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PROJECT DESCRIPTION

1 Introduction

Mapping Our Universe: The earliest examples of astronomy included following the nearby planets and charting the “fixed” stars which were projected onto the celestial sphere and organized into constellations. Ultimately this led to a physics-based, low resolution, 3D description of the Galaxy. The situation today in cosmology is somewhat similar. We have large surveys of comparatively nearby galaxies [1–10] and a splendid two dimensional map of the microwave background [11], all of which have led to a “standard cosmological model” of the Universe in which inflation-based, Gaussian, potential fluctuations, with a well-defined spectrum, grew according to deterministic laws to produce contemporary large scale structure in a flat Universe endowed with a cosmological constant. However, the traditional goal of astronomy, to describe the complete disposition of this actual structure, has hitherto been subsumed into statistical investigations designed to elucidate the underlying physics.

We present a staged proposal to combine recent observations with what we have learned about the physics to *make the best map we can of the 3D structure of the Universe within and slightly beyond our horizon*. In addition to satisfying a natural desire to describe our Universe, success in this program will naturally furnish ongoing and planned physics investigations with additional priors which should tighten up their accuracy, and enable us to make scientific predictions about future surveys.

Before proceeding to a detailed description of our proposed program in Section 2, we first provide a brief summary of the context in which it will be carried out. Brief outlines of our plans can be found in Sections 3–5.

Our Universe’s Contents: The last decade has seen remarkable advances in cosmology, spearheaded by increasingly detailed measurements of the cosmic microwave background (CMB) radiation (see e.g. [11–14]). These accurate measurements have affirmed that a description of a homogeneous, spatially flat general relativistic Universe with relatively few ingredients – photons ($T_\gamma = 2.7$ K), neutrinos (three flavors), baryons ($\Omega_b = 0.05$), dark matter ($\Omega_d = 0.26$) and a cosmological constant ($\Omega_\Lambda = 0.69$) supplemented by (almost) scale-free, adiabatic, Gaussian initial perturbations suffices to describe essentially all that is secure in the observations [14]. There is still room for revision, retraction and major discovery but, right now, we have a good working hypothesis that the Universe is basically this simple (e.g. [15, 16]). There is some tension in the reported measurements, *e.g.* of the Hubble constant, but this is not important for our purpose and we shall simply adopt Planck values. Much effort is being expended to see if a ubiquitous and eternal cosmological constant needs to be replaced by a dynamical dark energy. If this turns out to be true then only simple changes will be needed to what follows.

Our Universe’s Evolution: The description of the average expansion of the Universe is relatively uncontroversial. When $t \sim 50$ kyr, the scale factor – the size of a region relative to its contemporary size – was $a \sim 0.0003$ and the Universe became (dark) matter-dominated. When $t \sim 380$ kyr, $a = 0.00093$, the hydrogen plasma quickly formed

atoms, decoupling from the radiation and forming the inside-out, CMB photosphere where the majority of CMB photons we observe today were last scattered with a temperature ~ 2900 K. When $t \sim 600$ Myr, $a \sim 0.1$, the first stars formed and the Universe (re-)ionized. This epoch is becoming accessible to observation especially by HST [17]. Finally when $t \sim 8$ Gyr, $a \sim 0.6$, the cosmological constant began to dominate the matter, and the universal expansion started to accelerate.

Fluctuations in Our Universe: The observed fluctuations are adequately described by a set of spatial Fourier modes expressed in terms of contemporary or comoving coordinates. These modes are longitudinal and adiabatic, and the ones that mostly concern us here evolved linearly, so we only need to their amplitudes and phases at one epoch, e.g. recombination, to predict them for all times. It is convenient to describe their amplitude using the (effective) Newtonian potential/gauge Φ from which the density and fluid velocity perturbations can be computed (in the “Sachs-Wolfe” limit at long wavelength [18]).¹

It has recently been demonstrated, mainly using CMB observations [14], that the adiabatic hypothesis is quite accurate. Furthermore, the amplitudes associated with each mode of the initial potential scale approximately as $k^{-3/2}$ and are drawn from a Gaussian distribution with random phase, so that the potential fluctuations associated with each length scale are scale-independent. This behavior is consistent with a remarkable early conjecture by Harrison [19] as elaborated by Zel'dovich [20].

The potential associated with a mode was essentially frozen until it “entered the horizon,” that is, until the timescale for its dynamical evolution, became smaller than the expansion timescale. We are mostly concerned with long wavelength modes for which this happened after recombination and $k \lesssim 40 \text{Gpc}^{-1}$.² For such wavenumbers, the waves evolve at roughly constant Φ until the cosmological constant takes over and the potential falls by roughly 20 percent today. We make this explicit in Fig. 1 where we show the interior of the last scattering surface in comoving coordinate space and a particular wave whose amplitude and phase we are trying to measure.

The Inflation of Our Universe: The flatness of the geometry today, the isotropy of the CMB temperature, and the very existence of fluctuations with wavelengths longer than naively allowed by causality are all consistent with the simplest version of a much more specific and even bolder conjecture by Guth [21], Linde [22] and others (e.g. [23–28]), that the Universe underwent a period of “inflation” at much earlier times. This theory is based on the idea that all the structures in the observed Universe emerged from quantum fluctuations about 10^{-33} seconds after the Big Bang. Inflation, which describes a phase of accelerated cosmic expansion, is the leading theory providing a causal mechanism for generating these fluctuations and stretching them to cosmological scales. The microphysics of inflation makes detailed predictions for the spectra of these fluctuations as observed in the CMB, in particular a slight tilt in the power spectrum, which has been measured (see e.g. [29, 30] and references therein).

Qualitatively, the causal mechanism seeding the primordial perturbations is easily

¹There may also be tensor modes which we shall ignore here. If, and when, they are detected, only minor modifications will be needed.

² k_0 can be considered as approximately the wavenumber associated with the first acoustic peak and its consequence, Baryon Acoustic Oscillations (BAO).

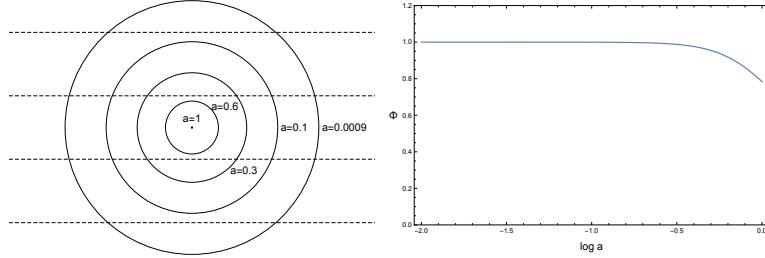


Figure 1: a) The local Universe interior to the CMB photosphere expressed in comoving coordinates. The circles are, in order, $a = 0.6$, ($z \sim 0.7$), schematically the limit of present surveys, $a = 0.3$, ($z \sim 2$) roughly the effective limit of future surveys, the nominal Epoch of Reionization at $a = 0.1$, ($z \sim 9$) and the CMB photosphere at $a = 0.00093$, ($z \sim 1100$) and a distance $x_{\text{CMB}} \sim 13.9$ Gpc. The comoving radius of the big bang is 14.2 Gpc. Also shown as dashed lines are the nodes of a single wave mode with $k \sim 0.45$ Gpc $^{-1}$ which contributes significantly to spherical harmonics with $\ell \lesssim 10$. b) Variation of the amplitude of this wave with scale factor a .

understood. During inflation, the physical Hubble radius, H^{-1} , which can be thought of as the “apparent horizon”, was roughly constant. Meanwhile, quantum fluctuations in the matter field(s) and metric are constantly generated with wavelength H^{-1} at most [31]. Once produced, a fluctuation with comoving wavelength λ is stretched with the expansion of space past the Hubble radius, at which point its dynamical timescale, $\sim ac/k$ was larger than the expansion time and it “exited” the horizon and its amplitude froze. Throughout inflation, such fluctuations are continuously created at the physical scale H^{-1} . Therefore, by the end of inflation, perturbations will finally have been produced on a whole spectrum of physical scales.

