

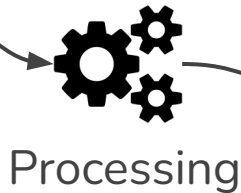
Fundamentals of Image Processing

BIP -DLF - Jean-Christophe Taveau





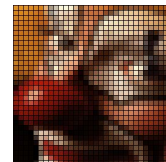
Why Image Processing?



Measurements - Quantification

Results										
File Edit Font Results										
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	1	338.500	18.500	1.000	1.414	338	18	135	1	1.000
2	113	329.969	36.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000

- Statistics
- Machine Learning



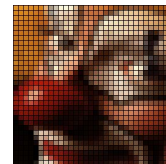
Why Image Processing?



Measurements of ROI

Results										
File	Edit	Font	Results							
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	1	338.500	18.500	1.000	1.414	338	18	135	1	1.000
2	113	329.969	36.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
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6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000

- Objects of Interest (Region of Interest)
- Background





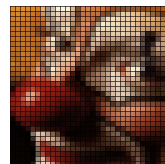
Why Image Processing?

Measurements - Quantification

Columns: Features

Rows: Samples (ROI)

Results										
File	Edit	Font	Results							
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	1	338.500	18.500	1.000	1.414	338	18	135	1	1.000
2	113	329.969	36.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000





Digital Image

Properties

Image is characterized by:

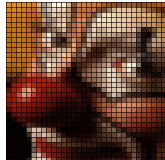
① Pixels number → Resolution

- Pixels number per unit of length of the object to digitize
- Units : dpi (dots per inch) ou ppp (point par pouce)

② Range of gray levels or colors

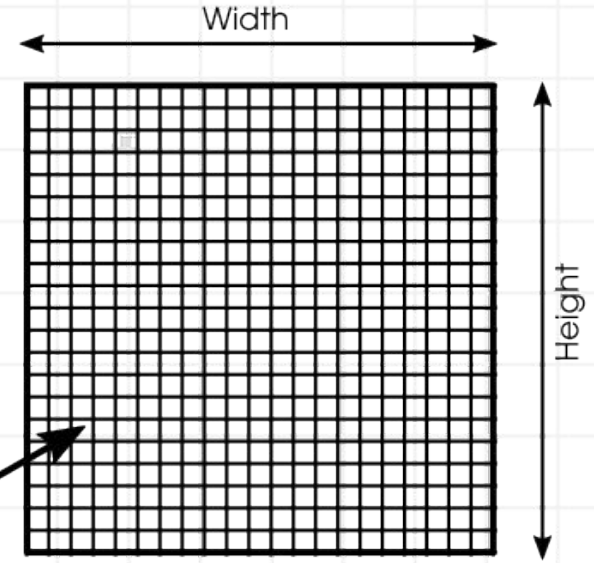
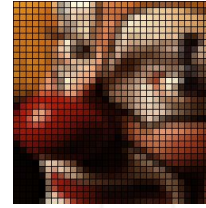
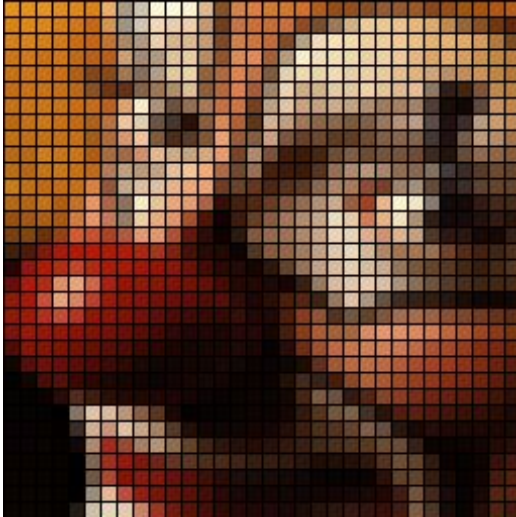
→ Dynamic range

1-bit, 8-bits (256), 16-bits ($2^{16} = 65536$), RGB, etc.

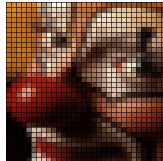


Digital Image

2D array of pixels



Pixel = Picture Element





Digital Image

2D arrays of pixels in a spreadsheet

The screenshot shows the LibreOffice Calc application window titled "Sans nom 1 - LibreOffice". The menu bar includes "Fichier", "Édition", "Affichage", "Insertion", "Format", "Styles", and "Feuille". The toolbar contains icons for file operations and editing. The text area shows "Liberation San" and "10". The formula bar shows "A1" and "0". The spreadsheet grid shows a 7x7 area with the following values:

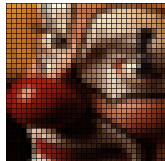
	A	B	C	D	E	F	G
1	0	1	2	3	4		
2	5	6	7	8	9		
3	10	11	12	13	14		
4	15	16	17	18	19		
5	20	21	22	23	24		
6							
7							

Two yellow sticky notes are placed on the right side of the spreadsheet:

- A yellow sticky note with the text "PIXEL VALUES" written in black marker.
- A yellow sticky note with the text "COMMA SEPARATED VALUES" written in black marker.

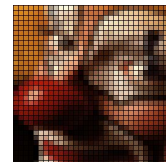
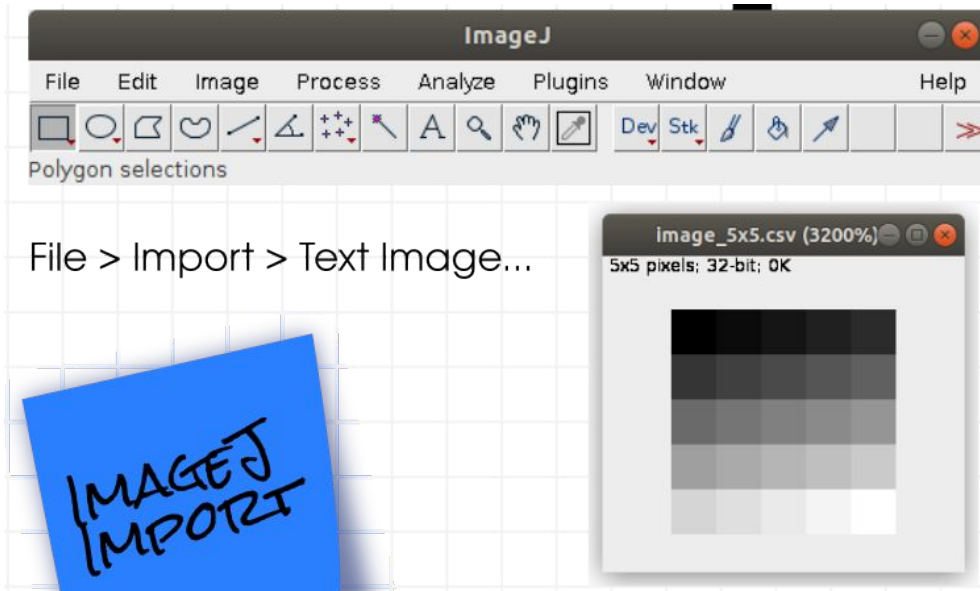
Below the spreadsheet, a sidebar shows a "Taille" (Size) section with the following information:

- 50 octets
- 39 octets



Digital Image

2D arrays of pixels in ImageJ





Digital Image

2D arrays of pixels in Python

```
import numpy as np
import matplotlib.pyplot as plt

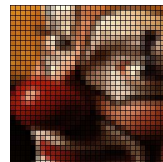
img = np.arange(25).reshape(5,5)

print(img)
```

✓
0 s

```
[3] print(img)
```

```
[[ 0  1  2  3  4]
 [ 5  6  7  8  9]
 [10 11 12 13 14]
 [15 16 17 18 19]
 [20 21 22 23 24]]
```





Digital Image

2D arrays of pixels in Python

```
import numpy as np
import matplotlib.pyplot as plt
```

```
img = np.arange(25).reshape(5,5)
plt.imshow(img, cmap='gray')
```

Web Python Environment: Google Colab



Commentaire



Partager



RAM

Disque



BIP-image000.ipynb ☆

Fichier Modifier Affichage Insérer Exécution Outils Aide



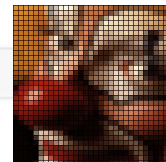
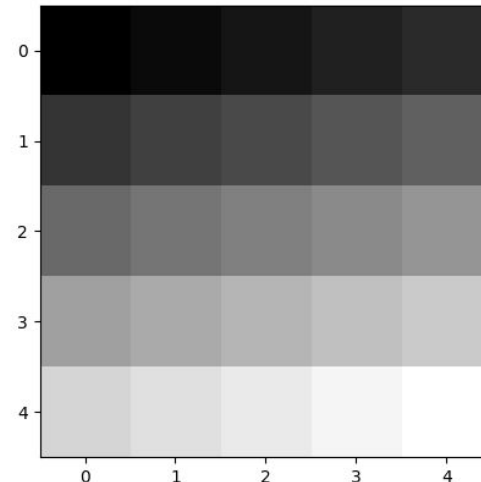
+ Code + Texte



```
import numpy as np
import matplotlib.pyplot as plt

img = np.arange(25).reshape(5,5)
plt.imshow(img, cmap='gray')
```

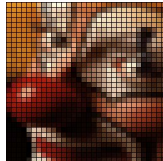
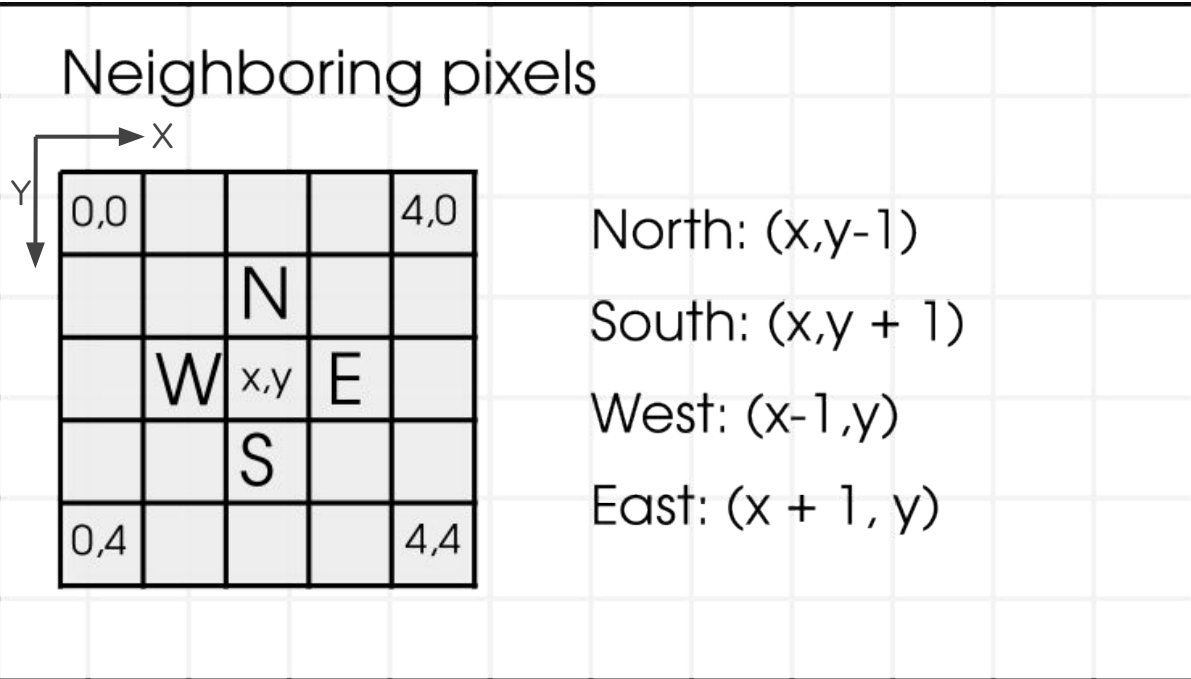
<matplotlib.image.AxesImage at 0x79e6c08f20e0>



Digital Image

Coordinates

View:7





Digital Image

Coordinates in Python with numpy

0,0				4,0
		N		
	W	x,y	E	
		S		
0,4				4,4

```
import numpy as np
```

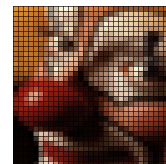
```
img = np.arange(25).reshape(5,5)
```

```
pix_XY00 = img[0,0] # Top left
```

```
pix_XY40 = img[0,4] # img[Y,X]
```

```
pix_XY04 = img[4,0] # Bottom left
```

```
pix_XY44 = img[4,4] # Bottom right
```





Digital Image

Dynamic Range

1 bit = 2 values: 0 (False) or 1 (True)

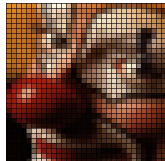


1 byte = 8 bits = 256 gray levels

$$00000000 = 0_{10}$$

$$11111111 = 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 = 2^8 - 1 = 255$$

Other storages: 16bits, float32, float64





Digital Image

Dynamic Range of Color Image



color = Red + Green + Blue = $8 + 8 + 8 = 24$ bits

color = Hue + Saturation + Value = $8 + 8 + 8 = 24$ bits

color = 3-channel image (+ 4th for alpha or transparency)



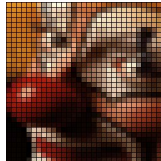
RED Channel



GREEN Channel



BLUE Channel



Digital Image

Dynamic Range of RGB color image

```
import numpy as np
import matplotlib.pyplot as plt
import skimage as ski
```

```
cup = ski.data.coffee()
```

```
cup.ndim # Return the dim. number
```

```
[1] import skimage as ski
```

