SH	38000	435	285	51.707	4.833	-27.6	452	0
471EA8	S	5205	WZZ9CS	37025	446	105	51.650	4.404	-32.6	2928	1
471F33	S	2246	WZZ1751	37025	435	106			-34.3	7279	37
0CA56D	S	1347	RYR74PQ	40000	436	266	52.029	4.579	-29.7	7400	0

Figure 2.5: Example of a dump1090 interactive output

2.4.2 pyModeS

`pyModeS` is an open-source Mode S decoder project that I started in 2015, during my PhD research at TU Delft. It is a library that was originally designed to focus on lower level inference and decoding of individual raw Mode S messages. Many users of `pyModeS` were researchers or developers who needed a Mode S decoder package in the Python programming language. Later on, hardware support and live decoding were added, which made it more akin to `dump1090` of late.

2.4.2.1 Installation of pyModeS

As a Python library, it is possible to install the most recent stable version of `pyModeS` as:

```
pip install pyModeS
```

The latest development version for the GitHub can be installed as:

```
pip install git+https://github.com/junzis/pyModeS
```

2.4.2.2 Live traffic view

`pyModeS` provides the possibility to view live traffic through the `modeslive` command. The usage of this command is shown as follows:

```
$ modeslive [-h] --source SOURCE [--connect SERVER PORT DATATYPE]
            [--latlon LAT LON] [--show-uncertainty] [--dumpto DUMPTO]

arguments:
-h, --help            show this help message and exit
--source SOURCE       Choose data source, "rtlsdr" or "net"
--connect SERVER PORT DATATYPE
                    Define server, port and data type. Supported data
                    types are: ['raw', 'beast', 'skysense']
--latlon LAT LON      Receiver latitude and longitude, needed for the surface
                    position, default none
--show-uncertainty    Display uncertainty values, default off
--dumpto DUMPTO       Folder to dump decoded output, default none
```

When an RTL-SDR device is connected, the following command can be used to display live traffic:

```
$ modeslive --source rtlsdr
```

Data source can also be supplied through the network (for example, from `dump1090` TCP output stream) as:

```
$ dump1090 --net --quiet
$ modeslive --source net --connect localhost 30002 raw
```

An example of the live view is shown in Figure 2.6.

Online aircraft [49] ('Ctrl+C' to exit, 'Enter' to lock one)													
icao	call	lat	lon	alt	gs	tas	ias	mach	roc	trk	hdg	live	
06A0AF	QTR7DH	52.12263	7.88057	40975	494	486	251	0.844	-64	106.31	103.008	-14s	
0CA56D	RYR74PQ	52.2496	8.68286	40000	438	434	229	0.76	0	263.98	266.66	-25s	
3C0C99	TUI150	49.75224	4.25416	36000	438	452	263	0.792	-64	53.44	48.516	-1s	
3C4969	TUI2417	49.23816	4.00952	38000	456	464	256	0.808	0	45.89	45.0	0s	
3C4B2B	DLH506	49.40909	3.88867	33000	481	474	294	0.824	0	256.19	255.059	-4s	
3CC187	DCAPB	49.97695	5.82468	38000	415	420	233	0.744	0	46.75	42.539	0s	
(1 / 7)													

Figure 2.6: Example of a `modeslive` aircraft live view

2.4.2.3 Programming interface

Since `pyModeS` is designed as a low-level development library, its decoding functionalities can be easily accessed in Python. Some examples of accessing `pyModeS` are shown here.

Core functions that provide access to extract the Downlink Format, ICAO address, ADS-B Type Code, as well as to perform parity check. For example:

```
import pyModeS as pms

pms.df(msg)           # Downlink Format
pms.icao(msg)          # Infer the ICAO address from the message
pms.crc(msg)          # Perform parity check
pms.typecode(msg)     # Obtain ADS-B message Type Code
```

ADS-B related functions allow information such as identity, position, and velocities to be decoded. For example:

```
# position messages
pms.adsb.position(msg_even, msg_odd, t_even, t_odd)
pms.adsb.altitude(msg)

# velocity messages
pms.adsb.velocity(msg)
```

There are also a large number of functions designed to infer and decode Mode S downlink messages. For example:

```

# Mode S DF=4/20 altitude code
pms.common.altcode(msg)

# Mode S DF=5/21 squawk code
pms.common.idcode(msg)

# Infer the Modes-S BDS code
pms.bds.infer(msg)

# BDS 4,0
pms.commb.selalt40mcp(msg) # MCP/FCU selected altitude (ft)
pms.commb.selalt40fms(msg) # FMS selected altitude (ft)
pms.commb.p40baro(msg)     # Barometric pressure (mb)

# BDS 5,0
pms.commb.roll50(msg)      # Roll angle (deg)
pms.commb.trk50(msg)       # True track angle (deg)
pms.commb.gs50(msg)        # Ground speed (kt)
pms.commb.rtrk50(msg)      # Track angle rate (deg/sec)
pms.commb.tas50(msg)       # True airspeed (kt)

# BDS 6,0
pms.commb.hdg60(msg)       # Magnetic heading (deg)
pms.commb.ias60(msg)       # Indicated airspeed (kt)
pms.commb.mach60(msg)      # Mach number (-)
pms.commb.vr60baro(msg)    # Barometric altitude rate (ft/min)
pms.commb.vr60ins(msg)     # Inertial vertical speed (ft/min)

```

There are several commonly used functions related to Mode S decoding. A complete list of the APIs can be found in the `pyModeS` library API documentation.

In the rest of this book, most of the decoding details will be explained, which will often reflect the source code from `pyModeS`.

Part II

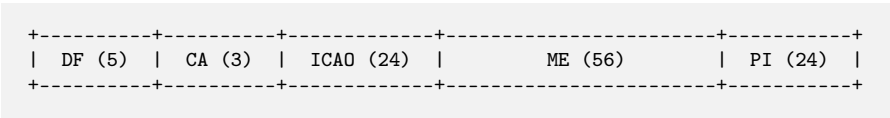
Fundamental ADS-B Decoding

3 | ADS-B Basics

ADS-B is short for Automatic Dependent Surveillance-Broadcast. It is a satellite-based surveillance system. Parameters such as position, velocity, and identification are transmitted through Mode S Extended Squitter (1090 MHz). Nowadays, the majority of the aircraft are broadcasting ADS-B messages constantly.

3.1 Message structure

An ADS-B frame is 112 bits long and consists of 5 main parts, as follows:



Any ADS-B message must start with the Downlink Format 17. In case of a TIS-B message, the Downlink Format is 18. They correspond to 10001 or 10010 in binary for the first 5 bits. Bits 6-8 are used as an additional identifier, which presents different meanings within each ADS-B subtype.

In Table 3.1, the key information of an ADS-B message is listed.

Table 3.1: Structure of ADS-B frame

Bit	No. bits	Abbreviation	Information
1-5	5	DF	Downlink Format
6-8	3	CA	Transponder capability
9-32	24	ICAO	ICAO aircraft address
33-88 (33-37)	56 (5)	ME (TC)	Payload message (Type code)
89-112	24	PI	Parity/Interrogator ID

It is worth noting that the ADS-B Extended Squitter sent from a Mode S transponder uses Downlink Format 17 (DF=17). Non-Transponder-Based ADS-B Transmitting Subsystems and TIS-B Transmitting equipment use Downlink Format 18 (DF=18). By using DF=18 instead of DF=17 , an ADS-B/TIS-B Receiving Subsystem will know that the message comes from equipment that cannot be interrogated.

3.2 Capability

The second field consists of three bits that indicate the transponder level. The capability value can be between 0 and 7. The definitions of these values are shown in Table 3.2.

Table 3.2: Mode S transponder capability (CA)

CA	Definition
0	Level 1 transponder
1-3	Reserved
4	Level 2+ transponder, with ability to set CA to 7, on-ground
5	Level 2+ transponder, with ability to set CA to 7, airborne
6	Level 2+ transponder, with ability to set CA to 7, either on-ground or airborne
7	Signifies the Downlink Request value is 0, or the Flight Status is 2, 3, 4 or 5, either airborne or on the ground

3.3 ICAO address

In each ADS-B message, the sender (originating aircraft) can be identified using the Mode S transponder address assigned accordingly ICAO regulations. Very often this is referred as ICAO address.

The ICAO address is located from 9 to 32 bits in binary (or 3 to 8 in hexadecimal positions). A unique ICAO address is assigned to each Mode S transponder of an aircraft and serves as the unique identifier for each aircraft.

3.4 ADS-B message types

To identify what information is contained in an ADS-B message, we need to take a look at the Type Code of the message, indicated at bits 33 - 37 (or first 5 bits of the `ME` segment).

In following Table 3.3, the relationships between each Type Code and its information contained in the `ME` segment are shown.

Table 3.3: ADS-B Type Code and content

Type Code	Data frame content
1 - 4	Aircraft identification
5 - 8	Surface position
9 - 18	Airborne position (w/ Baro Altitude)
19	Airborne velocities
20 - 22	Airborne position (w/ GNSS Height)
23 - 27	Reserved
28	Aircraft status
29	Target state and status information
31	Aircraft operation status

3.5 Example of ADS-B message structure

Let us use an example to illustrate the decoding process. First, a raw message is received, which is represented in hexadecimal format:

```
8D4840D6202CC371C32CE0576098
```

It can be converted into binary conveniently. The structure of the binary message is shown as follows:

```

+-----+-----+-----+-----+
| HEX | 8D      | 4840D6    | 202CC371C32CE0 | 576098 |
+-----+-----+-----+-----+
| BIN | 10001 101 | 010010000100 | [00100]0000010110011 | 010101110110 |
|     |           | 000011010110 | 00001101110001110000 | 000010011000 |
|     |           |           | 110010110011100000 |           |
+-----+-----+-----+-----+
| DEC | 17    5  |           | [4] ..... |           |
+-----+-----+-----+-----+
|     | DF    CA | ICAO      | ME         | PI       |
|     |         |           | [TC] ..... |           |
+-----+-----+-----+-----+

```

The first five bits show that the downlink format is 17 (or 10001 in binary), which indicates the message is an ADS-B message. The first five bits of the ME field shows that the type code is 4 (or binary 00100), which indicates the message is an identification message.

In the example above, The ICAO address is 4840D6 (or 010010000100 in binary format). Various online tools can be used to find out more about the aircraft with a given ICAO address.¹ For instance, using the previous ICAO 4840D6 example,

¹ For example, an online database from OpenSky can be used:
<https://opensky-network.org/aircraft-database>

it will return the result of a `Fokker 70` with the registration of `PH-KZD` .

Try it out

Using `pyModeS` , we can find out what information is contained in this ADS-B message:

```
import pyModeS as pms
pms.tell("8D4840D6202CC371C32CE0576098")
```

Output:

```
Message: 8D4840D6202CC371C32CE0576098
ICAO address: 4840D6
Downlink Format: 17
Protocol: Mode S Extended Squitter (ADS-B)
Type: Identification and category
Callsign: KLM1023_
```

3.6 Availability and transmission rate

Different ADS-B messages have different transmission rates. The update frequency also differs depending on if the aircraft is on-ground or airborne, as well as if the aircraft is still or moving when on the ground.

In Table 3.4, the transmission rate of these messages are indicated.

Table 3.4: ADS-B message transmission rates

Messages	TC	Ground (still)	Ground (moving)	Airborne
Aircraft identification	1-4	0.1 Hz	0.2 Hz	0.2 Hz
Surface position	5-8	0.2 Hz	2 Hz	-
Airborne position	9-18, 20-22	-	-	2 Hz
Airborne velocity	19	-	-	2 Hz
Aircraft status	28	0.2 Hz (no TCAS RA and Squawk Code change)		
		1.25 Hz (change in TCAS RA or Squawk Code)		
Target states	29	-	-	0.8 Hz
Operational status	31	0.2 Hz	0.4 Hz (no NIC/NAC/SIL change)	
			1.25 Hz (change in NIC/NAC/SIL)	

For Target states and Operational status messages, when there is a change in some key parameters, the transmission is changed to a higher rate for approximately 24 seconds.

3.7 ADS-B versions

In this section, we are going to look into different versions and the evolution of ADS-B.

Since start of ADS-B until now, there have been three different implementation versions. The major reason for these updates is to include more information (types of data) in ADS-B. The documentation available on these versions and differences is quite far from user friendly and generally presented in a very scattered fashion. Even the official ICAO_9871 document is confusing to read. Here, I am going to put the pieces of scattered information together.

There are three versions implemented so far, starting from version 0, then version 1 around 2008, and version 2 around 2012. Major changes in version 1 and version 2 are listed as follows:

3.7.1 From version 0 to 1

The changes introduced in version 1 are summarized as follows:

- Added Type Code 28 and 31 messages.
 - TC=28 : Aircraft status - Emergency/priority status and ACAS RA Broadcast.
 - TC=31 : Operational status.
- Removed the *Navigational uncertainty categories* (NUC). Introduced the *Navigation integrity category* (NIC) and *Surveillance integrity level* (SIL).
 - Type Code and a NIC Supplement bit (NICs) are used to define the NIC.
 - NIC Supplement bit included in operation status message (TC=31).
- The ADS-B version number is now indicated in operation status message (TC=31).

3.7.2 From version 1 to 2

The changes introduced in version 2 are summarized as follows:

- Re-defined the structure and content of TC=28 and TC=31 messages.
- Introduced two additional NIC supplement bits.
- NICa is defined in operational status messages. (TC=31)
- NICb is defined in airborne position messages. (TC=9-18)
- NICc is defined in operational status messages. (TC=31)
- Introduced an additional *Horizontal Containment Radius* (Rc) level within NIC=6 of the airborne position message (TC=13).

3.7.3 Identification of the ADS-B Version

There are two steps to check the ADS-B version. This is because ADS-B Version 0 is not included in any message.

1. Step 1: Check whether an aircraft is broadcasting ADS-B messages with TC=31 at all. If no message is ever reported, it is safe to assume that the version is Version 0.
2. Step 2: If messages with TC=31 are received, check the version numbers located in the 41-43 bit of the payload (or 73-75 bit of the message).

After identifying the correct ADS-B version for an aircraft (which does not change often), one can decode related TC=28 and TC=31 messages accordingly.

4 | Aircraft Identification and Category

Within the group of ADS-B messages, the *Aircraft Identification and Category* message is designed to broadcast the identification (also known as the *callsign*), and the wake vortex category of the aircraft.

In this message, the Type Code can be from 1 to 4. The 56-bit message payload consists of 10 parts and is structured as follows:

```
+-----+-----+-----+-----+-----+-----+-----+-----+-----+-----+
| TC,5 | CA,3 | C1,6 | C2,6 | C3,6 | C4,6 | C5,6 | C6,6 | C7,6 | C8,6 |
+-----+-----+-----+-----+-----+-----+-----+-----+-----+-----+

TC: Type code
CA: Aircraft category
C*: A character
```

Here, number 6 represents the number of bits used to encode each of the characters.

4.1 Identification (Call Sign)

The aircraft identification included in the message is the callsign. Be aware that callsign is not a unique identifier of an aircraft, since different aircraft flying the same route at different times would share the same callsign.

The last 8 fields in the previous structure diagram represent the callsign characters. In order to decode each character, a lookup table is needed to map the corresponding decimal number (represented in binary code) to each character.

The character mapping is shown as follows:

```
#ABCDEFGHIJKLMNQRSTUUVWXYZ##### 0123456789#####
```

Firstly, the # symbols represent characters that are not used. In summary, characters and their decimal representations are as follows, where □ symbol refers to a space character.

A - Z	:	1 - 26
0 - 9	:	48 - 57
□	:	32

If you are familiar with the ASCII (American Standard Code for Information Interchange) code, it is easy to identify that a callsign character is encoded using the lower 6 bits of the same character in ASCII.

4.2 Wake vortex category

The `CA` value in combination with `TC` value defines the wake vortex category of the aircraft. Note ADS-B has its own definition of wake categories, which is different from the common ICAO wake turbulence category definition. In Table 4.1, the definitions and related `TC` and `CA` codes are indicated.

Table 4.1: Wake vortex in ADS-B identification and category message

TC	CA	Category
1	ANY	Reserved
ANY	0	No category information
2	1	Surface emergency vehicle
2	3	Surface service vehicle
2	4 - 7	Ground obstruction
3	1	Glider, sailplane
3	2	Lighter-than-air
3	3	Parachutist, skydiver
3	4	Ultralight, hang-glider, paraglider
3	5	Reserved
3	6	Unmanned aerial vehicle
3	7	Space or transatmospheric vehicle
4	1	Light (less than 7000 kg)
4	2	Medium 1 (between 7000 kg and 34000 kg)
4	3	Medium 2 (between 34000 kg to 136000 kg)
4	4	High vortex aircraft
4	5	Heavy (larger than 136000 kg)
4	6	High performance (>5 g acceleration) and high speed (>400 kt)
4	7	Rotocraft

4.3 Example

Let us use the following raw message as an example for decoding:

8D4840D6202CC371C32CE0576098

The message payload is:

```
HEX: 202CC371C32CE0
BIN: 00100000001011001100001101110001110000110010110011100000
```

The structure of the payload can be decomposed as follows:

```
+-----+-----+-----+-----+-----+-----+-----+-----+-----+
|00100|000|001011|001100|001101|110001|110000|110010|110011|100000|
+-----+-----+-----+-----+-----+-----+-----+-----+-----+
|TC  |CA  |11   |12   |13   |49   |48   |50   |51   |32   |
+-----+-----+-----+-----+-----+-----+-----+-----+-----+
|4   |0   |K    |L    |M    |1    |0    |2    |3    |_    |
+-----+-----+-----+-----+-----+-----+-----+-----+-----+
```

With `TC=4` , we can confirm it is an identification and category message. The decoded identity (callsign) of the aircraft is `KLM1023` (with the tailing space ignored). With `CA=0` , we can see that the aircraft did not transmit any information on the wake vortex category.

Try it out

Using `pyModeS` , we can decode the callsign as follows:

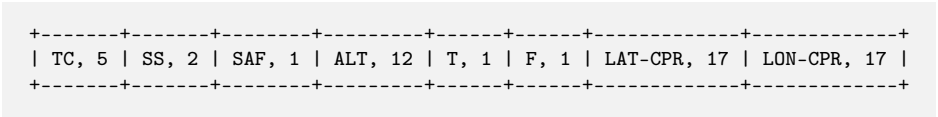
```
import pyModeS as pms

category = pms.adsb.category("8D4840D6202CC371C32CE0576098")
callsign = pms.adsb.callsign("8D4840D6202CC371C32CE0576098")
```

5 | Airborne Position

The aircraft airborne position message is used to broadcast the position and altitude of the aircraft. It has the Type Code from 9 to 18 or from 20 to 22. When Type Code is from 9 to 18, the encoded altitude represents the barometric altitude of the aircraft. When the Type Code is from 20 to 22, the encoded altitude contains the GNSS altitude of the aircraft. The Type Code value is related to the uncertainties in the position, which will be discussed in a later chapter.

The structure of the ADS-B airborne position message payload is shown as follows:



There are eight fields in the message payload, and the details of all fields are listed in Table 5.1.

Table 5.1: Airborne position message structure

FIELD		MSG	MB	BITS
Type Code 9-18: with barometric altitude 20-22: with GNSS altitude	TC	33-37	1-5	5
Surveillance status 0: No condition 1: Permanent alert 2: Temporary alert 3: SPI condition	SS	38-39	6-7	2
Single antenna flag	SAF	40	8	1
Encoded altitude	ALT	41-52	9-20	12
Time	T	53	21	1
CPR Format 0: even frame 1: odd frame	F	54	22	1
Encoded latitude	LAR-CPR	55-71	23-39	17
Encoded longitude	LON-CPR	72-88	40-56	17

It is important to emphasize that the encoded latitude and longitude are not the actual latitude and longitude values. Instead, the position information is encoded in a Compact Position Reporting (CPR) format, which requires fewer bits to en-

code positions with higher resolution. Two types of position messages (identified by the odd and even frame flag) are broadcast alternately. There are two different ways to decode an airborne position based on these messages:

1. **Globally unambiguous position decoding:** Without a known position to start with, using both types of messages to decode the position.
2. **Locally unambiguous position decoding:** Knowing a reference position from previous sets of messages, using only one message for the decoding.

The position information in ADS-B messages is encoded in a compact position reporting (CPR) format. The general idea behind CPR is to encode more coordinate decimals using fewer bits. The CPR offers a trade-off between global position ambiguity and local position accuracy.

5.1 A over-simplified example

First of all, we will use a simple example to explain the basic ideas behind the CPR position encoding. CPR divides 2D space into two different grids. Two message types are used to encode the positions with different grids.

In the following simple example, we want to encode position (9, 7) in a 16×16 discrete world. Normally, this would require 4 bits each to encode the x and y coordinates, which is (1001, 0111).

In the simple "CPR" algorithm, we first define two different grids. The even grid has a size of 4×4 , while the odd grid has a size of 5×5 . The is illustrated in Figure 5.1.

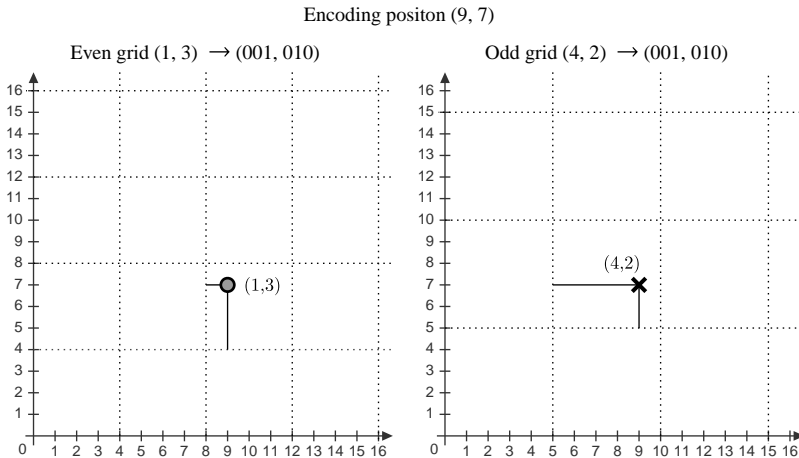


Figure 5.1: Simplified CPR position coding (encoding)

With these two grids, we can encode the local positions within each grid systems,

which are (1, 3) and (4, 2) respectively. Now, the position can be encoded only using 3 bits.

