

# COMS30017 Coursework exam 2022/23 Resit

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## Overview

This coursework exam will have two main parts: data analysis (part 1) and modelling (part 2). The modelling part will also contain two sub-parts: Associative networks (part 2.1) and Integrate and fire neurons (part 2.2). The main submission will be a brief report, answering the questions in this document. As a guide, *if a sentence is in red italics, I expect to see a written response*. **For sentences formatted bold I expect to see a plot**. Most sections have a basic part and an advanced part. To get a higher mark you will also need to answer the advanced parts well, which require some critical interpretation of the results.

There is no page limit, but there is also no need write excessively. Please use at least 2 cm margins and 10 pt fonts. Please make sure your plots are high-quality, and have reasonably sized axis labels (don't take screenshots for your figures). All plots should have clear x- and y-axis labels, and units. Marks will be docked for every plot that has missing or unclear labels, or looks like a screenshot.

You can use whatever programming language you like (and it won't affect your mark), however we can only support Python in the QA sessions. And Python would probably be the easiest. We ask you to submit both your report and code. The final mark will entirely be based on the report. (We're only going to look at the code in the unlikely event of a plagiarism investigation.) **Please submit the report to the “Computational Neuroscience Coursework Report” submission point, and the code to the “Computational Neuroscience Coursework” submission point**. Please check and double check the submitted file! In previous years we've had people submitting the question sheet, or submitting password protected pdfs.

Other logistic information is included at the end of this document.

## 1 Data analysis [30 marks]

This part will focus on analysing some fictional spike train data and the random-dot motion task.

### 1.0.1 Question 1 [10 marks]

In the data folder associated with the coursework, you will find a file called neuron A `data.csv`. Load this file, for example using the python command

`np.loadtxt('neuron A.csv', delimiter=',')`. This contains a set of spike times from a fictional neuron, in milliseconds.

Compute the coefficient of variation (CV) for the inter-spike intervals. Also compute the Fano factor for time bins of 100 ms, 200 ms, 500ms and 1 s (start the first bin at 0 ms, so the first bin runs from 0–100 ms, 0–200 ms etc.) *State the values of both the CV and Fano factor in your report.* The Fano Factor is defined as,

$$\text{Fano Factor} = \frac{\text{Var}[N_t]}{\text{E}[N_t]}, \quad (1)$$

where  $N_t$  is the number of spikes in a time-bin.

Now load the file `trial ID.csv`, which contains an array of zeros and ones. Assume that the spike times above came from a neuron recorded from the visual cortex of a monkey during a series of sequential trials, each lasting one second long. So trial 4 lasts from  $t = 3000$  to  $t = 3999$ , trial 18 lasts from  $t = 17000$  to  $t = 17999$ , and so on. The corresponding trial IDs are given by the values in the trial ID array. `trial id = 0` corresponds to a random-dot visual stimulus where there was no net motion. `trial id = 1` corresponds to a moving random-dot stimulus. Now separate the spike times corresponding to trials where `trial id = 0` and trials where `trial id = 1`. Compute the CV and Fano factors again separately on the data corresponding to each trial type. For Fano factor, use the same time bins as before. For the CV, just include spike intervals for pairs within the same time bin (exclude spike pairs that span across bins). *State the values you find in your report. Do these values differ from what you found above on the total data? Offer an explanation for why or why not.*

### 1.0.2 Question 2 [10 marks]

Now you will decode the stimulus from the spike data using the procedure described in week 3 video 5. You will work with the spike counts. Count the number of spikes on each trial, and **plot histograms of the spike count for the stimulus off and stimulus on trials.** *Compute the  $d'$  value for these data.* Now write a function to do the decoding. It should take as input a spike count from a single trial, and the decision boundary. If the spike count is greater than the decision boundary, predict the motion stimulus (1), if it is less than the boundary, predict the no-motion stimulus (0). Then run the decoder on all the trials in the dataset, multiple times for various values of the decision boundary between 0 and 40 spikes/trial. Call a correct detection of a motion stimulus a 'true positive', a correct detection of no-motion stimulus a 'true negative'. **Make a plot overlaying three curves: the true positive rate, the true negative rate, and the total correct rate, all as a function of the decision boundary value.** Note that random guessing would correspond to a total correct rate of 50%. *Comment on what you observe in the plots. If we wanted to maximise the total fraction of correct responses, what would you estimate the optimal decision boundary to be? Explain how this relates to the count histograms you calculated above.*

