

Representation of information

UNIT 1: USE OF MICROCOMPUTING SYSTEMS. SECOND PART



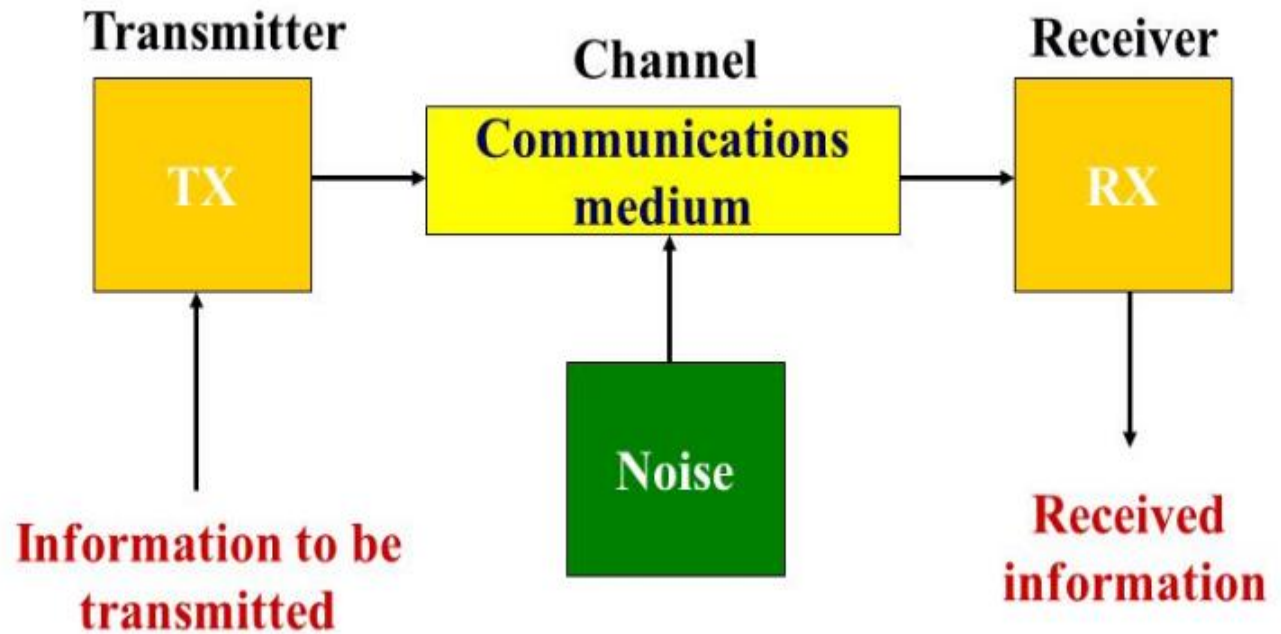
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1. Introduction

- Computers basically get input data, transform this data and produce results.
- The purpose of computers is to automate work.
- Computer components understand neither letters nor numbers, but electric current and other physical magnitudes.
- We need codification systems, which convert letters and numbers to something understandable for computers.
- The OS, together with the hardware components, converts the information into electricity and vice versa.

1. Introduction

- Communication system:
 - Transmitter
 - Receiver
 - Channel
- Unidirectional or bidirectional



2. Encoding information

- Information broadcasting
 - Alphanumeric characters (a...z, A..Z, 0....9)
 - Sounds
 - Videos
 - Graphs and pictures

Each type of information works different and has its own way of representing data.

The existence of information requires a common code between transmitter and receiver.

2. Encoding information

- All the information in a computer is stored with two symbols: 1 and 0.
- These two numbers represent two electrical states, which make possible to build reliable internal computer circuits.
- It is necessary a clear correspondence between human symbols (characters, numbers, signs, etc.) and binary symbols (1 and 0),
- This process is called encoding, while decoding is the opposite one.