When the odd and even messages are received, each message alone has different possible global positions, which are shown in Figure 5.2.

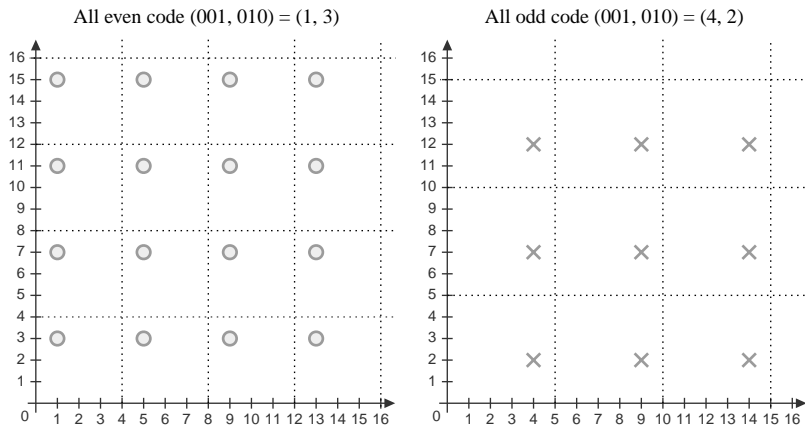


Figure 5.2: Simplified CPR position coding (all position possibilities)

Combining the possible positions from both even and odd messages, we can recover the global position where the solutions from both grids overlap with each other. This is shown in Figure 5.3.

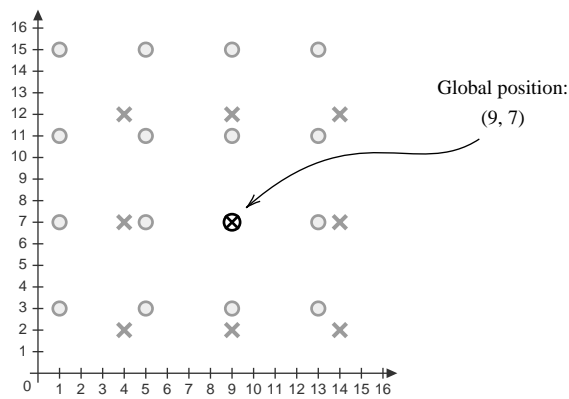


Figure 5.3: Simplified CPR position coding (final global position)

5.2 Compact Position Reporting

5.2.1 CPR zones

The actual CPR algorithm is more sophisticated. First of all, more zones are defined. There are 15 latitude zones defined for each hemisphere. Up to 59 longitude zones are used, and the number of longitude zones is different at different altitudes.

In Figure 5.4, the latitude zones are illustrated. The solid and dashed lines represent the latitude zone size of even and odd messages.

In Figure 5.5, the latitude zones are illustrated. On the right-hand side of the figure is a zoomed-in view of the gird of northern Europe. The black and gray lines represent the longitude zone size of even and odd messages. We can see that the number of longitude zones (and the sizes) also differs depending on the latitude.

To report a position, the fractions of latitude and longitude in respective zones are encoded using 17 bits. These bits are transmitted in the position messages.

5.2.2 Core functions and parameters

To decode the CPR positions, we first introduce relevant parameters and common functions.

5.2.2.1 N_Z

N_Z represents the number of latitude zones between the equator and a pole. In Mode S, N_Z is defined to be 15.

5.2.2.2 $\text{floor}(x)$

The floor function $\text{floor}(x)$ returns the greatest integer value k , where $k \leq x$. For example:

$$\begin{aligned}\text{floor}(5.6) &= 5 \\ \text{floor}(-5.6) &= -6\end{aligned}\tag{5.1}$$

5.2.2.3 $\text{mod}(x, y)$

The modulo function is defined as:

$$\text{mod}(x, y) = x - y \cdot \text{floor}\left(\frac{x}{y}\right), \quad y \neq 0\tag{5.2}$$

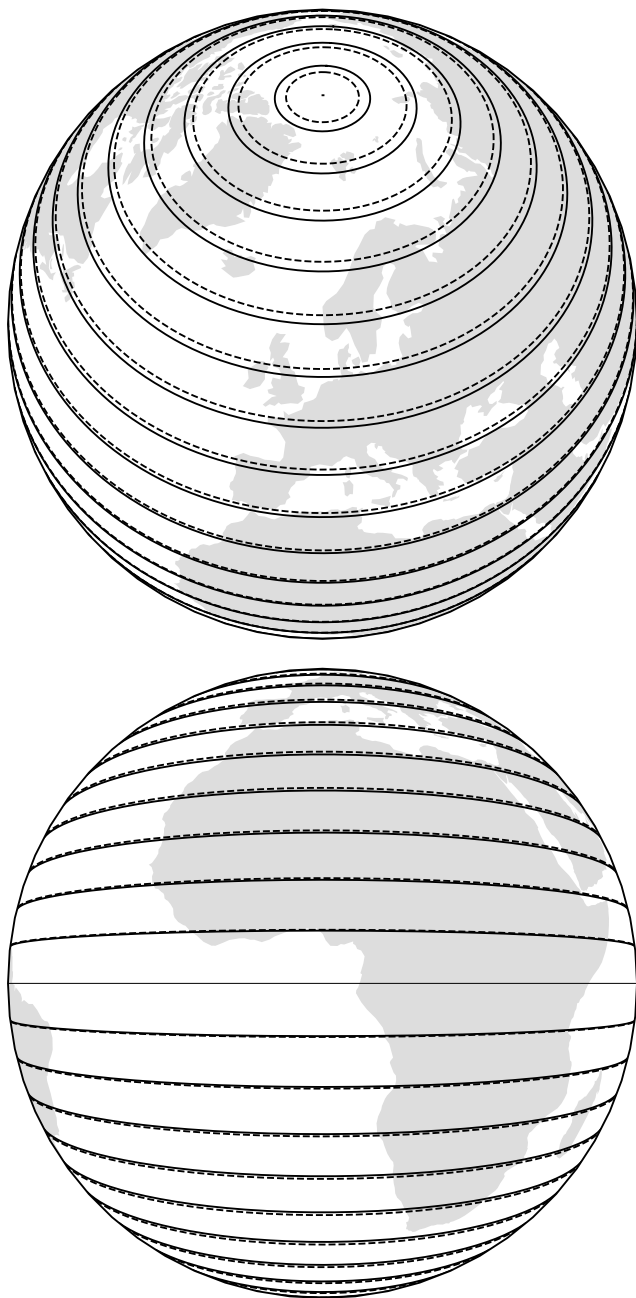


Figure 5.4: Latitude zones in compact position reporting, from different view points.

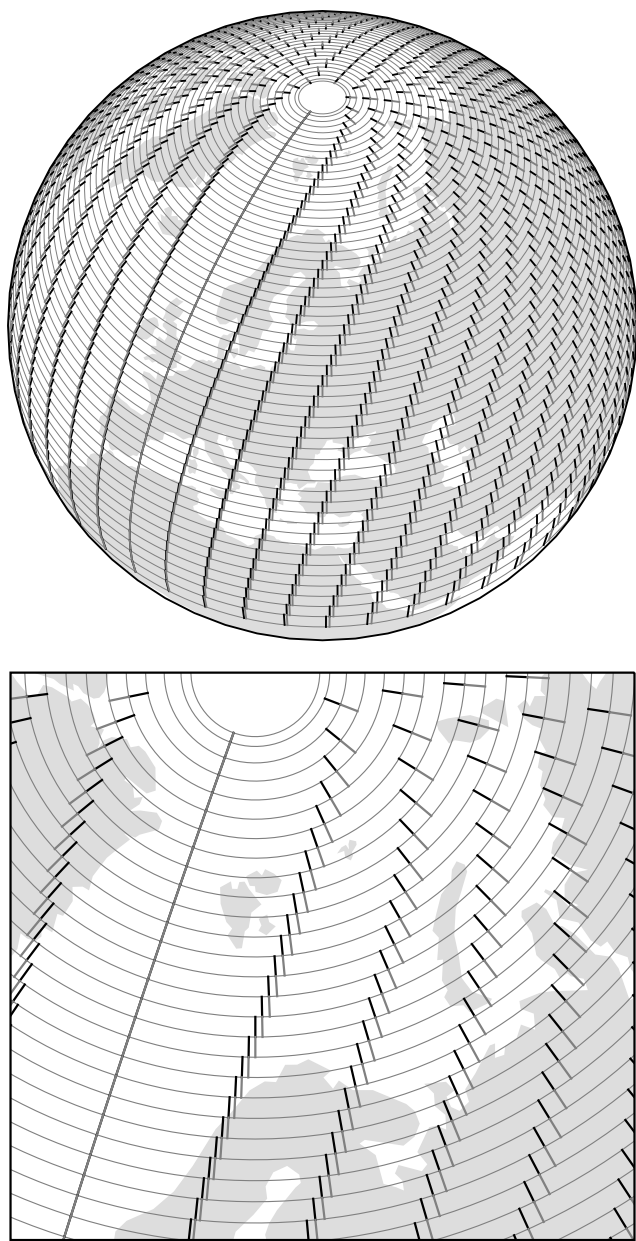


Figure 5.5: Longitude zones in position reporting

5.2.2.4 NL(lat) - Longitude zone number

Given the latitude, this function yields the number of longitude zones between 1 and 59. The function is expressed as:

$$NL(lat) = floor \left\{ \frac{2\pi}{\arccos \left[1 - \frac{1 - \cos \left(\frac{\pi}{2 N_Z} \right)}{\cos^2 \left(\frac{\pi}{180} \cdot lat \right)} \right]} \right\} \quad (5.3)$$

For latitudes that are close to the equator or the poles, one of following values is returned:

lat = 0	->	NL = 59
lat = +87	->	NL = 2
lat = -87	->	NL = 2
lat > +87	->	NL = 1
lat < -87	->	NL = 1

5.3 Globally unambiguous position decoding

5.3.1 Calculation of latitude

In each position message, bit 54 determines whether it is an odd or even type. **0** indicates an even message, while **1** indicates an odd message.

Bits 55-71 and bits 72-88 represent the fractions of the latitude and longitude within the latitude and longitude grid, denoted as lat_{cpr} and lon_{cpr} :

$$\begin{aligned} lat_{cpr} &= \frac{N_{cpr,lat}}{2^{17}} \\ lon_{cpr} &= \frac{N_{cpr,lon}}{2^{17}} \end{aligned} \quad (5.4)$$

For even and odd messages, the latitude zone sizes are defined as follows:

$$\begin{aligned} dLat_{even} &= \frac{360^\circ}{4N_Z} \\ dLat_{odd} &= \frac{360^\circ}{4N_Z - 1} \end{aligned} \quad (5.5)$$

To decode the latitude, first, use the following equation to calculate the latitude zone index, demoted as j :

$$j = \text{floor} \left(59 \cdot \text{lat}_{\text{cpr,even}} - 60 \cdot \text{lat}_{\text{cpr,odd}} + \frac{1}{2} \right) \quad (5.6)$$

Based on both even and odd frames, two latitudes are computed as follows:

$$\begin{aligned} \text{lat}_{\text{even}} &= \text{dLat}_{\text{even}} \left(\text{mod}(j, 60) + \text{lat}_{\text{cpr,even}} \right) \\ \text{lat}_{\text{odd}} &= \text{dLat}_{\text{odd}} \left(\text{mod}(j, 59) + \text{lat}_{\text{cpr,odd}} \right) \end{aligned} \quad (5.7)$$

For the southern hemisphere, values returned from previous equations range from 270 to 360 degrees. Hence, we need to make sure the latitude is within the range of $[-90, +90]$ by applying the following equations:

$$\begin{aligned} \text{lat}_{\text{even}} &= \text{lat}_{\text{even}} - 360, & \text{if } \text{lat}_{\text{even}} \geq 270 \\ \text{lat}_{\text{odd}} &= \text{lat}_{\text{odd}} - 360, & \text{if } \text{lat}_{\text{odd}} \geq 270 \end{aligned} \quad (5.8)$$

Before proceeding to the longitude calculation, we need to compute $\text{NL}(\text{lat}_{\text{even}})$ and $\text{NL}(\text{lat}_{\text{odd}})$ to check if both values are the same. If not, this means the pair of messages are from different longitude zones, and it is not possible to compute the correct global position.

In this case, decoding should be stopped, and it is necessary to wait for a pair of messages that are from the same latitude zone. This situation happens when aircraft are flying across the boundaries of longitude zones.

The final latitude is chosen according to the time stamps of the messages as:

$$\text{lat} = \begin{cases} \text{lat}_{\text{even}} & \text{if } T_{\text{even}} \geq T_{\text{odd}} \\ \text{lat}_{\text{odd}} & \text{otherwise} \end{cases} \quad (5.9)$$

where the current latitude is the more recent of these two latitudes.

5.3.2 Calculation of longitude

First, the longitude index, m , can be calculated as:

$$m = \text{floor} \left(\text{lon}_{\text{cpr,even}} \cdot \left[\text{NL}(\text{lat}) - 1 \right] - \text{lon}_{\text{cpr,odd}} \cdot \text{NL}(\text{lat}) + \frac{1}{2} \right) \quad (5.10)$$

We also need to calculate the longitude zone size, which is dependent on the latitude. For even and odd messages, the number of longitude zones is defined as:

$$\begin{aligned} n_{\text{even}} &= \max[\text{NL}(\text{lat}), 1] \\ n_{\text{odd}} &= \max[\text{NL}(\text{lat} - 1), 1] \end{aligned} \quad (5.11)$$

The longitude zone sizes are defined as follows:

$$\begin{aligned} \text{dLon}_{\text{even}} &= \frac{360^\circ}{n_{\text{even}}} \\ \text{dLon}_{\text{odd}} &= \frac{360^\circ}{n_{\text{odd}}} \end{aligned} \quad (5.12)$$

Then, the longitude is calculated as:

$$\begin{aligned} \text{lon}_{\text{even}} &= \text{dLon}_{\text{even}} \left[\text{mod}(m, n_{\text{even}}) + \text{lon}_{\text{cpr,even}} \right] \\ \text{lon}_{\text{odd}} &= \text{dLon}_{\text{odd}} \left[\text{mod}(m, n_{\text{odd}}) + \text{lon}_{\text{cpr,odd}} \right] \end{aligned} \quad (5.13)$$

Similarly, the final longitude is chosen according to the time stamps of the messages as:

$$\text{lon} = \begin{cases} \text{lon}_{\text{even}} & \text{if } T_{\text{even}} \geq T_{\text{odd}} \\ \text{lon}_{\text{odd}} & \text{otherwise} \end{cases} \quad (5.14)$$

It is worth noting that the longitudes in position messages are between 0 and 360 degrees. We often need to convert them to the range between -180 and 180 degrees, which is consistent with aviation conventions. We can convert them as:

$$\text{lon} = \text{lon} - 360, \quad \text{if } \text{lon} \geq 180 \quad (5.15)$$

5.3.3 Example

The example contains two position messages that are received within 10 seconds. The first message is the most recent position message transmitted by the aircraft.

```
8D40621D58C382D690C8AC2863A7    (most recent)
8D40621D58C386435CC412692AD6
```

Following the common ADS-B message structure, we can identify the ICAO address and payload as follows:

+-----+		+-----+		+-----+	
	ICAO	Data		PI	
+-----+					
8D	40621D	58C382D690C8AC	2863A7		
8D	40621D	58C386435CC412	692AD6		
+-----+					

We can convert the message data into binary format:

+-----+		+-----+		+-----+		+-----+	
TC		ALT	T F	CPR-LAT		CPR-LON	
+-----+							
01011	000	110000111000	0 0	10110101101001000	01100100010101100		
01011	000	110000111000	0 1	10010000110101110	01100010000010010		
+-----+							

It is possible to extract the encoded CPR latitude and longitude binary and convert them to decimal format. Then, these values are divided by the 2^{17} , representing the fractions of the positions within the latitude and longitude grids:

$$\begin{aligned}
 \text{lat}_{\text{cpr,even}} &= \frac{93000}{2^{17}} \\
 \text{lon}_{\text{cpr,even}} &= \frac{51372}{2^{17}} \\
 \text{lat}_{\text{cpr,odd}} &= \frac{74158}{2^{17}} \\
 \text{lon}_{\text{cpr,odd}} &= \frac{50194}{2^{17}}
 \end{aligned} \tag{5.16}$$

We can calculate the latitude index, j , as:

$$j = \text{floor} \left(59 \times \frac{93000}{2^{17}} - 60 \times \frac{51372}{2^{17}} + \frac{1}{2} \right) = 8 \tag{5.17}$$

Then, we can decode the latitudes from both even and odd messages:

$$\begin{aligned}
 \text{lat}_{\text{even}} &= \frac{360}{4 \times 15} \left[\text{mod}(8, 60) + \frac{93000}{2^{17}} \right] = 52.25720214843750 \\
 \text{lat}_{\text{odd}} &= \frac{360}{4 \times 15 - 1} \left[\text{mod}(8, 59) + \frac{74158}{2^{17}} \right] = 52.26578017412606
 \end{aligned} \tag{5.18}$$

After validating the longitude zone of both messages:

$$\begin{aligned} \text{NL}(\text{lat}_{\text{even}}) &= \text{NL}(52.25720214843750) = 36 \\ \text{NL}(\text{lat}_{\text{odd}}) &= \text{NL}(52.26578017412606) = 36 \end{aligned} \quad (5.19)$$

we can continue to calculate the global position. Since the even message is the most recent message, the latitude is:

$$\text{lat} = \text{lat}_{\text{even}} = 52.25720214843750 \quad (5.20)$$

The final longitude (based on the even message) is calculated as:

$$m = \text{floor} \left(\frac{51372}{2^{17}} \times (36 - 1) - \frac{50194}{2^{17}} \times 36 + \frac{1}{2} \right) = 0 \quad (5.21)$$

$$n = \text{max} \left(36 - 0, 1 \right) = 36 \quad (5.22)$$

$$\text{lon} = \frac{360}{36} \left[\text{mod}(0, 36) + \frac{51372}{2^{17}} \right] = 3.91937255859375 \quad (5.23)$$

Try it out

Using `pyModeS`, we can perform the previous calculation of globally unambiguous position as:

```
import pyModeS as pms

msg0 = "8D40621D58C382D690C8AC2863A7"
msg1 = "8D40621D58C386435CC412692AD6"
t0 = 1457996402
t1 = 1457996400

position = pms.adsb.position(msg0, msg1, t0, t1)
```

5.4 Locally unambiguous position decoding

Previously, a globally unambiguous position has been decoded using a pair of odd and even messages. In this part, we will discuss how to decode the ADS-B position with one message and a previous reference position that is obtained using globally unambiguous decoding.

This method offers the possibility to continuous decode aircraft using only one message. It computes the latitude index (j) and the longitude index (m) based on this existing reference position and can be applied to both odd and even messages.

5.4.1 The reference position

The reference position should be close to the actual position, which must be within a 180 NM range. For example, this can be the position of aircraft that is decoded in the previous update. The range limitation is to ensure the consistency of the latitude and longitude zones between the reference position and decoding position. The reference position is denoted as $(\text{lat}_{\text{ref}}, \text{lon}_{\text{ref}})$.

5.4.2 Calculation of latitude

Denote i as the value dependent on the type of the message:

$$i = \begin{cases} 0, & \text{even message} \\ 1, & \text{odd message} \end{cases} \quad (5.24)$$

The latitude zone size is different depending on the message type:

$$\text{dLat} = \frac{360}{4n_z - i} \quad (5.25)$$

Then, the latitude zone index, j , is calculated as:

$$j = \text{floor}\left(\frac{\text{lat}_{\text{ref}}}{\text{dLat}}\right) + \text{floor}\left[\frac{\text{mod}(\text{lat}_{\text{ref}}, \text{dLat})}{\text{dLat}} - \text{lat}_{\text{cpr}} + \frac{1}{2}\right] \quad (5.26)$$

Knowing the latitude zone index, the latitude of the new position is:

$$\text{lat} = \text{dLat} \cdot (j + \text{lat}_{\text{cpr}}) \quad (5.27)$$

5.4.3 Calculation of longitude

Next, we can calculate the increment of the longitude per zone based on the decoded latitude, which is dependent on both message type and latitude:

$$\text{dLon} = \frac{360}{\max(\text{NL}(\text{lat}) - i, 1)} \quad (5.28)$$

Then, the longitude zone index, m , is calculated as:

$$m = \text{floor}\left(\frac{\text{lon}_{\text{ref}}}{\text{dLon}}\right) + \text{floor}\left(\frac{\text{mod}(\text{lon}_{\text{ref}}, \text{dLon})}{\text{dLon}} - \text{lon}_{\text{cpr}} + \frac{1}{2}\right) \quad (5.29)$$

Knowing the longitude zone index, the longitude of the new position is:

$$\text{lon} = \text{dLon} \cdot (m + \text{lon}_{\text{cpr}}) \quad (5.30)$$

5.4.4 Example

Next, we illustrate the decoding process of the messages from the previous example with a reference position. The message and the reference position are as follows:

```

Message: 8D40621D58C382D690C8AC2863A7
Data:      58C382D690C8AC

Reference position: (52.258, 3.918)

```

We can easily covert the message data to binary:

TC	ALT	T	F	CPR-LAT	CPR-LON
01011	000	110000111000	0	0	10110101101001000
				93000	51372

First, since this is an even message ($i = 0$), we can calculate the latitude as follows:

$$dLat = \frac{360}{4 \times 15 - 0} = 6 \quad (5.31)$$

$$j = \text{floor}\left(\frac{52.258}{6}\right) + \text{floor}\left[\frac{\text{mod}(52.258, 6)}{6} - \frac{93000}{2^{17}} + \frac{1}{2}\right] = 8 \quad (5.32)$$

$$\text{lat} = 6 \times \left(8 + \frac{93000}{2^{17}}\right) = 52.2572021484375 \quad (5.33)$$

Next, the longitude can be calculated as follows:

$$dLon = \frac{360}{\max(\text{NL}(\text{lat}_{\text{even}}) - 0, 1)} = \frac{360}{\max(36, 1)} = 10 \quad (5.34)$$

$$m = \text{floor}\left(\frac{3.918}{10}\right) + \text{floor}\left(\frac{\text{mod}(3.918, 10)}{10} - \frac{51372}{2^{17}} + \frac{1}{2}\right) = 0 \quad (5.35)$$

$$\text{lon} = 10 \times \left(0 + \frac{51372}{2^{17}}\right) = 3.91937255859375 \quad (5.36)$$

Try it out

Using `pyModeS`, we can perform the previous locally unambiguous position calculation as:

```
import pyModeS as pms

msg = "8D40621D58C382D690C8AC2863A7"
lat_ref = 52.258
lon_ref = 3.918

position = pms.adsb.position_with_ref(msg, lat_ref, lon_ref)
```

5.5 Altitude decoding

The altitude of the aircraft can be decoded with one position message, regardless of it being an even or odd type. However, depending on the type code of the messages, the altitudes are decoded differently. In Table 3.3 from chapter 3, two different types of altitudes are shown. They are:

- **TC=9-18:** Airborne position, with barometric altitude encoded (in feet)
- **TC=20-22:** Airborne position, with GNSS Height encoded (in meters)

5.5.1 Barometric altitude

For barometric altitude (TC between 9 and 18), the 8th bit of the 12-bit altitude field is the *Q bit*. It indicates whether the altitude is encoded with an increment of 25 ft or 100 ft.