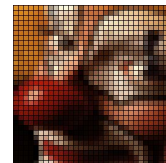
```
cup = ski.data.coffee()
plt.imshow(cup)
```

```
<matplotlib.image.AxesImage at 0x79e68539c850>
```



```
[12] cup.ndim
```

```
3
```



Digital Image

Dynamic Range of RGB color image

```
[1] import skimage as ski
```

```
cup = ski.data.coffee()  
plt.imshow(cup)
```

```
<matplotlib.image.AxesImage at 0x79e68539c850>
```

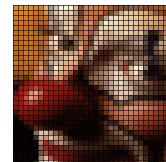


```
import numpy as np  
import matplotlib.pyplot as plt  
import skimage as ski
```

```
cup = ski.data.coffee()
```

```
cup.shape # Return the H x W x Ch
```

```
(400, 600, 3)
```





Digital Image

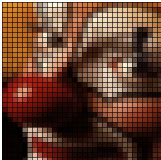
Storage 2D → 1D

0	1	2	3	4	20	21	22	23	24
---	---	---	---	---	------	----	----	----	----	----

2D → 1D Array

0,0				4,0
		2,2		
0,4				4,4

0	1	2	3	4
5	6	7	8	9
10	11	12	13	14
15	16	17	18	19
20	21	22	23	24



Digital Image

Storage 2D → 1D

View:11. FX:12,13

$$\text{index} = x + w * y$$

$$x = \text{index} \% w$$

$$y = \text{index} / w$$

Pixel @ (3,2)

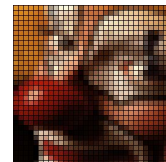
$$i = 3 + 5 * 2 = 13$$

$$x = 13 \% 5 = 3$$

$$y = 13 / 5 = 2$$

0	1	2	3	4
5	6	7	8	9
10	11	12	13	14
15	16	17	18	19
20	21	22	23	24

INDEX





Digital Image

Storage 2D → 1D

```
index = 9
```

```
# Wrong !!
```

```
right_neighbor = 9 + 1
```

View:14

Neighboring pixels

North: index - w

South: index + w

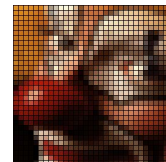
West: index - 1

East: index + 1



0	1	2	3	4
5	6	7	8	9
10	11	12	13	14
15	16	17	18	19
20	21	22	23	24

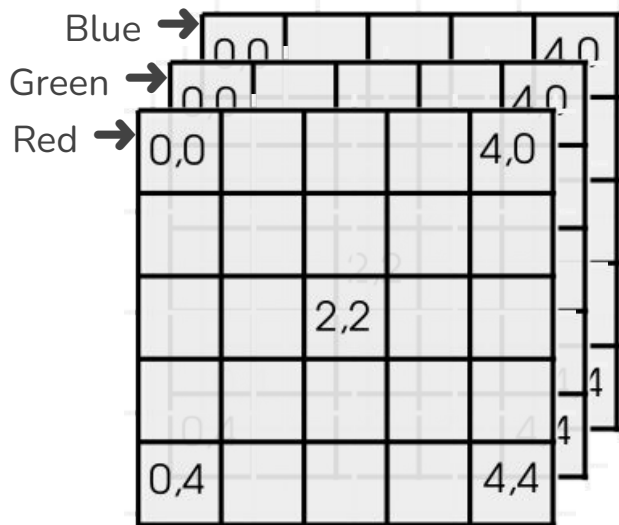
XY-
COORDS





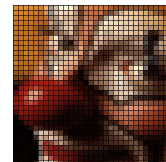
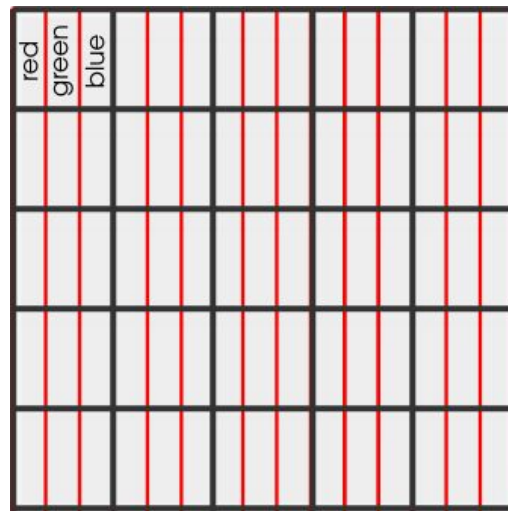
Digital Image

Other Storages: color image



Planar RGB images
shape: (3,5,5)

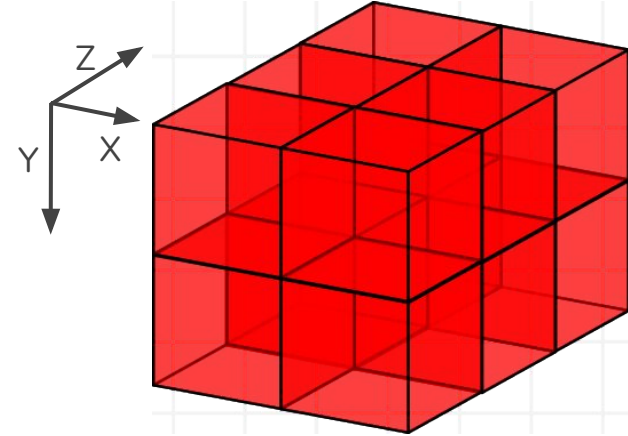
Packed RGB images →
shape: (5,5,3)



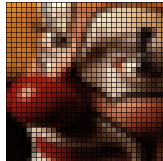
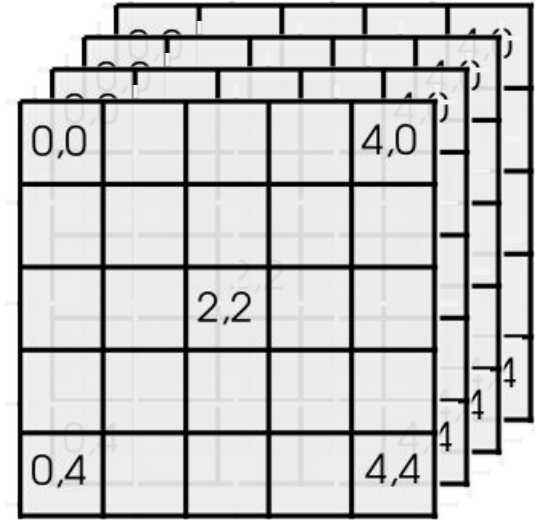


Digital Image

Other Storages



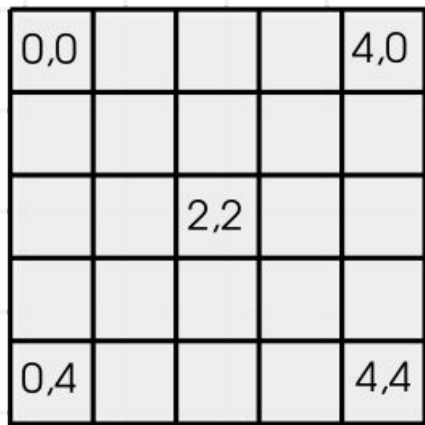
- Volume (3D) with voxels
- RGB Volume (4D)
- Stack of n 2D images (nD)



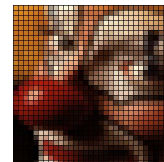
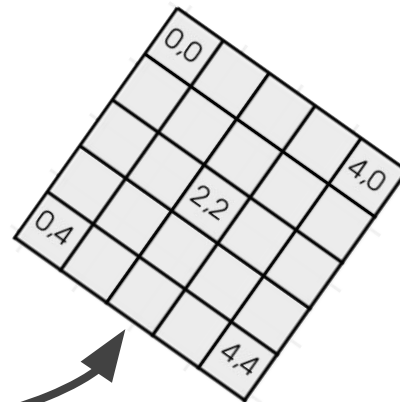


Geometrical Transforms

Translation, Rotation, Flip, Scaling



Rotation +
Scaling





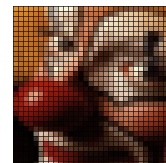
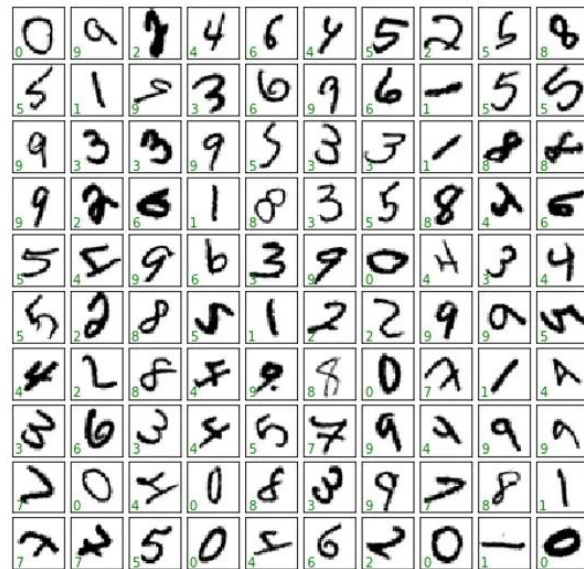
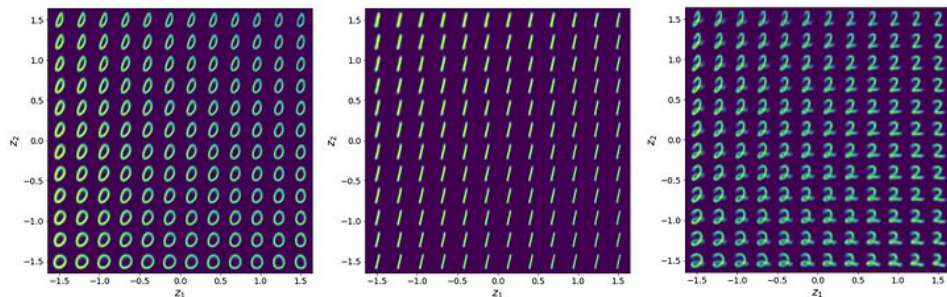
Geometrical Transforms

Translation, Rotation, Flip, Scaling

Popular Image manipulation

Clustering

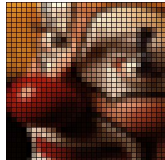
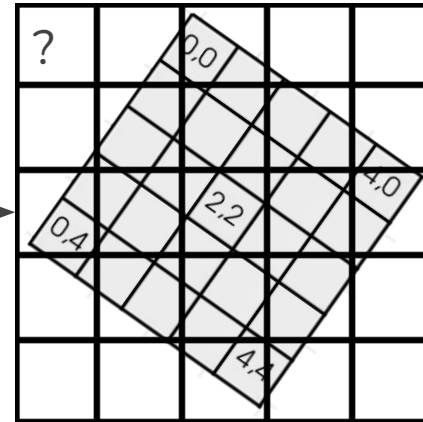
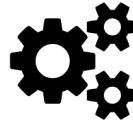
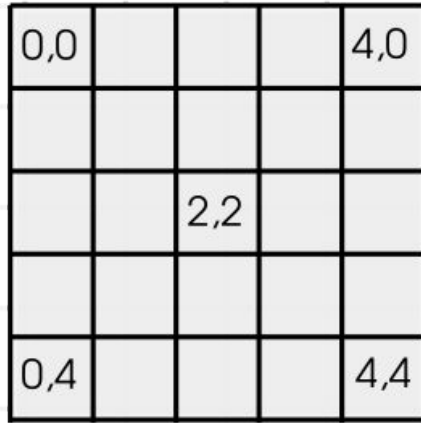
Data Augmentation (Deep Learning)





Geometrical Transforms

Translation, Rotation, Flip, Scaling





Geometrical Transforms

Translation, Rotation, Flip, Scaling

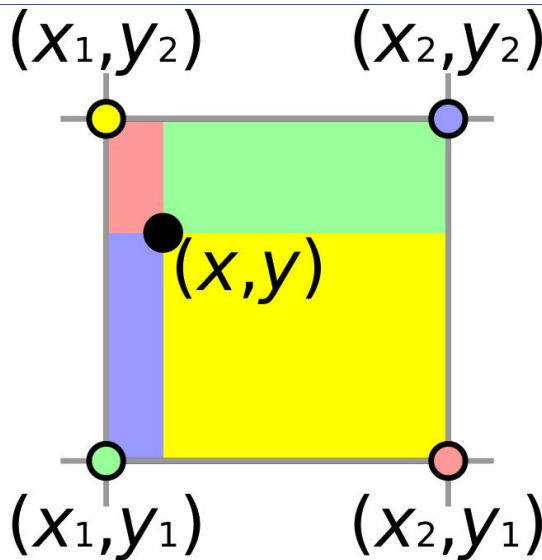
Pseudo-code

for each pixel(x',y') of output:

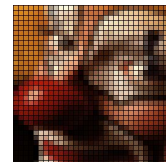
$out[y',x'] = calc_intensity(img,T)$

Interpolation Schemes

- Nearest Neighbor
- Bilinear Interpolation
- Bicubic Interpolation



From Wikipedia

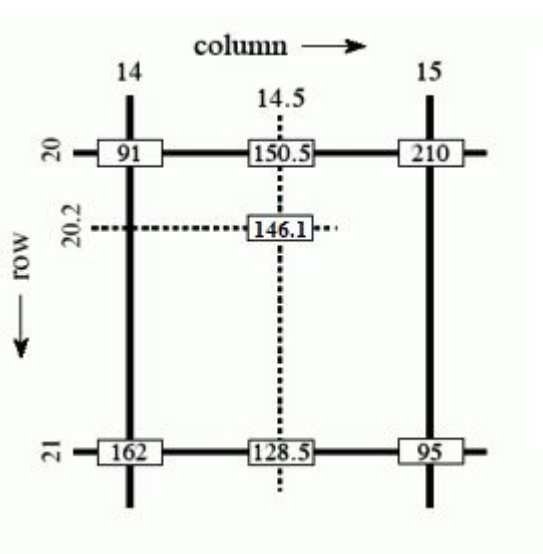




Geometrical Transforms

Translation, Rotation, Flip, Scaling

→ Bilinear Interpolation

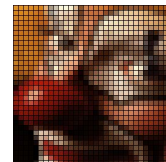


$$I_{20,14.5} = \frac{15 - 14.5}{15 - 14} \cdot 91 + \frac{14.5 - 14}{15 - 14} \cdot 210 = 150.5,$$

$$I_{21,14.5} = \frac{15 - 14.5}{15 - 14} \cdot 162 + \frac{14.5 - 14}{15 - 14} \cdot 95 = 128.5,$$

$$I_{20.2,14.5} = \frac{21 - 20.2}{21 - 20} \cdot 150.5 + \frac{20.2 - 20}{21 - 20} \cdot 128.5 = 146.1.$$

From Wikipedia





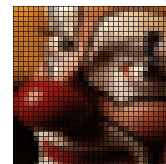
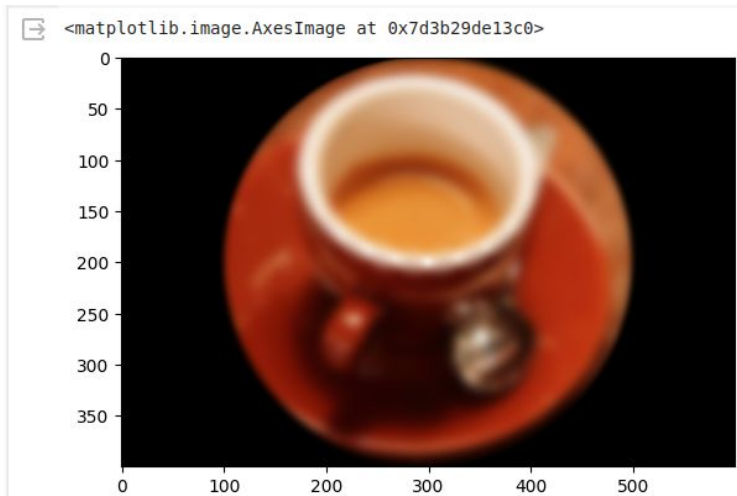
Geometrical Transforms

Accumulating Transforms

→ Repeating many small rotations of 2° over 360° .

```
▶ rotated = cup
  angle = 360 / 180
  for i in range(180):
    rotated = ski.transform.rotate(rotated, angle, resize=False)

  plt.imshow(rotated)
```

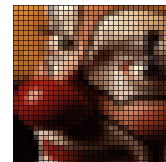
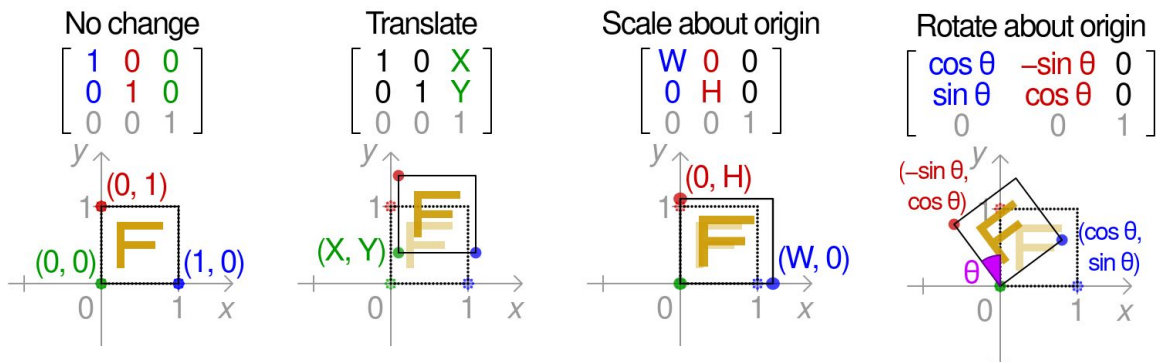




Geometrical Transforms

Accumulating Transforms

→ Using 2D matrix of 3x3. Accumulating Transforms = Multiplying matrices



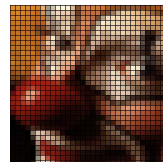


Geometrical Transforms

Accumulating Transforms

```
shift = ski.transform.EuclideanTransform(translation=-np.array([300,200]) ) # Image center
rot= ski.transform.EuclideanTransform(rotation= np.deg2rad(2.0) )
# Compose transforms by multiplying their matrices for the rotations
rots = np.identity(3)
for i in range(180):
    rots = np.matmul(rot,rots)
# Compose transforms by multiplying their matrices to rotate around the image center
matrix = np.linalg.inv(shift.params) @ rots @ shift.params

[[ 1.00000000e+00  1.01708908e-15 -2.27373675e-12]
 [-6.30919087e-16  1.00000000e+00 -1.10844667e-12]
 [ 0.00000000e+00  0.00000000e+00  1.00000000e+00]]
```



Fundamentals of Image Processing

BIP -DLF - Jean-Christophe Taveau





Digital Image

Pipeline

Image Enhancement

- Brightness/contrast
- Non Uniform Illumination
- Noise Removal

Segmentation

- Threshold
- Math. Morphology



Results											
File Edit Font Results											
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR	
1	338.500	18.500	1.000	1.414	338	18	135	1	1.000		
2	113	329.969	35.969	0.112	41.485	324	60	74.624	8.995	6.254	
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000	
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210	
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342	
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000	
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000	
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646	
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697	
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000	
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000	
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000	

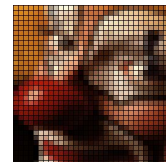
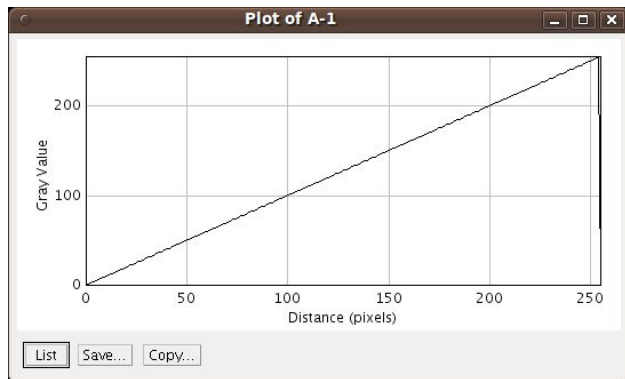




Image Enhancement

Principle - Brightness / Contrast



Transfer Function: $Y = a \cdot x + b$

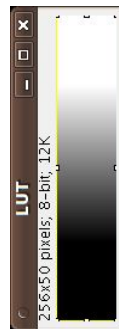
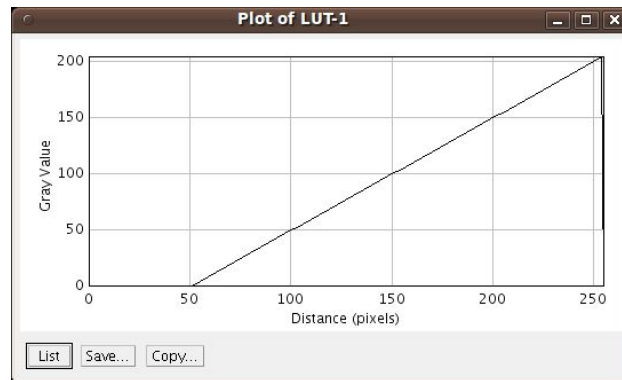
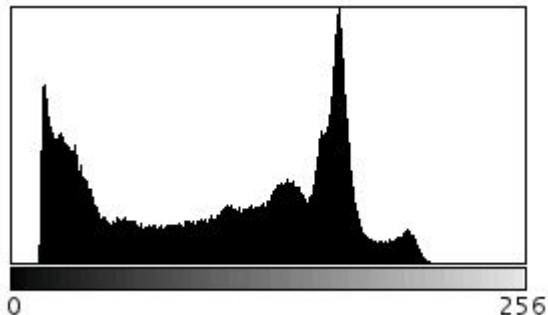


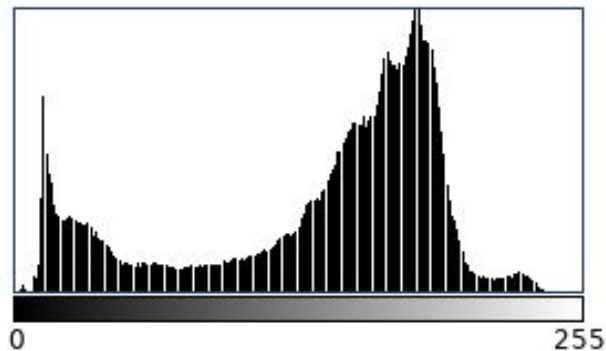


Image Enhancement

Principle - Normalization



$$v' = (v - \min) / (\max - \min)$$



N: 414720
Mean: 137.016
StdDev: 57.807
Value: 112

Min: 0
Max: 255
Mode: 180 (7480)
Count: 1131

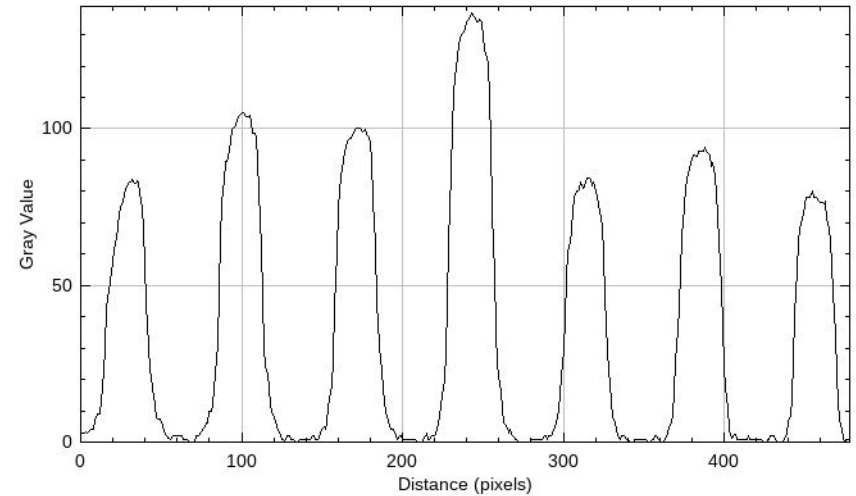
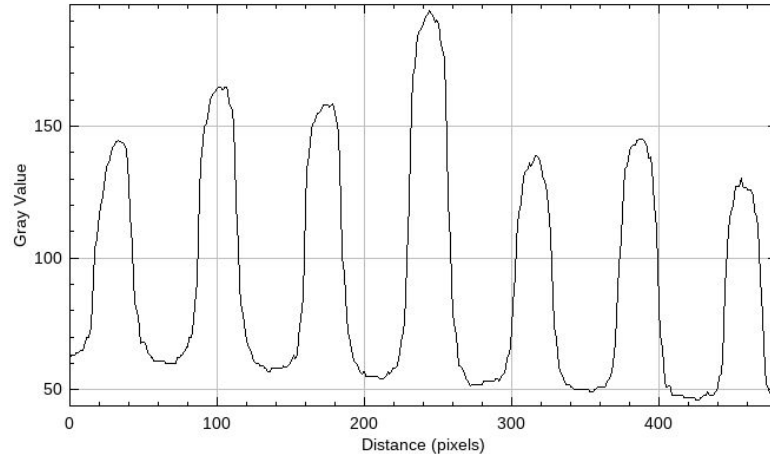


Image Enhancement

Non Uniform Illumination - Subtract Background

Removing the Baseline

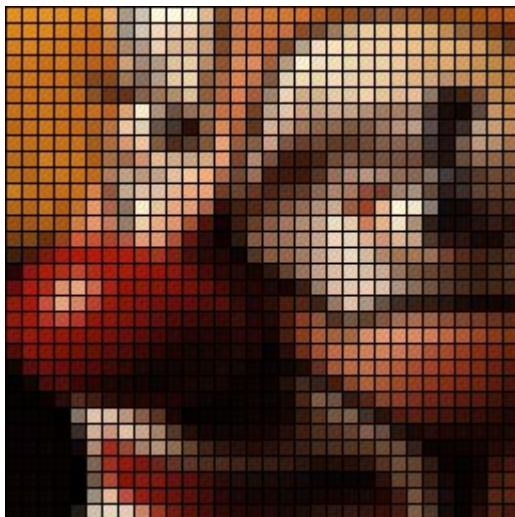
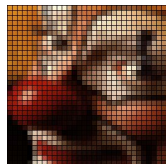
- Polynomial Functions
- Rolling Ball



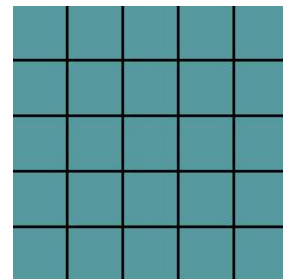
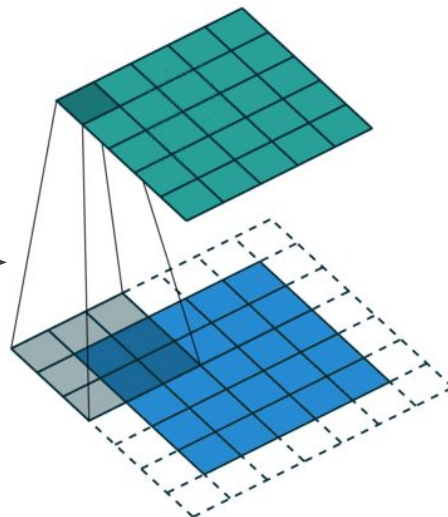