3. Numeral systems

- A numeral system (also known as system of numeration or number system) is a mathematical notation for representing numbers of a given set, using digits or other symbols, according to some rules.
- The common system uses 10 digits, but we have different bases depending on how many digits are used in a system of numeration to represent numbers
 - **Decimal system (base 10):** 0,1,2,3,4,5,6,7,8,9.
 - **Binary system (base 2):** 0,1
 - **Octal system (base 8):** 0,1,2,3,4,5,6,7
 - **Hexadecimal system (base 16):** 0,1,2,3,4,5,6,7,8,9,A,B,C,D,E,F

3. Numeral systems

- The most commonly used systems today are positional
- Value of numbers is determined by **weight** and **position** of each digit.
- The value of each digit position is the value of its digit, multiplied by a power of the base.
- In general, if b is the base, one writes a number in the numeral system of base b by expressing it in the form $a_n b^n + a_{n-1} b^{n-1} + a_{n-2} b^{n-2} + \dots + a_0 b^0$ and writing the enumerated digits $a_n a_{n-1} a_{n-2} \dots a_0$ in descending order.

3. Numeral systems

- Any numeral system can be summarized by the following relationship:

$$N = \sum b_i q^i$$

where: N is a real positive number
 b is the digit
 q is the base value
 and integer (i) can be positive, negative or zero

- So, in positional base-10 notation: $458 \text{ (base 10)} = 4 \cdot 10^2 + 5 \cdot 10^1 + 8 \cdot 10^0$
- And, in positional base-2 notation: $1110000 \text{ (base 2)} = 1 \cdot 2^6 + 1 \cdot 2^5 + 1 \cdot 2^4 + 0 \cdot 2^3 + 0 \cdot 2^2 + 0 \cdot 2^1 + 0 \cdot 2^0$

3.1. Binary system

- It is composed of two symbols: 0,1
- Base 2
- Digital systems are based on binary numbers.

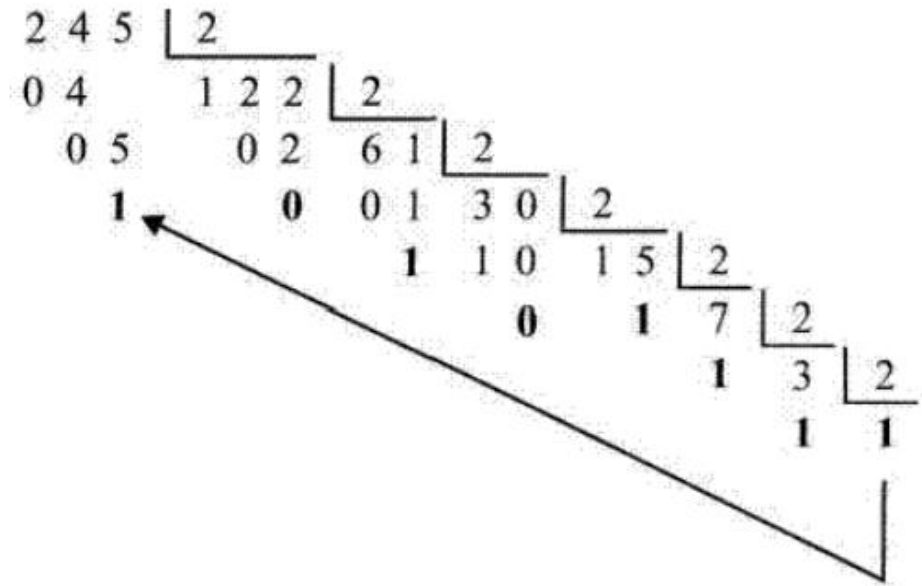
0	0 volts	OFF	NO
1	5 volts	ON	YES

- Ex: $1110000 \text{ (base 2)} = 1 \cdot 2^6 + 1 \cdot 2^5 + 1 \cdot 2^4 + 0 \cdot 2^3 + 0 \cdot 2^2 + 0 \cdot 2^1 + 0 \cdot 2^0$
- To convert a binary number to decimal, just add the final value of each power of two.
According to the example: $1110000 \text{ (base 2)} = 112 \text{ (base 10)}$

3.1. Binary system

- **To convert a decimal number to binary:**
 - Divide the input decimal number by 2.
 - Repeat this process till quotient becomes zero.
 - Equivalent binary number will be the remainders in above process in reverse order.

- Example: $N = 245$



- Result = 11110101

3.1. Binary system

- Having n bits, we can represent 2^n values
- Basic powers of 2:
 - $2^1 = 2$... Having 1 bit we represent 2 numbers
 - $2^2 = 4$... Having 2 bits we represent 4 numbers
 - $2^3 = 8$... Having 3 bits we represent 8 numbers
 - $2^4 = 16$... Having 4 bits we represent 16 numbers
- And so on...