When $Q = 1$, the altitude is encoded with a 25 ft increment. Removing the *Q-bit*, the altitude shall be the multiple of 25 ft minus 1000 ft:

$$h = 25 N - 1000 \quad (\text{ft}) \quad (5.37)$$

For example, based the example message in the previous section, the 12 bits in the altitude field can be read as follows:

```
1100001 1 1000
          ^
          Q-bit
```

Once the *Q-bit* is removed, the decimal representation of the remaining bits is 1560:

```
11000011000 -> 1560
```

The altitude of the aircraft becomes:

$$1560 \times 25 - 1000 = 38000 \quad (\text{ft}) \quad (5.38)$$

In the case where the altitude is higher than 50175 ft, a 100 ft increment is used. In this situation, the Q bit is set to 0, and the rest of the bits are encoded using Gray code.

It is worth noting that when all bits of the altitude fields are zeros, the altitude information is not available or not valid.

5.5.2 GNSS height

When the position message has the Type Code from 20 to 22, the 12-bit altitude field is used for the encoding of the GNSS height. The GNSS height is derived from the global positioning satellites, and the decimal value of all 12 bits translates into the height of aircraft in meters.

Try it out

Using `pyModeS`, we can perform the altitude decoding as:

```
import pyModeS as pms

msg = "8D40621D58C382D690C8AC2863A7"

altitude = pms.adsb.altitude(msg)
```

5.6 Verification of decoded positions

It is recommended to perform a *reasonable test* to validate the decoded position. There are a couple of ways to perform such a reasonable test:

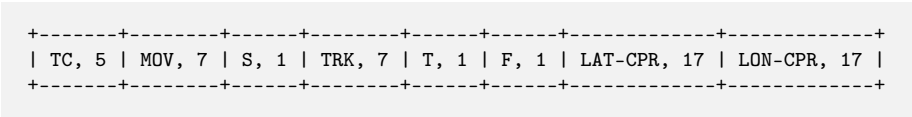
1. The first approach is to use the receiver position. The decoded position should not exceed the coverage of the receiver. See chapter 2, Figure 2.2.
2. A further test is to use more than one pair of different messages to produce multiple globally unambiguous positions. Then, the distance between these positions can be used to examine whether the decoded positions are reasonable.

If the decoded position fails the reasonable tests, it should be discarded.

6 | Surface Position

When an aircraft is on the ground, a different type of message is used to broadcast its position information. Unlike the airborne position message, the surface position message also includes the speed of the aircraft. Since no altitude information needs to be transmitted, this provides extra bits for extra information, such as speed and track angle.

The surface position message has the Type Code from 5 to 8, which also represents the level of uncertainties in the position. And the structure of the surface position message payload is shown as follows:



We can see that the fields are defined similarly to the ones from airborne messages, except that the surveillance status and altitude bits are replaced by movement and ground track. The details of the fields are shown in Table 6.1

Table 6.1: Surface position message structure

FIELD		MSG	MB	BITS
Type Code	TC	33-37	1-5	5
Movement	MOV	38-44	6-12	7
Status for ground track 0: Invalid 1: Valid	S	45	13	1
Ground track	TRK	46-52	14-20	7
Time	T	53	21	1
CPR Format 0: even frame 1: odd frame	F	54	22	1
Encoded latitude	LAR-CPR	55-71	23-39	17
Encoded longitude	LON-CPR	72-88	40-56	17

6.1 Movement

The movement field encodes the aircraft ground speed. The ground speed of the aircraft is encoded non-linearly and with different quantizations. This is to ensure that a lower speed can be encoded with a improved precision than a higher speed. Different levels of quantizations are defined in Table 6.2.

Table 6.2: Surface position movement (ground speed) decoding

Encoded speed	Ground speed range	Quantization
0	Speed not available	
1	Stopped ($v < 0.125$ kt)	
2 - 8	$0.125 \leq v < 1$ kt	0.125 kt steps
9 - 12	$1 \text{ kt} \leq v < 2$ kt	0.25 kt steps
13 - 38	$2 \text{ kt} \leq v < 15$ kt	0.5 kt steps
39 - 93	$15 \text{ kt} \leq v < 70$ kt	1 kt steps
94 - 108	$70 \text{ kt} \leq v < 100$ kt	2 kt steps
109 - 123	$100 \text{ kt} \leq v < 175$ kt	5 kt steps
124	$v \geq 175$ kt	
125 - 127	Reserved	

6.2 Ground track

The ground track is encoded with a precision of (and rounded to) $360/128$ degrees. Zero degrees represents an aircraft ground track that is aligned with the true north. Based on the encoded value (n), the ground track (χ) is calculated as:

$$\chi = \frac{360}{128} n \quad (\text{degrees}) \quad (6.1)$$

When the status for the ground track field is set to 0, the information contained in the ground track fields should be considered as invalid.

6.3 Position

Like coordinates from airborne messages, the surface latitude and longitude are also encoded in the Compact Position Reporting (CPR) format. CPR format bit indicates whether the message is a *even* or *odd* message. There are only a few slight differences in decoding the surface position positions.

First, the latitude zone size is four times smaller, which is defined as:

$$\begin{aligned} d\text{Lat}_{\text{even}} &= \frac{90^\circ}{4N_Z} \\ d\text{Lat}_{\text{odd}} &= \frac{90^\circ}{4N_Z - 1} \end{aligned} \quad (6.2)$$

Similarly, the longitude zone size is also smaller, which is:

$$\begin{aligned} d\text{Lon}_{\text{even}} &= \frac{90^\circ}{n_{\text{even}}} \\ d\text{Lon}_{\text{odd}} &= \frac{90^\circ}{n_{\text{odd}}} \end{aligned} \quad (6.3)$$

The algorithm used to encode the position is essentially the same as the one used for encoding airborne position. All the other equations from chapter 5 can be used to decode surface position.

The main difference, when compared to the airborne position, is that the original number of bits used for encoding surface coordinates is 19 instead of 17. However in the message, only the lower-order 17 bits are included and transmitted in the surface message. Thus, there can be multiple solutions for a pair of odd and even messages, even when globally unambiguous decoding is used. To identify the correct solution, a reference position needs to be given. This can be the position of the receiver or the location of the airfield.

When employing locally unambiguous decoding, the reference position needs to be within 45 nautical miles of the actual location. Commonly, the positions of the airport is used.

With the equations from section 5.3.1, the solution refers to the latitude located at the northern hemisphere. We need to compute a southern hemisphere solution by subtracting this value with 90 degrees. The final correct latitude is the one that is closet to the reference position.

Similarly, with the equations from section 5.3.2, the solution refers only the longitude in the 0 to 90 degrees quadrant. We need to compute the other three possible solutions by adding 90, 180, and 270 degrees. The final correct longitude is also the one that is closet to the reference position.

6.4 Example

6.4.1 Globally unambiguous decoding

First, we decode the location using globally unambiguous decoding. The following example contains an even/odd pair of surface position messages:

```
8C4841753AAB238733C8CD4020B1
8C4841753A8A35323FAEBDAC702D (most recent)
```

Based on the ADS-B message structure, we can identify the ICAO address and message payload data as follows:

```

+-----+-----+-----+-----+
|   |   | ICAO |   | Data   |   | PI   |   |
+-----+-----+-----+-----+
| 8C | 484175 | 3AAB238733C8CD | 4020B1 |
| 8C | 484175 | 3A8A35323FAEBD | AC702D |
+-----+-----+-----+-----+

```

We can covert the message data into binary format:

```

+-----+-----+-----+-----+-----+-----+-----+-----+
| TC   | MOV   | S | TRK   | T | F | CPR-LAT   | CPR-LON   |
+-----+-----+-----+-----+-----+-----+-----+-----+
| 00111 | 0101010 | 1 | 0110010 | 0 | 0 | 11100001110011001 | 11100100011001101 |
| 00111 | 0101000 | 1 | 0100011 | 0 | 1 | 01001100100011111 | 11010111010111101 |
+-----+-----+-----+-----+-----+-----+-----+-----+

```

Knowing the receiver location:

```

reference latitude: 51.990
reference longitude: 4.375

```

it is possible to extract the encoded CPR latitude and longitude binary and convert them to decimal format. Then, they are divided by the 2^{17} , representing the fractions of the positions within the latitude and longitude grids:

$$\begin{aligned}
 \text{lat}_{\text{cpr,even}} &= \frac{115609}{2^{17}} \\
 \text{lon}_{\text{cpr,even}} &= \frac{116941}{2^{17}} \\
 \text{lat}_{\text{cpr,odd}} &= \frac{39199}{2^{17}} \\
 \text{lon}_{\text{cpr,odd}} &= \frac{110269}{2^{17}}
 \end{aligned} \tag{6.4}$$

We can calculate the latitude index, j , as:

$$j = \text{floor} \left(59 \times \frac{115609}{2^{17}} - 60 \times \frac{39199}{2^{17}} + \frac{1}{2} \right) = 34 \tag{6.5}$$

Then, we can decode the latitudes from both even and odd messages:

$$\begin{aligned}
 \text{lat}_{\text{even}} &= \frac{90}{4 \times 15} \left[\text{mod}(34, 60) + \frac{115609}{2^{17}} \right] = 52.323040008544920 \\
 \text{lat}_{\text{odd}} &= \frac{90}{4 \times 15 - 1} \left[\text{mod}(34, 59) + \frac{39199}{2^{17}} \right] = 52.320607072215964
 \end{aligned} \tag{6.6}$$

After validating the longitude zone of both messages are the same:

$$\begin{aligned} \text{NL}(\text{lat}_{\text{even}}) &= \text{NL}(52.323040008544920) = 36 \\ \text{NL}(\text{lat}_{\text{odd}}) &= \text{NL}(52.320607072215964) = 36 \end{aligned} \quad (6.7)$$

we can continue to calculate the global position. Since the even message is the most recent message, the northern hemisphere latitude solution is:

$$\text{lat}_N = \text{lat}_{\text{odd}} = 52.320607072215964 \quad (6.8)$$

The southern hemisphere latitude solution is:

$$\text{lat}_S = 52.320607072215964 - 90 = -37.679392927784036 \quad (6.9)$$

By comparing the result with the reference latitude (51.990), the final latitude value is the one located in the northern hemisphere.

$$\text{lat} = \text{lat}_N = 52.320607072215964 \quad (6.10)$$

The longitude solution in the first quadrant of 0 to 90 degree is calculated based on the most recent (odd) message:

$$m = \text{floor} \left(\frac{116941}{2^{17}} \times (36 - 1) - \frac{110269}{2^{17}} \times 36 + \frac{1}{2} \right) = 1 \quad (6.11)$$

$$n = \text{max} \left(36 - 1, 1 \right) = 35 \quad (6.12)$$

$$\text{lon}_1 = \frac{90}{35} \left[\text{mod}(1, 36 - 1) + \frac{110269}{2^{17}} \right] = 4.734734671456474 \quad (6.13)$$

The three other possible solutions are:

$$\begin{aligned} \text{lon}_2 &= \text{lon}_1 + 90 = 94.734734671456474 \\ \text{lon}_3 &= \text{lon}_1 + 180 = 184.734734671456474 \\ \text{lon}_4 &= \text{lon}_1 + 270 = 274.734734671456474 \end{aligned} \quad (6.14)$$

By comparing with the reference longitude (4.375), the final longitude is the one located in the first quadrant. Combining the result of previously obtained latitude, the final decoded coordinates (rounded up to 6 decimal position) are:

latitude: 52.320607
longitude: 4.734735

Try it out

Using `pyModeS` , we can perform the decoding of this globally unambiguous surface position as:

```
import pyModeS as pms

msg0 = "8C4841753AAB238733C8CD4020B1"
msg1 = "8C4841753A8A35323FAEBDAC702D"
t0 = 1457996410
t1 = 1457996412
lat_ref = 51.990
lon_ref = 4.375

position = pms.adsb.position(msg0, msg1, t0, t1, lat_ref, lon_ref)
```

Note that the reference coordinates are needed for decoding the surface position. In this case the reference is the coordinates of the airfield.

6.4.2 Locally unambiguous decoding

Secondly, we decode the location using locally unambiguous decoding. In this case, we want to use the position obtained previously as the reference.

The new message received is:

8C4841753A9A153237AEF0F275BE

The structure of the ADS-B message is:

+-----+-----+-----+-----+		+-----+-----+-----+-----+				
	ICAO		Data		PI	
+-----+-----+-----+-----+		+-----+-----+-----+-----+				
	8C 484175		3A9A153237AEF0		F275BE	
+-----+-----+-----+-----+		+-----+-----+-----+-----+				

We can covert the message data into binary format:

+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	
TC	MOV	S TRK	T F	CPR-LAT		CPR-LON	
+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	
00111	0101001	1 0100001	0 1	01001100100011011		11010111011110000	
+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	

$$dLat = \frac{90}{4 \times 15 - 1} = \frac{90}{59} \quad (6.15)$$

$$j = \text{floor} \left(\frac{52.320607}{90/59} \right) + \text{floor} \left[\frac{\text{mod}(52.320607, 90/59)}{90/59} - \frac{39195}{2^{17}} + \frac{1}{2} \right] = 34 \quad (6.16)$$

$$\text{lat} = \text{lat}_{\text{odd}} = \frac{90}{59} \times \left(34 + \frac{39195}{2^{17}} \right) = 52.32056051997815 \quad (6.17)$$

Next, the longitude can be calculated as follows:

$$dLon = \frac{90}{\max(\text{NL}(\text{lat}_{\text{odd}}) - 1, 1)} = \frac{90}{\max(36 - 1, 1)} = \frac{90}{35} \quad (6.18)$$

$$m = \text{floor} \left(\frac{4.734735}{90/35} \right) + \text{floor} \left(\frac{\text{mod}(4.734735, 90/35)}{90/35} - \frac{110320}{2^{17}} + \frac{1}{2} \right) = 1 \quad (6.19)$$

$$\text{lon} = \frac{90}{35} \times \left(1 + \frac{110320}{2^{17}} \right) = 4.735735212053571 \quad (6.20)$$

The final decoded coordinates (rounded up to 6 decimal positions) are:

```
latitude: 52.320561
longitude: 4.735735
```

Try it out

Using `pyModeS`, we can perform the decoding of this locally unambiguous surface position as:

```
import pyModeS as pms

msg = "8C4841753A9A153237AEF0F275BE"
lat_ref = 51.990
lon_ref = 4.375

position = pms.adsb.position_with_ref(msg, lat_ref, lon_ref)
```

6.4.3 Movement and track

As a continuation of the previous example, we can also calculate the speed and track angle from the movement and track fields.

The decimal value of movement `0101001` is `41`. Based on Table 6.2, the speed is encoded using 1 kt steps. Thus, the speed of aircraft is:

$$15 + (42 - 39) \times 1 = 17kt \quad (6.21)$$

The decimal value of track angle 0100001 is 33 . The track angle can be calculated as:

$$\frac{360^\circ}{128} \times 33 = 92.8125^\circ \quad (6.22)$$

Try it out

Using `pyModeS` , we can perform the decoding aircraft speed and track angle as:

```
import pyModeS as pms

msg = "8C4841753A9A153237AEF0F275BE"

spd, trk, vs, tag = pms.adsb.velocity(msg)
```

Note that the last two parameters returned by the previous function are vertical speed and a tag indicate whether the speed is ground speed (GS) or airspeed (IAS/-TAS).

7 | Airborne Velocity

Airborne velocities are all transmitted with Type Code 19 (TC=19). Four different subtypes are defined with bit 6 to 8 in the message payload bits. With subtypes 1 and 2, ground speeds of aircraft are reported. With subtypes 3 and 4, aircraft true airspeed or indicated airspeed are included. Reporting of airspeed in ADS-B only occurs when aircraft position can not be determined based on the GNSS system.¹

Among all four different sub-types, sub-type 2 and 4 are designed for supersonic aircraft. Their message structures are identical to subtypes 1 and 3, but with the speed resolution of 4 kt instead of 1 kt. However, since there are no operational supersonic airliners currently, there is no ADS-B airborne velocity message with sub-type 2 and 4.

These messages contain more information than just horizontal and vertical velocity. Two other significant types of information are the navigation uncertainty category for velocity, and the difference between the GNSS height and barometric altitude. For instance, the study in [15] has made use of the later information to better model the air temperature at higher altitudes.

All sub-types share a similar overall message structure, with the different definitions from message bits 14 to 35 (or frame bits 46 to 67). The general structure of the message is shown in Table 7.1.

Comparing to position messages, the decoding of velocity messages is more straight forward since there is no complicated encoding scheme. In this chapter, we are going to explain the decoding process.

7.1 Example messages

Throughout this chapter, we will use two example messages to illustrate the decoding process:

```
Message A: 8D485020994409940838175B284F (sub-type 1)
Message B: 8DA05F219B06B6AF189400CBC33F (sub-type 3)
```

By decomposing the messages, the downlink format, ICAO address, message payload, and CRC remainder are shown as follows:

¹ In the real world, subtype 3 messages are very rare.

Table 7.1: Airborne velocity message structure

FIELD	ABBR	FB	ME	N-BITS
Type Code TC=19 [Binary: 10011]	TC	33 : 37	1 : 5	5
Sub-type 1: Subsonic 2: Supersonic	ST	38 : 40	6 : 8	3
Intent change flag	IC	41	9	1
IFR capability flag	IFR	42	10	1
Navigation uncertainty category for velocity Denoted as NUCr for ADS-B version 0 Denoted as NUCv for ADS-B version 1-2	NUCr or NUCv	43 : 45	11 : 13	3
Sub-type specific fileds Refer to Table 7.2 and Table 7.3		46 : 67	14 : 35	22
Source bit for vertical rate 0: GNSS, 1: Barometer	VrSrc	38	36	1
Sign bit for vertical rate 0: Up, 1: Down	Svr	69	37	1
Vertical rate All zeros: no information LSB: 64 ft/min VR = 64 x (Decimal value - 1)	VR	70 : 78	38 : 46	9
Reserved		79 80	47 48	2
Sign bit for GNSS and Baro altitudes difference 0: GNSS alt above Baro alt 1: GNSS alt below Baro alt	SDif	81	49	1
Differen between GNSS and Baro altitudes All zeros: no information LSB: 25 ft	DAlt	82 : 88	50 : 56	7

Message A (sub-type 1):

```
+-----+-----+-----+-----+
| DF | ICAO | ME | CRC |
+-----+-----+-----+-----+
| 8D | 485020 | 99440994083817 | 5B284F |
+-----+-----+-----+-----+
```

Message B (sub-type 3):

```
+-----+-----+-----+-----+
| | ICAO | ME | CRC |
+-----+-----+-----+-----+
| 8D | A05F21 | 9B06B6AF189400 | CBC33F |
+-----+-----+-----+-----+
```

Next, we can convert both message payloads (ME fields) into binary and decompose the structure further as follows:

Message A (sub-type 1):

```
+-----+-----+-----+-----+-----+-----+-----+-----+
| TC | ST | IC | IFR | NUC | VrSrc | Svr | VR | RESV | SDif | DA1t |
+-----+-----+-----+-----+-----+-----+-----+-----+
| 10011 | 001 | 0 | 1 | 000 | 10000001001 | 0 | 1 | 000001110 | 00 | 0 | 0010111 |
| | | | | | | | | | | | | |
+-----+-----+-----+-----+-----+-----+-----+-----+
| 19 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 14 | 0 | 0 | 23 |
+-----+-----+-----+-----+-----+-----+-----+-----+
```

Message B (sub-type 3):

```
+-----+-----+-----+-----+-----+-----+-----+-----+
| TC | ST | IC | IFR | NUC | VrSrc | Svr | VR | RESV | SDif | DA1t |
+-----+-----+-----+-----+-----+-----+-----+-----+
| 10011 | 011 | 0 | 0 | 000 | 11010110110 | 1 | 1 | 000100101 | 00 | 0 | 0000000 |
| | | | | | | | | | | | | |
+-----+-----+-----+-----+-----+-----+-----+-----+
| 15 | 13 | 0 | 0 | 0 | 0 | 1 | 1 | 37 | 0 | 0 | 0 |
+-----+-----+-----+-----+-----+-----+-----+-----+
```

Here, the second rows and third rows of the messages are binary and decimal values respectively.

7.2 Vertical Rate

The method for decoding vertical rate and its related parameters are the same among all different sub-types of the messages.