2 Proposed Research

The long term goal of this proposal is to connect the CMB to local surveys by producing an evolving three-dimensional (or in other words, four-dimensional) map of the Universe that is valid from before 380 kyr to today, and out beyond 14 Gpc. The exercise is not purely cartographic, as it is essential that we use secure physical inferences about the early Universe in making this map. This research was originally envisaged as a three stage program.

The first stage of our proposed program is to use 2D CMB observations alone to test internal consistency and to recover as much as we can of the 3D potential, velocity and density fields interior to the last scattering surface. This stage is nearing completion. In the second stage, we will augment CMB data with existing 3D measurements from galaxy surveys, gravitational lensing, intermediate Sachs-Wolfe measurements and so on. This should improve the resolution. This second stage requires detailed and careful analysis of several existing data sets and we request funding to complete the second stage. The third and final stage will be to use our constrained model to make quantitative predictions about the density field as could be probed by future surveys, and will include an investigation

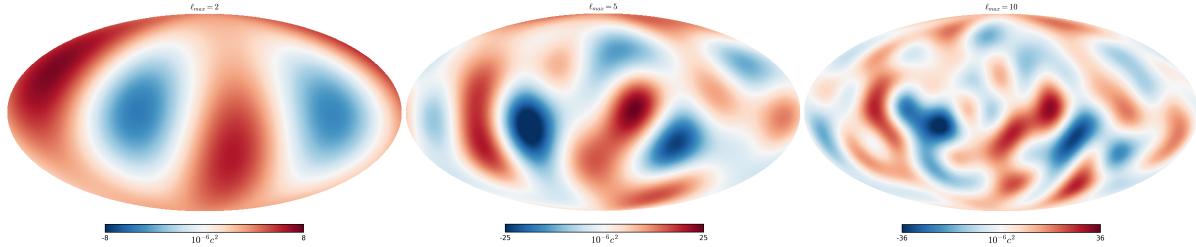


Figure 2: Photospheric potential fluctuations of the CMB for $\ell_{\max} = 2, 5, 10$ derived from Planck data shown as Mollweide projections.

of how far it is possible, even in principle, to reconstruct the structure of the Universe including what can be inferred beyond our horizon. We anticipate that we will only commence work on this third stage towards the end of the proposed funding but do discuss it here as it is our long range goal.

2.1 Stage 1. From 2D to 3D: Potential Reconstruction from CMB Data Alone

During the first phase of our program we are extending our methodology to carry out an independent analysis of the data provided by WMAP and Planck to investigate of the inflationary paradigm in various different new ways. We first provide a brief review of our results so far, to place this proposed investigation in context.

CMB Temperature Fluctuation Input Data: Observations of the CMB are the foundation on which modern quantitative cosmology rests. The conventional way to describe the observations is in terms of spherical harmonics – the generalization of Fourier modes to a sphere – labeled by ℓ and m . It is convenient to use an equivalent vector of real spherical harmonics, $Y_y(\theta, \phi) = \{Y_{0,0}, Y_{1,0}, 2^{1/2}\Re[Y_{1,1}], 2^{1/2}\Im[Y_{1,1}], Y_{2,0}, \dots, 2^{1/2}\Im[Y_{\ell_{\max}, \ell_{\max}}]\}$ of length $(\ell_{\max}+1)^2$ and where θ, ϕ are standard spherical polar coordinates. Note that there are $2\ell+1$ independent, real, basis function in each ℓ -shell. Note also that $\int d\Omega Y_y Y_{y'} = \delta_{yy'}$. It is convenient to treat ℓ_{\max} as a continuous variable by adding a fraction between zero and unity of the largest ℓ shell and therefore smoothly change the angular resolution. (The use of a real basis helps identify systematic effects.)

Most investigations have to date focused on measuring the “power” in the temperature fluctuations (including polarization) associated with a given ℓ , obtained by summing products of the coefficients of the harmonic components over m , and comparing it with the predictions of various cosmological models. This program has been wonderfully productive, and has resulted in the world model outlined in the introduction. Furthermore this power spectrum has been successfully reconciled with features of the local Universe, such as galaxy counts. One common assumption is that the particular realization of the Universe that we are observing is drawn from a statistical ensemble of universes. When ℓ is large, we have many independent measurements on the associated angular scale, $\sim \pi/\ell$, and so we can measure an rms value for the harmonic component with a small variance. However, when ℓ is small, we have only a few such measurements and the “cosmic” variance is large. Despite their great value, these statistical measurements inevitably discard

information which may be valuable.³ In the proposed study, only one specific realization of the Universe – the one we inhabit – is considered.

In order to start us on a pilot investigation, Planck team members Wehus & Eriksen (Oslo) kindly supplied us with 100 sample Commander Planck temperature fluctuation maps for $0 \leq \ell \leq 10$ or $1 \leq y \leq 121$. From this ensemble we compute the mean 2D photospheric potential fluctuation map at the time of recombination, $\Phi = a_y Y_y$, up to various ℓ_{max} as shown in Figure 2 (including the monopole and dipole components and adopting the summation convention) and the covariance matrix $C_{yy'}$ associated with the harmonic components a_y . We find that this matrix is invertible and can be used directly up to $\ell_{max} = 8$. More careful treatment of the data is needed beyond this. The fractional variance in individual harmonics varies between ~ 0.0001 and ~ 0.01 . Undoubtedly, there are systematic effects present in this data set which need to be explored, but the accuracy is high enough to proceed without this. More samples are available on request: we will continue to work with Wehus & Eriksen to make sure the data quality keeps up with the reconstruction methodology as our map resolution increases.

Fourier Mode Modeling of the 3D Potential: It is convenient to represent the 3D potential Φ at the epoch of last scattering with a Fourier expansion; the potential at other times is then calculable through simple manipulation of the resulting modes. Although the full spectrum of the Fourier modes we are discussing is continuous in \mathbf{k} , the fact that our observations are made over a restricted volume means that we can treat the waves as a discrete Fourier transform of modes associated with a box in comoving space of side L on which periodic boundary conditions are imposed. L is chosen here to have a compromise value of four times the radius of the CMB photosphere, 13.9 Gpc which we adopt as our unit of length.

$$\Phi[\mathbf{x}(r, \theta, \phi)] = \sum_{n=1}^{N/2} [f_n \cos(\mathbf{k}_n \cdot \mathbf{x}) + f_{N+1-n} \sin(\mathbf{k}_n \cdot \mathbf{x})] \quad (1)$$

where the coefficients f_n are also real and $\mathbf{k} = \Delta k \{n_1, n_2, n_3\} = k \{\sin \theta' \cos \phi', \sin \theta' \sin \phi', \cos \theta'\}$, with n_1, n_2, n_3 integers and $\Delta k = 2\pi/L = \pi/2$. We restrict the sum to $(n_1^2 + n_2^2 + n_3^2)^{1/2} \leq n_{max}$ and only need consider \mathbf{k} over a hemisphere (since the potential must everywhere be real.) We label the coefficients by the index n running from 1 to $N \sim 4\pi n_{max}^3/3$. ($N = 6$ through 4168 for $n_{max} = 1$ through 10.) $\Phi(\mathbf{x})$ can be expanded formally as an infinite sum of Legendre polynomials and approximately as a finite sum:

$$\Phi(\mathbf{x}; \ell_{max}) = \sum_{\ell=0}^{\ell_{max}} (2\ell + 1) \sum_{n=1}^{N/2} j_\ell(k_n x) P_\ell(\hat{\mathbf{k}}_n \cdot \hat{\mathbf{x}}) [\cos(\ell\pi/2) f_n + \sin(\ell\pi/2) f_{N+1-n}]. \quad (2)$$

Gaussian Prior: Detailed study of the CMB (e.g. [32, 33]) has led to the conclusion that the amplitude of each discrete mode with wave vector \mathbf{k} is well modeled as having been drawn from a Gaussian distribution of variance $\sigma_{\mathbf{n}}^2 = \alpha^2 (n_1^2 + n_2^2 + n_3^2)^{-3+(n_s-1)}$, where n_s

³This is in the sense that music is far more than a “flicker” power spectrum. To pursue our musical metaphor, different voices and instruments contribute different ranges of frequencies to a musical performance over a total range of roughly ten octaves. We are only listening to the bass range but higher voices and instruments can still contribute to what we hear.