3.1. Binary system

- Exercises:

1. Convert from decimal to binary

- 517

- 425

- 315

2. Convert from binary to decimal

- 1011

- 10100110

- 11011

3.2. Conversion between numeral systems

- We have studied how to transform a binary number into decimal and vice versa.
- To convert a binary number to decimal, the equivalent value is equal to the sum of binary digits (d_n) times their power of 2 (2^n). To convert from any numeral system to decimal, we can use the same method, replacing base-2 with the corresponding base.
- To convert a decimal number to binary, we divided and multiplied by 2. To convert from a decimal number to any other numeral system, we can divide and multiply in the same way, but using the corresponding base.
- So...

3.2. Conversion between numeral systems

- We can set a general rule to convert a base-a number to a base-b number:
 - Convert the original number to a decimal number (base 10).
 - Convert the decimal number obtained to the new base number.
- $N_A \Rightarrow N_{10}$
- $N_{10} \Rightarrow N_B$

3.2. Conversion between numeral systems

- Exercises:
 1. Convert 5270_{10} to base 8
 2. Convert 543_{10} to base 8.
 3. Convert 3456_8 to binary.
 4. Convert 243_{10} to base 5
 5. Convert 531_6 to base 10

3.3. Octal and hexadecimal numbers

- Binary system becomes complicated because of the amount of digits used to represent numbers.
- Computers sometimes use base 8 and 16.
- This way, it is easier to convert from and to 2, 8 and 16 bases.
- Octal uses 8 symbols (0..7)
- Hexadecimal uses 16 symbols (0..9, A..F)
- **Let's take a look on the conversion table in the next slide.**

3.3. Octal and hexadecimal numbers

Dec	Hex	Oct	Bin
0	0	000	0000
1	1	001	0001
2	2	002	0010
3	3	003	0011
4	4	004	0100
5	5	005	0101
6	6	006	0110
7	7	007	0111
8	8	010	1000
9	9	011	1001
10	A	012	1010
11	B	013	1011
12	C	014	1100
13	D	015	1101
14	E	016	1110
15	F	017	1111

3.3. Octal and hexadecimal numbers

- There is a shortcut method for conversions between octal and binary and vice versa.

1. Octal to binary

- Convert each octal digit to a 3 digit binary number (the octal digits may be treated as decimal for this conversion), according to the previous table.
- Combine all the resulting binary groups (of 3 digits each) into a single binary number.
- ✓ $351)_8 = \underline{011} \underline{101} \underline{001})_2$ (we can pad zeros on the left)

3.3. Octal and hexadecimal numbers

2. Binary to octal

- Divide the binary digits into groups of three (starting from the right).
- Convert each group of three binary digits to one octal digit.

✓ 010 101 100₂ = 254₈ (if there are less than 3 numbers on the left, we pad with zeros)

3.3. Octal and hexadecimal numbers

- To convert from hexadecimal to binary and vice versa, we use the same method as before, but grouping in four.
- Each four numbers are equivalent to an hexadecimal digit.
 - ✓ $15F_{16} = \underline{0001} \underline{0101} \underline{1111}_2$ (we can pad zeros on the left)
 - ✓ $\underline{0011} \underline{1101}_2 = 3D_{16}$ (if there are less than 4 numbers on the left, we pad with zeros)

3.3. Octal and hexadecimal numbers

- Exercises:
 1. Convert 5270_{10} to octal.
 2. Convert 3456_8 to binary.
 3. Convert 5270_{10} to hexadecimal
 4. Convert 3456_{16} to binary.
 5. Convert 454_8 to hexadecimal.
 6. Convert $1C_{16}$ to octal.

4. Alphanumeric characters

- Computers not only process numbers, but also letters, special symbols or complex types of data such as sound and pictures.
- In computer science, **alphanumeric is a combination of letters and numbers.**
- Each character has a numeric representation, whose binary conversion allows to store data in a “human” format.
- We have different character sets and encodings to represent information.
- ASCII, EBCDIC, UNICODE or UTF-8 are four of the most important ones.