First of all, the vertical rate source bit `VrSrc` (payload bit 36) indicates the source of the altitude measurements. In the case of `0`, the GNSS altitude is encoded. In the case of `1`, the barometer altitude is encoded.

The direction of vertical movement of aircraft can be read from S_{vr} bit (payload bit 37), with 0 and 1 referring to climb and descent respectively. The encoded vertical rate value VR can be computed using message payload bits 38 to 46. If the 9-bit block contains all zeros, the vertical rate information is not available.

The final vertical rate (VS) is calculated as:

$$VS = (2S_{vr} - 1) \cdot 64 \cdot (V_R - 1) \quad (7.1)$$

where the final vertical speed has the unit of ft/min.

Based on the example **Message A**, the vertical speed is calculated as:

$$VS_A = (2 \times 0 - 1) \times 64 \times (37 - 1) = -832 \text{ ft/min} \quad (7.2)$$

which indicates that the aircraft A is descending with a vertical speed of 832 ft/min.

Based on the example **Message B**, the vertical speed is calculated as:

$$VS_B = (2 \times 0 - 1) \times 64 \times (14 - 1) = -2304 \text{ ft/min} \quad (7.3)$$

which indicates that the aircraft B is descending with a vertical speed of 2304 ft/min.

7.3 Difference between GNSS and barometric altitudes

The last 8 bits of the ME filed contain the difference between the barometric and GNSS altitudes.

Within these 8 bits, the first bit indicates the sign for the value in the last 7 bits. When it is 1, the value is negative. This means the GNSS altitude is below the barometric altitude.

The value is encoded with the increment of 25 ft, and the equation to calculate the altitude difference is:

$$\Delta h = s(n - 1) \times 25 \quad (7.4)$$

where s is the sign and n is the decimal value of the encoded difference.

Based on the example **Message A**, the difference between GNSS and barometric altitude is:

$$\Delta h = 1(23 - 1) \times 25 = 550 \text{ ft} \quad (7.5)$$

When all the bits are zeros (as shown in **Message B**) or ones, the information is not available.

7.4 Sub-type 1 and 2: Ground Speed decoding

The velocity information fields of sub-type 1 and 2 messages consist of the East-West velocity component and the North-South velocity component, as well as the signs for these two values. The structure of message payload bits 14 to 35 is shown in Table 7.2.

Table 7.2: Velocity fields of sub-type 1 and 2 (message payload bit 14 to 35)

FIELD	ABBR	FB	MB	N-BITS
Direction for E-W velocity component 0: from West to East 1: from East to West	Dew	46	14	1
East-West velocity component All zeros: no information available Sub-type 1: Speed = Decimal value - 1 Sub-type 2: Speed = 4 x (Decimal value - 1) Unit: knots	Vew	47 : 56	15 : 24	10
Direction for N-S velocity component 0: from South to North 1: from North to South	Dns	57	25	1
North-South velocity component All zeros: no information available Sub-type 1: Speed = Decimal value - 1 Sub-type 2: Speed = 4 x (Decimal value - 1) Unit: knots	Dns	58 : 67	26 : 35	10

Here, we can see that message payload bit 14 and 25 are sign bits indicating the directions of each component. Each 10-bit block following these sign bits encodes a velocity component. It is important to point out that when any of the 10-bit blocks contains only zeros, no velocity information is available. For supersonic velocity (sub-type 2), the final velocity components are multiplied by a factor of 4.

To calculate the velocity, four values are needed: **Sew**, **Vew**, **Sns**, **Vns**. In aviation, it is commonly considers the West-East and South-North components as positive values, which are denoted as V_x and V_y . The formulas for sub-type 1 (subsonic) and sub-type 2 (supersonic) differ by a factor of 4.

For subsonic speed (sub-type 1), the speed components can be computed as:

$$V_x = (-2S_{ew} + 1)(V_{ew} - 1) \quad (7.6)$$

$$V_y = (-2S_{ns} + 1)(V_{ns} - 1) \quad (7.7)$$

For supersonic speed (sub-type 2), the speed components can be computed as:

$$V_x = 4 \cdot (-2S_{ew} + 1)(V_{ew} - 1) \quad (7.8)$$

$$V_y = 4 \cdot (-2S_{ns} + 1)(V_{ns} - 1) \quad (7.9)$$

The final ground speed (V) of aircraft is:

$$V = \sqrt{V_x^2 + V_y^2} \quad (7.10)$$

With these two speed components, the ground track angle (λ) of the aircraft can also be calculated conveniently:

$$\lambda = \arctan2(V_x, V_y) \cdot \frac{360}{2\pi} \quad (7.11)$$

$$\lambda = \text{mod}(\lambda, 360) \quad (7.12)$$

where Equation 7.12 ensures the track angle range of $[0, 360]$ degree, with North at 0 degrees, which is the case for most aviation applications and studies.

Base on the example message A given earlier:

Message A, payload bit 14-35

+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	
Sew	Vew	Sns	Vns	VrSrc	
+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	
1	0000001001	1	0010100000	0	
+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	
1	9	1	160	0	
+-----+-----+-----+-----+		+-----+-----+-----+-----+		+-----+-----+-----+-----+	

The final aircraft speed and track angle are calculated as:

$$V_x = (-2 + 1) \times (9 - 1) = -8 \quad (7.13)$$

$$V_y = (-2 + 1) \times (160 - 1) = -159 \quad (7.14)$$

$$V = \sqrt{(-9)^2 + (-160)^2} = 159.20 \quad (7.15)$$

$$\lambda = \arctan2(-9, -160) \times \frac{360}{2\pi} = 182.88 \quad (7.16)$$

where the aircraft speed is 159.20 kt and the track angle is 182.88 degrees.

7.5 Subtype 3 and 4: Airspeed decoding

ADS-B velocity messages with sub-type 3 or 4 are broadcast when the ground speed of the aircraft is not known. This could happen when, for example, aircraft positions cannot be obtained due to the low availability of GNSS satellites.

Previously, we see the ground speeds in sub-type 1 and 2 are encoded as the East-West and North-South components. We then convert these two components to speed and track angle. In sub-type 3 or 4, the speed and heading directly encoded. The details on related fields are described in Table 7.3.

Table 7.3: Velocity fields of sub-type 3 and 4 (message payload bit 14 to 35)

FIELD	ABBR	FB	MB	N-BITS
Status bit for magnetic heading 0: not available 1: available	SH	46	14	1
Magnetic heading LSB: 360/1024 degrees Heading = Decimal value x 360 / 1024	HDG	47 : 56	15 : 24	10
Airspeed type 0: Indicated airspeed (IAS) 1: True airspeed (TAS)	T	57	25	1
Airspeed All zeros: no information available Sub-type 1: Speed = Decimal value - 1 Sub-type 2: Speed = 4 x (Decimal value - 1) Unit: knots	AS	58 : 67	26 : 35	10

The magnetic heading (ϕ) of the aircraft is calculated as:

$$\phi = \text{HDG} \cdot \frac{360}{1024} \text{ degrees} \quad (7.17)$$

The speed calculations also differ between sub-type 3 and 4. For sub-type 3, the airspeed can be computed as:

$$V_{as} = \text{AS} - 1 \quad (7.18)$$

While for sub-type 4, the airspeed is computed as:

$$V_{as} = 4 \cdot (\text{AS} - 1) \quad (7.19)$$

Note that the airspeed type bit **T** represents whether the value is the indicated airspeed (IAS, **T=0**) or true airspeed (TAS, **T=1**).

Now, let us reflect on our previous example **Message B**:

Message B, payload bit 14-35

+---+-----+---+-----+
SH HDG T AS
+---+-----+---+-----+
1 1010110110 1 0101111000
+---+-----+---+-----+
1 694 1 376
+---+-----+---+-----+

With heading status `SH=1` , we know that the magnetic heading information is available. Thus, the heading and airspeed can be derived as:

$$\phi = 694 \times \frac{360}{1024} = 243.98 \quad (7.20)$$

$$V_{as} = 376 - 1 = 375 \quad (7.21)$$

With airspeed type `T=1` , we can also determine that the speed refers to the true airspeed of the aircraft.

Try it out

Using `pyModeS` , we can perform the decoding the airborne velocities messages as follows:

```
import pyModeS as pms

msgA = "8D485020994409940838175B284F"
msgB = "8DA05F219B06B6AF189400CBC33F"

vA = pms.adsb.velocity(msgA)
vB = pms.adsb.velocity(msgB)
```

We have the following decoded values.

```
vA: (159, 182.88, -832, 'GS')
vB: (375, 243.98, -2304, 'TAS')
```

Note that the parameters returned by the `velocity()` function are speed, track angle (or heading), vertical speed, and speed type.

8 | Aircraft Operation Status

The aircraft operational status message is designed to provide various information on an aircraft. The message has been defined in all ADS-B versions. But in practice, it is not implemented in ADS-B version 0. In ADS-B version 0, the structures include information related to aircraft operational capabilities and status for different stages of the flight. From version 1 onward, the operational status includes more information, such as ADS-B version, accuracy, and integrity indicators.

The operation status message is transmitted with Type Code 31 (TC=31). The structures of this message type differ significantly over different ADS-B versions.

8.1 Version 0

In version 0, the structure of the message is shown in Table 8.1. Two main blocks contain the status information, which includes operational capabilities (16 bits) and operational status (16 bits). Each block contains 4 parameters, and each parameter is encoded with 4 bits.

Table 8.1: Aircraft operational status (Version 0)

FIELD	ABBR	FB	MB	N-BITS
Type code = 31 Binary: 11111	TC	33 : 37	1 : 5	5
Sub-type code = 0 Binary: 000	ST	38 : 40	6 : 8	3
Enroute operational capabilities (4 bits) Terminal area operational capabilities (4 bits) Approach/landing operational capabilities (4 bits) Surface operational capabilities (4 bits)	CC4 CC3 CC2 CC1	41 : 56	9 : 24	16
Enroute operational status (4 bits) Terminal area operational status (4 bits) Approach/landing operational status (4 bits) Surface operational status (4 bits)	OM4 OM3 OM2 OM1	57 : 72	25 : 40	16
Reserved		73 : 88	41 : 56	16

However, even all the parameter fields are defined. All CC and OM bits are reserved in the third and fourth blocks according to [9], which eventually made the definitions un-usable for version 0 transponders. As version 0 transponders

do not transmit any operation status messages, the absence of TC=31 messages can help identify transponder version 0, which is discussed in chapter 3.

8.2 Version 1

From version 1 onward, the operational status report is implemented and broadcast by the transponder. In Table 8.2, the structure of operational message in version 1 is defined.

Table 8.2: Aircraft operational status (Version 1)

FIELD	ABBR	FB	MB	N-BITS
Type code = 31 Binary: 11111	TC	33 : 37	1 : 5	5
Sub-type code 0: airborne 1: surface 2-7: reserved	ST	38 : 40	6 : 8	3
ST=0: Airborne capacity class codes (16 bits) ST=1: Surface capacity codes (12 bits) + Length/width code (4 bits)	CC	41 : 56	9 : 24	16
Operational mode codes	OM	57 : 72	25 : 40	16
ADS-B version number 0: Conformant to DOC 9871, Appendix A 1: Conformant to DOC 9871, Appendix B 2-7: Reserved	VER	73 : 75	41 : 43	3
NIC supplement	NICs	76	44	1
Navigational accuracy category - position	NACp	45 : 48	77 : 80	4
ST=0: Barometric altitude quality ST=1: Reserved	BAQ –	81 82	49 50	2
Surveillance integrity level	SIL	83 84	51 52	2
ST=0: Barometric altitude integrity ST=1: Track angle or heading	BICbaro T/H	85	53	1
Horizontal reference direction	HRD	86	54	1
Reserved		87 88	55 56	2

Bits 73 to 86, which are unused in the previous version, are now defined with new parameters. These parameters include ADS-B version number and various

indicators related to the accuracy of the state measurements broadcast by the aircraft in other types of ADS-B messages.

It is worth noting that the definitions of some fields with the sub-type of the message, which differentiate between airborne status messages and surface status messages.

8.3 Version 2

Compared to the previous update, the changes in the operational status report from version 1 to 2 are minimal. Several fields are renamed and a SIL supplement bit is added to bit-87. The structure is shown in Table 8.3.

Table 8.3: Aircraft operational status (Version 2)

FIELD	ABBR	FB	MB	N-BITS
Type code = 31 Binary: 11111	TC	33 : 37	1 : 5	5
Sub-type code 0: Airborne status message 1: Surface status message	ST	38 : 40	6 : 8	3
ST=0: Airborne capacity class codes (16 bits) ST=1: Surface capacity codes (12 bits) + Length/width code (4 bits)	CC	41 : 56	9 : 24	16
ST=0: Airborne operational mode codes ST=1: Surface operational mode codes	OM	57 : 72	25 : 40	16
ADS-B version number 0: Conformance with DOC 9871, Appendix A 1: Conformance with DOC 9871, Appendix B 2: Conformance with DOC 9871, Appendix C 3-7: Reserved	VER	73 : 75	41 : 43	3
NIC supplement - A	NICa	76	44	
Navigational accuracy category - position	NACp	45 : 48	77 : 80	4
ST=0: Geometric vertical accuracy ST=1: Reserved	GVA –	81 82	49 50	2
Source integrity level	SIL	83 84	51 52	2
ST=0: Barometric altitude integrity ST=1: Track angle or heading	NICbaro T/H	85	53	1
Horizontal reference direction	HRD	86	54	1
SIL supplement	SILs	87	55	1
Reserved		88	56	1

9 | Uncertainties in ADS-B

There are many parameters in ADS-B that define the data quality of the position and velocity reports. With each evolution of the ADS-B versions, these parameters have been renamed and redefined. This creates a complicated landscape to understand and to analyze these indicators. This chapter is designed to give a better overview and mapping among data quality parameters across different ADS-B versions.

9.1 Terminology

In general, there are three types of data quality indicators:

- **Uncertainty indicators:** These indicators are introduced in version 0. Parameter values indicate that at least 95% of measurements are within the allowed uncertainty (accuracy) bounds.
- **Accuracy indicators:** These indicators are first introduced in version 1 and are intended to replace previous uncertainty indicators. Parameter values also indicate that at least 95% of measurements are within the allowed accuracy bounds.
- **Integrity indicators:** These indicators are also first introduced in version 1. Each value corresponds to a probability of a measurement being outside of the expected accuracy/uncertainty bounds.

Commonly, two parameters are related to the position and velocity separately in each group of indicators. Table 9.1 shows the six major uncertainty indicators related ADS-B versions and their value ranges.

Table 9.1: Data quality indicators

Indicator	Acronym	Version	Values
Navigation uncertainty category - position	NUCp	0	0 - 9
Navigation uncertainty category - rate (velocity)	NUCr	0	0 - 4
Navigation accuracy category - position	NACp	1, 2	0 - 11
Navigation accuracy category - velocity	NACv	1, 2	0 - 4
Navigation integrity category	NIC	1, 2	0 - 11
Surveillance integrity level	SIL	1, 2	0 - 3

Each quality indicator also relates to a set of parameters that express the exact amount of uncertainties, errors, or probabilities. In Table 9.2, these parameters are listed.

Table 9.2: Parameters related with uncertainty, accuracy, and integrity

	Paramter	
NUCp (V0)	Horizontal protection limit	HPL
	95% containment radius on horizontal position error	RCxy
	95% containment radius on vertical position error	RCz
NUCr (V0)	Horizontal velocity error (95%)	HVE
	Vertical velocity error (95%)	VVE
NACp (V1,2)	Estimated position uncertainty (95% horizontal accuracy - p) a.k.a. horizontal figure of merit (HFOM) in GNSS	EPU
	Vertical estimated position uncertainty (95% vertical accuracy - p) a.k.a. vertical figure of merit (VHPM) in GNSS	VEPU
NACv (V1,2)	Horizontal figure of merit (95% horizontal accuracy - v)	HFOMr
	Vertical figure of merit (95% horizontal accuracy - v)	VFOMr
NIC (V1,2)	Horizontal containment radius limit	RC
	Vertical protection limit	VPL
SIL (V1,2)	Probability of exceeding horizontal containment radius	P-RC
	Probability of exceeding vertical integrity containment region	P-VPL

These parameters are identified by different bits from different messages. Due to the evolution of ADS-B versions, the definitions can also differ. In order to correctly obtain these parameters, the version of ADS-B transponder used must be identified. This can be based on the logic explained in chapter 3.

In the rest of this chapter, these parameters are explained in detail according to different ADS-B versions. The changes in the same parameters between different versions are also indicated.

9.2 Version 0

In ADS-B version 0, only uncertainties are defined. Two sets of parameters are related to the position and velocity (or rate) separately.

9.2.1 Navigation uncertainty category - position (NUCp)

NUCp is directly related to ADS-B Type Code with one-to-one mapping. The mapping between Type Code and NUCp in surface position messages and the two types of airborne position messages is shown in Table 9.3.

In general, a higher NUCp number (lower TC number) represents higher confidence in the position measurement. When dealing with position uncertainty, the horizontal protection limit (HPL), the containment radius on horizontal position

Table 9.3: Mapping between TC and NUCp

	Surface position				
TC	0	5	6	7	8
NUCp	0	9	8	7	6

	Airborne position (Barometric altitude)									
TC	9	10	11	12	13	14	15	16	17	18
NUCp	9	8	7	6	5	4	3	2	1	0

	(GNSS altitude)		
TC	20	21	22
NUCp	9	8	0

error (RCxy), and the containment radius on vertical position error (RCz) are used to quantify the uncertainties. All values are shown in Table 9.4.

Table 9.4: NUCp parameters and their values

TC	NUCp	HPL	RCxy	RCz
0	0	N/A	N/A	N/A
5	9	<7.5 m	<3 m	N/A
6	8	<25 m	<10 m	N/A
7	7	<0.1 NM (185 m)	<0.05 NM (93 m)	N/A
8	6	>0.1 NM (185 m)	>0.05 NM (93 m)	N/A
9	9	<7.5 m	<3 m	N/A
10	8	<25 m	<10 m	N/A
11	7	<0.1 NM (185 m)	<0.05 NM (93 m)	N/A
12	6	<0.2 NM (370 m)	<0.1 NM (185 m)	N/A
13	5	<0.5 NM (926 m)	<0.25 NM (463 m)	N/A
14	4	<1 NM (1852 m)	<0.5 NM (926 m)	N/A
15	3	<2 NM (3704 m)	<1 NM (1852 m)	N/A
16	2	<10 NM (18520 m)	<5 NM (9260 m)	N/A
17	1	<20 NM (37040 m)	<10 NM (18520 m)	N/A
18	0	>20 NM (37040 m)	>10 NM (18520 m)	N/A
20	9	<7.5 m	<3 m	<4 m
21	8	<25 m	<10 m	<15 m
22	0	>25 m	>10 m	>15 m

It is worth noting that, in the case of airborne position with GNSS height (TC=20-22), HPL and RCxy are defined with slight differences compared to

other types of position messages. In addition, the containment radius for the vertical position (RCv) is also defined in this message. This is possible because the altitude is obtained from GNSS sources.

9.2.2 Navigation uncertainty category - rate (NUCr)

The Navigation Uncertainty Category - rate (NUCr) is used to indicate the uncertainty of the horizontal and vertical speeds. The bits representing NUCr can be found in the airborne velocity message (TC=19). The NUCr is located at message bit 43-45 (or payload bit 11-13), which defines the 95% of the error in horizontal and vertical speed as shown in Table 9.5.

Table 9.5: NUCr parameters and their values

NUCp	HVE (95%)	VVE (95%)
0	N/A	N/A
1	<10 m/s	<15.2 m/s (50 pfs)
2	<3 m/s	<4.5 m/s (15 fps)
3	<1 m/s	<1.5 m/s (5 fps)
4	<0.3 m/s	<0.46 m/s (1.5 fps)

9.3 Version 1

In ADS-B version 1, the uncertainty category is removed, replaced by the accuracy category and the integrity category. Both NUCp and NUCr from version 0 do not exist in version 1. New indicators introduced in version 1 are NACp, NACv, NIC, and SIL.

9.3.1 Navigation integrity category (NIC)

NIC is designed to replace NUCp from version 0, but with more levels included. Like NUCp in version 0, the Navigation Integrity Category (NIC) is related to the Type Code. However, Type Code and NIC do not have a one-to-one mapping relationship. With more levels defined, a supplemental bit is required to distinguish two levels represented by some of the same Type Codes.

The NIC Supplement bit (NICs) is introduced in the operation status messages (TC=31) and located at the message bit 76 (or payload bit 44). The relationship between TC, NIC, and Rc are listed in Table 9.6.

9.3.2 Navigation accuracy category - position (NACp)

NACp is introduced in ADS-B version 1 as a complementary indicator of NIC. The NACp can be obtained from the operational status message, message frame bits 77-80 (or payload bits 45-48).

Table 9.6: NIC parameters and their values (version 1)

TC	NICs	NIC	RC	VPL
0	N/A	N/A	N/A	N/A
5	0	11	<7.5 m	N/A
6	0	10	<25 m	N/A
7	1	9	<75 m	N/A
	0	8	<0.1 NM (185 m)	N/A
8	0	0	>0.1 NM or Unknown	N/A
9	0	11	<7.5 m	<11 m
10	0	10	<25 m	<37.5 m
11	1	9	<75 m	<112 m
	0	8	<0.1 NM (185 m)	N/A
12	0	7	<0.2 NM (370 m)	N/A
13	0	6	<0.5 NM (926 m)	N/A
	1		<0.6 NM (1111 m)	N/A
14	0	5	<1.0 NM (1852 m)	N/A
15	0	4	<2 NM (3704 m)	N/A
16	1	3	<4 NM (7408 m)	N/A
	0	2	<8 NM (14.8 km)	N/A
17	0	1	<20 NM (37.0 km)	N/A
18	0	0	>20 NM or Unknown	N/A
20	0	11	<7.5 m	<11 m
21	0	10	<25 m	<37.5 m
22	0	0	>25 m	>112 m

With NACp, the 95% horizontal and vertical accuracy bounds can be determined. They are the estimated position uncertainty (EPU) and the vertical estimated position uncertainty (EPU), which are also known as the horizontal figure of merit (HFOM) and the vertical figure of merit (VFOM) in GNSS.