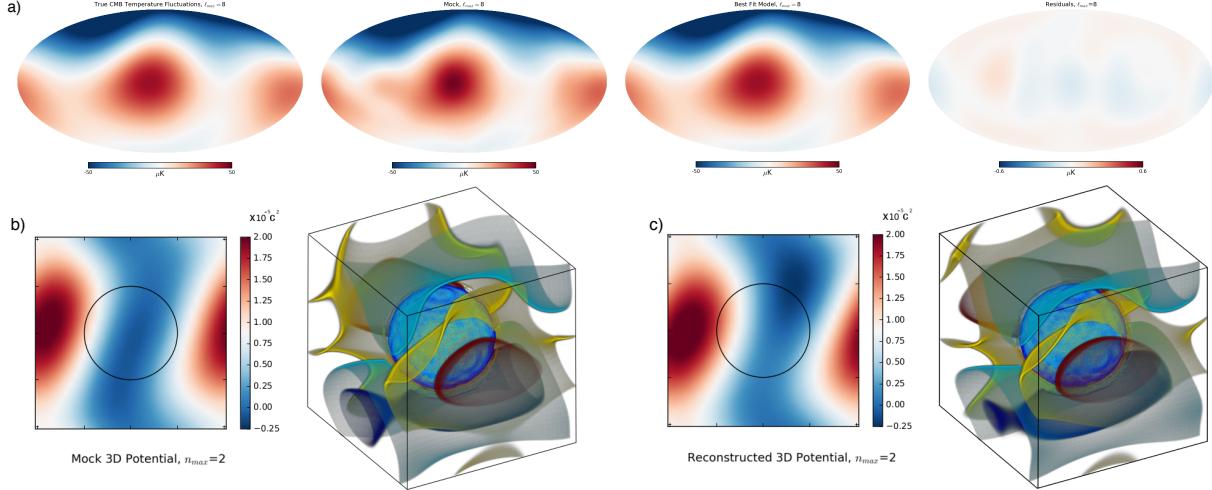


Figure 3: a) Demonstration of the reconstruction pipeline. In this pilot study, 81 spherical harmonics and a Gaussian prior were used to recover 122 Fourier components with $n_{\max} = 2$. The monopole and dipole were not removed. *First panel:* Simulated, noiseless 2D potential fluctuations on the CMB photosphere. *Second panel:* Noisy mock observation. *Thrid panel:* Most probable model, as given by equation 5. *Fourth panel:* Residuals. As expected, the posterior predicted potential maps have higher uncertainty in the galactic plane. b) Simulated 3D gravitational potential at the time of recombination. *First panel:* Slice of the 3D potential in the $x_3 = 0$ plane. The CMB photosphere is represented by the black circle. *Second panel:* 3D visualization of the potential. c) 3D reconstructed potential, recovered from the noisy 2D fluctuations on the CMB photosphere. Both panels a analogous to the ones in b), and show very good agreement between simulation and reconstruction.

is the scalar spectral index. Adopting this model, we can fix the spectral tilt to the Planck best-fit value (this assumption will be relaxed in the next subsection in order to estimate the inflationary hyperparameters) and we fix the regularization constant α following the evidence analysis of [34]. As will be explained below, this constitute the first step towards a hierarchical modeling of the system where α is one of a set of hyperparameters governing the statistics of the potential field.

Preliminary Results: The simple question that motivated this investigation, and which did not seem to have a well-known answer, was how much of the 3D potential could be reconstructed interior to the 2D CMB photosphere using CMB observations alone. This is an example of what is sometimes called *holography*. At first sight this might seem hopeless, because if one associates ℓ_{\max} with $k x_{\text{CMB}}$, then we are trying to solve for $O((k_{\max} x_{\text{CMB}})^3)$ Fourier modes using only $O(\ell_{\max}^2)$ spherical harmonics. However, if we confine our attention to the longest wavelength waves, and use all the information that is at our disposal to exploit the high accuracy of the measurements while accepting uncertainty in the result, then it is possible to complete this task.⁴

⁴Our approach is quite complementary to that of Yadav and Wandelt [35] who are concerned with wavelengths comparable with the thickness of the recombination surface around the acoustic peak near $\ell \sim 200$.

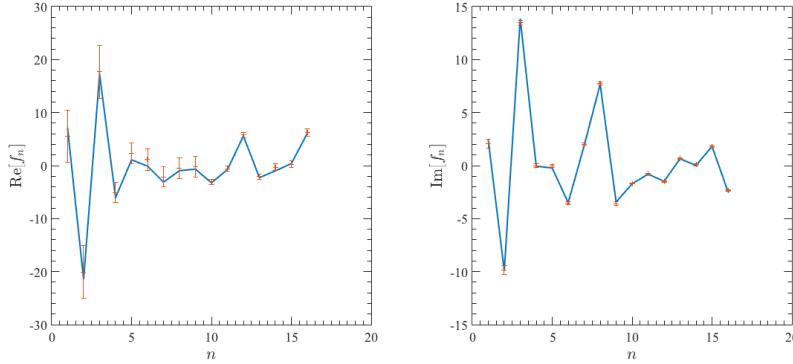


Figure 4: Error on the reconstructed f_n parameters in the reconstruction from Figure 3. The left panel shows the real part of the coefficients while the right panel shows the corresponding imaginary part. *Blue:* True f_n values. *Orange:* Reconstructed f_n values. The error bars are given by the posterior covariance matrix $\mathbf{A}_{nn'}^{-1}$.

For a set of f_n parameters, our model for the 2-dimensional sky is defined by computing the spherical harmonic coefficients $a_y = \mathbf{R}_{y n} f_n$, where the “response matrix” is given by:

$$\mathbf{R}_{y n} = 4\pi Y_y(\theta' \phi') j_\ell(k) [\cos(\pi\ell/2), \sin(\pi\ell/2)] \text{ for } [1 \leq n \leq N/2, N/2 < n \leq N]. \quad (3)$$

For a given data set of a_y measurements, we approximately characterize the posterior PDF (which under our assumptions is a multivariate Gaussian distribution) for the coefficients f_n , $\mathcal{P}(f_n|a_y)$, by first finding its peak, by minimizing the quantity

$$-2 \ln \mathcal{P}(f_n|a_y) \approx (a_y - f_n \mathbf{R}_{ny}) C_{yy'}^{-1} (a_{y'} - \mathbf{R}_{y'n'} f_{n'}) + \frac{f_n^2}{\sigma_n^2} + \text{const.} \quad (4)$$

with respect to variation of f_n . Note that σ_n contains the normalization α . Here, $C_{yy'}^{-1}$ is the inverse of the covariance matrix. This leads to the following set of linear equations, which can be solved using standard library routines:

$$f_n = \left(\mathbf{R}_{ny} C_{yy'}^{-1} \mathbf{R}_{y'n'} + \frac{\delta_{nn'}}{\sigma_n^2} \right)^{-1} \mathbf{R}_{n'y} C_{yy'}^{-1} a_{y'} \quad (5)$$

For the purpose of this pilot study, the modes that mostly concern us remain linear and are “adiabatic”, so that we need not to worry about secondary effects that usually enter the transfer function. The approximate form given above is sufficient for a feasibility check: as shown in Figure 3 using mock data, we have found that *it is possible to solve for stable, low order maximum posterior Fourier coefficients, which can recover harmonic coefficients a_y that are consistent with the original data.* We have applied this approximate procedure to the actual Planck data, and our results are exhibited in Figure 5.

