

Numerical Methods

Introduction to Programming in Matlab

lecturer: R. Luppes (r.luppes@rug.nl)

1 Assignment

Type the following commands in the command window, followed by the enter key. Try to predict the result each time and check your prediction.

```
clear all
a=2
b=a+1
a=a+3
c=b*sqrt(a-1)
d=a*cos(c*pi)+2
x=[1 \ 4 \ 9]
y=2*sqrt(x)
y(3)
y=y-1
y(2:3)
z=[2 \ 4]
v=zeros(1,5)
W=Z+X
A=[1 \ 2; \ 3 \ 4]
A(2,1)
IA=inv(A)
x=[-1 \ 2]
x=[-1 \ 2],
A*x
B=ones(5,5)
x=1:1:14
y=1:3:20
size(y)
z=60:-10:10
M=[1\ 2\ 3;\ 4\ 5\ 6;\ 7\ 8\ 9]
size(M)
M(1,:)
M(:,2)=23
```

1. Calculate for x=2, by introducing a number of auxiliary variables, the value of

$$p = \sin\sqrt{(5x+1)}$$

2. Calculate (the -1 denotes inverse matrix)

$$\left(\begin{array}{cc} 1 & -3 \\ 2 & 4 \end{array}\right)^{-1} \left(\begin{array}{c} 1 \\ -6 \end{array}\right)$$

- 3. Create an array r containing the numbers 0,5,10,15..,200. How many numbers does this array contain?
- 4. Define a 20x10 matrix M containing only zeros, except in the second row, which contains the number 4 everywhere:

$$M = \begin{pmatrix} 0 & \cdots & \cdots & 0 \\ 4 & \cdots & \cdots & 4 \\ 0 & \cdots & \cdots & 0 \\ \vdots & & & \vdots \\ 0 & \cdots & \cdots & 0 \end{pmatrix}$$

2 If statement

Create a file 'pietje.m' by typing edit pietje, enter the following program (use copy-paste) and save the file.

```
% this is my if program
% input: a
% output: z
if a>2,
   z=5
else
   z=15
end
```

Then enter the following commands in the command window. Figure out each time the expected result before typing.

```
clear all
help pietje
a=4
pietje
a=-1
pietje
b=3
pietje
a=2
pietje
z=4
pietje
```

- 1. Write a program that, depending on the sign of the variable $x \neq 0$, assigns the value +1 or -1 to the variable p. Check your program for x = -3 and x = 3.
- 2. Write a program that reads an input variable x and changes the value of that x to zero when x is positive and not larger than 15. Check your program for x = -3, x = 3 and x = 30.

3 For statement

Create a file 'jantje.m' by typing edit jantje, enter the following program (use copy-paste) and save the file.

```
% this is my for program
% input: N (integer number)
% output: x (array)
x=zeros(1,N);
for i=1:N,
    x(i)=i*i;
end
```

Enter the following commands in the command window. Figure out the expected results before typing.

```
clear all
help jantje
N=7
jantje
x
x(1:3)
```

Exercises

- 1. Write a program that stores the multiplication table of 7 in an array taf(1:10) by means of a for-loop.
- 2. (a) Someone saves a sum of 100 Euro on the bank against an interest rate of 5%. The interest is paid at the end of each year. Compute the total sum after 16 years using a for-loop.
 - (b) Compute the total sum when in the 7th year the interest rate is increased to 6%. To do this, insert an if-statement inside the for-next loop.
- 3. Create a 7x7 matrix M, with all elements zero, except on the diagonal where $A_{ii} = i$.
- 4. Consider the forward recurrence relation $a_n = n * a_{n-1} + 0.1$, with initial value $a_1 = 0$. Check that $a_7 = 362$ by means of a for-loop. Remark: this can be done without using arrays.



5. Consider the backward recurrence relation $a_{n-1} = (a_n - 0.1)/n$, with initial value $a_7 = 362$. Check that $a_1 = 0$ using a for-loop. Convince yourself that this formula is the reverse of the one given in exercise 4.

4 While statement

Create a file 'hallo.m' by typing edit hallo, enter the following program (use copy-paste) and save the file.

```
% programma hallo
% input: m
% output: xm,i
i=0;
xm=m;
while xm>1e-8
    xm=xm/2
    i=i+1
end
```

Enter the following commands. Figure out the expected results before typing.

m=100 hallo m=512 hallo m=0 hallo

Exercises

- 1. What is the role of the output variable *i* in 'hallo.m'? The condition xm>1e-8 is known as the 'guard'. Why? What happens if in 'hallo.m' the line xm=xm/2 is replaced by xm=xm*2 and the program is started with m=100?
- 2. Someone saves a sum of 100 Euro on the bank against an interest rate of 5%. The interest is paid at the end of each year. Use a while-statement to determine after how many years the total sum will be greater than 200 Euro.
- 3. Determine the largest integer n for which $2^n < Inf$ (infinity) by means of a while-statement.