EPU and Rc in NIC have the following relationship:

$$\begin{aligned}
 \text{EPU} &\approx \text{Rc}/2.5 && \text{for NACp} \geq 9 \\
 \text{EPU} &\approx \text{Rc}/2.0 && \text{for NACp} < 9
 \end{aligned}
 \tag{9.1}$$

NACp and its related parameter values are defined in Table 9.7.

Table 9.7: NACp parameters and their values

NACp	EPU (or HFOM)	VEPU (or VFOM)
11	<3 m	<4 m
10	<10 m	<15 m
9	<30 m	<45 m
8	<0.05 NM (93 m)	N/A
7	<0.1 NM (185 m)	N/A
6	<0.3 NM (556 m)	N/A
5	<0.5 NM (926 m)	N/A
4	<1.0 NM (1852 m)	N/A
3	<2 NM (3704 m)	N/A
2	<4 NM (7408 m)	N/A
1	<10 NM (18520 km)	N/A
0	>10 NM or Unknown	N/A

9.3.3 Navigation accuracy category - velocity (NACv)

NACv is introduced in version 1 to replace the NUCv from version 0. The bits are located at the same location and have the same definitions of values. These bits are contained in airborne velocity message (TC=19) message bits 43-45 (or ME bits 11-13). It defines the 95% of the errors in horizontal and vertical speeds. The detailed definitions of the Horizontal Figure of Merit for rate (HFOMr) and Vertical Figure of Merit for rate (VFOMr) are shown in Table 9.8.

Table 9.8: NACv parameters and their values

NACv	HFOMr	VFOMr
0	N/A	N/A
1	<10 m/s	<15.2 m/s (50 pfs)
2	<3 m/s	<4.5 m/s (15 fps)
3	<1 m/s	<1.5 m/s (5 fps)
4	<0.3 m/s	<0.46 m/s (1.5 fps)

9.3.4 Surveillance integrity level (SIL)

SIL is introduced in version 1 and used to indicate the probability of measurements exceeding the containment radius. The SIL value can also be found in the operational status message (TC=31), message bits 83-84 (or ME bits 51-52)

Each SIL value corresponds to two probabilities that describe the horizontal (P-RC) and vertical (P-VPL) components respectively. The definitions are as follows:

Table 9.9: SIL parameters and their values

SIL	P-RC	P-VPL
0	unknown	unknown
1	$< 1 \times 10^{-3}$	$< 1 \times 10^{-3}$
2	$< 1 \times 10^{-5}$	$< 1 \times 10^{-5}$
3	$< 1 \times 10^{-7}$	$< 2 \times 10^{-7}$

The unit for P-RCu and P-VPL can be per flight hour or per sample, except when SIL=3, the unit for P-VPL becomes per 150 seconds per sample.

9.4 Version 2

There are fewer changes between version 1 and version 2 when compared to the earlier update. The major changes are the further refined NIC levels and minor updates of SIL parameters.

9.4.1 Navigation integrity category (NIC)

In version 2, NIC levels can be obtained with three additional supplement bits named NIC supplement bit A (NICa), NIC supplement bit B (NICb), and NIC supplement bit C (NICc). These bits can be found as follows:

- NICa is located in the operational status message (TC=31) (message bit 76 or ME bit 44), which is the same as in ADS-B version 1.
- NICb is located in the airborne position message (TC=9-18), message bit 40 or payload bit 8), where the Single Antenna Flag was located in previous ADS-B versions.
- NICc is also located in the operational status message (TC=31) (message bit 52 or payload bit 20).

With these supplemental bits and the Type Code, the NIC value in version 2 can be calculated. NIC values and their related Rc values are shown in Table 9.10.

9.4.2 Surveillance integrity level (SIL)

In version 2, an additional SIL supplement bit (SILs) is introduced to better distinguish whether the value has the unit of per flight hour or per sample. The SILs bit can also be found in the operational status message, message bit 87 (or ME bit 55). The definitions are:

- SILs=0: probability is *per hour* based
- SILs=1: probability is *per sample* based

The values related to SIL remain the same as what is shown in Table 9.9.

Table 9.10: NIC parameters and their values (version 2)

TC	NICa	NICb	NICc	NIC	Rc
5	0	N/A	0	11	<7.5 m
6	0	N/A	0	10	<25 m
7	1	N/A	0	9	<75 m
	0	N/A	0	8	<0.1 NM (185 m)
8	1	N/A	1	7	<0.2 NM (370 m)
	1	N/A	0	6	<0.3 NM (556 m)
	0	N/A	1		<0.6 NM (1111 m)
	0	N/A	0	0	>0.6 NM or unknown
9	0	0	N/A	11	<7.5 m
10	0	0	N/A	10	<25 m
11	1	1	N/A	9	<75 m
	0	0	N/A	8	<0.1 NM (185 m)
12	0	0	N/A	7	<0.2 NM (370 m)
13	0	1	N/A	6	<0.3 NM (556 m)
	0	0	N/A		<0.5 NM (926 m)
	1	1	N/A		<0.6 NM (1111 m)
14	0	0	N/A	5	<1.0 NM (1852 m)
15	0	0	N/A	4	<2 NM (3704 m)
16	1	1	N/A	3	<4 NM (7408 m)
	0	0	N/A	2	<8 NM (14.8 km)
17	0	0	N/A	1	<20 NM (37.0 km)
18	0	0	N/A	0	>20 NM or unknown
20	N/A	N/A	N/A	11	<7.5 m
21	N/A	N/A	N/A	10	<25 m
22	N/A	N/A	N/A	0	>25 m

9.4.3 NACp and NACv

NACp and NACv in version 2 remain the same as in version 1. Related parameters and definitions can be found in the previous Table 9.7 and Table 9.8 respectively.

10 | Error control in ADS-B

In almost all digital telecommunications, error control is an essential capability. An adequate error control coding scheme in telecommunication allows a receiver to validate the correctness of the information that has been transmitted. Sometimes, it also provides the receiver with the ability to correct errors. Depending on the characteristics of the communication channel and the types of messages, different error control coding schemes can be adopted.

For error detection, three types of error control codes are broadly used, which are 1) parity, 2) checksum, and 3) cyclic redundancy check (CRC)[4]. Though there are similarities among these concepts, they should not be confused:

- Parity is the simplest form of error detection. Commonly, the message is divided into segments of equal length. One parity bit is added to each segment and sent along with the message. The parity bit ensures either an even or odd number of 1 bits are contained in the segment. It guarantees the detection of at least one-bit errors. A two-dimensional parity check is also common, where additional parity bits are added to the same n-th bit in the segments.
- Checksum bits are longer and computed differently. The message is also first divided into segments of equal length. The checksum is generated by adding the segments using the *ones' complements arithmetic* and sent along with the message. At the receiving side, the same arithmetic can be applied, where the complement of the sum should be zero.
- CRC is an algorithm based on binary polynomial arithmetic. A pre-defined divisor (also known as *generator*) is used to compute the remainder using the binary polynomial division. The CRC remainder is appended to the message. The receiving side can run the same process on the entire message to check whether the remainder is zero. CRC is a much stronger method for error detection. It also offers the ability to correct errors [11].

Note

The CRC *remainder* term is confusingly defined in Mode S literature and standards. Many documents refer it as *parity* or *checksum*. To be consistent with Mode S standards, such as [9, 13], parity, checksum, and CRC remainder are considered to be synonyms in this book. They all refer to the CTC remainder.

10.1 CRC error control

In Mode S communications (including ADS-B), CRC error control coding is used. In all types of Mode S downlink messages, the last 24 bits are reserved for the

CRC remainder. In ADS-B, the CRC remainder is directly appended as the final 24 bits of the messages. However, in other types of Mode S messages, those bits can be overlaid with other information (such as the ICAO address) using the **XOR** (*exclusive disjunction*) operator before being appended to the message.

A basic CRC workflow is shown in Figure 10.1. The diagram on the left-hand side shows how the CRC remainder is generated on the sender side. The diagram on the right-hand side shows how the same arithmetic can be used on the receiver side to validate the message.

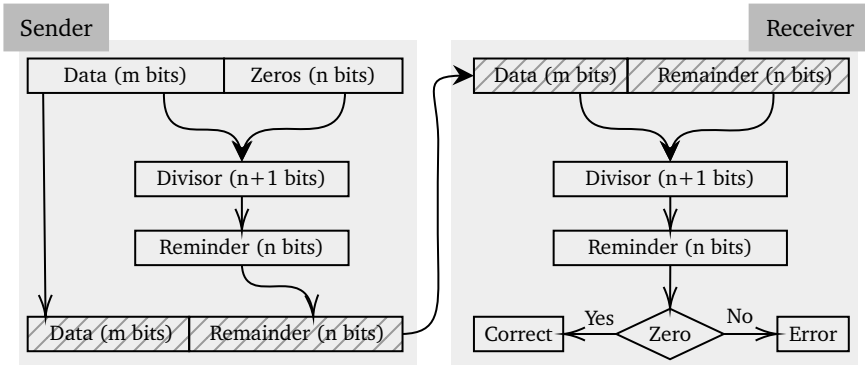


Figure 10.1: The CRC error control processes

The binary polynomial falls in the finite field arithmetic [1]. The divisions of binary polynomials can essentially be considered as the **XOR** bitwise operations, which can be easily implemented and calculated by computers. In Figure 10.2, a CRC remainder calculation example is shown.

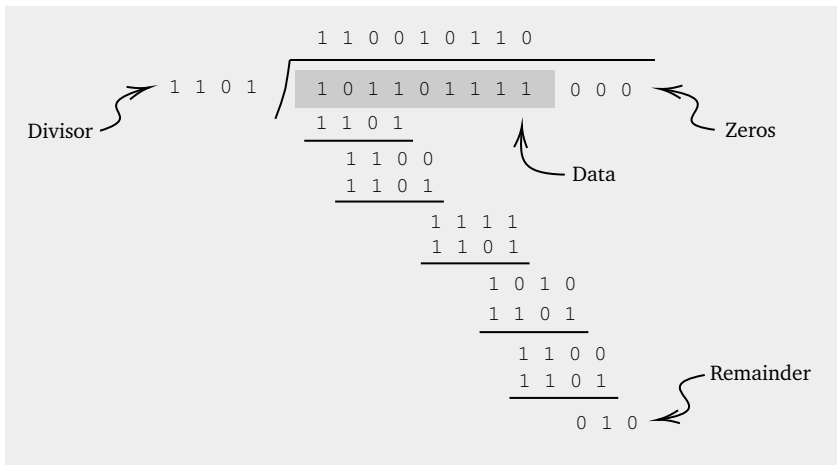


Figure 10.2: A CRC example with a 4-bit divisor and 3-bit remainder

10.2 ADS-B parity

The polynomial form of the divisor (generator) used for ADS-B (as well as other Mode S messages) is shown as following [3]:

$$G(x) = x^{24} + x^{23} + x^{22} + x^{21} + x^{20} + x^{19} + x^{18} + x^{17} + x^{16} + x^{15} + x^{14} + x^{13} + x^{12} + x^{10} + x^3 + 1 \quad (10.1)$$

where $G(x)$ represents the generator function. This generator code was found by [10], which is known for its efficiency to correct burst errors. A 24-bit remainder is generated using this generator. It can also be written in different formats as:

Binary:	1111111111111010000001001
Decimal:	33551369
Octal:	177772011
HEX:	1FFF409

Knowing the logic of CRC, the computation of the remainder and the verification of error is fairly simple. Let x^i represent each bit of the message and $M(x)$ represent the polynomial corresponding ADS-B message, the CRC remainder (parity) $P(x)$ can thus be calculated as:

$$M(x) = \sum_{i=0}^{87} a_i x^i, \quad a_i \in (0, 1) \quad (10.2)$$

$$P(x) = M(x) \% G(x)$$

In the following pseudocode, the algorithm for computing the remainder of an ADS-B message is shown:

```
generator = 1111111111111010000001001

data_hex = 8D406B902015A678D4D220[000000]    # 11 + 3 zero bytes

data = 1000110101000000011010                # 88 bits
      1110010000001000000001
      0101101001100111100011
      0101001101001000100000
      [000000000000000000000000]             # append 24 zero bits

FOR i FROM 0 TO 112:
  IF data[i] IS 1:
    data[i:i+24] = data[i:i+24] XOR generator

remainder = data[-24:]

# final result: 101010100100101111011010, or AA4BDA in hexadecimal
```

To check whether an error occurs in the message, replace the `data_hex` in the previous example with the received message and run the same CRC process. The message is correct if all final 24 remainder bits are zeros.

Try it out

Using `pyModeS`, we can check the correctness of a ADS-B message as:

```
import pyModeS as pms

msgA = "8D406B902015A678D4D220AA4BDA"
msgB = "8D4CA251204994B1C36E60A5343D"

remainderA = pms.crc(msgA) # should be 0
remainderB = pms.crc(msgB) # should be 16
```

When the remainder is zero, the message is not corrupted. Otherwise, the error has occurred during the transmission.

Part III

Advanced Mode S Decoding

11 | Basics of Mode S services

In chapter 1, an overview of different Mode S services is given. Most of the services except the extended squitter are interrogations based, which means information is only transmitted upon request. The request, also known as *uplink*, is transmitted using 1030 megahertz radio frequency. The reply (*downlink*) signals are all transmitted using the 1090 megahertz radio frequency. Hence, all Mode S downlink messages can be intercepted using the same setup as ADS-B.

In the following chapters of this book, we are going to explain the interrogation based Mode S services in four groups, specifically:

1. All-call reply (DF 11)
2. ACAS short and long replies (DF 0/16)
3. Altitude and identity replies (DF 4/5)
4. Comm-B, with altitude and identity replies (DF 20/21)
 - (a) Mode S elementary surveillance (ELS)
 - (b) Mode S enhanced surveillance (EHS)
 - (c) Meteorological information

In this chapter, we discuss some of the common aspects regarding the decoding of Mode S messages. First of all, the structure of Mode S services is reviewed. Then, Mode S parity and ICAO address recovery are discussed. Finally, some common terminologies related to Comm-B messages are explained.

11.1 Mode S message structures

Based on Figure 1.3 from the introduction chapter, we see that there are two types of Mode S messages in terms of message length. Table 1.1 indicates that among the current 11 different downlink formats, 4 are short messages consisting of 56 bits. The other 7 are long messages with 112 bits. All formats share the same structure of a header consisting of 5 bits format code and 24 bits parity at the end, as shown in the Figure 11.1.

DF:5	27 bits	Parity:24
DF:5	83 bits	Parity:24

Figure 11.1: The structures of Mode S short and long messages

11.2 Parity

Mode S uses three types of parity. The first one is what is used for ADS-B in the extended squitter (see chapter 10). The other two types of parities are Address Parity (AP) and Data Parity (DP).

For any type of Mode S messages, the parity can be calculated as follows:

1) Let x^i represent each bit of the message and $M(x)$ represent the polynomial corresponding Mode S message, the parity $P(x)$ can thus be calculated as the CRC remainder:

$$M(x) = \sum_{i=0}^{87 \text{ or } 32} a_i x^i, \quad a_i \in (0, 1) \quad (11.1)$$

$$P(x) = M(x) \% G(x)$$

2) For an extended squitter message, $P(x)$ is directly transmitted as the parity in the last 24 bits of the message. Errors can be detected by performing the same computation process at the receiving side when received parity differs from this newly computed remainder.

However, for other types of Mode S messages, *Address Parity* (AP) is generated by overlaying the normal CRC remainder with the 24-bit transponder ICAO address. Thus, the final parity included in the message is not $P(x)$, but a new parity $P_A(x)$:

$$P_A(x) = P(x) + A(x) \quad (11.2)$$

where $A(x)$ is the polynomial representing the ICAO address of the transponder.

3) For some of the Downlink Format 20 and 21 Mode S messages, upon request of the SSR interrogation, another addition with the Comm-B Data Selector (BDS) number is performed [3]. In this case, the *Data Parity* (DP), is included in the last 24 bits of the Mode S message and transmitted.

When DP is in use, the parity is overlaid with the modified ICAO address, Modified AA (MA). The MA is calculated as the polynomial addition of ICAO address and BDS code (with 16 bits of zeros appended after), for example:

ICAO:	DD33AA	1101 1101 0011 0011 1010 1010
		XOR
BDS 4,4	440000	0100 0100 0000 0000 0000 0000
Modified AA	9933AA	1001 1001 0011 0011 1010 1010

Denote the modified address as $P_{MA}(x)$ and the Data Parity as $P_D(x)$, the calculation is of $P_D(x)$ is:

$$\begin{aligned}
 P_D(x) &= P(x) + P_{MA}(x) \\
 &= P(x) + A(x) + D(x)
 \end{aligned}
 \tag{11.3}$$

where $D(x)$ is the polynomial representing the BDS code of the Mode S Comm-B message.

11.3 ICAO address recovery

Since the interrogations are not known, information such as the transponder address is not known to third party receivers. The lack of this information makes error detection difficult.

For AP, the message parity field is produced by overlaying the direct parity with the transponder address. Hence, in order to recover the ICAO address, we can simply overlay the received parity (AP) with the parity calculated again from the payload data:

$$A'(x) = P_A(x) + P(x) \tag{11.4}$$

where $P_A(x)$ is the last 24-bit (assuming Address Parity) for the received message.

In order to demonstrate how to recover an ICAO address, we use the following example message:

Message:	A0001838CA380031440000F24177
-----	-----
Payload:	A0001838CA380031440000
-----	-----
Parity (AP):	F24177

In Figure 11.2, the ICAO address recovering process is illustrated. We first use the Mode S CRC algorithm to compute the remainder (parity) from only the payload data `A0001838CA380031440000`. The remainder is found to be `CE2CA7`. Then, by performing the polynomial addition (XOR for bitwise operation) with the actual parity included in the message, the ICAO address can be computed as `3C6DD0`.

For the cases of Data Parity, it is still possible to recover the transponder address using a similar process. However, we need to overlay again the previous result with the BDS code, assuming that the BDS code can be identified from the data:

$$A'(x) = P_D(x) + P(x) + D(x) \tag{11.5}$$

where $P_D(x)$ is the last 24-bit (assuming Data Parity) for the received message.

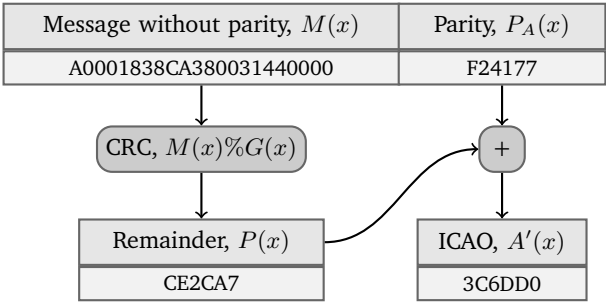


Figure 11.2: The ICAO address recovery logic

It is worth noting that in either case, the resulting $A'(x)$ is the same as the actual transponder address ($A(x)$) only if no error has occurred during the transmission. If the message is corrupted, the obtained address will be different from the actual one.

By combining with ICAO addresses obtained in ADS-B and other information independently decoded from Mode S message, this process can also be used for detecting Mode S errors as a third party observer. This method is described in [16].

Try it out

Using `pyModeS` , we can obtain the ICAO address as:

```
import pyModeS as pms

msg = "A0001838CA380031440000F24177"
icao = pms.icao(msg)
```

11.4 Two’s complement coding

Two’s complement coding is used for representing negative numbers in some Mode S messages, for example, heading and vertical rates in BDS 50 and BDS 60 messages. Every parameter in Mode S using two’s complement coding include a 1-bit sign and n-bit value.

1) If the sign bit is 0 , the result is simply the decimal representation of the value bits.

For example, we have the following representation of a signed parameter:

sign	value
0	111010011

The result is the decimal representation of the last nine value bits, which is 467 .

2) If the sign bit is 1 , we first calculate the decimal representation of the value bits (x) and then calculate the negative value as:

$$x - 2^n \quad (11.6)$$

For example, if we changed the signed bit in the previous example to 1 , as follows:

sign	value

1	111010011

since the sign bit is 1 and there are 9 value bits, the final value is calculated as:

$$467 - 2^9 = -45 \quad (11.7)$$

12 | All-call reply

In chapter 1, Figure 1.6 shows that Mode S all-call replies can be generated by Mode S transponder to answer Mode S only all-call interrogations and Mode A/C/S all-call interrogations.

Downlink format 11 is used for the all-call reply, and the length of the messages is 56 bits. The structure of an all-call reply message is quite simple. It only contains four fields, which are shown in Table 12.1.

Table 12.1: All-call reply

FIELD		MSG	BITS
Downlink format	DF	1-5	5
Capability	CA	6-8	3
Address announced	AA	9-32	24
Parity/interrogator identifier	PI	33-56	24

The fields can be decoded as follows:

- The definition of transponder capability is the same as in ADS-B messages (Table 3.2 in chapter 3).
- The address refers to the 24-bit transponder address.
- The decoding of PI is similar to the decoding of ADS-B parity (chapter 10). For a message with downlink format 11, PI is overlaid with the interrogator identifier.¹ Hence, assuming there is no error in the data, the CRC will produce the interrogator identifier code for all-call replies.

A decoding example is shown as follows:

```
MSG HEX: 5D484FDEA248F5
MSG BIN: 01011 101 010010000100111111011110 101000100100100011110101
         [DF=11] [CA=5] [AA=484FDE] [CRC=22]
```

From the capability (CA=5), we can see the aircraft has a Level 2+ transponder, with the ability to set CA to 7 and that it is airborne. The CRC remainder indicates the interrogator identifier code is 22.

¹ In fact, PI in ADS-B is also overlaid with the interrogator identifier. However, since ADS-B is not interrogation based, the identifier is set to 0. Thus, PI is always the same as the CRC remainder in ADS-B.