The error on the recovered Fourier coefficients f_n is given by the covariance of the posterior distribution, $C_{posterior} = \mathbf{A}_{nn'}^{-1} = (\mathbf{R}_{ny} C_{yy'}^{-1} \mathbf{R}_{y'n'} + C_{nn'}^{-1})^{-1}$. Therefore, the marginalized error on individual reconstructed f_n parameters is given by the square root of the

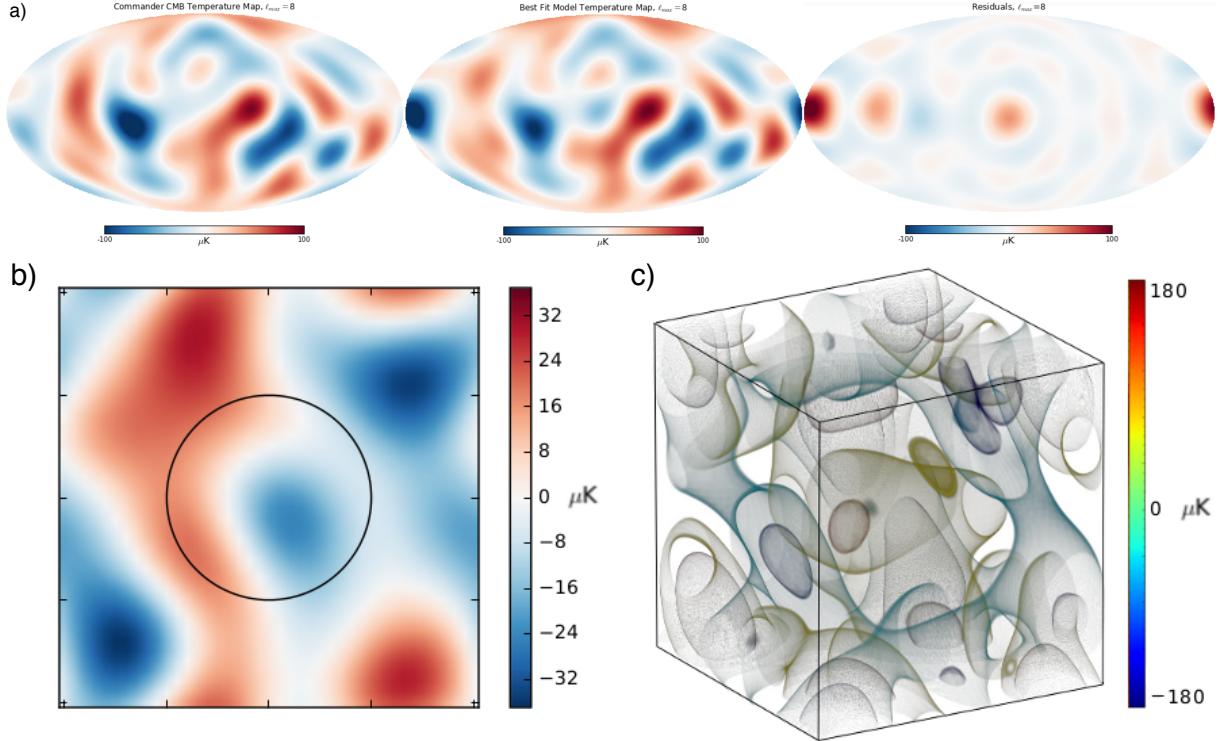


Figure 5: a) Reconstruction of the 3D temperature map from the Planck 2D CMB photosphere. In this pilot study, 81 spherical harmonics and a Gaussian prior were used to recover 122 Fourier components with $n_{\max} = 3$. The monopole and dipole were not removed. *First panel:* Planck temperature map on the CMB photosphere. *Second panel:* Most probable model, as given by equation 5. *Fourth panel:* Residuals. As expected, the posterior predicted temperature maps have higher uncertainty in the galactic plane. b) Slice of the 3D temperature map in the $x_3 = 0$ plane. The CMB photosphere is represented by the black circle. c) 3D visualization of the temperature map. The potential can be obtained by multiplying the temperature map by 1/3.

corresponding diagonal elements of $\mathbf{A}_{nn'}^{-1}$. The error on the recovered parameters for the reconstruction displayed in Figure 3 is shown in Figure 4

There are features of the data which we have yet to understand, but this suffices to illustrate what we hope will be possible. It is proposed to refine and improve upon this basic approach to obtain the best map we can based upon the CMB data alone. In particular we intend to set clear, statistical criteria for assessing when it is significant to add additional Fourier components to the map. With a better understanding of the robustness of the inference, we will be equipped to proceed with our further investigation. To extend our analysis to larger l , when density and velocity effects are also important. It will become necessary to use the standard transfer function to relate the observed temperature fluctuation to the inflationary perturbations and the contemporary potential (and density) perturbations.

Hierarchical Modeling of the Inflationary Origin of Perturbations: As explained above, inflation provides a mechanism for seeding perturbations in the CMB from quantum fluctuations in the early Universe. The resulting statistical distribution of pertur-

bation amplitudes provides a conditional PDF for the parameters of the 3D potential in the Universe: *inflation provides a physically-motivated prior for us to use when mapping the potential*. Because we do not know the exact values of the parameters (or rather, hyper-parameters) of the inflation model, we must infer them from the data as well, in a hierachical model for the CMB data. In this section we step through the construction of this statistical model.

It is standard, as we shall do here, for most inflation models to assume that the main matter components during inflation are in the form of scalar fields. Moreover, for simplicity, we shall assume that only one scalar field is dynamically relevant, so that we will work within the framework of “single-field” inflation. Apart from these caveats, the framework developed in what follows will remain model-independent.

We want to describe perturbations of the scalar field, which we call φ , about a homogeneous background. It is common to quantify these perturbations with the gauge-invariant curvature perturbation, ζ .⁵ In the co-moving gauge, the Fourier modes of ζ as they exit the horizon are

$$\zeta_{\mathbf{k}} = \sqrt{\frac{\pi}{2}} e^{i\theta} e^{i\frac{\pi}{2}(\nu+\frac{1}{2})} (-\tau)^{\nu} \mathcal{H}_{\nu}^{(1)}(-k\tau). \quad (6)$$

Here, ν is a slowly varying function which encapsulates the specific dynamics of the inflationary model, $\mathcal{H}_{\nu}^{(1)}$ is a Hankel function of the first kind, τ is the conformal time, defined by $d\tau = a(t)dt$, and θ is a random variable endowing each mode with a random phase. One prediction of inflation is that θ *should have a uniform probability distribution between 0 and 2π* .

This is a fundamental prediction of inflation, which stems from the assumption that the fluctuations are quantum mechanical in origin, the very assumption the idea of inflation is based upon. However, the actual distribution of the phases for the modes of ζ (or Φ) in the CMB has yet to be measured. This is because, so far, most analyses of CMB data have been restricted to measuring the power spectrum of fluctuations, Δ_{ζ}^2 . Because the power spectrum is proportional to $|\zeta_{\mathbf{k}}|^2$, when such a measurement is made, the phase information of the modes is lost. Since our proposed hierarchical model explicitly includes the 3D potential interior to the sphere of last scattering explicitly, this phase information will be readily available: we will be able to perform a direct test of the quantum origin of the CMB fluctuations. In Figure 6 we show an example visualization of the phases of a mock 3D potential: a key part of our research program will be to develop robust statistical tests of the posterior inferences of such phases, first using realistic mock data (to avoid a posteriori bias), and then on the Planck temperature map.

