

Measuring Cross-Modal Interactions in Multimodal Models

Laura Wenderoth¹, Konstantin Hemker¹, Nikola Simidjievski^{2,1}, Mateja Jamnik¹

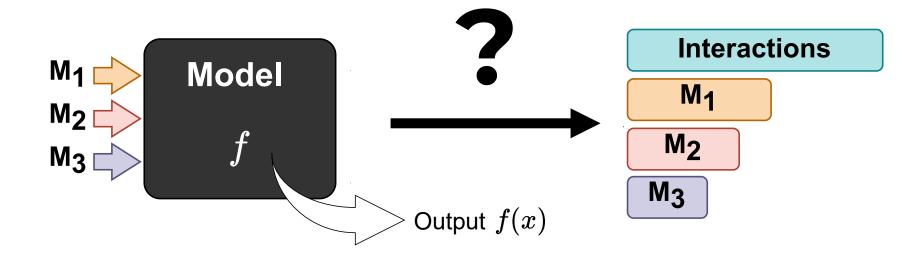
¹Department of Computer Science and Technology, University of Cambridge, Cambridge, UK

²PBCI, Department of Oncology, University of Cambridge, Cambridge, United Kingdom

{lw457, kh701, ns779, mj201}@cam.ac.uk



Motivation





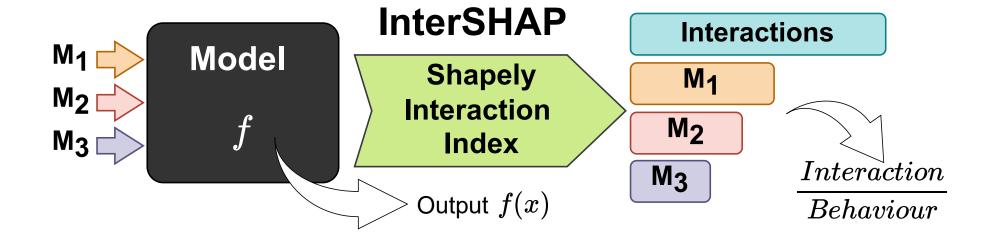
Limitations of Previous Work

InterSHAP overcomes the limitations of other cross-modal interaction scores: it is unsupervised, performance agnostic, applicable to more than two modalities, and allows for dataset- (global) and sample-level (local) explainability

Score	Modalities > 2	Local	Unsupervised	Performance Agnostic
$PID^{[1]}$	×	×	\checkmark	\checkmark
$EMAP^{[2]}$	×	×	×	×
SHAPE ^[3]	\checkmark	×	×	×
InterSHAP (Ours)	\checkmark	\checkmark	\checkmark	\checkmark

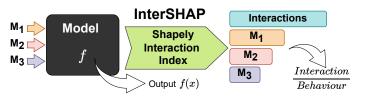


InterSHAP





InterSHAP



$$\Phi_{ij} = \left| \frac{1}{N} \sum_{a=1}^{N} \phi_{ij}((m_1^a, \dots, m_M^a), f) \right|, \quad i, j \in \{1, \dots, M\}$$
 (1)

$$\Phi = \begin{bmatrix}
\Phi_{11} & \Phi_{12} & \dots & \Phi_{1M} \\
\Phi_{21} & \Phi_{22} & \dots & \Phi_{2M} \\
\vdots & \vdots & \ddots & \vdots \\
\Phi_{M1} & \Phi_{M2} & \dots & \Phi_{MM}
\end{bmatrix} (2)$$

$$InterSHAP = \frac{Interactions}{Behaviour} \tag{3}$$

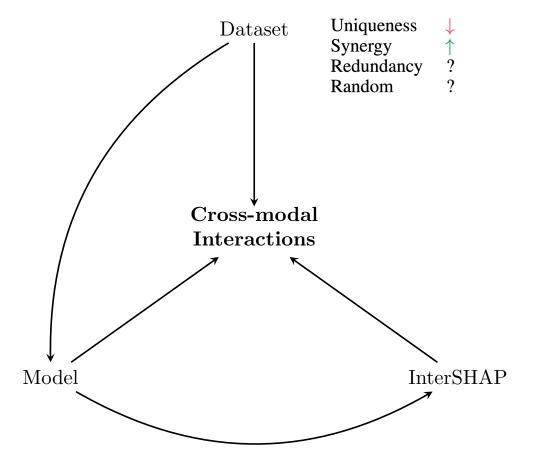


Verification on Synthetic Data

Three main factors influencing the captured cross-modal interactionsdataset, the model, and metric.

XOR

FCNN





Results _ 2 Modalities

InterSHAP values are presented as percentages for both the XOR function and FCNN with early fusion on the HD-XOR datasets. Results for XOR align with expectations, confirming the effectiveness of InterSHAP. For the FCNN, slightly higher values for uniqueness and lower values for synergy suggest the FCNN model did not fully capture all underlying cross-modal interactions from the dataset.

	Uni	Uniqueness		ynergy	Redundancy	Random
	XOR	FCNN	XOR	FCNN	FCNN	FCNN
InterSHAP	0.0	$0.2_{\ \pm0.1}$	99.7	$98.0_{\ \pm 0.5}$	38.6 ± 0.5	$57.8_{\pm 1.1}$



Visualisation of Results



Visualisation of results with FCNN with early fusion on the HD-XOR datasets. M1 represents modality 1, M2 modality 2, and I interactions...