Denoising - Filters

Principle - Convolution



w_1	w_2	w_3
w_4	w_5	w_6
w_7	w_8	w_9



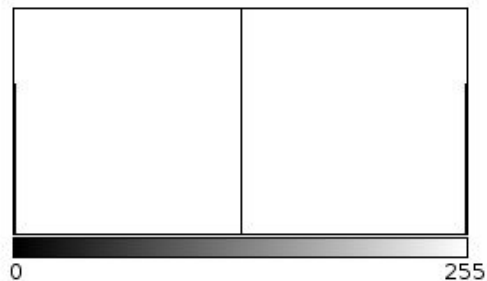
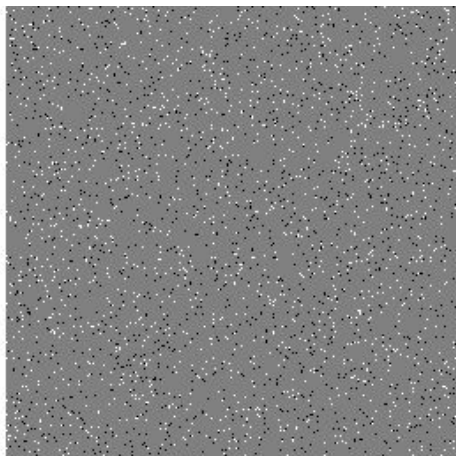
Mean 3x3
Gaussian 7x7
Median 3x3



Denoising - Filters

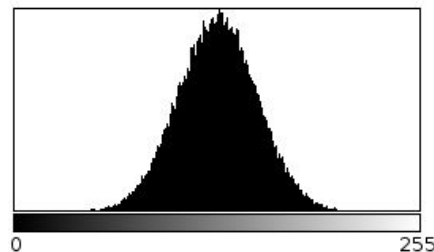
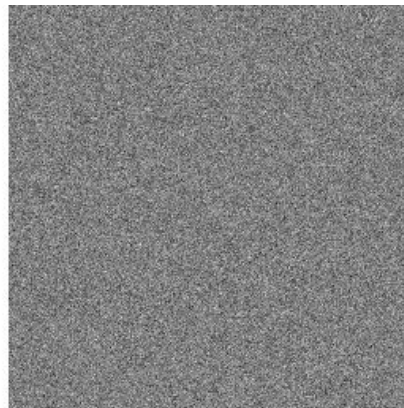
Principle - Noise

Impulse Noise (Salt and Pepper)



N: 65536	Min: 0
Mean: 127.974	Max: 255
StdDev: 28.161	Mode: 128 (62339)
Value: 167	Count: 0

Gaussian Noise



N: 65536	Min: 26
Mean: 127.915	Max: 232
StdDev: 24.918	Mode: 129 (1092)
Value: 176	Count: 171

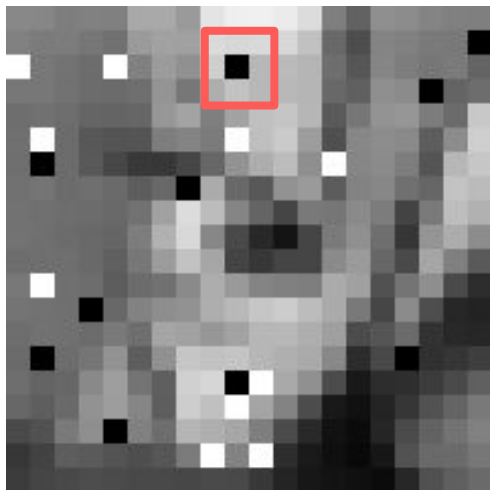


Denoising - Filters

Principle - Noise

Denoise Filters:

- Mean 3x3
- Median 3x3



219	216	218
207	0	184
174	195	184

Mean 3x3: All the weights are equal to 1:

$$219+216+218+207+0+184+174+195+184 \Rightarrow 177$$

Median 3x3: Sorting + Median value

$$0 < 174 < 184 < 184 < 195 < 207 < 216 < 218 < 219 \Rightarrow 195$$



Denoising - Filters

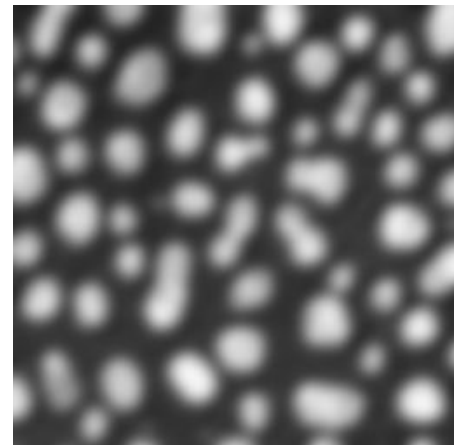
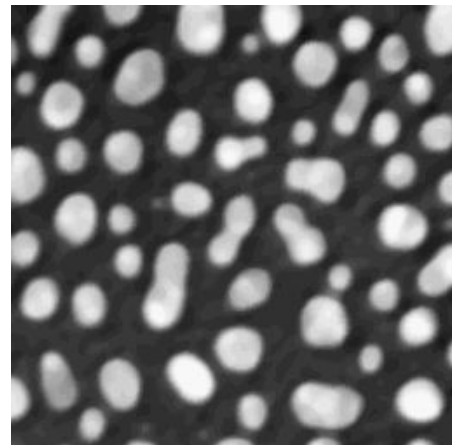
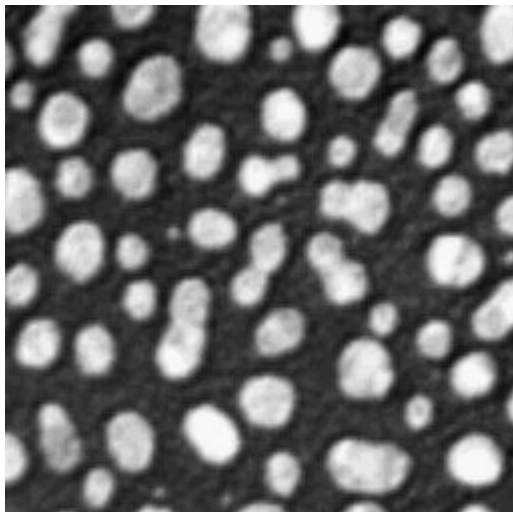
Principle - Noise

Linear Filters:

- Mean
- Weighted Mean

Non-linear Filters:

- Median ***



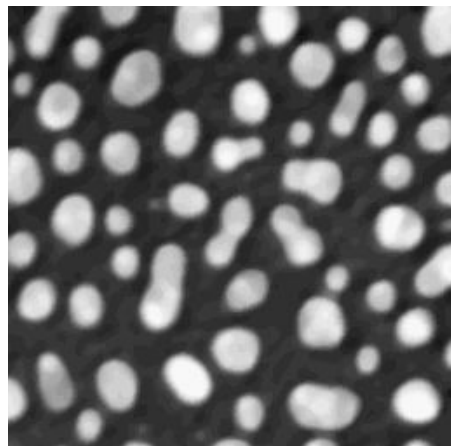


Segmentation

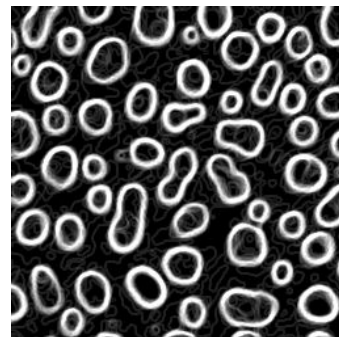
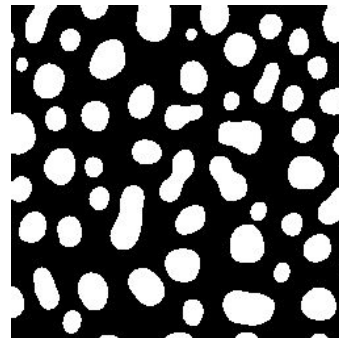
Separating ROI from background

Methods

- Threshold
- Edges
- Clustering



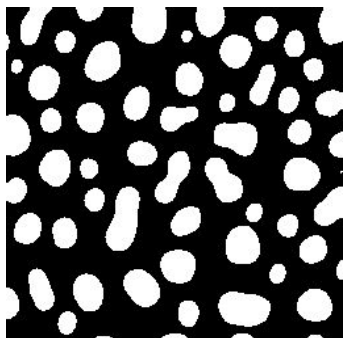
Binary (1bit) Image





Analyze

Measurements



Results										
File	Edit	Font	Results							
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	1	338.500	18.500	1.000	1.414	338	18	135	1	1.000
2	113	329.969	36.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000

Analyze - Measurements

Principle

- Euclidian Distance :
 $\sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2}$
- Pixel connectivity
- Distance north-south-east-west
(city-block or Manhattan).
 $|x_0 - x_1| + |y_0 - y_1|$

0 1 2 3 4 5 6 7 8

9 0 1 2 3 4 5 6 7 8 9 Learning Step with a labelled dataset (measurements/features + labels).

2. Prediction Step with an unknown dataset (measurements).

8

7

6

5

4

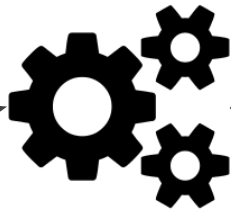
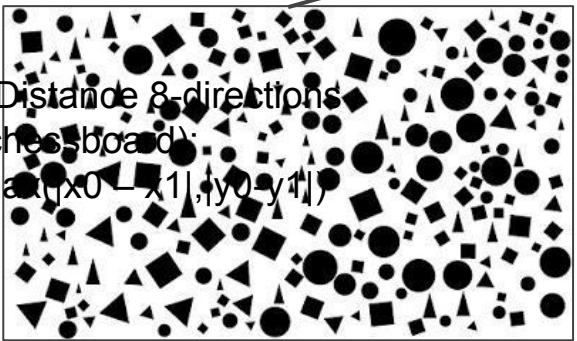
3

2

1

0

- Distance 8-directions
(chessboard):
 $\max(|x_0 - x_1|, |y_0 - y_1|)$



Results						
File Edit Font Results						
	Area	Circ.	AR	Round	Solidity	
224	43	0.671	1.012	0.988	0.827	
225	63	0.983	1.056	0.947	0.913	
226	36	0.832	1.040	0.962	0.847	
227	358	0.968	1.015	0.986	0.957	
228	24	0.702	1.152	0.868	0.828	
229	92	0.897	1.019	0.981	0.958	
230	86	0.980	1.056	0.947	0.925	
231	34	0.654	1.015	0.985	0.773	
232	85	0.604	1.023	0.977	0.821	
233	52	1.000	1.022	0.979	0.920	
234	98	0.801	1.072	0.933	0.875	
235	126	0.948	1.032	0.969	0.913	
236	20	0.717	1.138	0.879	0.769	
237	20	0.717	1.057	0.946	0.800	
238	33	0.810	1.104	0.906	0.776	
239	64	0.998	1.034	0.968	0.921	

Analyze - Measurements



Distance

- Euclidean Distance :

$$\sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2}$$

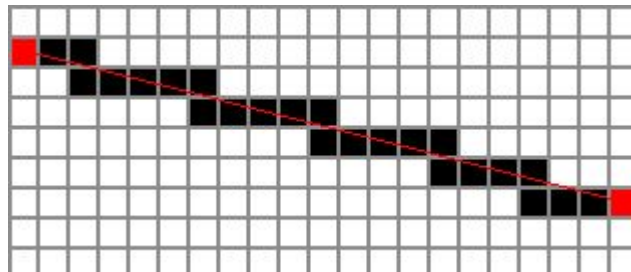
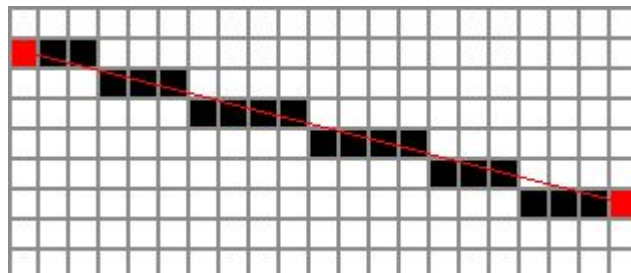
Pixel connectivity

- Distance north-south-east-west (city-block or Manhattan):

$$|x_0 - x_1| + |y_0 - y_1|$$

- Distance 8-directions (chessboard):

$$\max(|x_0 - x_1|, |y_0 - y_1|)$$



Analyze - Measurements

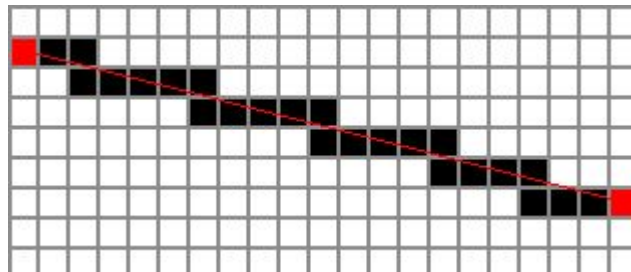
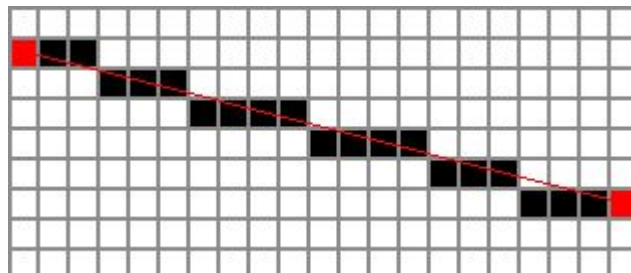