One of the main uncertainties pertaining to inflation remains the shape of the potential for the scalar field φ , which determines the specific dynamics of inflation, e.g. its energy scale and the precise shape of the power spectrum, bi-spectrum, etc. it produces. Using our low- k 3D reconstruction of the potential Φ , it will be possible to *reconstruct the inflationary potential over a limited range of φ* . This can be achieved by expanding the potential locally around a fixed $\varphi = \varphi_*$ in terms of the “slow-roll” parameters. We can

⁵At late times (i.e. after the time of BBN) and inside of the horizon, when we use the Newtonian gauge to describe the Newtonian potential Φ , one can think of ζ and Φ interchangably. The main advantage of using ζ during inflation is that, in single-field inflation, the amplitude of its Fourier modes remain constant from horizon exit to horizon re-entry, significantly simplifying their evaluation [15].

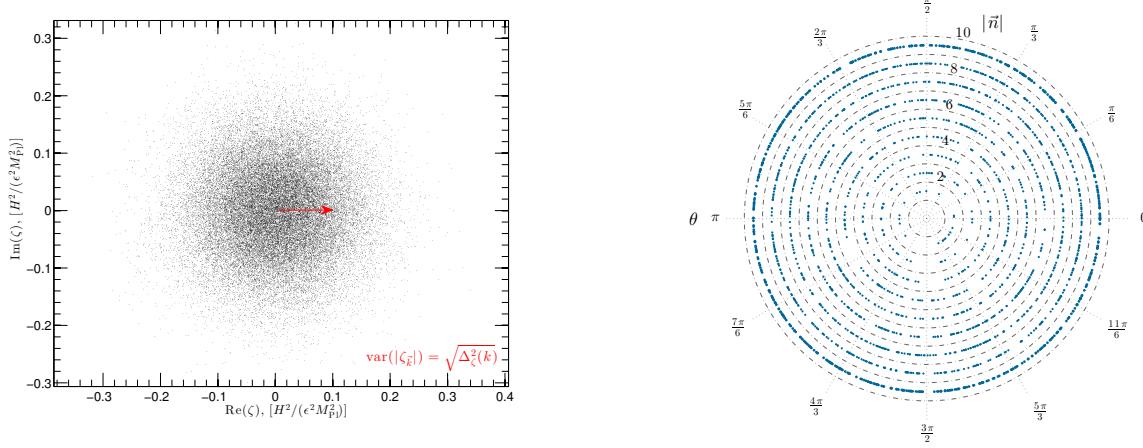


Figure 6: *Left panel:* Distribution of the modes of ζ_k at fixed $|\mathbf{k}|$. *Right panel:* Representation of the norm of the first few k -modes ($|\mathbf{n}|$ from 2 to 10), versus their random spatial angle θ . If the individual modes were clustering around an angle, this would demonstrate that θ is actually not a uniformly distributed random variable, representing a serious challenge for inflation. Regardless of the distribution of θ , observations of Δ_ζ^2 would not be affected.

then define the inflationary hyperparameter vector

$$\vec{\eta} = (H_*^2/\epsilon_*, \epsilon_*, \eta_*, (\eta_2)_*, (\eta_3)_*) , \quad (7)$$

which defines uniquely a shape for the potential around φ_* . Here, the star quantities refer to their values when $\varphi = \varphi_*$. We then infer the probability of a given vector $\vec{\eta}$ given the data a_y , via the potential map f_n , which we marginalize over, as

$$\mathcal{P}(\vec{\eta}|a_y) = \frac{1}{(2\pi)^{p/2}} [\text{Det}(C_{nn'})\text{Det}(C_{yy'})\text{Det } \mathbf{A}_{nn'}]^{-1/2} e^{\left\{ \frac{1}{2} \mathbf{B}_n \mathbf{A}_{nn'}^{-1} \mathbf{B}_{n'} - \frac{1}{2} a_{y'}^\top C_{y'y}^{-1} a_y \right\}} \frac{\mathcal{P}(\vec{\eta})}{\mathcal{P}(a_y)} , \quad (8)$$

where $\mathcal{P}(\vec{\eta})$ is the prior on the hyperparameters $\vec{\eta}$, $C_{n'n}^{-1}$ is a diagonal matrix with diagonal elements given by $1/|\zeta_k|^2$. Note that this generalizes the simple $1/\sigma_n^2$ term in the Gaussian prior introduced above, by relaxing the assumption of fixed spectral index n_s and amplitude α . The \mathbf{A} matrix is defined as above and \mathbf{B} vector are given by:

$$\mathbf{A}_{nn'} = \mathbf{R}_{ny'} C_{y'y}^{-1} \mathbf{R}_{yn'} + C_{nn'}^{-1}, \quad \mathbf{B}_n = \mathbf{R}_{ny'} C_{y'y}^{-1} a_y . \quad (9)$$

Generalizing this analytic formalism to include the inflationary parameters that produce *primordial non-Gaussianities* is straightforward. However, a key assumption in the implementation of the above inference is the assumption of a Gaussian prior for the f_n . To exploit the full information present in data samples containing an increasingly larger range of ℓ modes to look for signs of non-Gaussianity, we will investigate suitable approximations for a non-Gaussian $\mathcal{P}(f_n|\vec{\eta})$. These approximations will need to preserve the computational efficiency of the linear modeling inherent to their Gaussian precursor; this could be achieved via extensions such as Gaussian mixture models, or Gaussian processes, depending on the form of the non-Gaussianity. An alternative route could be to implement the requisite non-Gaussian prior directly, and sample the f_n and the $\vec{\eta}$ using MCMC sampling. Hamiltonian Monte Carlo has been shown to work well in similar situations [36]; Gibbs sampling (as used by the Planck team themselves) could also be a good way to cope with the high dimensionality of the problem [37].

Detailed Approach Incorporating Planck and WMAP Polarization Data: Up to this point, we have only considered the CMB temperature data. We anticipate making significant gains in map fidelity when we incorporate the existing polarization data as well. While these will be more sensitive to systematic effects (such as galactic dust and synchrotron emission), the additional signal to noise alone should allow us to make maps of higher spatial resolution. The prediction of E and B mode CMB polarization at low ℓ from a 3D model potential is more involved compared to the temperature field. Initial simple Monte Carlo ray tracing experiments suggest that this may be an instructive way to capture the dependence of the polarized radiation field on the underlying potential – a challenge will be to capture this in a form that preserves our ability to use only the fast linear inversions described above.

Then, we will carry out an extensive systematic error analysis, assessing sources of contamination from the various foregrounds (using the Planck products as templates) and quantifying the robustness of our results to them. We expect all our inferences to increase in precision as a result of including the polarization information; whether we can reach the commensurate degree of accuracy will depend on both the computational and modeling problems outlined here.

Tree Representation and Non-Parametric Investigation of Gaussianity: There is another way to think about this problem. Let us build up the resolution of the potential on the CMB photosphere by increasing ℓ continuously from zero. Saddle points – designated S – accompanied by extrema – either maxima, designated H, or minima, designated L – will be created. They will be accompanied by fresh separatrices – the contours that pass through the saddles. These come in two types - “lemniscates”, like an infinity symbol, and designated X, and “limaçons”, with the shape of a pinched annulus, and designated K [38]. New separatrices may be created between existing separatrices or out of a contour encircling a *L* or a *H*. Occasionally, the inverse process – annihilation – will occur. If we designate the total number of maxima, minima, saddles, lemniscates and limaçons by N_H, N_L, N_S, N_X, N_K , respectively, then clearly $N_S = N_X + N_K = N_H + N_L - 2$.⁶

The nesting of these contours defines a specific topology which suffices to describe all the equipotentials. It is convenient to represent it using a “tree” containing “forks” (corresponding to separatrices and labeled K or S), and branches terminating on “leaves” (corresponding to extrema and labeled H or L) [40]. There is only one “path” connecting any two leaves. Although our investigation has only begun, it is already clear that the statistics and structure of the tree, satisfy many rules if the underlying fluctuations are truly drawn from a random distribution, for example $N_K \sim N_X$ as $\ell \rightarrow \infty$. We propose to explore this novel approach to testing Gaussianity. We can actually extend this 2D approach on the photosphere to a 3D approach⁷ exploring the nesting of the equipotential surfaces within the photosphere. This leads to similar type of tree. Although these trees are essentially topological, they can only be measured in 3D if there is very careful control

⁶It is also instructive to calculate the Hessian matrix for the potential on the sphere and divide the sphere into “H-zones” (where both eigenvalues are negative), “L-zones” (where they are both positive) and “S-zones” (where they have opposite signs). These “curvature maps” [39] are complementary to the tree representation.