Results > 2 Modalities

	Uniqueness	Synergy	Redundancy
2 Modalities	$0.2_{\ \pm0.1}$	$98.0_{\ \pm0.5}$	38.6 ± 0.5
3 Modalities	$0.6_{\pm0.2}$	$88.8_{\ \pm 0.5}$	$51.9_{\pm 0.3}$
4 Modalities	$1.2_{\ \pm0.1}$	$64.1_{\ \pm0.8}$	40.2 ± 0.2



Limitations

• Runtime: O(N^M)



Application to healthcare domain

Single Cell Dataset [4]

Modalities

- RNA
- Protein

Task: Cell Class Classification

Table 7: Details of Single Cell.

Class Distribution					
Neutrophil Erythrocyte B-Lymphocytes Monocyte					
43.7%	49.8%	1.4%	5.1%		

MIMIC III [5]

Modalities

- 12 physiological measurements (e.g. heart rate, 24h)
- static information on patients

Tasks: ICD and Mortality Classification

Table 8: Details of MIMIC III, ICD 1 and mortality.

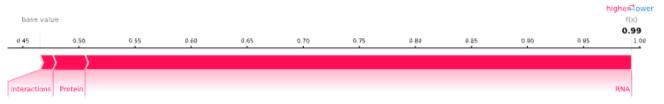
Class Distribution							
ICD Mortality							
No	Yes	1d	2d	3d	7d	1 year	> 1 year
82.5%	17.5%	76.0%	0.4%	1.3%	1.0%	11.0%	10.3%



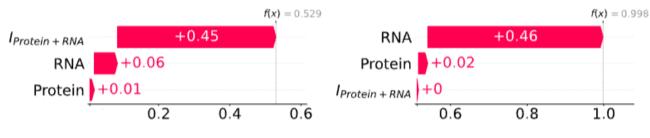
Single Cell Dataset [4]

Table 4: Cross-modal interactions scores on the multimodal single-cell dataset for FCNN with early, intermediate and late fusion. InterSHAP aligns with other SOTA methods, capturing the decline in cross-modal information from early to late fusion.

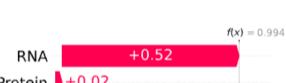
		Single-Cell	
	early	intermediate	late
InterSHAP	$1.9_{\ \pm0.4}$	$1.5_{\ \pm0.4}$	$0.4_{\ \pm 0.1}$
PID	$0.08_{~\pm0.01}$	$0.08_{\ \pm 0.01}$	$0.06_{\ \pm0.0}$
EMAP_{gab}	$0_{\pm 0}$	$_{0\pm 0}$	0 ± 0
SHAPĔ	$1.0 \; \scriptstyle{\pm 0.2}$	$0.7_{~\pm0.2}$	$0_{\pm 0}$



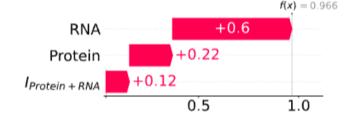
(a) Explanation over the whole dataset



(b) B-Cell Progenitor



(c) Erythrocyte Progenitor



(d) Monocyte Progenitor



(e) Neutrophil Progenito



MIMIC || [5]

Table 5: Cross-modal interactions scores on the MIMIC III dataset for baseline model and MVAE model from Multi-Bench implementation. InterSHAP aligns with other SOTA methods, capturing greater cross-modal interaction in the baseline compared to MVAE, while uniquely quantifying the proportional contribution of cross-modal interactions.

	IC	D-9	Mortality		
	baseline	MVAE	baseline	MVAE	
InterSHAP	$1.2_{\ \pm 0.2}$	$6.8_{\ \pm 1.3}$	$11.0_{\ \pm 0.5}$	$12.3_{\ \pm 2.8}$	
PID	$0.06_{\pm 0.01}$	$0.09_{\ \pm 0.01}$	$0.10_{\ \pm 0.01}$	$0.11_{\ \pm 0.01}$	
EMAP_{gap}	$_{0\pm0}$	$1.2_{\ \pm 0.0}$	-0.8 $_{\pm0.1}$	$0.9_{~\pm0.1}$	
SHAPE	$0.2_{\ \pm 0}$	$0.6_{\ \pm 0}$	$0.2 \; \scriptstyle{\pm 0.2}$	$0.7_{\ \pm0.2}$	

Summary

- Novel cross-modal interaction score: InterSHAP Open-Source implementation with integration into SHAP package
 - >2 Modalities
 - Local
 - Unsupervised
 - Performance agnostic
- Application to healthcare multimodal datasets

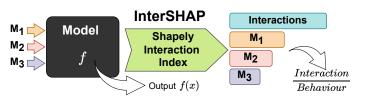
More in our paper:

Quantitative evaluation of existing cross-modal interaction scores



References

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- [4] Burkhardt, D.; Luecken, M.; Benz, A.; Holderrieth, P.; Bloom, J.; Lance, C.; Chow, A.; and Holbrook, R. 2022. Open Problems Multimodal Single-Cell Integration.
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Shapley Interaction Index

$$\phi_{ij}(M,f) = \sum_{S \subseteq M \setminus \{i,j\}} \frac{|S|!(M-|S|-2)!}{2(M-1)!} \nabla i j(S,f), \quad i \neq j.$$

$$\nabla i j(S, f) = \left[f_{S \cup \{ij\}} \left(S \cup \{ij\} \right) - f_{S \cup \{i\}} \left(S \cup \{i\} \right) - f_{S \cup \{j\}} \left(S \cup \{j\} \right) + f_{S}(S) \right] \right]$$

$$\phi_{ii}(M, f) = \phi_i(M, f) - \sum_{j \in M} \phi_{ij}(M, f) \quad \forall i \neq j.$$

$$\phi_i(M, f) = \sum_{S \subseteq M \setminus \{i\}} \frac{|S|!(|M| - |S| - 1)!}{|M|!} \Delta$$

$$\Delta = \left[f_{S \cup \{i\}} \left(S \cup \{i\} \right) - f_S \left(S \right) \right].$$