### 1.0.3 Question 3 [10 marks]

Now load the other data file neuron B data. This contains spike times from another neuron simultaneously recorded during the same task. *Compute the  $d'$  value for these data.* Recompute the true-positive rate, true-negative rate, and total correct rate for neuron B as a function of the decision boundary and **plot the three together on a graph, as you did before for neuron A.** Now let's try to decode the stimulus from the joint activity from the pair of neurons. Let  $x_A$  and  $x_B$  correspond to single-trial spike counts from neurons A and B respectively. Write a function to decode the stimulus value from a single trial spike count pair  $(x_A, x_B)$ , using the following rule:

$$\text{predicted trial} = \begin{cases} 1 & \text{if } x_A - x_B - 4 > 0 \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

Apply this function to the spike data to decode the stimulus state on each trial. *Report the total correct rate you find using this joint rule. Comment on how this compares with the best decoding accuracy you found for the individual neurons above. Offer an explanation for what you observe, including additional plots if necessary to support your explanation.*

## 2 Modelling [70 marks]

### 2.1 Auto-associative networks [30 marks]

This part is on Hopfield networks.

#### 2.1.1 Question 1 [10 marks]

Begin by loading the partial Fashion MNIST dataset stored in the files `train_images.csv` and `test_images.csv` (originally taken from [github.com/zalando-research/fashion-mnist](https://github.com/zalando-research/fashion-mnist)). The total dataset consists of three training patterns and two test patterns. Each individual image is actually a 784-element array of +1s and -1s, corresponding to pixels in a 28x28 image. You can visualise the images using a command like `plt.imshow(np.reshape(x, (28, 28)))`. The values of the weights in a Hopfield network are zero on-diagonal,

$$w_{ii} = 0 \quad (3)$$

and off-diagonal, they are given by,

$$w_{i \neq j} = \frac{1}{N} \sum_a x_i^a x_j^a \quad (4)$$

$x_i^a$  is the activation of the  $i$ th node in the  $a$ th pattern, and  $N$  is the total number of training patterns (here,  $N = 3$ ). You should:

- Create a weight matrix of  $w_{ij}$ s.
- Fix the weight values to store the three training patterns. **Plot the weight matrix as a  $784 \times 784$  image.**

- Write a function to evolve the network according to the McCulloch- Pitts formula; this should be done asynchronously, so one random node is update each timestep. Assume the threshold  $\theta = 0$ .
- For each of the two test patterns, evolve the patterns until they stop changing. **For each case make plots of the network state at timesteps 0, 1000, and 3000.**

### 2.1.2 Question 2 [10 marks]

Now write a function to calculate the energy of a configuration

$$E = -\frac{1}{2} \sum_{ij} w_{ij} x_i^a x_j^a \quad (5)$$

Re-run the two test plot simulations, recording the energy value at each iteration. **For each case, make plots of the energy as a function of timestep number.** *Describe what the plots show. Explain in your own words why this happens, referring to the network update equation or energy equation if needed.*

### 2.1.3 Question 3 [10 marks]

Now we will examine the network's "basins of attraction". Write a function that when given a pair of images A and B, can generate a mixed image which has  $p\%$  of the pixels from image A and the remaining  $(100 - p)\%$  pixels from image B. For each of three pairs of images in the training set, compute such mixed images, varying  $p$  in increments between 0 and 100%, and compute the energy of the mixed image at each increment. **Plot the energy as a function of the mixing fraction  $p$ , overlaid for each of the three pairs of images.** *Comment on the relative shapes of the three curves. List some predictions for the model dynamics based on these curves, explaining your reasoning in each case.*

## 2.2 Integrate-and-fire neurons [40 marks]

This part will look at integrate-and-fire neurons and short-term plasticity.

### 2.2.1 Question 1 [7 marks]

Make a simulation of a single leaky-integrate-and-fire neuron. Set the resting potential  $V_{\text{rest}} = E_L = -70 \text{ mV}$ , spike threshold  $V_{\text{th}} = -50 \text{ mV}$ , reset voltage  $V_{\text{reset}} = -60 \text{ mV}$ , a passive membrane leak conductance  $g_L = 10 \text{ nSiemens}$ , and a membrane capacitance of  $C = 0.3 \text{ nF}$ . Use:

$$C \frac{dV(t)}{dt} = g_L(E_L - V(t)) + I_e \quad (6)$$

Set the injected current  $I_e = 0.21 \text{ nA}$ . Use Euler's method with timestep  $\delta t = 0.1 \text{ ms}$  to solve the differential equations numerically. Make sure to use the differential equations, do not just plot the analytical solution for  $V(t)$  given in the lectures – this will be useless for later questions anyway. For simplicity assume that the neuron does not have a refractory period after producing a spike. You do not need to plot spikes — once the membrane potential exceeds