Try it out

Using `pyModeS` , we can obtain the ICAO address as:

```
import pyModeS as pms

msg = "5D484FDEA248F5"
icao = pms.icao(msg)
```

13 | Surveillance replies

Surveillance replies consist of short messages (56 bits) that respond to the selective interrogations of the secondary surveillance radar based on the 24-bit transponder addresses of the aircraft. Two types of information are transmitted: altitude (DF=4) and identity (DF=5).

13.1 Message structure

The structure of altitude and identity surveillance replies are similar, as shown in Table 13.1. The main difference is that bits 20 to 32 are used to encode either the altitude or the squawk code.

Table 13.1: Surveillance replies

(a) Altitude reply (DF=4)

FIELD		MSG	BITS
Downlink format	DF	1-5	5
Flight status	FS	6-8	3
Downlink request	DR	9-13	5
Utility message	UM	14-19	6
Altitude code	AC	20-32	13
Address parity	AP	33-56	24

(b) Identity reply (DF=5)

FIELD		MSG	BITS
Downlink format	DF	1-5	5
Flight status	FS	6-8	3
Downlink request	DR	9-13	5
Utility message	UM	14-19	6
Identity code	ID	20-32	13
Address parity	AP	33-56	24

The definitions of the common fields are:

- *Flight status (FS)*: 3 bits, shows status of alert, special position pulse (SPI, in Mode A only) and aircraft status (airborne or on-ground). The field is interpreted as:

000 : no alert, no SPI, aircraft is airborne
001 : no alert, no SPI, aircraft is on-ground
010 : alert, no SPI, aircraft is airborne
011 : alert, no SPI, aircraft is on-ground
100 : alert, SPI, aircraft is airborne or on-ground
101 : no alert, SPI, aircraft is airborne or on-ground
110 : reserved
111 : not assigned

- *Downlink request (DR)*: 5 bits, contains the type of request. In surveillance replies, only values 0, 1, 4, and 5 are used. The field can be decoded as:

00000 : no downlink request
00001 : request to send Comm-B message

00100 : Comm-B broadcast messages 1 available

00101 : Comm-B broadcast messages 2 available

- *Utility message (UM)*: 6 bits, contains transponder communication status information.

13.2 Altitude code

The 13-bit altitude code can be encoded in 25-ft increments, 100-ft increments, or in metric units (m). The 7th bit (MSG bit 28) is defined as the M bit. When the M bit is set to 0, the 9th bit (MSG bit 30) is defined as the Q bit.

The decoding rules are as follows:

- When all bits are set to 0, altitude information is not available or invalid.
- When M=1, removing the M bit, the reset 12 bits represent the altitude in meters.
- When M=0 and Q=1, removing the M and Q bits, the remaining 11 bits encode the altitude with 25 ft increments. Denote N as the decimal value of the remaining 11 bits. The altitude is calculated as $25 \times N - 1000$ ft.
- When M=0 and Q=0, the rest bits are defined as follows:

M							Q					
+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+
C1	A1	C2	A2	C4	A4	0	B1	0	B2	D2	B4	D4
+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+

This structure corresponds to the Mode C altitude reply. This structure is used to encode altitudes above 50187.5 ft.

Try it out

Using `pyModeS`, we can calculate the altitude code as:

```
import pyModeS as pms

msg = "2000171806A983"
altitude = pms.altcode(msg) # 36000 (ft)
```

13.3 Identity code

The 13-bit identity code encodes the 4 octal digit squawk code (from 0000 to 7777). The structure of this field is shown as follows:

+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+
C1	A1	C2	A2	C4	A4	X	B1	D1	B2	D2	B4	D4	
+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+	+-----+

The binary representation of the octal digit is:

A4	A2	A1		B4	B2	B1		C4	C2	C1		D4	D2	D1
----	----	----	--	----	----	----	--	----	----	----	--	----	----	----

Next, we will use an example to explain the decoding of the identity code. The example message is:

```
MSG HEX: 2A00516D492B80
MSG BIN: 00101 01000000000010 1000101101101 010010010010101110000000
          [DF=5]                [identity code]
```

The binary identity code can be interpreted as follows:

C1	A1	C2	A2	C4	A4	X	B1	D1	B2	D2	B4	D4
1	0	0	0	1	0	1	1	0	1	1	0	1

Rearranging the bits, we have three groups of binaries:

A4	A2	A1		B4	B2	B1		C4	C2	C1		D4	D2	D1
0	0	0		0	1	1		1	0	1		1	1	0

Finally, the four octal digit squawk code can be decoded from the binary groups as:

0	3	5	6
---	---	---	---

Try it out

Using `pyModeS` , we can calculate the squawk code as:

```
import pyModeS as pms

msg = "2A00516D492B80"
altitude = pms.idcode(msg)  # 0356
```

14 | Airborne Collision Avoidance System

14.1 Background

Airborne Collision Avoidance System (ACAS) is a system to reduce the risk of mid-air collisions and near mid-air collisions between aircraft. There are three types of ACAS systems according to [6], which are:

- ACAS I: Gives traffic advisories (TA), without recommending manoeuvres.
- ACAS II: Gives traffic advisories (TA) and resolution advisories (RA) only in vertical directions.
- ACAS III: Gives traffic advisories (TA) and resolution advisories (RA) in both horizontal and vertical directions. ACAS III is not currently implemented

This chapter will focus on ACAS II. The ACAS II is a system that utilizes the aircraft transponder, which interrogates the Mode C and Mode S transponders of nearby aircraft. When threats are detected, corresponding alerts are given to the pilots.

Currently, the most common implementation of ACAS II is *Traffic alert and Collision Avoidance System* (TCAS) II version 7.1, which was initiated by EUROCONTROL. It has been mandatory for aircraft in Europe since 2015. ACAS II works independently of the navigation system, FMS, and ATC. No input from these systems is considered for producing the alerts.

In ACAS II, TA and RA are triggered when certain thresholds to the closest point of approach (CPA) are passed. The thresholds depend on the altitude, speed, and heading of the aircraft. The examples of the TA and RA regions are illustrated in Figure 14.1.

14.2 ACAS with Mode C Transponders

ACAS system uses Mod C only all-call interrogation (see Figure 1.6 in chapter 1) to detect aircraft that are only equipped with Mode A/C transponders. In this case, the ACAS system initiates a sequence of interrogations with increasing power.

The interrogation pulse is slightly different from a Mode A/C-only all-call interrogation. A special S_1 pulse (also known as "whisper-shout") is designed to reduce interference. The S_1 pulse is inserted $2 \mu s$ ($\pm 0.15 \mu s$) before the P_1 pulse.

The reply should be sent with the following rules:

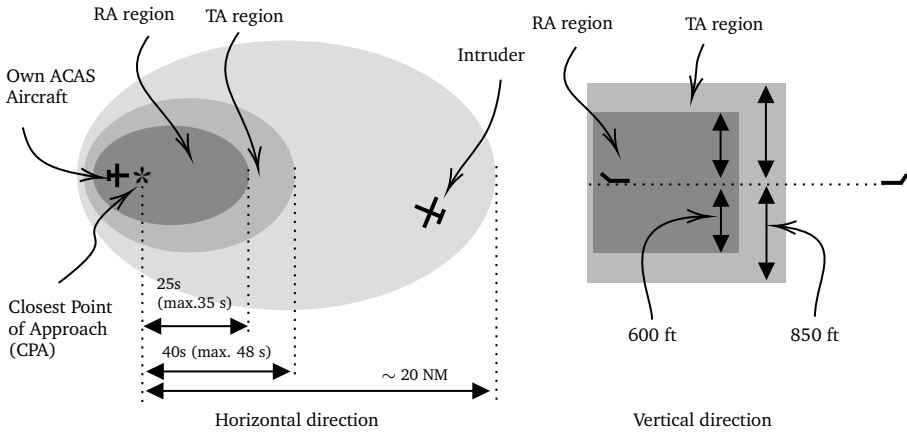


Figure 14.1: Example of an ACAS protection volume in horizontal and vertical directions (between FL50 and FL100)

- With both S_1 and P_1 above the minimum triggering level (MTL), no reply will be generated.
- With both S_1 and P_1 at MTL, the transponder will response to 10% of the interrogations.
- With P_1 at MTL and S_1 at MTL - 3 dB, the transponder will response to 70% of the interrogation.
- With P_1 at MTL and S_1 at MTL - 6 dB, the transponder will response to 90% of the interrogations.

14.3 ACAS with Mode S Transponders

For Mode S transponders, ACAS system employs a three-phase process, which includes the phases of *detection*, *surveillance*, and *coordination*.

For the detection phase, ACAS passively listens to Mode S only all-call replies (DF=11). These all-call replies are usually generated as a result of ground SSR interrogations or as spontaneous replies. In this process, aircraft with Mode S transponders in the vicinity are discovered. ACAS may also listen to extended squitter messages (Downlink Format 17, ADS-B) to detect other aircraft.

Once an aircraft is determined to be within the ACAS surveillance range, and within 10,000 ft of the own ACAS aircraft, ACAS will initiate a short air-air interrogation (UF=11) to acquire the range. The interrogation rate is defined as:

- Once every five cycles: when the target aircraft maintains in the surveillance range.

- Once every cycle: when the target aircraft is within 3 NM or with time to closest approach less than 60 s.

The surveillance interrogation is stopped when all the following conditions are met:

- A reply (DF=11) is received
- Both aircraft are below 18,000 ft.
- Target aircraft is more than 3 NM and 60 s away from the closest point of approach.

In Table 14.1, fields for ACAS surveillance interrogation and reply messages are listed.

Table 14.1: ACAS surveillance uplink and downlink messages

(a) Interrogation (uplink), UF=0

FIELD		MSG	BITS
Uplink Format	UF	1-5	5
Reserved		6-8	3
Reply length	RL	9	1
Reserved		10-13	4
Acquisition	AQ	14	1
Data selector	DS	15-22	8
Reserved		23-32	10
Address parity	AP	33-56	24

(b) Reply (downlink), DF=0

FIELD		MSG	BITS
Downlink Format	DF	1-5	5
Vertical status	VS	6	1
Cross-link capability	CC	7	1
Reserved		8	1
Sensitivity level	SL	9-11	3
Reserved		12-13	2
Reply information	RI	14-17	4
Reserved		18-19	2
Altitude code	AC	20-32	13
Address parity	AP	33-56	24

Once the target aircraft is within the RA region (a threat), ACAS initiates the co-ordination interrogation (UF=16). In this step, resolution information are trans-

mitted and received through coordination replies (DF=16). Information that is included in both coordination messages is shown in Table 14.2.

Table 14.2: ACAS coordination messages

(a) Interrogation (UF=16)

FIELD		MSG	BITS
Uplink Format	UF	1-5	5
Reserved		6-8	3
Reply length	RL	9	1
Reserved		10-13	4
Acquisition	AQ	14	1
Reserved		15-32	18
Message, U	MU	33-88	56
Address parity	AP	33-56	24

(b) Reply (DF=16)

FIELD		MSG	BITS
Downlink Format	DF	1-5	5
Vertical status	VS	6	1
Reserved		7-8	2
Sensitivity level	SL	9-11	3
Reserved		12-13	2
Reply information	RI	14-17	4
Reserved		18-19	2
Altitude code	AC	20-32	13
Message, V	MV	33-88	56
Address parity	AP	89-112	24

Specific fields in above messages are defined as follows:

- *Reply length (RL)*: 1 bit, defines the required reply format: 0 requires a reply with DF=0, while 1 requires reply with DF=16.
- *Acquisition (AQ)*: 1 bit, contains code that controls the content of RI field in the reply.
- *Data selector (DS)*: 8 bits, indicates the BDS code of the MV content in reply with DF=16.
- *Vertical status (VS)*: 1 bit, indicates whether the aircraft is airborne (0) or on the ground (1).
- *Cross-link capability (CC)*: 1 bit, refers to the capability of reply DF=16

upon request of UF=0. When this 1-bit field is set to 1, the cross-link is supported. Otherwise, the field is set to 0.

- *Sensitivity level (SL)*: 3 bits, represents the sensitivity level of the ACAS system. 0 indicates the ACAS is inoperative. Other values indicate the sensitivity level.
- *Reply information (RI)*: 4 bits, indicates the type of reply to interrogating aircraft. For ACAS message, valid values are 0 and from 2 to 4. Other values are not part of the ACAS:

0000 : No operating ACAS

0010 : ACAS with resolution capability inhibited

0011 : ACAS with vertical-only resolution capability

0111 : ACAS with vertical and horizontal resolution capability

- *Altitude Code (AC)*: 13 bits, encodes the altitude of the aircraft. It can be decoded according to section 13.2.

14.4 Message fields of ACAS coordination messages

Message U-definition (MU) and Message V-definition (MV) are transmitted in ACAS coordination interrogation and reply messages, respectively. MU is used to transit resolution, ACAS broadcast, and RA broadcast. MV is used for reply purposes.

14.4.1 MU (U-definition)

14.4.1.1 MU of ACAS resolution message

When ACAS resolution information is transmitted in the UF=16 message, the first 8 bits of MU, U-definition subfields (UDS), is set to 0011 0000 (UDS=3,0). The corresponding fields are indicated in Table 14.3.

The significance of fields are listed as follows:

- *Multiple threat bit (MTB)*: 1 bit, indicates whether multiple threats are present.
- *Vertical RAC¹ (VRC)*: 2 bits, contains vertical resolution advisory complement information:

00 : No vertical RAC information

01 : Do not pass below

10 : Do not pass above

11 : Not assigned

- *Cancel vertical RAC (CVC)*: 2 bits, cancels previously sent VRC:

¹ RAC: Resolution Advisory Complement

Table 14.3: UF=16, MU for ACAS resolution messages, UDS=3,0

FIELD		MSG	MU	BITS
U-definition subfield 1 [0011]	UDS1	33-36	1-4	4
U-definition subfield 2 [0000]	UDS2	37-40	5-8	4
Reserved		41	9	1
Multiple threat bit	MTB	42	10	1
Cancel vertical RAC	CVC	43-44	11-12	2
Vertical RAC	VRC	45-46	13-14	2
Cancel Horizontal RAC	CHC	47-49	15-17	3
Horizontal RAC	HRC	50-52	18-20	3
Reserved		53-55	21-23	3
Horizontal sense bits	HSB	56-60	24-28	5
Vertical sense bits	VSB	61-64	29-32	4
Aircraft address	MID	65-88	33-56	24

00 : No cancellation information

01 : Cancel "Do not pass below"

10 : Cancel "Do not pass above"

11 : Not assigned

- *Horizontal RAC (HRC)*: 3 bits, contains horizontal resolution advisory complementary information:

000 : No information

001 : Other ACAS sense is turn left; do not turn left

010 : Other ACAS sense is turn left; do not turn right

101 : Other ACAS sense is turn right; do not turn left

110 : Other ACAS sense is turn right; do not turn right

other : Not assigned

- *Cancel horizontal RAC (CHC)*: 3 bits, cancels previously sent HRC:

000 : No cancellation information

001 : Cancel "Do not turn left"

010 : Cancel "Do not turn right"

other : Not assigned

- *Horizontal sense bits (HSB)*: 5 bits, uses Hamming code with an extra parity bit to detect errors (up to 3 bits) in CHC and HRC fields.
- *Vertical sense bits (VSB)*: 4 bits, uses Hamming code with an extra parity bit to detect errors (up to 3 bits) in CVC and VRC fields.
- *Aircraft address (MID)*: 24 bits, contains the 24-bits aircraft transponder address of the interrogating ACAS aircraft.

14.4.1.2 MU of RA broadcast message

When UF=16 is used for RA broadcast, UDS is set to 0011 0001 (UDS=3,1). The corresponding fields are indicated in Table 14.4.

Table 14.4: UF=16, MU for RA broadcast, UDS=3,1

FIELD		MSG	MU	BITS
U-definition subfield 1 [0011]	UDS1	33-36	1-4	4
U-definition subfield 2 [0001]	UDS2	37-40	5-8	4
Active RAs	ARA	41-54	9-22	14
RAC's record	RAC	55-58	23-26	4
RA terminated indicator	RAT	59	27	1
Multiple threat encounter	MTE	60	28	1
Reserved		61-62	29-30	2
Mode A identity code	AID	63-75	31-43	13
Mode C altitude code	CAC	76-88	44-56	13

The significance of fields are listed as follows:

- *Active RA (ARA)*: 14 bits, indicates the resolution advisory characteristics. It has to be interpreted together with the MTB field.
 - When ARA first bit (MSG bit 41) is 1 and MTE is either 0 or 1 :
 - Bit 42: RA is corrective (1) or preventive (0)
 - Bit 43: RA is downward sense (1) or upward sense (0)
 - Bit 44: RA is increased rate (1) or not (0)
 - Bit 45: RA is a sense reversal (1) or not (0)
 - Bit 46: RA is altitude crossing (1) or not (0)
 - Bit 47: RA is positive (1) or vertical speed limit (0)
 - Bit 48-54: Reserved for ACAS III
 - When ARA first bit (MSG bit 41) is 0 and MTE is 1 :
 - Bit 42: RA requires a correction in the upward sense (1) or not (0)
 - Bit 43: RA requires a positive climb (1) or not (0)
 - Bit 44: RA requires a correction in the downward sense (1) or not (0)
 - Bit 45: RA requires a positive descent (1) or not (0)
 - Bit 46: RA requires a crossing (1) or not (0)
 - Bit 47: RA is a sense reversal (1) or not (0)
 - Bit 48-54: Reserved for ACAS III
 - When ARA first bit (MSG bit 41) is 0 and MTE is 0 , no vertical RA is generated.

- *RAC's record (RAC)*: 4 bits, contains current active RACs that are received from other ACAS aircraft (if any). Each of the four bits in this field indicates the following RAC when set to 1. When a bit is set to 0, the corresponding RAC is inactive.

Bit 55: Do not pass below

Bit 56: Do not pass above

Bit 57: Do not pass left

Bit 58: Do not pass right

- *RA terminated indicator (RAT)*: 1 bit, indicates whether ACAS is currently generating RA in the ARA field or RA in the ARA field has been terminated.²
- *Multiple threat encounter (MTE)*: 1 bit, indicates whether multiple threats are currently being processed by the ACAS resolution. When MTE is set to 0, either one threat is being processed (ARA bit 41 sets to 1) or no threat is being processed (ARA bit 41 sets to 0). When MTE is set to 1, multiple threats are being processed.
- *Mode A identity code (AID)*: 13 bits, contains the Mode A identity code (squawk code) of the reporting aircraft. It can be decoded according to section 13.3.
- *Mode C altitude code (CAC)*: 13 bits, contains the Mode C altitude code reporting aircraft. It can be decoded according to section 13.2.

14.4.1.3 MU of ACAS broadcast message

When UF=16 is used for ACAS broadcast, UDS is set to 0011 0010 (UDS=3,2). The corresponding fields are indicated in Table 14.5.

Table 14.5: UF=16, MU for ACAS broadcast, UDS=3,1

FIELD		MSG	MU	BITS
U-definition subfield 1 [0011]	UDS1	33-36	1-4	4
U-definition subfield 2 [0010]	UDS2	37-40	5-8	4
Reserved		41-64	9-32	24
Aircraft address	MID	65-8	33-56	24

The only information that is broadcast in the MU of this message is the 24-bit transponder address of the interrogating aircraft.

14.4.2 MV (V-definition)

Similar to MU in the UF=16 message, MV in the DF=16 message contains a few common fields. The corresponding fields are indicated in Table 14.6.

² The Mode S transponder is still required to report RA 18 seconds after it is terminated by ACAS. Hence, the RAT field is used.

Table 14.6: DF=16, MV for coordinated reply, VDS=3,0

FIELD		MSG	MU	BITS
V-definition subfield 1 [0011]	VDS1	33-36	1-4	4
V-definition subfield 2 [0001]	VDS2	37-40	5-8	4
Active RAs	ARA	41-54	9-22	14
RAC's record	RAC	55-58	23-26	4
RA terminated indicator	RAT	59	27	1
Multiple thread encounter	MTE	60	28	1
Reserved		61-88	29-56	28

We can see that the structure of the MV fields is similar to MU fields of RA broadcast (UDS=3,1) from Table 14.4. The interpretations of these fields are also the same as in section 14.4.1.2.

15 | Comm-B replies

Most of the Mode S selective interrogations responses in Comm-B messages. The message can have a downlink format of either 20 or 21, depending on whether the aircraft identity code or altitude code is included in the message.

Comm-B protocol supports many different types of messages (up to 255). Several important surveillance services utilize some of the Comm-B message types (see Figure 1.7 from the Chapter 1). In this book, we are mainly interested in three types of services, which are Mode S Elementary Surveillance (ELS), Mode S Enhanced Surveillance (EHS), and Meteorological information. By decoding these messages, we can discover some additional information regarding an aircraft.

15.1 Structure

Comm-B messages have similar structures as surveillance replies (DF=4/5). The structures are shown in the Table 15.1.

Table 15.1: Comm-B messages with altitude code and identity code

(a) Comm-B, altitude reply (DF=20)

FIELD		MSG	BITS
Downlink format	DF	1-5	5
Flight status	FS	6-8	3
Downlink request	DR	9-13	5
Utility message	UM	14-19	6
Altitude code	AC	20-32	13
Message, Comm-B	MB	33-88	56
Parity		89-112	24

(b) Comm-B, identity reply (DF=21)

FIELD		MSG	BITS
Downlink format	DF	1-5	5
Flight status	FS	6-8	3
Downlink request	DR	9-13	5
Utility message	UM	14-19	6
Identity code	ID	20-32	13
Message, Comm-B	MB	33-88	56
Parity		89-112	24

The definitions of common fields are the same as surveillance replies in chapter 13. The parity can be either address parity or data parity, which are defined in chapter 11.

15.2 BDS

Comm-B Data Selector (BDS) is an 8-bit code that determines which information to be included in the MB fields. It is often shown as a 2-digit hexadecimal, for example, 4,0 or 0,A . We can make a comparison between the BDS code and Type Code used in ADS-B. They both help to identify which structure shall be used to decode the message, except that the BDS code is only included in the uplink (Comm-A). For Comm-B messages, BDS codes are not always included.