⁷Another generalization that we plan to explore is describe the topological arrangement of the polarization patterns [41].

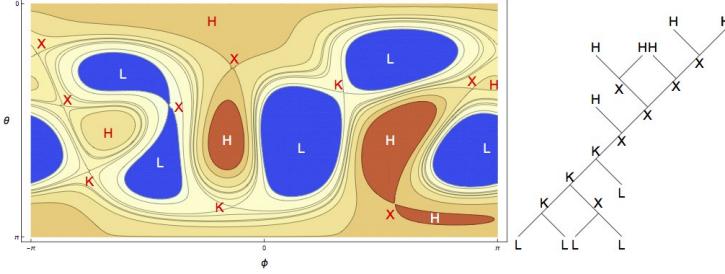


Figure 7: a) Nesting of separatrices for Planck data, with $\ell_{\max} = 4.5$. The extrema, H, L and saddles, K, X are identified. b) Equivalent tree describing the same data.

of the systematics in the data.

2.2 Stage 2. From 3D to 4D: Incorporating Existing “Local” Volumetric Data

At the end of Stage 1, we will have in hand the posterior PDF for the Fourier mode amplitudes of a 3D model of the potential on large scales throughout the observable Universe (and slightly beyond) at the epoch of last scattering. Our main goal in Stage 2 which is the principal object of this proposal is to improve the linear resolution of our map as far as we can. If we now assume a Friedman-Robertson-Walker expansion model, with suitably-parameterized expansion rate and a particular choice of those expansion parameters, we can evolve the Fourier modes of any sample potential map we draw from this PDF forward in cosmic time in order to make posterior predictions about the local $z << 1000$ Universe. The likelihood of these predictions given various observations in the local Universe will allow us to downweight some possible models, and hence further reduce the uncertainty in the map. As we discuss below, the process of combining CMB data with local surveys will not always be as straightforward as this simple picture of prediction and evaluation: Stage 2 of this program will involve investigation of how to carry out the joint inferences robustly and efficiently.

CMB Lensing and ISW Measurements: An important way to add 3D information on the potential throughout a significant fraction of the Universe’s volume is to include the lensing of the CMB [14]. A uniform CMB is unchanged by gravitational lensing. However, if there is a gradient in the background temperature, intervening structure will appear as extra power on the scale of intervening large scale structure.⁸ The consequences are largest on much smaller scales than those in which we are primarily interested. However there are still integral effects with $\ell \sim 30 - 100$ which are relevant. Furthermore the intense interest in the claim that inflationary B-modes have been detected [14] has focused much observational and analytical effort on this region of the spectrum. It is proposed to see if the addition of these measurements will improve the specification of the 3D body modes.

Note that in the case of CMB lensing, it is the same 3D potential model that will be predicting both the lensing effect on the CMB temperature map (due to structures

⁸More subtle manifestations including those involving polarization are possible [42], but this is the main effect.

at $z < 1000$), and also the intrinsic structure in this “background” temperature map (at $z \sim 1000$) itself. The consequence will be a non-linear system, which will need to be treated with care in the inference. The posterior PDF for the Fourier modes will no longer have a Gaussian form, but the weakness of the lensing effect may leave it to be close enough to Gaussian for a simple Gaussian approximation to give sufficient accuracy. This will be the starting point for our research in this area, which may develop into an exploration of better approximations to the posterior PDF for the Fourier modes which retain as much of the computational efficiency as the linear model as possible.

Similar remarks apply to the Integrated Sachs Wolfe effect which is caused by variation in the potential over time, attributable to the cosmological constant (or a “dark energy” component) at late times. It is proposed to see if such measurements can also contribute to the specification of structure on the largest scales.

Galaxy Surveys and the “Local” Universe: Most of the use of galaxy surveys to date has been for drawing statistical inferences relating the growth of structure to the CMB emphasizing shorter length scales, notably those associated with BAO and the largest voids ~ 0.1 Gpc. However, these same surveys can also be used to augment the long wavelength CMB data and improve the accuracy and resolution of the resulting 3D potential map. A good example is the he all-sky survey made by the WISE satellite.⁹ Another example is the SDSS/BOSS program,¹⁰ which covered nearly a third of the sky with over a million redshifts and photometry on galaxies out to $z \sim 0.7$.¹¹ For our purposes this translates to a comoving volume $\sim 50\text{Gpc}^3$, about 0.005 of the total. Surveys of much rarer quasars and the brightest star forming galaxies which extend to $z \sim 6$ provide much greater volumes over which the potential on Gpc scales can be estimated, albeit with inferior precision.

It is helpful at this point to consider a volume limited-survey of objects out to some radius r . Suppose we have a set of objects, (L^* galaxies, quasars, bright, star-forming galaxies ...) with space density n , and we want to measure the amplitude of a given Fourier component with wave vector k of the relative density perturbation associated with this potential $\delta \sim -2k^2\Phi/3a^2H^2$. Now, the accuracy with which the amplitude of a single relative density perturbation Fourier mode can be measured is comparable to the precision with which the fractional density perturbation can be measured in a single region of size equal to the associated length scale. This is $\sim k^{3/2}n^{-1/2}$, and must exceed δ . This suggests that the density of such objects must exceed $\sim H_0^4/c^2\Phi k_{\max}$, and systematic effects must be adequately controlled in order to connect local surveys with the CMB. We propose to carry out a careful study based upon trial data to determine when this is possible. If this is achievable using currently available data, as our exploration so far suggests is the case, then although the data increment will be small, its value will be much greater because it can act as a *phase reference* for anchoring the imperfectly specified modes measured by CMB observations.

One possible starting point for this part of the program could be to focus on existing weak lensing surveys, such as in the 1.5 square degree *HST COSMOS* field [43], sup-

⁹https://www.nasa.gov/mission_pages/WISE/mission/index.html

¹⁰<http://www.sdss.org>

¹¹21 cm redshift surveys provide an important complement to optical surveys but the survey volumes to date are comparatively modest.

plemented by the publically-available 150 square degree *CFHTLens* dataset [44]. These datasets could provide low signal to noise measurements of the long wavelength potential fluctuations along the line of sight to about $z \approx 1$, through a quantitative comparison with our model predictions.

2.3 Stage 3. Posterior Predictions and Ultimate Limits

The final stage of our research program, which is likely to be prosecuted towards the end of this proposal period, will be predictive in character. A fully constrained 4D model of the large scale gravitational potential in the Universe, with well characterized posterior PDF, will enable us to make predictions, with uncertainties, about the density field probed by a number of different upcoming sky surveys and proposed space CMB missions, such as LiteBIRD and PIXIE. Beyond the fundamental scientific importance of making, and so enabling the testing of, such predictions, our map will provide a new tool for the teams analyzing these future surveys. Systematic error control on these large scales is as yet uncharted territory: our 4D potential maps will enable the effective regularization of the analysis of new data on the largest angular scales, and thus potentially provide a higher contrast view of any anomalies present.

Over the next decade, a suite of all-sky (or at least, wide field) cosmological galaxy surveys are planned, including those to be carried out with LSST¹²), DESI¹³, SphereX¹⁴, Euclid¹⁵, WFIRST-AFTA¹⁶, and CHIME¹⁷. We will be able to make predictions about the large scale density of galaxies and clusters of galaxies, as well as the large scale tomographic weak lensing density fluctuations, that will be probed by these surveys.