4.1. ASCII

- ASCII is the abbreviated from American Standard Code for Information Interchange
- The original ASCII table is encoded on 7 bits therefore it has 128 characters.
- Nowadays most computers use an **extended ASCII table** (from ISO 8859-1), which is encoded on 8 bits
- Current ASCII can represent 256 characters (including Á, Ä, Æ, é, è and other characters useful for European languages as well as mathematical glyphs and other symbols).

4.1. ASCII (7 bits)

ASCII Code Chart

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	SO	SI
1	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
2		!	"	#	\$	%	&	'	()	*	+	,	-	.	/
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
4	@	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
5	P	Q	R	S	T	U	V	W	X	Y	Z	[\]	^	_
6	`	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o
7	p	q	r	s	t	u	v	w	x	y	z	{		}	~	DEL

4.1. ASCII (8 bits)

128	Ç	144	É	160	á	176	☐	193	⌞	209	ƒ	225	ß	241	±
129	ü	145	æ	161	í	177	☐	194	⌟	210	π	226	Γ	242	≥
130	é	146	Æ	162	ó	178	☐	195	⌠	211	ℓ	227	π	243	≤
131	â	147	ô	163	ú	179		196	—	212	ℓ	228	Σ	244	ƒ
132	ä	148	ö	164	ñ	180	†	197	†	213	ƒ	229	σ	245	∫
133	à	149	ò	165	Ñ	181	‡	198	‡	214	π	230	μ	246	+
134	â	150	û	166	ª	182	‡	199	‡	215	‡	231	τ	247	≈
135	ç	151	ù	167	º	183	¶	200	ℓ	216	‡	232	Φ	248	°
136	ê	152	—	168	¿	184	¶	201	ƒ	217	∫	233	⊖	249	.
137	ë	153	Ö	169	—	185	‡	202	≡	218	Γ	234	Ω	250	.
138	è	154	Ü	170	¬	186		203	ƒ	219	■	235	δ	251	√
139	ï	156	£	171	½	187	¶	204	‡	220	■	236	∞	252	—
140	î	157	¥	172	¼	188	¶	205	=	221	■	237	φ	253	²
141	ì	158	—	173	¡	189	¶	206	‡	222	■	238	ε	254	■
142	Ä	159	ƒ	174	«	190	¶	207	⌞	223	■	239	∩	255	
143	Å	192	ℒ	175	»	191	¶	208	ℓ	224	α	240	≡		

4.2. EBDIC

- **Extended Binary Coded Decimal Interchange Code (EBCDIC)** is an 8-bit character encoding used mainly on IBM mainframe and IBM midrange computer operating systems.
- When moving information between EBCDIC machines and ASCII machines it is quite often necessary to convert the information.
- It is not a straightforward process, as EBCDIC put lowercase letters before uppercase letters and letters before numbers, exactly the opposite of ASCII.
- EBCDIC is used nowadays in modern mainframes only to provide backwards compatibility.

4.2. EBDIC

	0000 0	0001 1	0010 2	0011 3	0100 4	0101 5	0110 6	0111 7	1000 8	1001 9	1010 A	1011 B	1100 C	1101 D	1110 E	1111 F
0000 0	NUL 0	DLE 16	DS 32		SP 64	& 80	- 96		128	144	160	176	{ 192	} 208	\ 224	0 240
0001 1	SOH 1	DCI 17	SOS 33			/ 81			a 129	j 145		161	A 193	J 209		1 241
0010 2	STX 2	DC2 18	FS 34	SYN 50					b 130	k 146	s 162		B 194	K 210	S 226	2 242
0011 3	ETX 3	TM 19							c 131	l 147	t 163		C 195	L 211	T 227	3 243
0100 4	PF 4	RES 20	BYP 36	PN 52					d 132	m 148	u 164		D 196	M 212	U 228	4 244
0101 5	HT 5	NL 21	LF 37	RS 53					e 133	n 149	v 165		E 197	N 213	V 229	5 245
0110 6	LC 6	BS 22	ETB 38	UC 54					f 134	o 150	w 166		F 198	O 214	W 230	6 246
0111 7	DEL 7	IL 23	ESC 39	EOT 55					g 135	p 151	x 167		G 199	P 215	X 231	7 247
1000 8		CAN 24							h 136	q 152	y 168		H 200	Q 216	Y 232	8 248
1001 9	RLF 9	EM 25							i 137	r 153	z 169		I 201	R 217	Z 233	9 249
1010 A	SMM 10	CC 26	SM 42		cent 74	! 90	 106	:								
1011 B	VT 11	CU1 27	CU2 43	CU3 59	.75	\$ 91	, 107	#								
1100 C	FF 12	IFS 28		DC4 60	< 76	* 92	% 108	@								
1101 D	CR 13	IGS 29	ENQ 45	NAK 61	(77) 93	- 109	'								
1110 E	SO 14	IRS 30	ACK 46		+ 78	; 94	> 110	=								
1111 F	SI 15	IUS 31	BEL 47	SUB 63	 79	~ 95	? 111	"								