Without knowing the BDS code of the downlink message, the information contained in the MB field can not be decoded. Fortunately, there are methods available that can be used to infer the BDS code for most of the messages and decode them. In a later chapter, we are going to explain how the BDS code inference process works.

The following is the list of BDS codes for messages that will be discussed in detail in the different chapters.

- BDS 1,0 - Data link capability report
- BDS 1,7 - Common usage GICB capability report
- BDS 2,0 - Aircraft identification
- BDS 3,0 - ACAS active resolution advisory
- BDS 4,0 - Selected vertical intention
- BDS 5,0 - Track and turn report
- BDS 6,0 - Heading and speed report
- BDS 4,4 - Meteorological routine air report
- BDS 4,5 - Meteorological hazard report

Here, the first four BDS codes (1,0 , 1,7 , 2,0 , 3,0) belong to the ELS service, next three codes (4,0 , 5,0 , 6,0) belong to EHS services, and the last two codes (4,4 , 4,5) report meteorological information. All ELS, EHS and meteorological services are discussed in the following chapters.

16 | Mode S Elementary Surveillance

Mode S Elementary Surveillance (ELS) includes provides a set of basic functionalities that are supported by the Mode S transponders. These basic functionalities include the reporting of aircraft identity, altitude, transponder capability, and flight status. The set of BDS codes included in ELS are 1,0 , 1,7 , 2,0 , and 3,0 .

16.1 Data link capability report (BDS 1,0)

This message is designed to report the data link capability of the Mode S transponder installed. In Table 16.1, all fields in this report are shown.

Table 16.1: Data link capability report (BDS 1,0), MB field

FIELD	MSG	MB	BITS
BDS Code [0001 0000]	33-40	1-8	8
Configuration flag	41	9	1
Reserved [00000]	42-46	10-14	6
Overlay Command Capability (OCC)	47	15	1
Reserved for ACAS	48	16	1
Mode S subnetwork version number	49-55	17-23	7
Transponder enhanced protocol indicator	56	24	1
Mode S specific services capability	57	25	1
Uplink ELM average throughput capacity	58-60	26-28	3
Downlink ELM throughput	61-64	29-32	4
Aircraft identification capability	65	33	1
Squitter capability subfield (SCS)	66	34	1
Surveillance identifier code (SIC)	67	35	1
Common usage GICB capability report	68	36	1
Reserved for ACAS	69-72	37-40	4
Data terminal equipment (DTE) status	73-80	41-56	16

In the data link capability report, the first eight bits indicate the BDS number 1,0, which is 0001 0000 in binary format. The definitions of the other fields are:

- 1) ACAS related bits are shown as follows:

MSG	MB	Coding
48	16	0: ACAS failed or on standby 1: ACAS operating
69	37	0: Hybrid surveillance not operational 1: Hybrid surveillance fitted and operational
70	38	0: ACAS generating TAs only 1: ACAS generating TAs and RAs
72 71	37 36	0 0: RTCA/DO-185 (pre-ACAS) 0 1: RTCA/DO-185A 1 0: RTCA/DO-185B or EUROCAE ED 143 1 1: Reserved for future versions

2) Valid values for *Mode S subnetwork version number* are from 0 to 5, corresponds to compliance to a different version of ICAO documentations. Numbers 6 to 127 are currently unassigned. Numbers 0 to 5 can be interpreted:

```

0: Subnetwork not available
1: ICAO Doc 9688 (1996)
2: ICAO Doc 9688 (1998)
3: ICAO Annex 10, Vol III, Amdt 77
4: ICAO Doc 9871 (Ed 1), RTCA DO-181D, EUROCAE ED-73C
5: ICAO Doc 9871 (Ed 2), RTCA DO-181E, EUROCAE ED-73E
>5: Reserved for future use

```

3) *Overlay Command Capability* indicated whether the transponder supports BDS overlay (Data Parity).

4) When *Transponder enhanced protocol indicator* bit is set to **1**, the transponder is a Level 5 transponder. Value **0** indicates a Level 2 to 4 transponder.

5) When *Mode S specific services capability* bit is set to **1**, at least one Mode S specific service is supported.¹

6) *Aircraft identification capability* indicates whether the aircraft identification is available.

7) When *Squitter capability subfield* bit is set to **1**, both BDS 05 and 06 registers have been updated in the past 9 to 11 seconds.

8) *Surveillance identifier code* determines whether the transponder has the surveillance identification code capability.

9) *Common usage GICB capability report* is set to **1** every time the GICB capacity report (BDS code 1,7) is changed. Register 1,7 is sampled every minute to check for changes.

¹ The additional specific services are BDS codes other than 02, 03, 10, 17-1C, 20, and 30

16.2 Common usage GICB capability report (BDS 1,7)

This message is designed to report Common usage Ground-initiated Comm-B (GICB) capabilities. The fields in this report are shown in Table 16.2. In this table, each bit indicates whether the corresponding service is available from the transponder.

A bit is set to 1 when the corresponding register has a valid input that has been updated with the required rate. This means that the same aircraft would response different GICB reports due to the availability of the source data.

Table 16.2: Data link capability report (BDS 1,0), MB field

FIELD	MSG	MB	BITS
0,5 Extended squitter airborne position	33	1	1
0,6 Extended squitter surface position	34	2	1
0,7 Extended squitter status	35	3	1
0,8 Extended squitter identification and category	36	4	1
0,9 Extended squitter airborne velocity information	37	5	1
0,A Extended squitter event-driven information	38	6	1
2,0 Aircraft identification	39	7	1
2,1 Aircraft registration number	40	8	1
4,0 Selected vertical intention	41	9	1
4,1 Next waypoint identifier	42	10	1
4,2 Next waypoint position	43	11	1
4,3 Next waypoint information	44	12	1
4,4 Meteorological routine report	45	13	1
4,5 Meteorological hazard report	46	14	1
4,8 VHF channel report	47	15	1
5,0 Track and turn report	48	16	1
5,1 Position coarse	49	17	1
5,2 Position fine	50	18	1
5,3 Air-referenced state vector	51	19	1
5,4 Waypoint 1	52	20	1
5,5 Waypoint 2	53	21	1
5,6 Waypoint 3	54	22	1
5,F Quasi-static parameter monitoring	55	23	1
6,0 Heading and speed report	56	24	1
Reserved for aircraft capability	57	25	1
Reserved for aircraft capability	58	26	1
E,1 Reserved for Mode S BITE (Built In Test Equipment)	59	27	1
E,2 Reserved for Mode S BITE (Built In Test Equipment)	60	28	1
F,1 Military applications	61	29	1
Reserved	62-80	30-56	17

We can use the following message as an example:

```
MSG:      A0000638FA81C10000000081A92F
MB:       FA81C100000000
MB BIN:   1111101010000001110000010000000000000000000000000000000000000000
```

From the MB field, we can identify that following bits are set to 1 :

```
Bit: 1, 2, 3, 4, 5, 7, 9, 16, 17, 18, 24
```

Hence, BDS codes supported by the transponder are:

```
BDS05 BDS06 BDS07 BDS08 BDS09    < ADSB
BDS20                                < ELS
BDS40 BDS50 BDS51 and BDS60      < EHS
```

Try it out

Using `pyModeS` , we can decode the GICB information as:

```
import pyModeS as pms

msg = "A0000638FA81C10000000081A92F"
capabilities = pms.commb.cap17(msg)
```

A list of supporting BDS code will be returned.

16.3 Aircraft identification (BDS 2,0)

Similar to an ADS-B aircraft identification message, the callsign of an aircraft can be decoded from BDS 2,0 messages. The structure of the MB field is defined in Table 16.3.

Table 16.3: Data link capability report (BDS 1,0), MB field

FIELD	MSG	MB	BITS
BDS Code [0010 0000]	33-40	1-8	8
Character 1	41-46	9-14	6
Character 2	47-52	15-20	6
Character 3	53-58	21-26	6
Character 4	59-64	27-32	6
Character 5	65-70	33-38	6
Character 6	71-76	39-44	6
Character 7	77-82	45-50	6
Character 8	83-88	51-56	6

The first 8 bits indicates the BDS code 0010 0000 (2,0 in hexadecimal). Each of the callsign characters is represented by 6 bits. We first need to convert the binary numbers to decimals. Each decimal value corresponds to the index of the letter in the following character map:

```
#ABCDEFGHIJKLMNOPQRSTUVWXYZ#####  #####0123456789#####
```

It is worth noting that this character mapping is the same as the one used for ADS-B identification, which also corresponds to a part of the ASCII code map.

The following is an example on how to decode the callsign from a sample BDS 2,0 message:

```
MSG:  A000083E202CC371C31DE0AA1CCF
MB:    202CC371C31DE0
-----
MB BIN: 0010 0000 001011 001100 001101 110001 110000 110001 110111 100000
HEX:      2      0
DEC:           11      12      13      49      48      49      55      32
CHR:           K      L      M      1      0      1      7      [SPACE]
-----
ID:    KLM1017
```

Try it out

Using `pyModeS` , we can decode the callsign in this message as:

```
import pyModeS as pms

msg = "A000083E202CC371C31DE0AA1CCF"
callsign = pms.commb.cs20(msg)
```

Callsign `KLM1017_` will be returned by the previous function since the space is replace by `_` in `pyModeS` .

16.4 ACAS active resolution advisory (BDS 3,0)

The BDS 3,0 message is used to report resolution advisories (RA) generated by ACAS equipment. The structure of the MB field is defined in Table 16.4.

Table 16.4: ACAS active resolution advisory (BDS 3,0), MB field

FIELD	MSG	MB	BITS
BDS Code [0011 0000]	33-40	1-8	8
Active resolution advisories	41-54	9-22	14
Resolution advisory complements record	55-58	23-26	4
RA teminated	59	27	1
Multiple threat encounter	60	28	1
Threat type indicator	61-62	29-30	2
Threat identity data	63-86	31-56	26

- 1) The first 8 bits show the BDS code 3,0 or 0011 0000 in binary format.
- 2) The 14-bit active resolution advisories (ARA) indicate the characteristics of the RA generated by the ACAS associated with the transponder. To decode the information, we need to decode MB bit 9 (MSG bit 41) and MB bit 28 (MSG bit 60). Table 16.5 shows how to interpret these two bits.

Table 16.5: BDS 3,0 MB bits 9 and 28

MB:9	MB:28	
0	0	No RA has been generated
0	1	Multiple threats, RA is intended to provide vertical separation blew some threats and above some other threats
1	0	Only one threat
0	1	Multiple threats, RA is intended to provide vertical separation in the same direction

MB bits 16-22 are reserved for ACAS III. When MB:9=1 , the meanings of MB bits from 10 to 15 are shown in Table 16.6.

When MB:9=0 and MB:28=1 , the meanings of MB bits from 10 to 15 are shown in Table 16.7.

Table 16.6: BDS 3,0 MB bits 10 to 15 (MB:9=1)

MB	Value	
10	0	RA is preventive
	1	RA is corrective
11	0	Upward sense RA has been generated
	1	Downward sense RA has been generated
12	0	RA is not increased rate
	1	RA is increased rate
13	0	RA is not a sense reversal
	1	RA is a sense reversal
14	0	RA is not altitude crossing
	1	RA is altitude crossing
15	0	RA is vertical speed limit
	1	RA is positive

Table 16.7: BDS 3,0 MB bits 10 to 15 (MB:9=0 MB:28=1)

MB	Value	
10	0	RA does not require a correction in the upward sense
	1	RA requires a correction in the upward sense
11	0	RA does not require a positive climb
	1	RA requires a positive climb
12	0	RA does not require a correction in the downward sense
	1	RA requires a correction in the downward sense
13	0	RA does not require a positive descend
	1	RA requires a positive descend
14	0	RA does not require a crossing
	1	RA requires a crossing
15	0	RA is not a sense reversal
	1	RA is a sense reversal

2) The resolution advisory complements (RAC) record consists of 4 bits, and each bit has the following meaning:

MB:23=1	Do not pass below
MB:24=1	Do not pass above
MB:25=1	Do not turn left
MB:26=1	Do not turn right

3) A RA terminated bit indicates whether previously generated RA has been terminated.

4) Threat type indicator contains 2 bits with the following meaning:

00	No identity data in threat identity data
01	Threat identity data contains a Mode S transponder address
10	Threat identity data contains altitude, range, and bearing
11	Not assigned

When the threat type indicator is **01**, MB bits 31-54 contain the 24-bit Mode S transponder address and the last two bits are set to zero.

When the threat type indicator is **10**, MB bits 31-56 is divided into three different segments.

- MB bits 31-43 contain the 13-bit threat altitude code. It is the same structure as the altitude code from section 13.2.
- MB bits 44-50 contain the most recent threat range from ACAS. When it is 0, no range estimation is available. When it is 127, the range is greater than 12.55 nautical miles. For other values, the range is calculated as $(n - 1)/10 \pm 0.05$ nautical miles.
- MB bits 51-56 contain the most recent estimated bearing of the threat aircraft, relative to their own heading. When it is 0, no estimation is available. Values larger than 60 are not assigned. For other values (from 1 to 60), the bearing range is calculated as $[6(n - 1), 6n]$ in degrees.

17 | Mode S Enhanced Surveillance

Mode S Enhanced Surveillance (EHS) provides a set of advanced functionalities for the Mode S transponders. Three different types of reports are included in EHS. They are designed to report vertical intent, turning performance, and air-speeds. In this chapter, the structures and decoding processes of these reports are explained.

17.1 Selected vertical intention (BDS 4,0)

The selected vertical intention message is designed for air traffic control to obtain an aircraft's current vertical intentions. For example, an aircraft controller can use this information to check whether an aircraft is complying with an altitude command.

Table 17.1 shows the structure of the message.

Table 17.1: Selected intention (BDS 4,0), MB field

FIELD	MSG	MB	BITS
Status (for MCP/FCU selected altitude)	33	1	1
MCP/FCU selected altitude			
Range: [0, 65520] ft	34-45	2-13	12
LSB: 16 ft			
Status (for FMS selected altitude)	46	14	1
FMS selected altitude			
Range: [0, 65520] ft	47-58	15-26	12
LSB: 16 ft			
Status (for barometric press setting)	59	27	1
Barometric pressure setting			
Note: actual value minus 800 mb			
Range: [0, 410] mb	60-71	28-39	12
LSB: 0.1 mb			
Reserved (all zeros)	72-79	40-47	8
Status of MCP/FCU mode	80	48	1
VNAV mode	81	49	1
Alt hold mode	82	50	1
Approach mode	83	51	1
Reserved (all zeros)	84-85	52-53	2
Status of target altitude source	86	54	1
Target altitude source	87-88	55-56	2

Two different types of selected altitude fields are included in the message. Values

in the *MCP/FCU selected altitude* field are from the mode control panel or flight control unit. These are often inputs from the pilot. Values in *FMS selected altitude* field are derived from the flight management system controlling the vertical profile, which often does not come from manual input.

The *barometric pressure setting* value is the actual pressure in millibars (mb) subtracted by a constant of 800. If the actual value is below 800 mb (or above 1209 mb), the corresponding status bit (MB:27) is set to 0.

The last two bits in the MB field show the source of the target altitude. They have the following meaning:

- 00: Unknown source
- 01: Aircraft altitude
- 10: FCU/MCP selected altitude
- 11: FMS selected altitude

In Figure 17.1, an example of how to decode a BDS 4,0 message is illustrated:

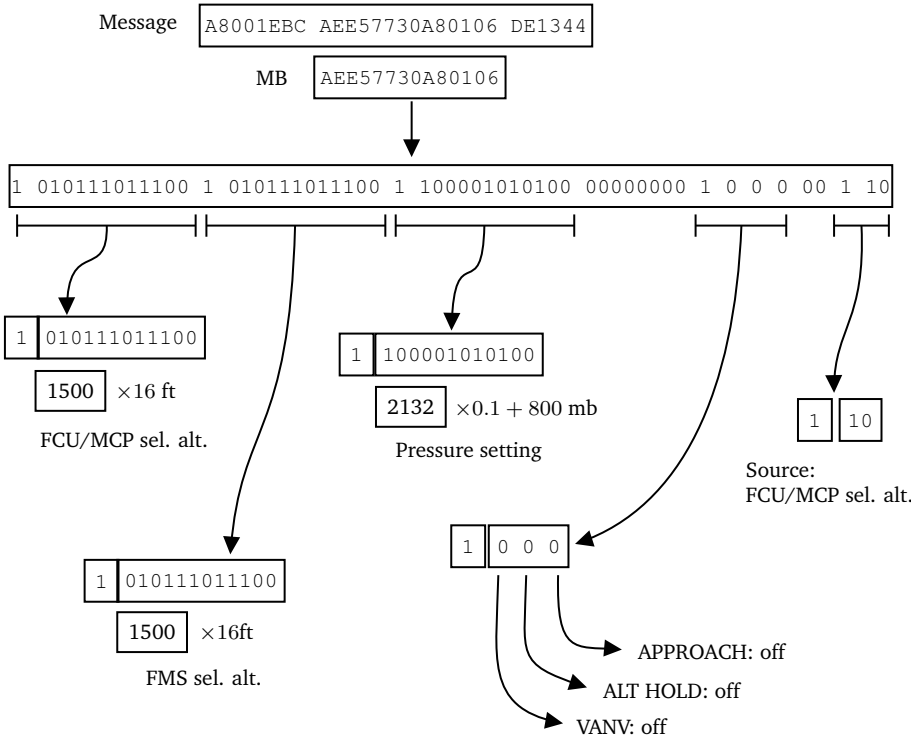


Figure 17.1: BDS 4,0 decoding example

Try it out

Using `pyModeS` , we can decode information of BDS 4,0 messages as:

```
import pyModeS as pms

msg = "A8001EBCAEE57730A80106DE1344"
selaltfms = pms.commb.selalt40fms(msg)
selaltmcp = pms.commb.selalt40mcp(msg)
pressure = pms.commb.p40baro(msg)
```

17.2 Track and turn report (BDS 5,0)

The track and turn report is designed to provide parameters to describe aircraft turns. In this type of message, roll angle, track angle, and track rate are provided. It also includes the ground speed and true airspeed (TAS) of the aircraft.

Table 17.2 shows the structure of the message.

Table 17.2: Track and turn report (BDS 5,0), MB field

FIELD	MSG	MB	BITS
Status (for roll angle)	33	1	1
Sign	34	2	1
Roll angle			
Range: [-90, +90] degrees	35-43	3-11	9
LSB: 45/256 degrees			
Status (for track angle)	44	12	1
Sign	45	13	1
True track angle			
Range: [-180, 180] degrees	46-55	14-23	10
LSB: 90/512 degrees			
Status (for ground speed)	56	24	1
Ground speed			
Range: [0, 2046] kt	57-66	25-34	10
LSB: 2 kt			
Status (for track angle rate)	67	35	1
Sign	68	36	1
Track angle rate			
Range: [-16, 16] degrees/second	69-77	37-45	9
LSB: 8/256 degrees/second			
Status (for true airspeed)	78	46	1
True airspeed			
Range: [0, 2046] kt	79-88	47-56	10
LSB: 2 kt			

In this message, we can see three signed values, which are roll angle, track angle, and track angle rate. Two's complement coding (see section 11.4) should be used to calculate these values.

In Figure 17.2, an example of how to decode a BDS 5,0 message is illustrated.

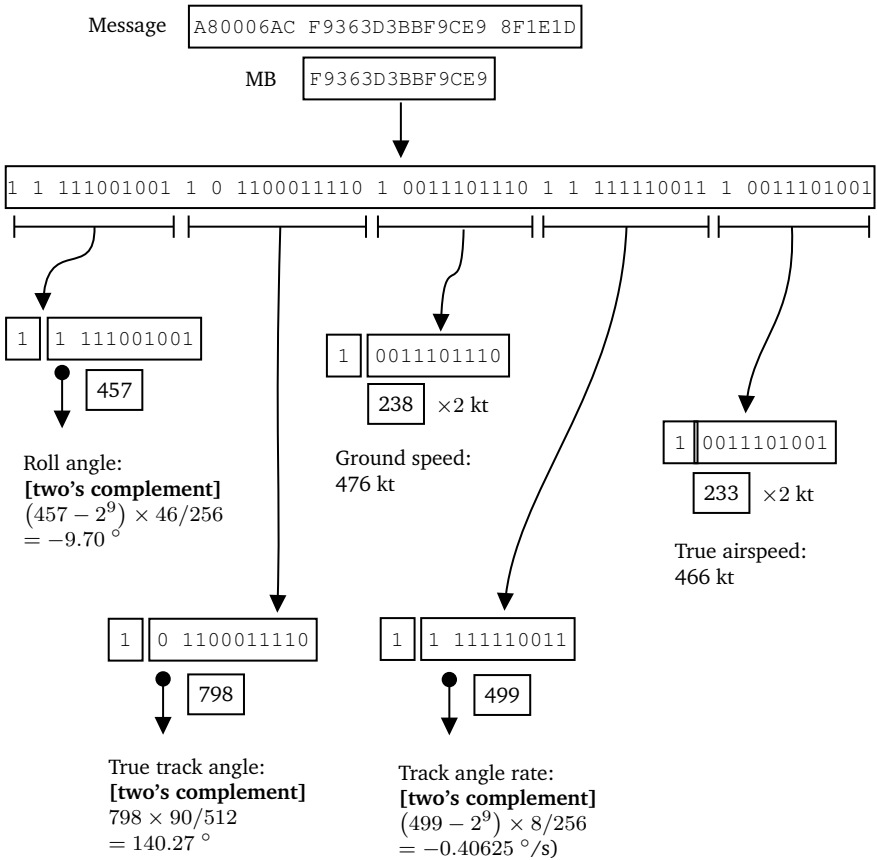


Figure 17.2: BDS 5,0 decoding example

Try it out

Using `pyModeS`, we can decode information of BDS 5,0 messages as:

```
import pyModeS as pms

msg = "A80006ACF9363D3BBF9CE98F1E1D"

roll_angle = pms.commb.roll150(msg)
track_angle = pms.commb.trk50(msg)
track_angle_rate = pms.commb.rtrk50(msg)
ground_speed = pms.commb.gs50(msg)
TAS = pms.commb.tas50(msg)
```

17.3 Heading and speed report (BDS 6,0)

The heading and speed report is designed to downlink various airspeed and vertical rate to air traffic controllers. In this type of message, indicated airspeed (IAS), Mach number, barometric altitude rate, inertial vertical velocity, and the magnetic heading of the aircraft are provided.