There is a large effort underway to probe the Epoch of Reionization, (EoR) $6 \lesssim z \lesssim 30$ through hydrogen line measurements, with facilities such as the planned Square Kilometer Array¹⁸ and its precursors. This is an exciting area of discovery, as the relevant physics depends upon many factors, notably the formation of the first stars and galaxies, that are very hard to anticipate. We will be able to make predictions about the large scale structure present in the volume at $6 \lesssim z \lesssim 30$ probed by these surveys. Again, such a prediction should assist in the interpretation of the survey data, and increase the fidelity of the new measurements made there.

It is also of interest to consider the limitations to what could be learned in principle about the idiosyncratic structure of our Universe with *any* conceivable observing facility. The many galaxy and EoR surveys referred to above, combined with CMB lensing and ISW measurement, should ultimately be able to give a quite detailed description of 4D potential. Exactly how detailed the map can be made is an interesting question to ask, and in doing so anticipate being led to new applications of our approach. Any explicit (not just statistical) linkage between large scale structure at recombination and today

¹²<http://www.lsst.org/lsst/>

¹³<http://desi.lbl.gov>

¹⁴<http://spherex.caltech.edu/>

¹⁵<http://www.euclid-ec.org>

¹⁶<http://wfirst.gsfc.nasa.gov>

¹⁷<http://chime.phas.ubc.ca>

¹⁸<https://www.skatelescope.org>

must strengthen investigations into basic physics questions including the properties of dynamical dark energy if it is present. Implicit in our approach is the opportunity to make statements about structure somewhat outside our horizon, predicated on our adopted inflationary model on these large scales. This raises interesting issues of theoretical principle which we intend to try to clarify.

3 Work Plan and Key Milestones

A first paper presenting the low resolution map is nearing completion and should be submitted over the summer. A second paper describing the tree description of nested contours is underway and should be finished in the fall. Essentially all of Stage 1 should be completed by the end of the year and the Stage 2 projects will be underway especially those involving polarization. 2017 will be devoted towards the Stage 2 projects and papers will be written presenting higher resolution maps of the contemporary universe and analyses of inflation. We expect to be able to carry out a series of tests of the self-consistency of the assumption of Gaussianity and random phases which underlies this entire approach. It remains to be seen if this is competitive with alternative approaches based upon the CMB and large scale structure. 2018 will be devoted to completing and writing up the Stage 2 results and starting work on Stage 3.

4 Relevance and Perceived Impact

The research program that we propose has a broad and popular interest, as we have already learned from popular and semi-popular presentations. As our potential map is a 3D object, we will explore the use of 3D printing as well as sophisticated 2D movie representations to exhibit the results. This project also necessarily brings together many disparate research communities both astronomical and statistical. As a consequence, we are developing the statistical machinery for combining the various cosmological datasets in the open, via the GitHub web service at <http://github.com/rogerblandford/Music>, to enable and encourage broad participation.¹⁹ If our approach is fruitful, we believe that it may be of value to other investigations. It will certainly help disseminate our 3D models and 2D posterior predictive distributions, in the interest of those working in other big dataset visualizations: interactive presentation of these products via IPython notebooks is ongoing, and can be supplemented by screenshared video recording to provide a narrative for a wider audience.

Blandford, Marshall and Perreault Levasseur all regularly give public presentations on cosmology and other topics, and are looking forward to including more of this material in future outreach activity.

¹⁹Program collaborator Marshall has worked in this way on other projects that lend themselves to this approach, most notably a recent Annual Reviews article on Ideas for Citizen Science in Astronomy [46], and the Space Warps citizen science project [47].

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Professor at the Stanford Linear Accelerator Center.

Professional Preparation

B.A. (Theoretical Physics), Cambridge, 1970
M.A. (Astronomy), Cambridge, 1973
Ph.D. (Applied Mathematics), Cambridge, 1973

Previous Appointments

2003 - 2013 Pehong and Adele Chen Director Kavli Institute for Particle Astrophysics and Cosmology
1992 - 1995 Executive Officer for Astronomy, Caltech
1989 - 2004 Richard Chace Tolman Professor Theoretical Astrophysics, Caltech
1979 - 1989 Professor, Caltech
1976 - 1979 Assistant Professor, Caltech
1973 - 1976 Research Fellow, St. John's College, Cambridge
1972 - 1973 Charles Kingsley Bye Fellow, Magdalene College, Cambridge

Societies

Fellow Royal Astronomical Society (1974)
Fellow of Royal Society (1989)Fellow of American Academy of Arts and Sciences (1993)
Member National Academy of Sciences (2005)
Fellow of American Physical Society (2010)

Synergistic Activities

Chair Astronomy and Astrophysics Decadal Survey (2010)
Chair: NSF Astronomy Senior Review Committee (2007)
Chair: American Astronomical Society, High Energy Astrophysics Division (2004-5)
Annual Reviews Astronomy and Astrophysics Editor (2002-4), Managing Editor (2005-10)
Instigator and co-organiser of First NSF-ITP Workshop for High School Physics Teachers (2001)
Instigator of and original lecturer for Caltech Core Curriculum course for freshman not intending to study astronomy: "The Evolving Universe" (2000)
Co-author (with K. Thorne) of graduate text: "Modern Classical Physics (2015, in press)

Selected Recent Publications

- Collett, T., et al. 2013 MNRAS 418 3183
Greene, Z. et al. 2013 ApJ 768
Hezaveh, Y., Marshall, P. & Blandford, R. 2014 ApJ submitted.
Morganson, E. et al 2010 MNRAS 406 2452
Oguri, M. et al. 2013 MNRAS 429 482
Ota, N. et al 2102A&A 547 A77
Suyu, S. 2010, ApJ 711 201
Suyu, S. et al. 2014 ApJ 788 L35
Thorne, K. & Blandford, R. 2015 Modern Classical Physics Princeton University Press
von der Linden, A. et al. 2014 MNRAS 439 2

Recent Collaborators

E. Agol, S. Allen, A. Broderick, M. Begelman, P. Coppi, C. Fassnacht, L. Koopmans, M. Lyutikov, M. Malkan, D. Rappetti, Y. Rathore, S. Suyu. T. Treu, M. Bietenholz, R. Buehler, P. Eggleton, S. Funk

Recent Graduate Students

P. Simeon, M. Amin, C. Zheng, E. Morganson, J. Dai, Y. Yuan, R. Anantua.

Recent Postdoctoral Scholars

P. Marshall, M. Oguri, L. Stawarz, W.

PhD Adviser

M. Rees

PHIL MARSHALL

Professional Preparation

University of Cambridge	Natural Sciences (Physics)	B. A. (Hons.) M. Sci. (class I), 2000
University of Cambridge KIPAC, SLAC	Astrophysics Observational Cosmology	Ph. D. ("Bayesian Analysis of Clusters of Galaxies,"), 2004 KIPAC Fellow, 2003–2006
Physics Dept., UCSB	Observational Cosmology	TABASAGO Fellow, 2006–2009
KIPAC, Stanford University	Observational Cosmology	Kavli Fellow, 2009–2010

Appointments

6/2013–onwards	Staff Scientist, SLAC National Accelerator Laboratory (Kavli Institute for Particle Astrophysics and Cosmology)
10/2010–5/2013	Royal Society University Research Fellow Department of Physics, University of Oxford