Distance

Pixel connectivity

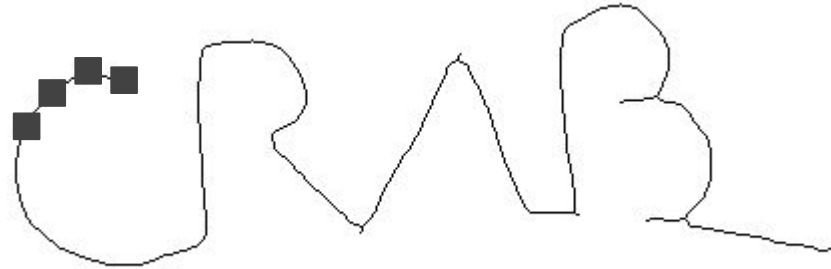
- Distance 4-pixel connectivity: factor = 1.273
- Distance 8-pixel connectivity: factor = 0.9
- Factor = NSEW (1.0) + Diagonals ($\sqrt{2}$)

A(0,0) \Leftrightarrow B(20,5)



Analyze - Measurements

Object Length



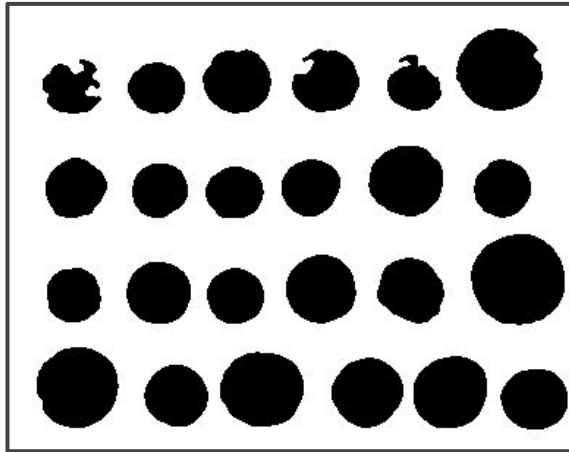
$$\text{Length} = \text{Pixel_Number} / \text{connectivity_factor}$$

Analyze - Measurements



Counting

Segmented Image



Convolution

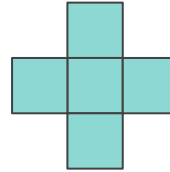


Table K	
X	Y
X _n	Y _n
X _i	Y _i
X _j	Y _j
X _w	Y _w

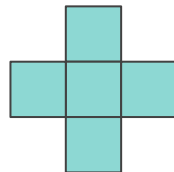
Table L	
X _i	Y _i
X _j	Y _j

Analyze - Measurements



Counting

Convolution



①

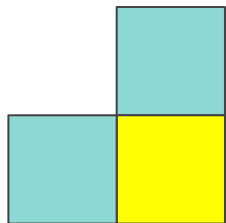


Table K	
X _m	Y _m

②

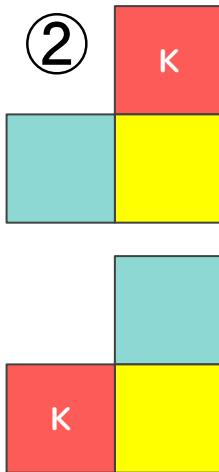


Table K	
X	Y
X _n	Y _n

③

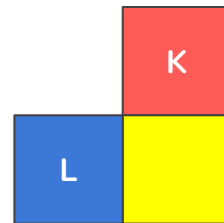


Table K	
X	Y
X _n	Y _n

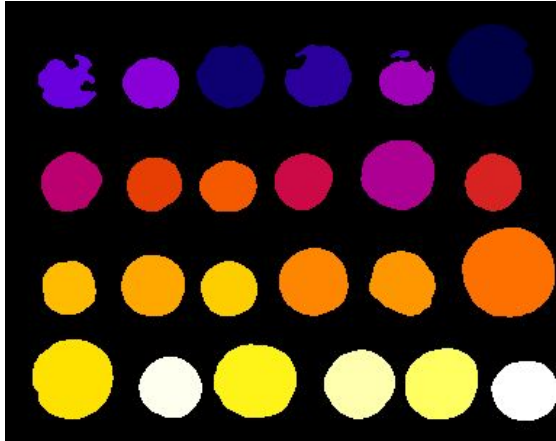
Table L	
X _i	Y _i
X _j	Y _j

Table K	
X	Y
X _n	Y _n
X _i	Y _i
X _j	Y _j
X _w	Y _w

Analyze - Measurements



Counting

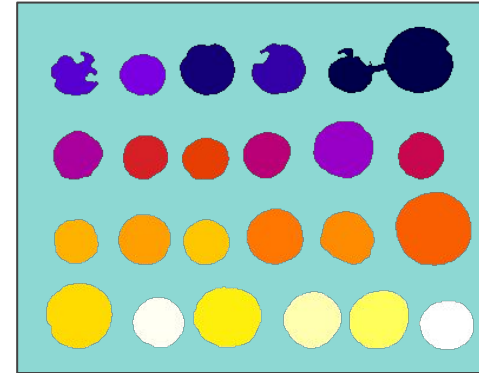


◀ 25 Objects

Table K	
X	Y
Xn	Yn
Xi	Yi
Xj	Yj
Xw	Yw

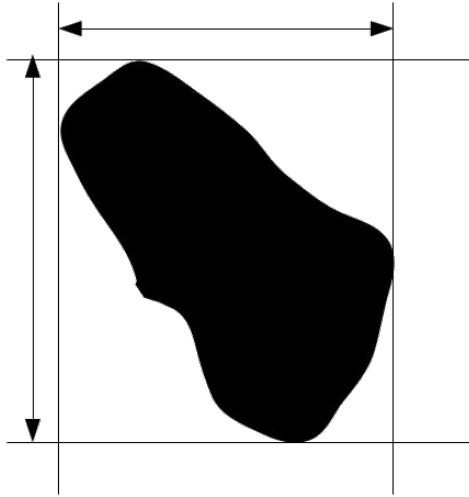
Table L	
Xi	Yi
Xj	Yj

23 Objects ▶

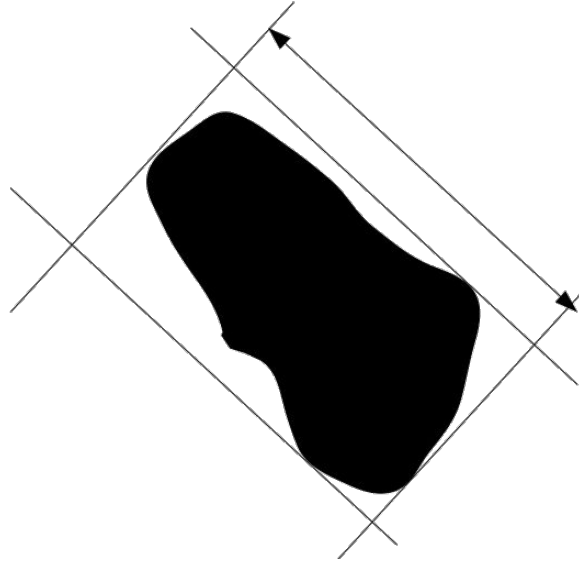


Analyze - Measurements

Bounding Box - Size



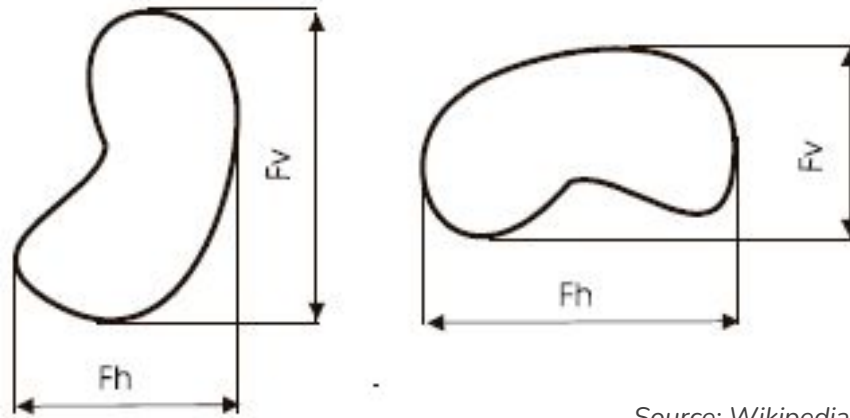
Axis-Aligned Bounding Box



Oriented Bounding Box

Analyze - Measurements

Size - Feret's Diameters



Source: Wikipedia

Size: Max. Feret Diameter x Min. Feret Diameter

Analyze - Measurements

Size - Ellipse

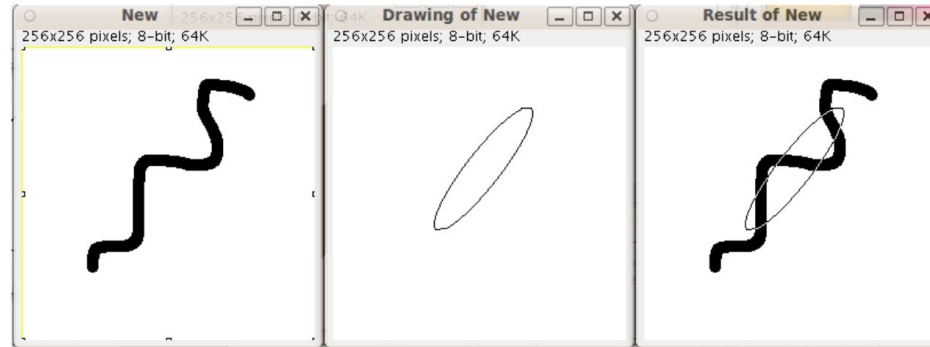
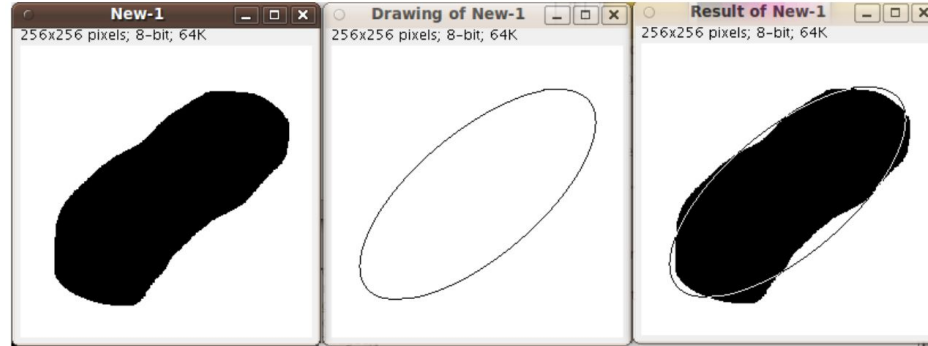
Ellipse

→ Major Axis

→ Minor Axis

→ Angle

→ Centroid



Analyze - Measurements



Shape Descriptors

Circularity = $(4 \cdot \text{Area}) / \sqrt{(\text{Perimeter})}$

Roundness = $4 \cdot \text{area} / (\text{Max_diameter} \cdot 2)$

Shape Factor = $\text{Perim} \cdot 2 / (4 \cdot \text{area})$

Aspect ratio = $\text{Max_diameter} / \text{Min_diameter}$

Compacity = $\sqrt{(4 / \text{Area})} / \text{Max_diameter}$

Analyze - Measurements



Shape Descriptors

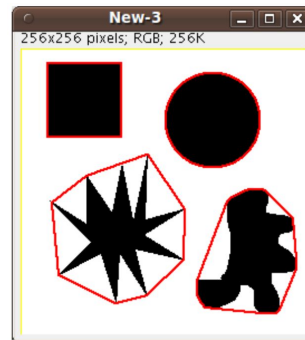
Circularity: $4\pi \cdot \text{area} / \text{sqrt}(\text{perimeter})$

- A value of 1.0 indicates a perfect circle.
- As the value approaches 0.0, it indicates an increasingly elongated shape.
- Values may not be valid for very small particles.

Aspect ratio: major axis/minor axis.

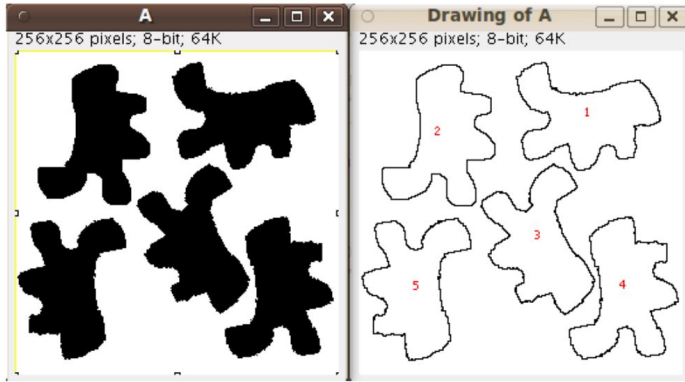
Roundness: $4 \cdot \text{area} / (\pi \cdot \text{sqrt}(\text{major axis}))$

Solidity: area/convex area.