4.3. Unicode vs UTF-8

- **UTF-8 is an encoding - Unicode is a character set**
- A character set is a list of characters with unique numbers. For example, in the Unicode character set, the number for A is 41.
- Unicode is a standard that defines a superset of all existing characters required to represent practically all known languages.
- UTF-8 encodes each of the 1,112,064 valid code points in Unicode using one to four 8-bit bytes.
- The first 128 characters of Unicode, which correspond one-to-one with ASCII, are encoded using a single octet with the same binary value as ASCII.
- There are other encodings, such UTF-8, UTF-16, UTF-32, UTF-EBCDIC or GB 18030

5. Units of information

- A **bit** is a binary digit, the smallest increment of data on a computer. As we mentioned at the beginning, a bit can hold only one of two values: 0 or 1, corresponding to the electrical values of off or on, respectively.
- Several conventional names are used for collections or groups of bits:
 - Nibble = 4 bits
 - Byte = 8 bits
 - Kilobyte (KB) = 1000 bytes = 10^3 bytes
 - Megabyte (MB) = 1000 KB = 10^6 bytes
 - Gigabyte (GB) = 1000 MB = 10^9 bytes
 - Terabyte (TB) = 1000 GB = 10^{12} bytes
 - Petabyte (PB) = 1000 TB = 10^{15} bytes
 - Exabyte (EB) = 1000 PB = 10^{18} bytes
- BE CAREFUL: We do not use the “1024” equivalences anymore because the prefixes kilo and mega mean 1000 and 1000000 respectively in the International System of Units.

5. Units of information

- Computers count by base 2, so we commonly use “binary” units of information.
 - Nibble = 4 bits
 - Byte = 8 bits
 - Kibibyte (KiB) = 1024 bytes
 - Mebibyte (MiB) = 1024 KiB = 1,048,576 bytes
 - Gibibyte (GiB) = 1024 MiB = 1,048,576 bytes
 - Tebibyte (TiB) = 1024 GiB = 1,099,511,627,776 bytes
 - Pebibyte (PiB) = 1024 TiB = 1,125,899,906,842,624 bytes
 - Exbibyte (EiB) = 1024 PiB = 1,152,921,504,606,846,976 bytes

5. Units of information

- Computers count by base 2, so we use “binary” conversions.
 - $1 \text{ KiB} = 1024 \text{ bytes} = 2^{10} \text{ bytes} = 2^{13} \text{ bits}$
 - $1 \text{ MiB} = 1024 \text{ KiB} = 2^{10} * 2^{10} = 2^{20} \text{ bytes} = 2^{23} \text{ bits}$
 - $1 \text{ GiB} = 1024 \text{ MiB} = 2^{10} * 2^{10} * 2^{10} = 2^{30} \text{ bytes} = 2^{33} \text{ bits}$
 - $1 \text{ TiB} = 1024 \text{ GiB} = 2^{10} * 2^{10} * 2^{10} * 2^{10} = 2^{40} \text{ bytes} = 2^{43} \text{ bits}$
 -
- Notice that: **B represents bytes** and **b means bit**. For example:
 - 30 MB = 30 megabytes (used in storage devices)
 - 30 MiB = 30 mebibytes (used in storage devices)
 - 30 Mbs = 30 megabits per second (used in networking or devices bandwidth)
 - 30 Mibs = 30 mebibits per second (used in networking or devices bandwidth)

END