Table 17.3 shows the structure of the message.

Table 17.3: Heading and speed report (BDS 6,0), MB field

FIELD	MSG	MB	BITS
Status (for magnetic heading)	33	1	1
Sign	34	2	1
Magnetic heading			
Range: [-180, +180] degrees	35-44	3-12	10
LSB: 90/512 degrees			
Status (for indicated airspeed)	45	13	1
Indicated airspeed			
Range: [0, 1023] kt	46-55	14-23	10
LSB: 1 kt			
Status (for Mach number)	56	24	1
Mach number			
Range: [0, 4.092]	57-66	25-34	10
LSB: 0.004			
Status (for barometric altitude rate)	67	35	1
Sign	68	36	1
Barometric altitude rate			
Range: [-16384, +16352] ft/min	69-77	37-45	9
LSB: 32 ft/min			
Status (for inertial vertical velocity)	78	46	1
Sign	79	47	1
Inertial vertical velocity			
Range: [-16384, +16352] ft/min	80-88	48-56	9
LSB: 32 ft/min			

In this message, we can see a few signed values, such as heading and two vertical rates. Two's complement coding (see section 11.4) should be used to calculate these values.

The magnetic heading is the aircraft's heading in respect to the magnetic North, which can be different from the true north (for example, used for the track angle from ADS-B and BDS 5,0). Often an aircraft obtains the magnetic heading by adding its true North heading with the magnetic declination from a world magnetic model, such as [2]. It is worth noting that the true North heading is not necessarily the same as the track angle due to the influence of wind.

In the heading and speed report, two different kinds of vertical rates are reported.

Barometric altitude rates are only derived from barometer measurements. Due to the lacking of filtering from air data input, significant noise is contained in these values. On the other hand, inertial vertical velocities are values provided by navigational equipment from different sources including the flight management computer. According to [7], data sources with different levels of priorities are defined for these two values, which are listed in Table 17.4.

Table 17.4: Data sources for two vertical rates in heading and speed report

Parameter	Input Data Source Priorities
Barometric altitude rate	1. Air Data System 2. Inertial Reference System / Flight Management System
Inertial vertical velocity	1. Flight Management Computer / GNSS integrated 2. Flight Management Computer (General) 3. Inertial Reference System / Flight Management System

In Figure 17.3, the example on how to decode a BDS 6,0 message is illustrated.

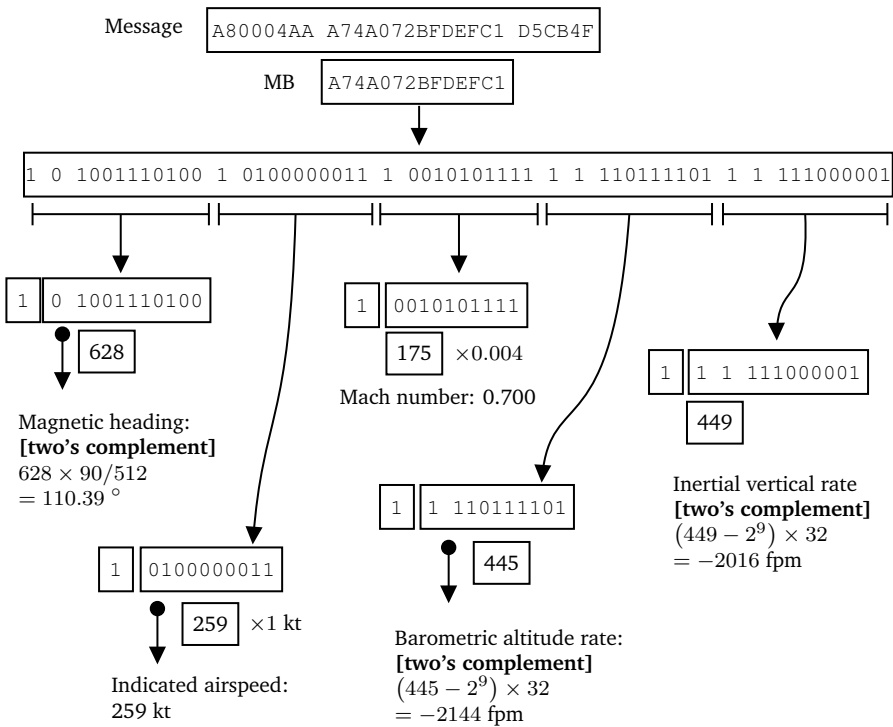


Figure 17.3: BDS 6,0 decoding example

Try it out

Using `pyModeS`, we can decode information of BDS 6,0 messages as:

```
import pyModeS as pms

msg = "A80004AAA74A072BFDEFC1D5CB4F"

heading = pms.commb.hdg60(msg)
IAS = pms.commb.ias60(msg)
Mach = pms.commb.mach60(msg)
vertical_rate_baro = pms.commb.vr60baro(msg)
vertical_rate_ins = pms.commb.vr60ins(msg)
```

18 | Mode S meteorological services

In the current Mode S design, two message formats are used for aircraft to communicate meteorological conditions. These messages are meteorological routine air report (MRAR) and meteorological hazard report (MHR). In this chapter, we focus on explaining the information contained in these two types of messages.

18.1 Meteorological routine air report (BDS 4,4)

In MRAR messages, information on wind, air temperature, pressure, and humidity is transmitted. The structure of the message is shown in Table 18.1.

Table 18.1: Meteorological routine air report (BDS 4,4), MB field

FIELD	MSG	MB	BITS
Figure of merit / source	33-36	1-4	4
Status (for wind)	37	5	1
Wind speed			
Range: [0, 511] knots	38-46	6-14	9
LSB: 1 knots			
Wind direction			
Range: [0, 360] degrees	47-55	15-23	9
LSB: 180/256 degrees			
Sign (for temperature)	56	24	1
Static air temperature			
Range: [-128, +128] °C	57-66	25-34	10
LSB: 0.25 °C			
Status (for pressure)	67	35	1
Average static pressure			
Range: [0, 2048] hPa	68-78	36-46	11
LSB: 1 hPa			
Status (for turbulence)	79	47	1
Turbulence	80-81	48-49	2
Status (for humidity)	82	50	1
Humidity			
Range: [0%, 100%]	83-88	51-56	6
LSB: 100/64 %			

The first field of the message defined the figure of merit (FOM) / source of the information. The values indicate the following:

- 0: Invalid
- 1: Inertial system (INS)
- 2: Global Navigation Satellite System (GNSS)
- 3: Distance measuring equipment-based navigation (DME/DME)
- 4: Very High Frequency omnidirectional range / distance measuring equipment-based navigation (VOR/DME)
- 5-15: Reserved

For static air temperature, the encoded value can be negative. Hence, two's complement coding (see section 11.4) is used for decoding. The actual maximum range of temperature is from -80 °C to +60 °C.

It is also worth pointing out a discrepancy in the design. The temperature is encoded using 10 bits, where the least significant bit value should have been 0.125°. However, according to the official document [9], the LSB value is 0.25°. ICAO has planned to update this to 0.125° in the future. Most current implementations still use 0.25°.

In Figure 18.1, the decoding of an MRAR example message is shown.

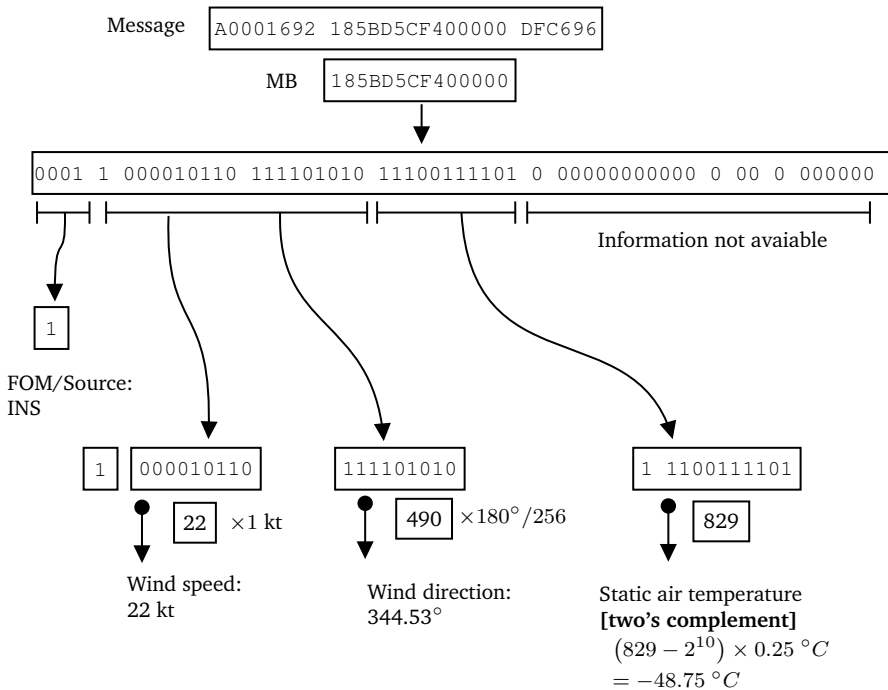


Figure 18.1: Meteorological routine air report (BDS 4,4) decoding example

Try it out

Using `pyModeS` , we can decode information of BDS 4,4 messages as:

```
import pyModeS as pms

msg = "A0001692185BD5CF400000DFC696"

wind = pms.commb.wind44(msg)
temperature = pms.commb.temp44(msg)
pressure = pms.commb.p44(msg)
humidity = pms.commb.hum44(msg)
```

18.2 Meteorological hazard report (BDS 4,5)

In MHR messages, different hazard condition levels are reported, such as turbulence, wind shear, microburst, icing, and wake vortex. It also includes temperature, pressure, and radio height. In Table 18.2, the structure of the MHR message is shown.

It is worth noting that during real flights, MHR messages are much rarer than MARA messages. Whenever they are available, most of the messages only contain temperature information.

Table 18.2: Meteorological harzard report (BDS 4,5), MB field

FIELD	MSG	MB	BITS
Status (for turbulence)	33	1	1
Turbulence	34-35	2-3	2
Status (for wind shear)	36	4	1
Wind shear	37-38	5-6	2
Status (for microburst)	39	7	1
Microburst	40-41	8-9	2
Status (for icing)	42	10	1
Icing	43-44	11-12	2
Status (for wake vortex)	45	13	1
Wake vortex	46-47	14-15	2
Status (for temperature)	48	16	1
Sign (for temperature)	49	17	1
Static air temperature Range: [-128, +128] °C LSB: 0.25 °C	50-58	18-26	9
Status (for pressure)	59	27	1
Average static pressure Range: [0, 2048] hPa LSB: 1 hPa	60-70	28-38	11
Status (for height)	71	39	1
Radio height Range: [0, 65 528] ft LSB: 16 ft	72-83	40-51	12
Reserved	84-88	52-56	5

The levels for turbulence, wind shear, microburst, icing, and wake vortex are encoded as follows:

- 00 : NIL
- 01 : LIGHT
- 10 : MODERATE

- 11 : SEVERE

As is the case for MRAR messages, the actual range of the temperature is from -80°C to $+60^{\circ}\text{C}$, and it is encoded using the two's complement coding.

In Figure 18.2, the decoding of an example message is shown. Note that in this example, only the air temperature information is included. None of the hazard conditions is reported.

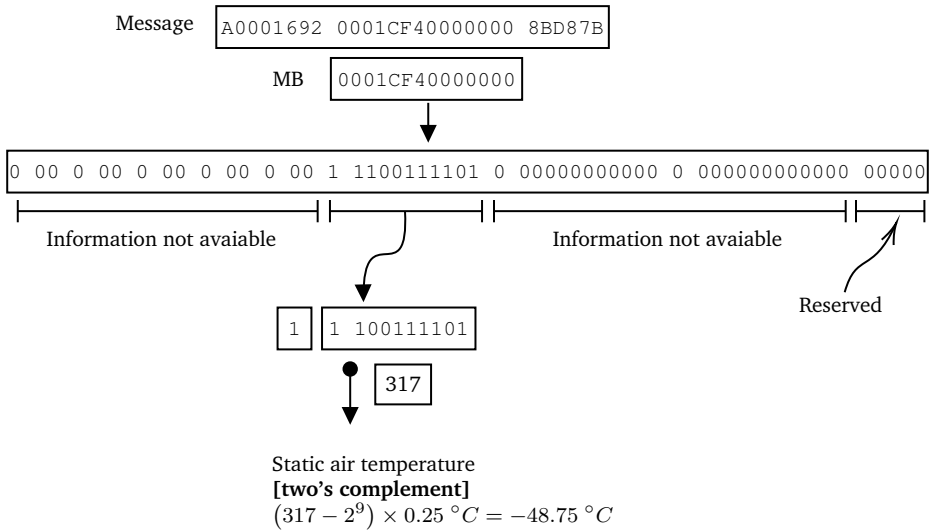


Figure 18.2: Meteorological hazard report (BDS 4,5) decoding example

Note

The availability of BDS 4,4 messages is quite low. Very few aircraft's transponders have these capabilities enabled. BDS 4,5 message is even rarer. When a message is transmitted, it is very common that information in many fields are not available.

19 | Inferencing of BDS codes

In chapter 15, we discussed the basic structure and protocols of Mode S Comm-B messages. Each message type is identified by an 8-bit Comm-B Data Selector (BDS) code, which is only transmitted in the uplink message but not included in the downlink message. As third parties observing the replies to Mode S surveillance interrogations, we must first determine the BDS code before decoding the content of any Comm-B messages.

19.1 BDS codes identification logics

Each Mode S message has a predefined structure and variables. For almost all common Comm-B message types, there are rules for certain bits. For example, these bits are:

- **Reserved bits:** Those are bits in the different message types that are reserved for future use. They all have to be zeros. If any of the bits is not zero, the possibility of a certain BDS code should be ruled out.
- **Status bits:** Some fields in Comm-B messages have their corresponding status bits. When a status bit is set to zero, all bits in the field must be zero. If the field contains non zero bits, the possibility of a certain BDS code can be ruled out.
- **Value rules:** Different fields in the messages also have different physical ranges. For example, the Mach number in BDS 6,0 should not be higher than 1, and the temperature value in BDS 4,4 should be between -80°C and 60°C . These constants can also be used to exclude certain BDS codes.

In Tables 19.1, 19.2, and 19.3, the rules for identifying different types of ELS, EHS, and meteorological messages are shown.

19.2 Identification of BSD 5,0 and 6,0

Of all the previously mentioned message types, BDS 5,0 and BDS 6,0 are the two message types that share the most similar structures. From Table 19.2, we can see the differences are present in bit 12/13 and bit 45/46 of BDS 5,0 and BDS 6,0. This similarity can cause a number of messages to be identified as both BDS 5,0 and 6,0 messages.

In order to distinguish between these two messages, we need to utilize the information contained in the messages. BDS 5,0 and BDS 6,0 both contain aircraft speed information. We can design the additional check using the following logic:

Table 19.1: Heuristic indenfication logic for ELS

BDS	MB bits	Parameter	Rules
1,0	1-8	BDS code	Equal to 0001 0000
	10-14	Reserved	All zeros
1,7	7	BDS 2,0 enabled	Equal to 1
	29-56	Reserved	All zeros
2,0	1-8	BDS code	Equal to 0010 0000
	9-56	Callsign	Only contains 0-9, A-Z, or space
3,0	1-8	BDS code	Equal to 0011 0000
	29-30	Threat type	Not equal to 11
	16-22	ACAS	less than 48

Table 19.2: Heuristic indenfication logic for EHS

BDS	MB bits	Parameter	Rules
4,0	1 : 2-13	MCP/FCU selected altitude	Status consistant
	14 : 15-26	FMS selected altitude	Status consistant
	27 : 28-39	Barometric pressure	Status consistant
	40 - 47	Reserved	All zeros
	52 - 53	Reserved	All zeros
5,0	1 : 2-11	Roll angle	Status consistant Between -50 and 50 degree
	12 : 13-23	True track angle	Status consistant
	24 : 25-34	Ground speed	Status consistant Between 0 and 600 kt
	35 : 36-45	Track angle rate	Status consistant
	45 : 46-56	True airspeed	Status consistant Between 0 and 500 kt
6,0	1 : 2-12	Magnetic heading	Status consistant
	13 : 14-23	Indicated airspeed	Status consistant Between 0 and 500 kt
	24 : 25-34	Mach number	Status consistant Between 0 and 1
	35 : 36-45	Barometric vertical rate	Status consistant Between -6000 and 6000 fpm
	46 : 47-56	Inertial vertical rate	Status consistant Between -6000 and 6000 fpm

Table 19.3: Heuristic indenfication logic for MRAR and MHR

BDS	MB bits	Parameter	Rules
4,4	1-4	FOM	Less than 5
	5 : 6-23	Wind speed / direction	Status consistant speed less than 250 kt
	24-34	Static air temperature	Between -80 and 60°C
4,5	1 : 2-3	Turbulence	Status consistant
	4 : 5-6	Wind shear	Status consistant
	7 : 8-9	Microburst	Status consistant
	10 : 11-12	Icing	Status consistant
	13 : 14-15	Wake vortex	Status consistant
	16 : 17-26	Static air temperature	Status consistant Between -80 and 60°C
	27 : 28-28	Static pressure	Status consistant
	39 : 40-51	Radio height	Status consistant
	52-56	Reserved	All zeros

- Assuming the message is BDS 5,0, compare the difference between the ground speed and true airspeed. The difference should not be too large. Empirically, this threshold can be set at approximately 200 kt to include possible wind speed.
- Assuming the message is BDS 6,0, convert the Mach number to calibrated airspeed based on altitude code under ISA condition [17]. The difference between calibrated airspeed and indicated airspeed should not be too large.

If the previous logic does not eliminate one of the two possibilities, we need to make use of the information collected in ADS-B (if available) to verify the information. ADS-B data from the same aircraft can be used as a reference, to check whether the speed from the assumed message type agrees with the groud speed from ADS-B. The details of this process is described in [16]. Wind information can also be taken into consideration to make the identification more accurate.

19.3 Examples

The basic BDS code identification logic is relatively simple. It checks all criteria from all message types and decides whether all but one BDS code can be eliminated. In this example section, we are only going to show how a message with both possibilities of BDS 5,0 and BDS 6,0 can be identified.

In Figure 19.1, the identification of a DF=20 message is shown.

We see that BDS 6,0 is identified since the difference between the ground speed

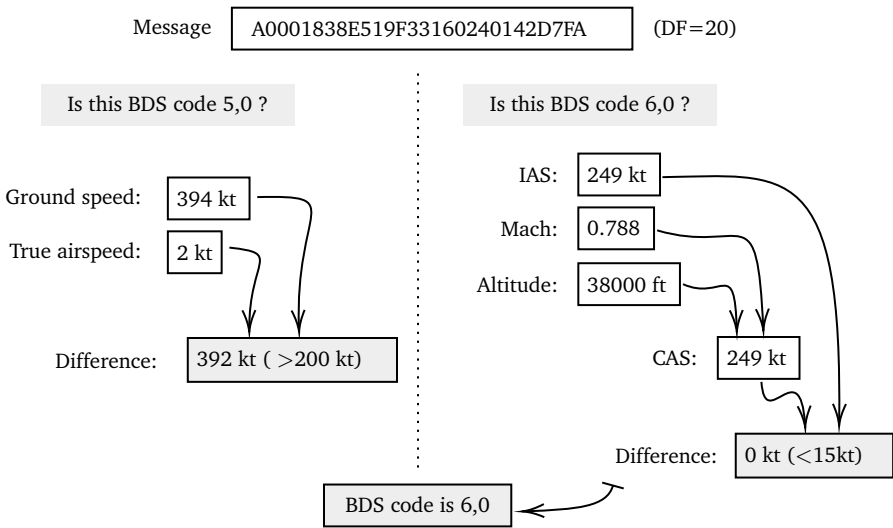


Figure 19.1: Identification of BDS code, DF=20

and airspeed is too high in the BDS 5,0 assumption.

In Figure 19.2, the identification of a DF=21 message is shown. In DF=21 messages, the altitude code is not included. Thus, we have to reply to other information, such as speed and track angle from ADS-B to validate the BDS code. The assumption from BDS 5,0 conforms to the ADS-B information.

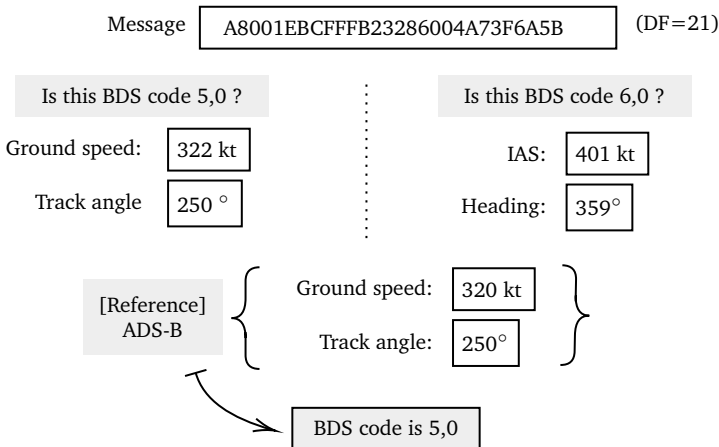


Figure 19.2: Identification of BDS code, DF=21

Try it out

Using `pyModeS` , we can infer the BDS code of a message as:

```
import pyModeS as pms

msg1 = "A0001838E519F33160240142D7FA"
bds1 = pms.bds.infer(msg1)

msg2 = "A8001EBCFFFB23286004A73F6A5B"
bds2 = pms.bds.infer(msg2)
```

This first BDS code should be `BDS60` and the second one should be `BDS50` .

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