Analyze - Measurements

Shape Descriptors

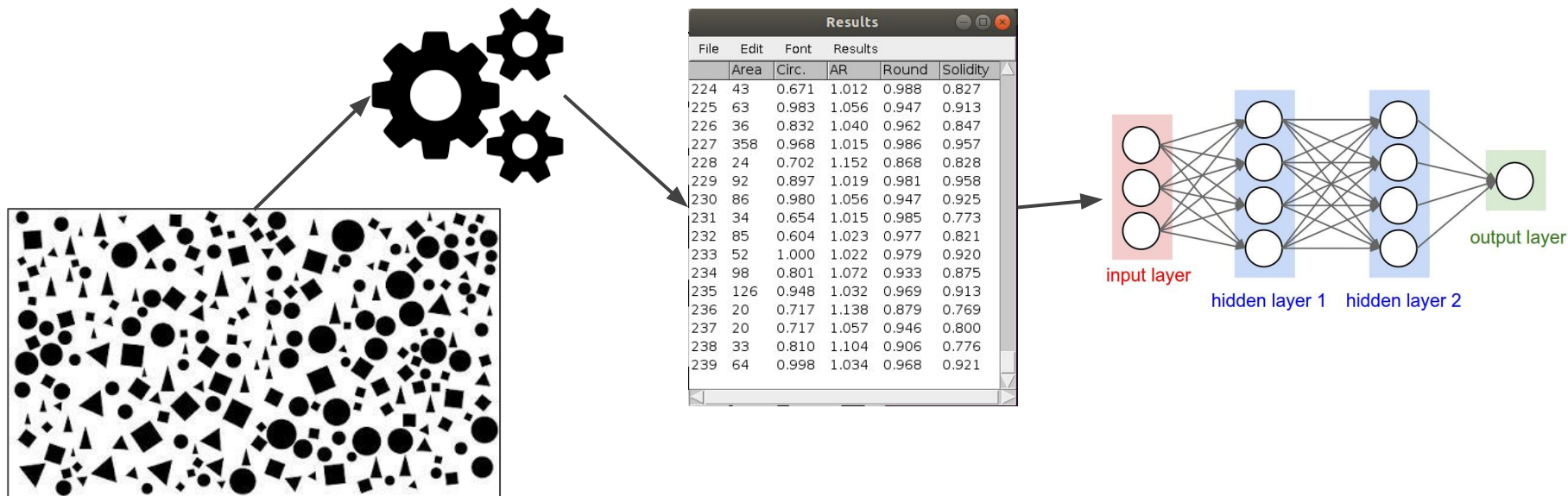


#	Label	Area	Circ.	AR	Round	Solidity
1	A	5312	0.335	1.604	0.624	0.701
2	A	5327	0.369	1.605	0.623	0.706
3	A	5304	0.328	1.603	0.624	0.699
4	A	5325	0.314	1.604	0.624	0.703
5	A	5322	0.325	1.601	0.625	0.702

Analyze - Machine Learning

Principle

1. Learning Step with a labelled dataset (measurements/features + labels).
2. Prediction Step with an unknown dataset (measurements).





Digital Image

Pipeline

Image Enhancement

- Brightness/contrast
- Non Uniform Illumination
- Noise Removal

Segmentation

- Threshold
- Math. Morphology



Results										
File Edit Font Results										
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	338.500	18.500	1.000	1.414	338	18	135	1	1.000	
2	113	329.969	35.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000

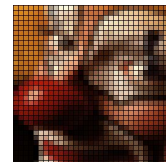
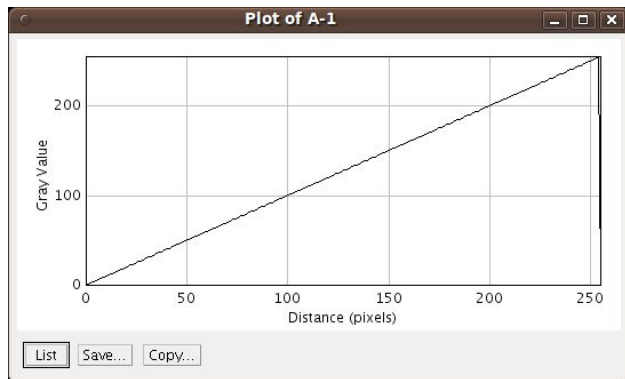




Image Enhancement

Principle - Brightness / Contrast



Transfer Function: $Y = a \cdot x + b$

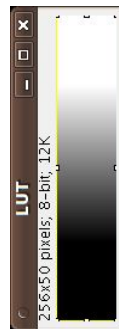
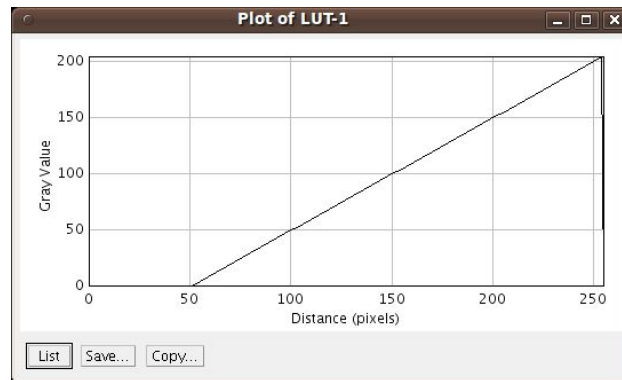
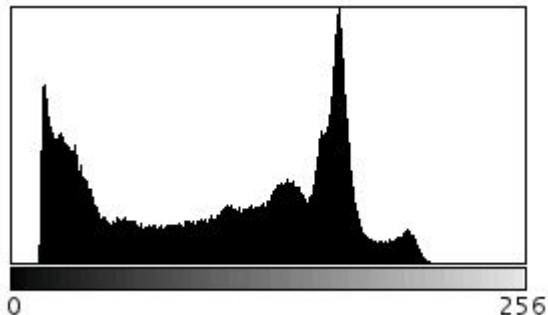


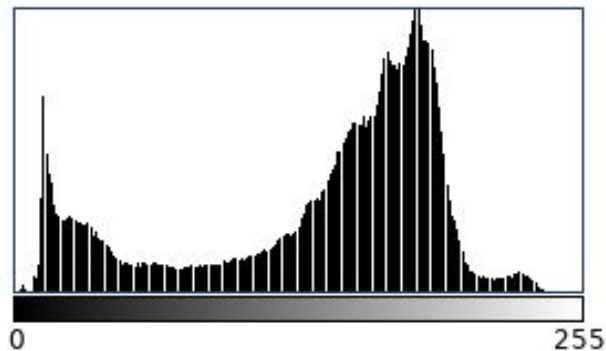


Image Enhancement

Principle - Normalization



$$v' = (v - \min) / (\max - \min)$$



N: 414720
Mean: 137.016
StdDev: 57.807
Value: 112

Min: 0
Max: 255
Mode: 180 (7480)
Count: 1131

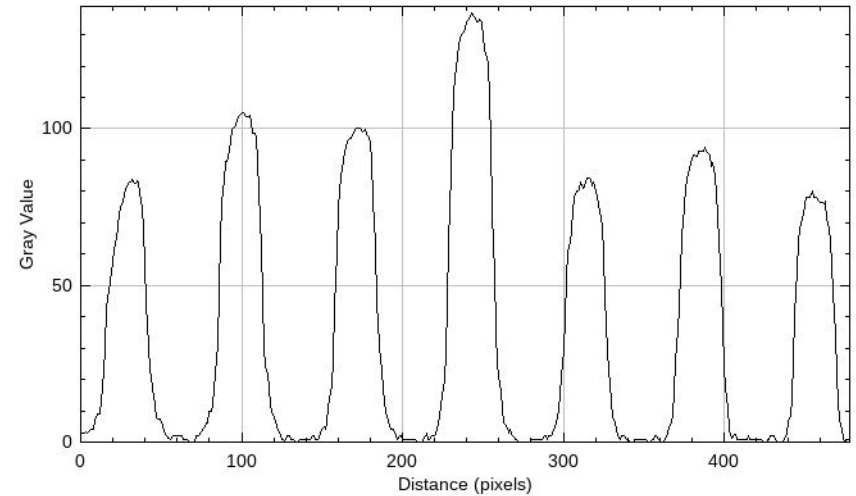
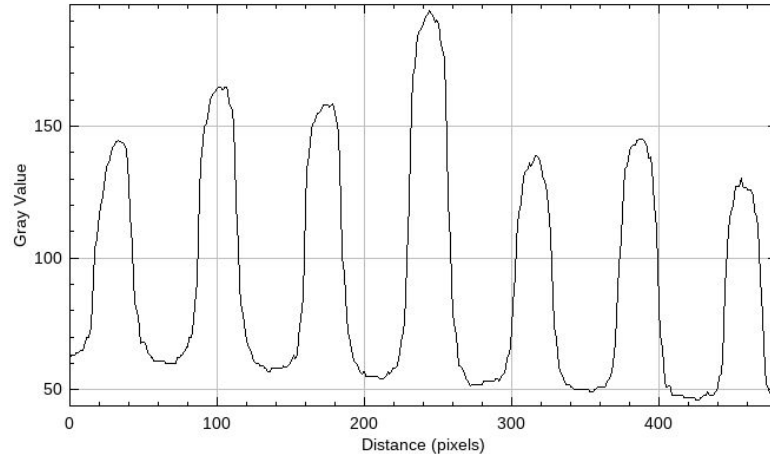


Image Enhancement

Non Uniform Illumination - Subtract Background

Removing the Baseline

- Polynomial Functions
- Rolling Ball

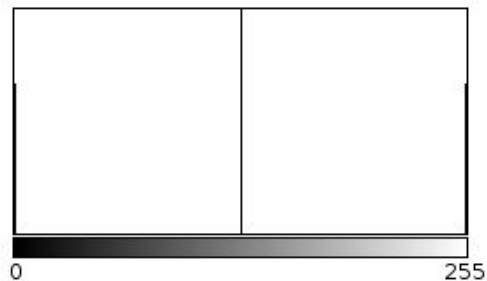
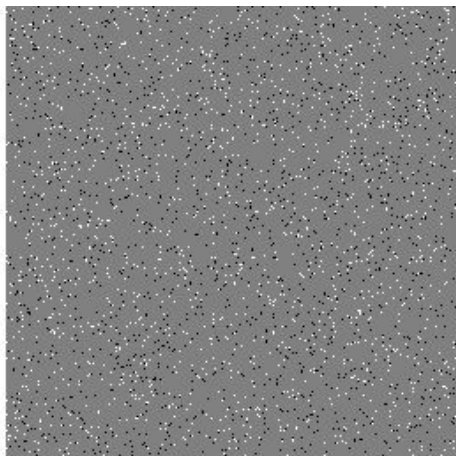




Denoising - Filters

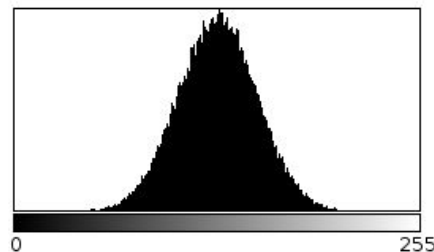
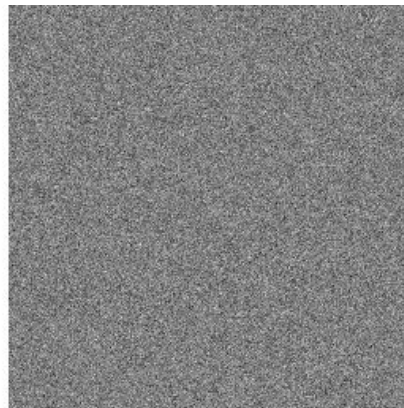
Principle - Noise

Impulse Noise (Salt and Pepper)



N: 65536	Min: 0
Mean: 127.974	Max: 255
StdDev: 28.161	Mode: 128 (62339)
Value: 167	Count: 0

Gaussian Noise



N: 65536	Min: 26
Mean: 127.915	Max: 232
StdDev: 24.918	Mode: 129 (1092)
Value: 176	Count: 171



Denoising - Filters

Principle - Noise

Denoise Filters:

- Mean 3x3
- Median 3x3

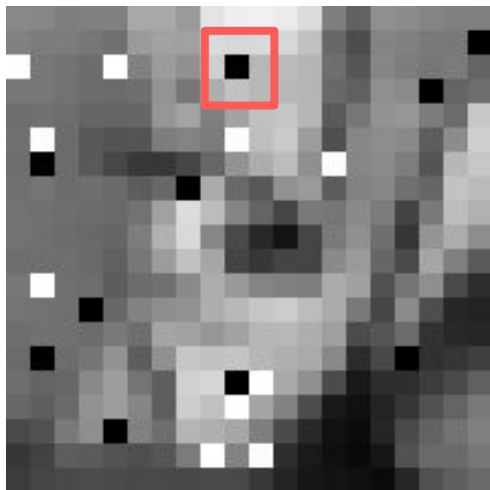
219	216	218
207	0	184
174	195	184

Mean 3x3: All the weights are equal to 1:

$$219+216+218+207+0+184+174+195+184 \Rightarrow 177$$

Median 3x3: Sorting + Median value

$$0 < 174 < 184 < 184 < 195 < 207 < 216 < 218 < 219 \Rightarrow 195$$





Denoising - Filters

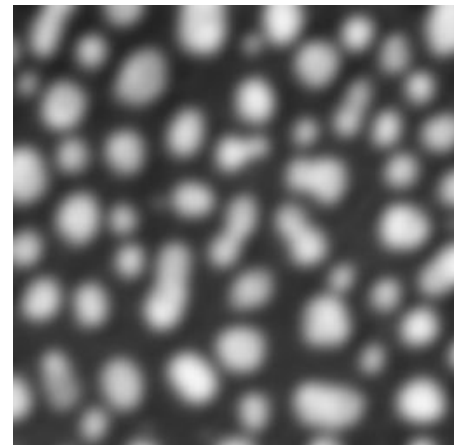
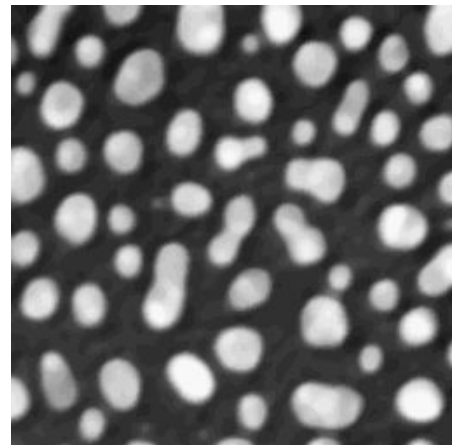
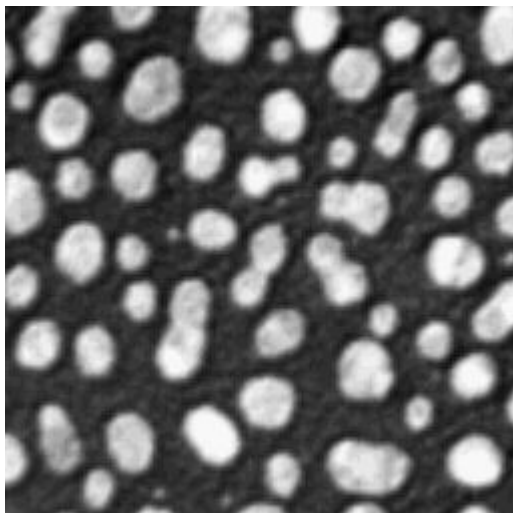
Principle - Noise

Linear Filters:

- Mean
- Weighted Mean

Non-linear Filters:

- Median ***



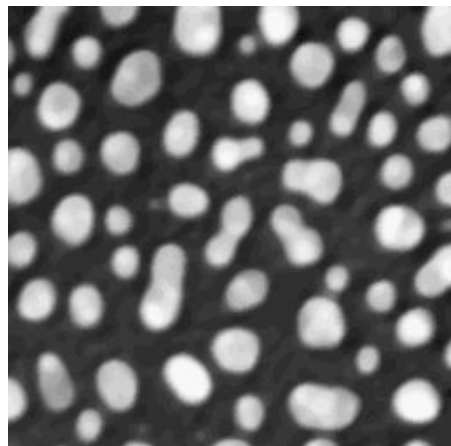


Segmentation

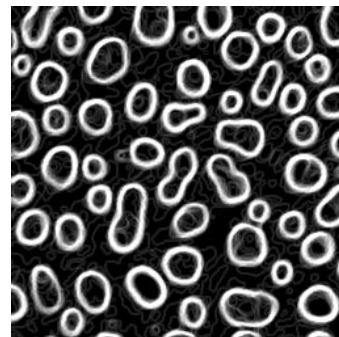
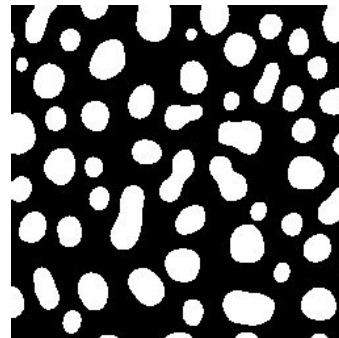
Separating ROI from background

Methods

- Threshold
- Edges
- Clustering



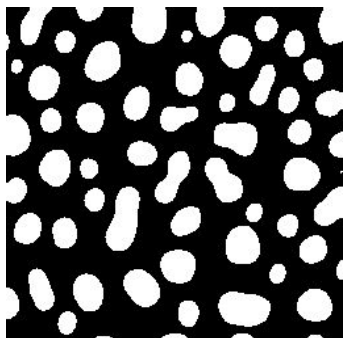
Binary (1bit) Image





Analyze

Measurements



Results										
File	Edit	Font	Results							
	Area	XM	YM	Circ.	Feret	FeretX	FeretY	FeretAngle	MinFeret	AR
1	1	338.500	18.500	1.000	1.414	338	18	135	1	1.000
2	113	329.969	36.969	0.112	41.485	324	60	74.624	8.995	6.254
3	2	325.500	22.000	1.000	2.236	325	21	116.565	1.000	2.000
4	51	357.520	33.578	0.123	30.529	346	21	121.608	7.203	5.210
5	67	321.739	35.828	0.095	21.954	314	43	59.931	12.000	2.342
6	2	334.500	25.000	1.000	2.236	334	24	116.565	1.000	2.000
7	1	345.500	27.500	1.000	1.414	345	27	135.000	1.000	1.000
8	2	348.000	28.000	0.785	2.828	347	29	45.000	1.414	2.646
9	7	335.357	32.357	0.621	4.472	335	30	116.565	3.000	1.697
10	2	348.000	30.500	1.000	2.236	347	30	153.435	1.000	2.000
11	4	315.000	32.000	1.000	2.828	314	31	135.000	2.000	1.000
12	1	318.500	31.500	1.000	1.414	318	31	135.000	1.000	1.000

Analyze - Measurements

Principle

- Euclidian Distance :
 $\sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2}$
- Pixel connectivity
- Distance north-south-east-west
(city-block or Manhattan).
 $|x_0 - x_1| + |y_0 - y_1|$

0 1 2 3 4 5 6 7 8

9 0 1 2 3 4 5 6 7 8 9 Learning Step with a labelled dataset (measurements/features + labels).

2. Prediction Step with an unknown dataset (measurements).

8

7

6

5

4

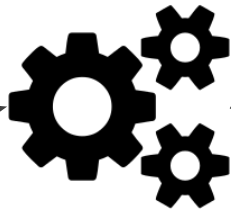
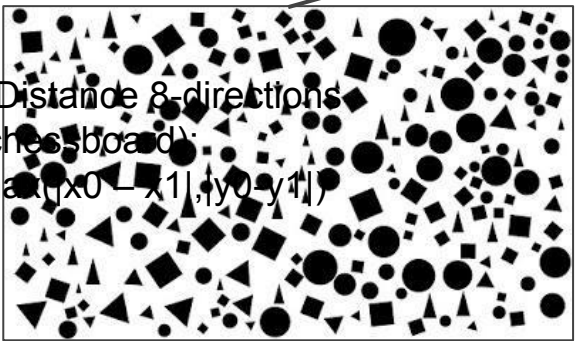
3

2

1

0

- Distance 8-directions
(chessboard):
 $\max(|x_0 - x_1|, |y_0 - y_1|)$



Results						
File Edit Font Results						
	Area	Circ.	AR	Round	Solidity	
224	43	0.671	1.012	0.988	0.827	
225	63	0.983	1.056	0.947	0.913	
226	36	0.832	1.040	0.962	0.847	
227	358	0.968	1.015	0.986	0.957	
228	24	0.702	1.152	0.868	0.828	
229	92	0.897	1.019	0.981	0.958	
230	86	0.980	1.056	0.947	0.925	
231	34	0.654	1.015	0.985	0.773	
232	85	0.604	1.023	0.977	0.821	
233	52	1.000	1.022	0.979	0.920	
234	98	0.801	1.072	0.933	0.875	
235	126	0.948	1.032	0.969	0.913	
236	20	0.717	1.138	0.879	0.769	
237	20	0.717	1.057	0.946	0.800	
238	33	0.810	1.104	0.906	0.776	
239	64	0.998	1.034	0.968	0.921	

Analyze - Measurements



Distance

- Euclidean Distance :

$$\sqrt{(x_0 - x_1)^2 + (y_0 - y_1)^2}$$

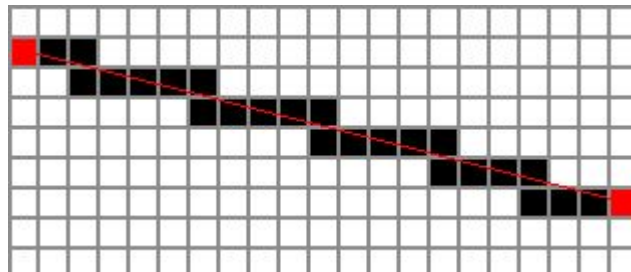
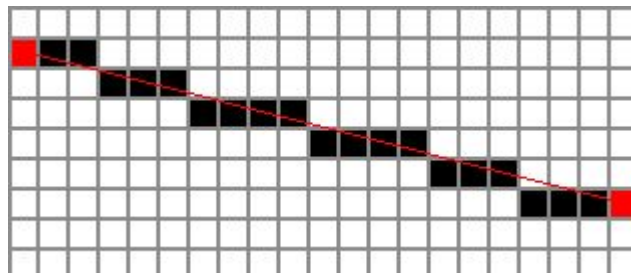
Pixel connectivity

- Distance north-south-east-west (city-block or Manhattan):

$$|x_0 - x_1| + |y_0 - y_1|$$

- Distance 8-directions (chessboard):

$$\max(|x_0 - x_1|, |y_0 - y_1|)$$



Analyze - Measurements

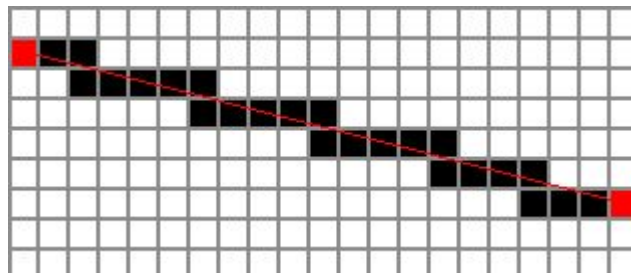
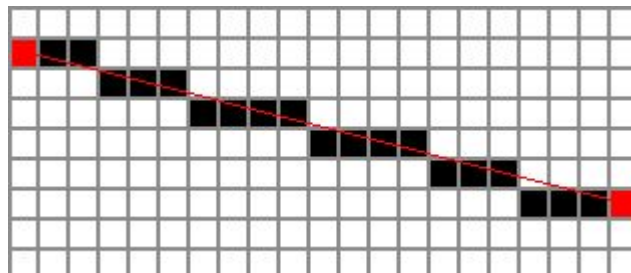


Distance

Pixel connectivity

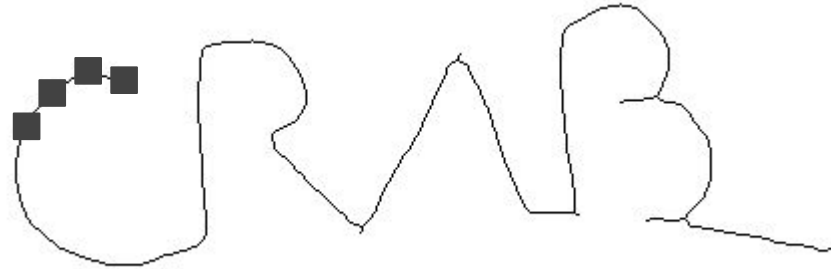
- Distance 4-pixel connectivity: factor = 1.273
- Distance 8-pixel connectivity: factor = 0.9
- Factor = NSEW (1.0) + Diagonals ($\sqrt{2}$)

A(0,0) \Leftrightarrow B(20,5)



Analyze - Measurements

Object Length



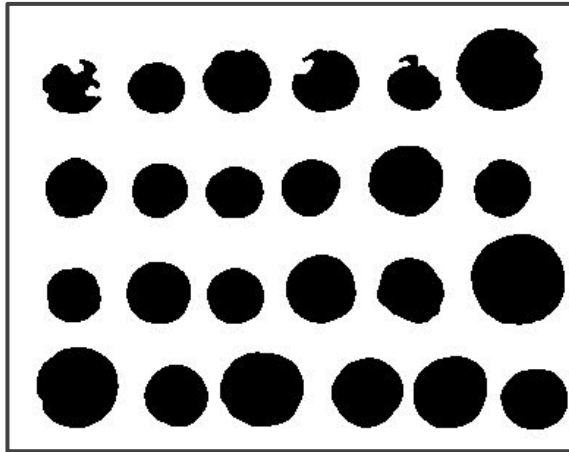
$$\text{Length} = \text{Pixel_Number} / \text{connectivity_factor}$$