threshold, simply set the membrane potential to  $V_{\text{reset}}$ . To keep track of the units I recommend converting everything to S.I. units inside your simulation code – you don’t strictly have to do this but it often makes things easier. Set the initial voltage value  $V(t = 0)$  to a random number between  $V_{\text{rest}}$  and  $V_{\text{th}}$ . Run the simulation for one second and **plot the voltage as a function of time**. Now run the simulation for ten seconds, for various levels of injected input current  $I_e$  between 0 nA and 0.5 nA, and computing the spike frequency in each case. **Plot the spike frequency as a function of the input current (the ‘f-I’ curve)**. *Analytically calculate the threshold input current and report its value.*

### 2.2.2 Question 2 [8 marks]

Now turn off the background input current,  $I_e = 0$ . Add  $N = 100$  total incoming synapses, split into two equal sized groups, ( $N_1 = 50$ ,  $N_2 = 50$ ). We will make these groups have different firing rates. You should just model the synaptic responses to spike trains, do not explicitly simulate the somatic voltages of these presynaptic neurons. Model all synapses as a conductance-based, following a single-exponential timecourse with decay time constant  $\tau_s = 2$  ms, the peak conductances (strengths) all  $\bar{g}_i = 0.5$  nanoSiemens for all synapses,  $E_s = 0$ , and  $\Delta s = 1$ . Let  $s_i(t = 0) = 0$  for all 100 synapses. It’s probably easier to store them all in arrays and update them together, rather than code each one by hand. Again use the Euler method to solve the system of ODEs (100  $s$  variables and 1 voltage variable), with the same timestep  $\delta t = 0.1$  ms. Simulate each input spike train as an independent homogeneous Poisson process with the same average firing rate  $r$ . A homogeneous Poisson process implies that average firing rate  $r$  is fixed in time, but that the spikes themselves arrive randomly. Initially set the rate for group 1  $r_1 = 10$  Hz and the rate for group 2  $r_2 = 100$  Hz. There are multiple ways to simulate Poisson spike trains. One simple method is to draw a random number on the unit interval for each synapse at every timestep, then if that number is less than  $r\delta t$ , assume a spike has occurred at that synapse. This method is valid as long as  $r\delta t \ll 1$ . Simulating your model at this stage should result in the neuron firing irregularly. **Plot the neuron’s voltage for one second of simulation time**. Now run the simulation for ten seconds, for various levels of  $r_1$  and  $r_2$  separately between 0 Hz and 150 Hz, and compute the spike frequency in each case. When varying  $r_1$ , keep  $r_2$  fixed at 100 Hz. When varying  $r_2$ , keep  $r_1$  fixed at 10 Hz. **Plot the output spike frequency as a function of the input spike frequency, overlaid for both cases**. *Describe what is shown in the plots and offer an explanation for the shapes of the curves.*

### 2.2.3 Question 3 [10 marks]

Now we will make the mean firing rate for each group vary sinusoidally in time:

$$r(t) = \bar{r} + B \sin(2\pi ft) \quad (7)$$

where  $\bar{r}$  is the average firing rate. The amplitude of the oscillation depends on the parameter  $B$ , while the timescale of oscillations depends on  $f$ . Fix  $f = 2$  Hz,  $\bar{r}_1 = 10$  Hz,  $\bar{r}_2 = 100$  Hz. Running the simulation for 1 s in each case, **make plots of the voltage as a function of time, for two different scenarios** (visualised in the left and centre panels in the figure below):

- $B_1 = 0$  Hz and  $B_2 = 50$  Hz.
- $B_1 = 5$  Hz and  $B_2 = 0$  Hz.

*Describe what you see in the plots. What was the mean firing rate of the neuron in each case, as averaged over a 30 second simulation?* Note that the mean total input firing rate (averaged over time) is the same in both cases, and also identical to that used in question 2. *Explain why the three different cases lead to different output firing rates.*