5 Functions

Create a file 'myfunc.m' by typing edit myfunc, enter the following program (use copy-paste) and save the file.

```
function [p,q]=myfunc(n,m)
% function myfunc
% input: m,n
% output: product and quotient of m and n
p=m*n;
q=m/n;
```

Enter the following commands. Figure out the expected results before typing.

```
clear all
[x,y]=myfunc(2,16)

n=3
m=6
[x,y]=myfunc(n,m)

myfunc(4,100)
y

x=zeros(1,6)
y=zeros(1,6)
for n=1:6, [x(n),y(n)]=myfunc(n,m), end
```

1. (a) What goes wrong if a new line m=5 is added inside the function:

```
p=m*n; q=m/n; NOTHING GOES WRONG ??? m=5;
```

Remove the extra line m=5, and continue with the original function.

- (b) Change the function 'myfunc.m', such that the variables have 'better' names. Why are these names better?
- (c) Change the name of the function, and store the function in a new .m file accordingly.
- 2. Create a program containing the function $p(x) = \sin \sqrt{(5x+1)}$. Use this program to calculate p(0) and check the result.
- 3. Calculate the values of p(x) at the points x = 0 : 0.1 : 2, with p(x) as in exercise 1). Store these values in the array pres. How many elements does pres contain?

6 Plot

Execute the following commands:

```
clear all
x=[0:0.01:4];
y=sin(x.^2);
plot(x,y)
plot(x,y,'*')
plot(x,y,'g--')
w=cos(x.^2);
hold on
plot(x,w,'m.')
wysum=abs(y+w);
plot(x,wysum,'d')
```

```
title('nice plot')
xlabel('x coord')
ylabel('function value')
hold off
plot(x,10*w-5,'m.')
```

- 1. Make a plot of the function $w(x) = \sqrt{x}$, for the domain $0 \le x \le 16$.
- 2. Make a plot of the function p(x) (see previous section) for x = 0:0.1:2.

7 Output format

Execute the following commands:

```
clear all
em1=exp(1)
i = 23
format long
em1
format short
em1
format long e
em1
fprintf('e= %8.6f \n',em1);
fprintf('e= %8.4e \n',em1);
fprintf('%6.0f %15.6e \n',i,em1);
disp('hello')
str1='uitv:';
str2=num2str(i);
str3=num2str(em1);
disp([str1 ' i=' str2 ' e=' str3])
```

Exercises

- 1. Print the number $\sqrt{3}$ with successively 1, 8 and 30 digits behind the decimal point.
- 2. Define the variables i=3, j=-5, $x=\sqrt{2}$. Print these 3 variables in a single line using a nice format with x having 6 digits behind the decimal point.

8 Structs (groups of variables)

Execute the following commands in the command window. Try to predict the result each time and check your prediction.

```
clear all
field1 = 'f1';
field2 = 'f2';
field3 = 'f3';
field4 = 'f4';
value1 = {[1 2 3 4 5], [10 20 30], [100 200 300 400]};
value2 = {'a', 'b', 'c'};
value3 = {pi, pi.^2, pi.^3};
value4 = {'first', 'second', ['hello', 'there']};
s = struct(field1,value1, field2,value2, field3,value3, field4,value4);
s(1)
s(2)
s(3)
s(4)
s(1).f1
s(1).f3
s(1).f1(5)
s(1).f3(2)
s(2).f1
s(2).f3
s(2).f1(3)
s(2).f1(5)
s(2).f3(2)
s(3).f2
s(3).f4
s(3).f4(6)
sdum = s(2)
for i=1:3
    s(i)
end
s(1).f1(5)=36
s(1)
```

- 1. Suppose this course is done by 5 students. Create a struct 'course' with 3 fields containing the names of the students (Adam, Bob, Chris, Dan, Elmo), their student number (11,12,13,14,15) and birthdate in an array with length 2 (day and month 20/01,21/02,22/03,23/04,24/05).
- 2. It appears that the student number of Dan was wrong, change it into 84. Moreover, Chris was born in July, not in March, so update it accordingly.