Analyze - Measurements



Counting

Segmented Image



Convolution

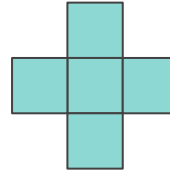


Table K	
X	Y
X _n	Y _n
X _i	Y _i
X _j	Y _j
X _w	Y _w

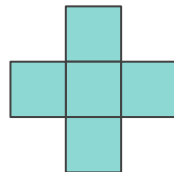
Table L	
X _i	Y _i
X _j	Y _j

Analyze - Measurements



Counting

Convolution



①

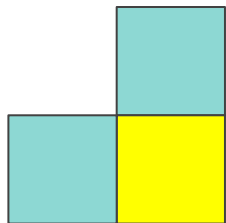


Table K	
X _m	Y _m

②

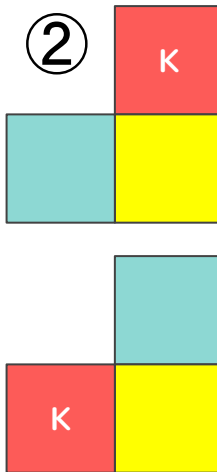


Table K	
X	Y
X _n	Y _n

③

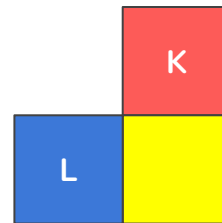


Table K	
X	Y
X _n	Y _n

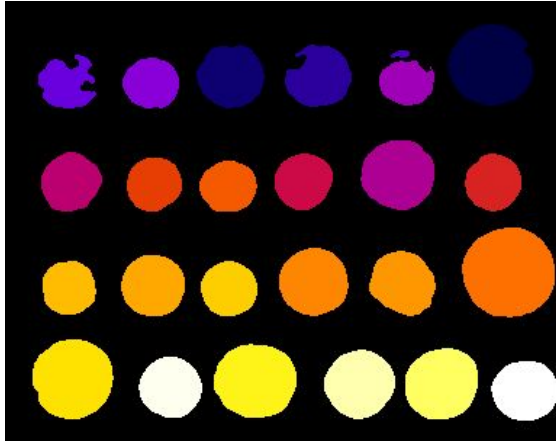
Table L	
X _i	Y _i
X _j	Y _j

Table K	
X	Y
X _n	Y _n
X _i	Y _i
X _j	Y _j
X _w	Y _w

Analyze - Measurements



Counting

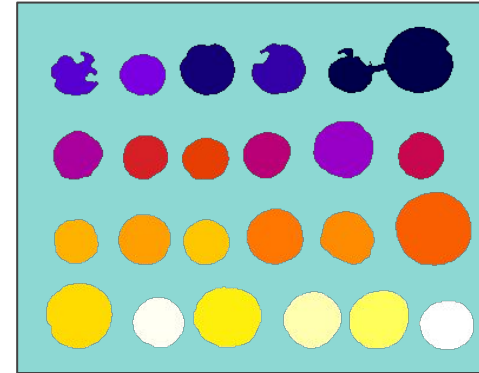


◀ 25 Objects

Table K	
X	Y
X _n	Y _n
X _i	Y _i
X _j	Y _j
X _w	Y _w

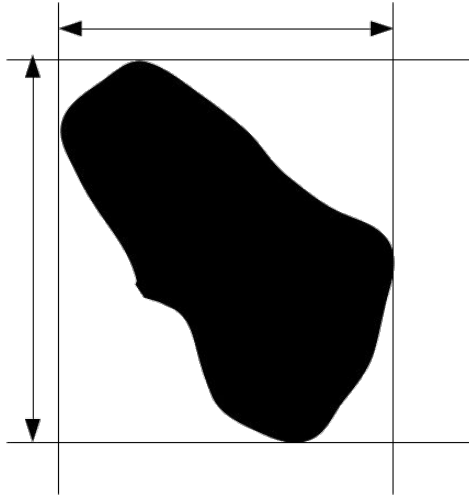
Table L	
X _i	Y _i
X _j	Y _j

23 Objects ▶

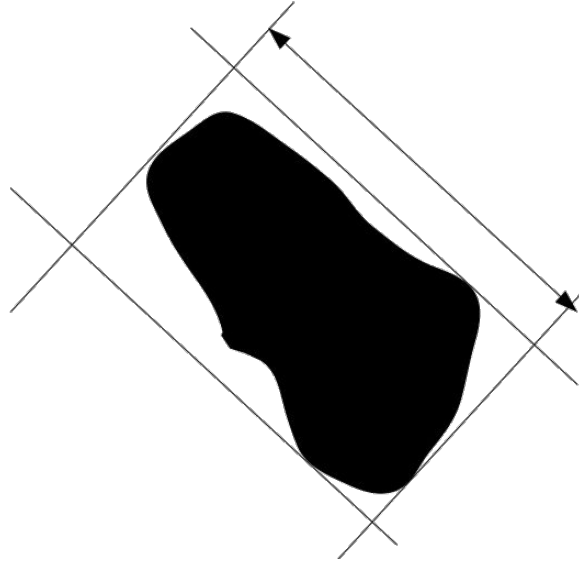


Analyze - Measurements

Bounding Box - Size



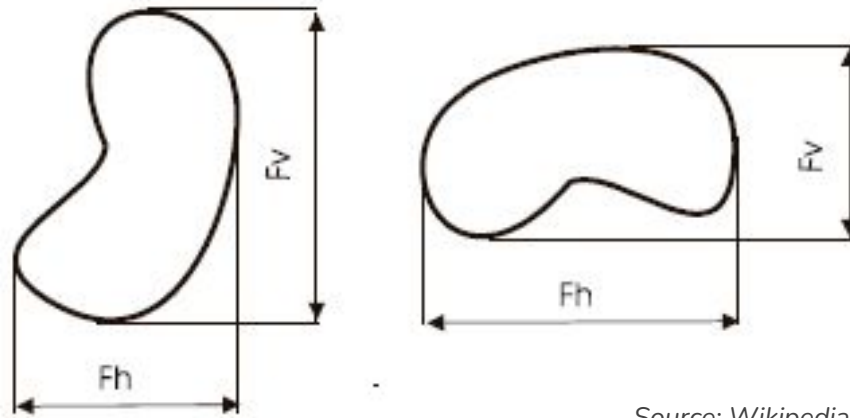
Axis-Aligned Bounding Box



Oriented Bounding Box

Analyze - Measurements

Size - Feret's Diameters



Source: Wikipedia

Size: Max. Feret Diameter x Min. Feret Diameter

Analyze - Measurements

Size - Ellipse

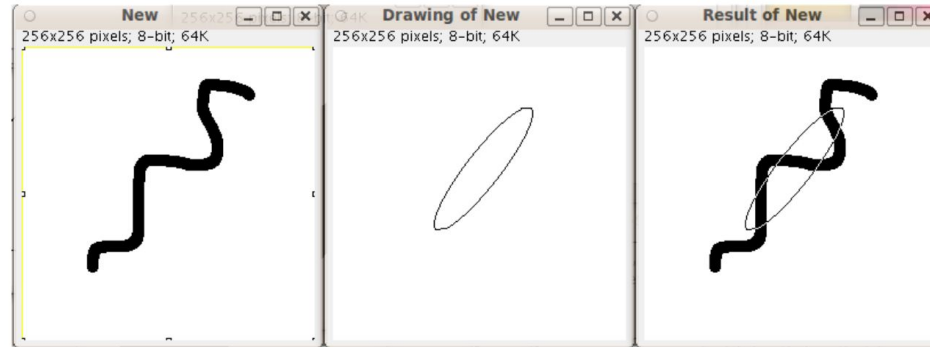
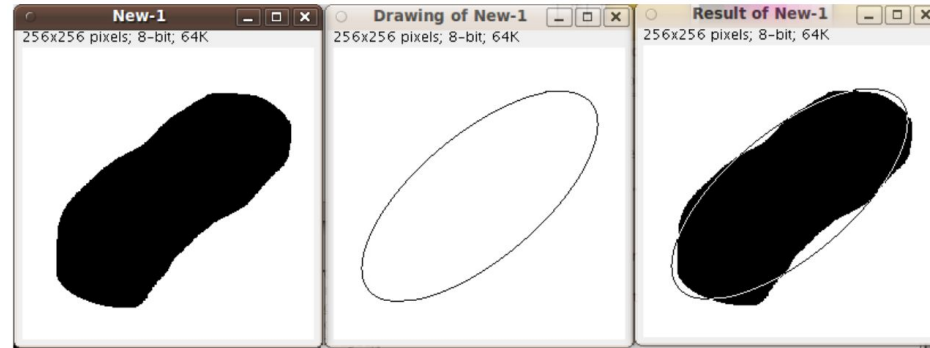
Ellipse

→ Major Axis

→ Minor Axis

→ Angle

→ Centroid



Analyze - Measurements



Shape Descriptors

Circularity = $(4 \cdot \text{Area}) / \sqrt{(\text{Perimeter})}$

Roundness = $4 \cdot \text{area} / (\text{Max_diameter} \cdot 2)$

Shape Factor = $\text{Perim} \cdot 2 / (4 \cdot \text{area})$

Aspect ratio = $\text{Max_diameter} / \text{Min_diameter}$

Compacity = $\sqrt{(4 / \text{Area}) / \text{Max_diameter}}$

Analyze - Measurements



Shape Descriptors

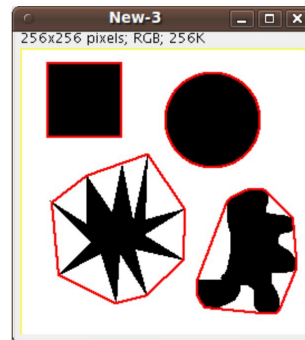
Circularity: $4\pi \cdot \text{area} / \text{sqrt}(\text{perimeter})$

- A value of 1.0 indicates a perfect circle.
- As the value approaches 0.0, it indicates an increasingly elongated shape.
- Values may not be valid for very small particles.

Aspect ratio: major axis/minor axis.

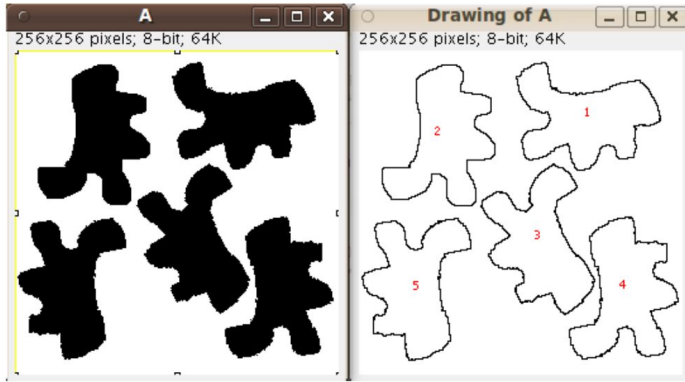
Roundness: $4 \cdot \text{area} / (\pi \cdot \text{sqrt}(\text{major axis}))$

Solidity: area/convex area.



Analyze - Measurements

Shape Descriptors

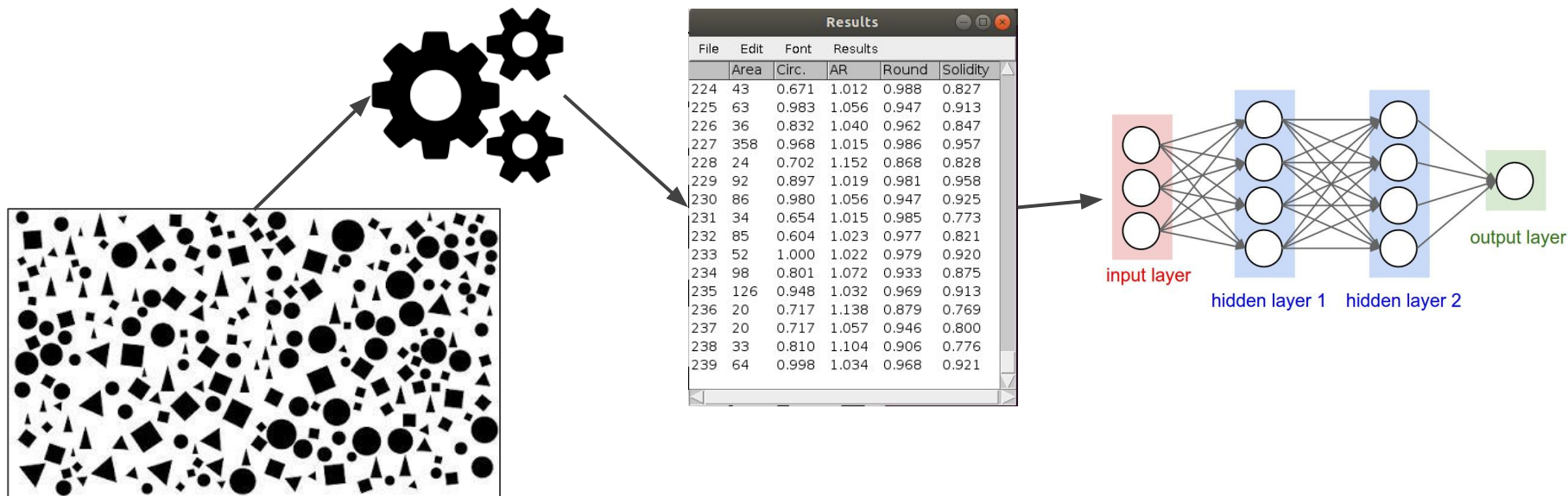


#	Label	Area	Circ.	AR	Round	Solidity
1	A	5312	0.335	1.604	0.624	0.701
2	A	5327	0.369	1.605	0.623	0.706
3	A	5304	0.328	1.603	0.624	0.699
4	A	5325	0.314	1.604	0.624	0.703
5	A	5322	0.325	1.601	0.625	0.702

Analyze - Machine Learning

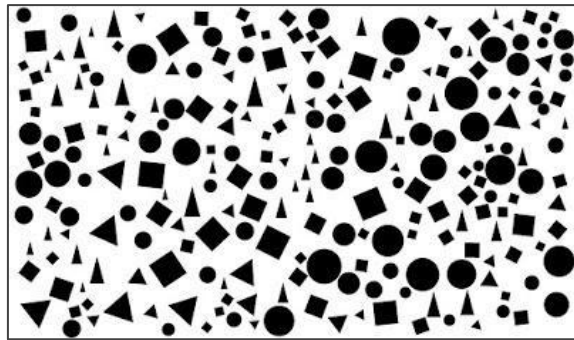
Principle

1. Learning Step with a labelled dataset (measurements/features + labels).
2. Prediction Step with an unknown dataset (measurements).



Analyze - Machine Learning

Deep Learning - End to End Approach



Convolutional Neural Network (CNN)