#### 2.2.4 Question 4 [15 marks]

Now implement short-term depression at each synapse. Introduce an additional variable  $A$  for each synapse, so that the total synaptic conductance will be  $g_i(t) = A_i(t)s_i(t)\bar{g}_i$ .  $A$  is going to represent the effects of short-term depression. Every time a spike arrives at the  $i$ th synapse, set  $A_i \leftarrow \alpha A_i$ , where  $\alpha = 0.75$ . In between spikes, let  $A_i$  recover back towards 1 by letting it follow the differential equation

$$\frac{dA_i(t)}{dt} = \frac{1}{\tau_A}(1 - A_i), \quad (8)$$

with  $\tau_A = 300$  ms. Also change all the synaptic strengths to  $\bar{g} = 3$  nS (to counter the effects of depression). Now repeat the two simulations from Q3 but with synaptic depression turned on. In this case run the simulation for 1 second first to let it ‘settle down’, then run it for a further 3 seconds to observe the steady-state dynamics. **Make plots of the voltage as a function of time in each case.** *Describe what you observe, and compare it to the plots obtained in Question 3. Offer an explanation for what is going on. You can make extra plots if they support your argument.* Finally, run the simulation with synaptic depression still on, but with  $B_1 = 0$  Hz and  $B_2 = 5$  Hz (visualised in the right panel of the above figure). Again run the simulation for 1 second warmup plus a further 3 seconds. **Make a plot of the voltage vs time.** *Describe the results and offer an explanation for what you observe, commenting on how it compares with the previous two plots.*

## Logistical information

The coursework will be supported in an online Q&A based on Teams and run by Laurence at 2:30 on Thursday 24th November and Thursday 1st December.

This coursework is individual work. You must not collaborate with other students, which would be considered cheating.

**Deadline** The coursework will be released on 13:00 on Thursday 17th November. The deadline for submission of all optional unit assignments is 13:00 on Thursday 8th of December (due to the fact that the University discourages Friday deadlines). The intention is that you submit by 12pm and keep the last hour as emergency reserve for e.g. technical problems. In case of problems with your submission, e-mail [coms-info@bristol.ac.uk](mailto:coms-info@bristol.ac.uk) before the 1pm final deadline! Students should submit all required materials to the “Assessment, submission and feedback” section of Blackboard - it is essential that this is done on the Blackboard page related to the “With Coursework” (COMS30063) variant of the unit.

**Time commitment** You are expected to work on both of your optional unit courseworks in the 3-week coursework period as if it were a working week in a regular job - that is 5 days a week for no more than 8 hours a day. The effort spent on the assignment for each unit should be approximately equal, being roughly equivalent to 1.5 working weeks each. It is up to you how you distribute your time and workload between the two units within those constraints.

You are strongly advised NOT to try and work excessive hours during the coursework period: this is more likely to make your health worse than to make your marks better. If you need further pastoral/mental health support, please talk to your personal tutor, a senior tutor, or the university wellbeing service.

**Academic Offences** Academic offences (including submission of work that is not your own, falsification of data/evidence or the use of materials without appropriate referencing) are all taken very seriously by the University. Suspected offences will be dealt with in accordance with the University’s policies and procedures. If an academic offence is suspected in your work, you will be asked to attend an interview with senior members of the school, where you will be given the opportunity to defend your work. The plagiarism panel are able to apply a range of penalties, depending the severity of the offence. These include: requirement to resubmit work, capping of grades and the award of no mark for an element of assessment.

**Extenuating circumstances** If the completion of your assignment has been significantly disrupted by serious health conditions, personal problems, periods of quarantine, or other similar issues, you may be able to apply for consideration of extenuating circumstances (in accordance with the normal university policy and processes). Students should apply for consideration of extenuating circumstances as soon as possible when the problem occurs, using the following online form: <https://www.bristol.ac.uk/request-extenuating-circumstances-form>

You should note however that extensions of any significant length are not possible for optional unit assignments. If your application for extenuating circumstances is successful, you may be required to retake the assessment of the unit at

the next available opportunity (e.g. during the summer reassessment period).



## Mark scheme

mark range	criteria
100–80	All plots completed and correct Excellent presentation Outstanding critical analysis and discussion of results Evidence of study and originality well beyond what has been taught
70–79	All plots completed and correct Excellent presentation Good critical analysis and discussion of results Some evidence of study and originality beyond what has been taught
60–69	Almost all plots completed and correct Good presentation Some critical analysis and discussion of results
50–59	Most plots completed and correct Coherent presentation Some discussion of results
40–49	Some plots completed and correct Coherent presentation Attempt at discussion of results
0–39	Insufficient plots completed and correct. Understandable presentation Little or no discussion of results

Broadly speaking, marks above  $\sim 60$  require not only most plots completed and correct, but also critical analysis and discussion of the results.

What does this mean? Computational neuroscience is a science. In science, we don't just compute numbers and make plots. Those numbers and plots are supposed to tell us something about the brain. So for the highest marks, it is important to think about the following issues when answering the written parts:

- do the numbers/plots we've computed make sense?
- what do the numbers/plots tell us about the underlying system?
- do the numbers/plots really capture what we want them to capture? (e.g. is FF/CV a “good” measure of variability?)