Selected Publications

1. Schneider, M. D., ..., **Marshall, P. J.** et al
Hierarchical probabilistic inference of cosmic shear
ApJ accepted, 2015. <http://arxiv.org/abs/1411.2608>
2. Brewer, B. J., **Marshall, P. J.** et al
The SWELLS survey - VI. Hierarchical inference of the initial mass functions of bulges and discs
MNRAS, **437**, 1950, 2014. <http://arxiv.org/abs/1310.5177>
3. Suyu, S. H., ..., **Marshall, P. J.** et al
Cosmology from gravitational lens time delays and Planck data
ApJ, **788**, 35, 2014. <http://arxiv.org/abs/1306.4732>
4. Collett, T. E., **Marshall, P. J.**, et al
Reconstructing the lensing mass in the Universe from photometric catalogue data
MNRAS, **432**, 679, 2013. <http://arxiv.org/abs/1303.6564>
5. Ivezić, Z., ..., **Marshall, P. J.**, and the LSST Collaboration.
LSST: from Science Drivers to Reference Design and Anticipated Data Products
<http://arxiv.org/abs/0805.2366>,
6. **Marshall, P. J.** et al
Space Warps – I. Crowd-sourcing the Discovery of Gravitational Lenses
MNRAS accepted, 2015. <http://arxiv.org/abs/1504.06148>
7. Sonnenfeld, Alessandro, ..., **Marshall, P. J.** et al
The SL2S Galaxy-scale Lens Sample. V. Dark Matter Halos and Stellar IMF of Massive ETGs out to Redshift 0.8
ApJ, **800**, 94, 2015. <http://arxiv.org/abs/1410.1881>
8. Busha, M. T., **Marshall, P. J.**, et al
The Mass Distribution and Assembly of the Milky Way from the Properties of the Magellanic Clouds

9. Oguri, M., & **Marshall, P.J.**
Gravitationally lensed quasars and supernovae in future wide-field optical imaging surveys
MNRAS, **405**, 2579, 2010. <http://arxiv.org/abs/1001.2037>
10. Suyu, S., **Marshall, P. J.**, Hobson, M. P. & Blandford, R. D.
A Bayesian analysis of regularised source inversions in gravitational lensing
MNRAS, **371**, 983, 2006. <http://arxiv.org/abs/0601493>

Synergistic Activities

2015–	Stanford Physics Graduate Lecture Course Leader, “Statistical Methods in Astrophysics”
2014–	Organizer and Lecturer, “Astro Hack Week”
2012–	Co-Principal Investigator, “Space Warps” citizen science project
2011	Workshop Organiser, “Cosmology Meets Machine Learning,” NIPS, Granada, Spain.
2010–	Outreach Coordinator, University of Oxford Astrophysics Group and KIPAC

Collaborators and Affiliations

Collaborators (**principals in bold**):

Abbott, T., Abdalla, F. B., Adami, C., Aghamousa, A., **Aguello, A.**, Ajello, M., Allam, S., Amin, M. A., Annis, J., Armstrong, R., Auger, M. W., Baeten, E., Bamford, S., Banerji, M., **Bard, D. J.**, **Barnabè, M.**, Barone-Nugent, R., Basa, S., Bastieri, D., Belles, P.-E., Benoist, C., Benoit-Lévy, A., Bertin, E., Beswick, R., Bisiglio, A., **Blandford, R. D.**, **Bolton, A. S.**, Bonvin, V., Bosch, J., Boutigny, D., Bradley, L. D., **Brewer, B. J.**, Briain, D. Ó., Brooks, D., Brownstein, J. R., Buckley-Geer, E. J., Bulmash, D., Burgett, W. S., Burke, D. L., Cappi, A., Carretero, J., Chambers, K. C., **Chan, J. H. H.**, Chekhtman, A., **Cheung, C. C.**, **Chiang, J.**, Chiueh, T., Cipriani, S., **Clowe, D.**, Coles, J., **Collett, T. E.**, Corbet, R. H. D., Cornen, C., Coupon, J., Courbin, F., Cox, B. E., Cunha, C. E., Cyriano, E. S., Czoske, O., D'Ammando, F., D'Andrea, C. B., **Dawson, W. A.**, Desai, S., Diehl, H. T., Dietrich, J. P., **Dobler, G.**, Doel, P., Donnarumma, A., Durret, F., **Dutton, A. A.**, Eifler, T. F., Erben, T., Erickson, N. J., Estrada, J., Falco, E. E., **Fassnacht, C. D.**, FenechConti, I., Finley, D., Flaugher, B., Fletcher, L. N., Fortson, L., Fosalba, P., Frieman, J., Garrington, S., **Gavazzi, R.**, **Geach, J. E.**, Gentile, M., Gerdes, D. W., Gill, M. S. S., Giroletti, M., Green, P. J., Grove, J. E., Gruen, D., Guennou, L., Gutierrez, G., Halliday, C., Harrison, P. A., Harrington, K., **Hezaveh, Y. D.**, **Hilbert, S.**, **Hogg, D. W.**, Hojjati, A., Honscheid, K., Huff, E. M., Hughes, D. H., Ilbert, O., Ivison, R. J., Jackson, N., James, D. J., Gee, M. J., Johnston, D., Jordan, C., **Jullo, E.**, Just, D., Kacprzak, T., Kaiser, N., Kapadia, A., Kashyap, V., Kaviraj, S., Kelly, B. C., Kilbinger, M., Kind, M. C., **Kneib, J.-P.**, **Koopmans, L. V. E.**, Kubo, J. M., Kuehn, K., Kuntzer, T., Kuropatkin, N., Küng, R., Lahav, O., **Lang, D.**, Larsson, S., LeBrun, V., Leauthaud, A., **Liao, K.**, LimaNeto, G. B., Lima, M., Limousin, M., **Linder, E.**, **Lintott, C. J.**, Lin, H., Lin, Y.-T., Lott, B., Luo, W., **Lynn, S.**, Macmillan, C., Magnier, E. A., Maia, M. A. G., Makler, M., Mamon, G. A., Mandelbaum, R., Mandel, K., March, M. C., Marshall, J. L., Martinet, N., Martini, P., Mason, C. A., Masters, K. L., Maurogordato, S., Mazure, A., McKean, J., McMahon, R. G., Melchior, P., Melvin, T., Meng, X.-L., Metcalf, R. B., **Meyers, J. E.**, Meylan, G., Miller, C. J., Miller, G., Miller, L., Miquel, R., Miyatake, H., Montaña, A., Montero-Dorta, A. D., **More, A.**, **More, S.**, **Morganson, E.**, Morgan, J. S., **Moustakas, L. A.**, Mujica, R., Murphy, K. J., Muxlow, T., Márquez, I., Nakajima, R., Narayanan, G., Neto, A. F., NgoléMboula, F. M., Nichol, R. C., Nipoti, C., Nurbaeva, G., O'Brien, T., Odermatt, J., Ogando, R., **Oguri, M.**, Ojha, R., Okura, Y., Orienti, M., Ostrovski, F., Paget, E., Pandey-Pommier, M., Parrish, M., Paulin-Henriksson, S., Perkins, J. S., Plana, H., Plazas, A. A., Prabhu, T. P., Price, P. A., RathnaKumar, S., Razzano, M., Reil, K., Rhodes, J., Rix, H.-W., Romero-Wolf, A., Romer, A. K., Roodman, A., Rosell, A. C., Ross, N. P., Rostagni, F., Rowe, B., **Rozo, E.**, Rumbaugh, N., Russeil, D., Rusu, C. E., Rybak, M., **Rykoff, E. S.**, **Saha, P.**, Sako, M., Sanchez-Argüelles, D., Sanchez, E., Santiago, B., Scargle, J. D., Scarpine, V., Schawinski, K., Schechter, P. L., Schirmer, M., Schlafly, E. F., Schloerb, F. P., **Schmidt, K. B.**, **Schneider, M. D.**, Schrabback, T., Schubnell, M., Serjeant, S., Sevilla-Noarbe, I., Shafieloo, A., Shan, H., Sheldon, E. S., Shu, Y., Siemiginowska, A., Simet, M., **Simmons, B. D.**, **Simpson, R.**, Skibba, R. A., Slezak, E., Smethurst, R. J., Smith, A. W., Smith, R. C., Snyder, C., Soares-Santos, M., Sobreira, F., **Sonnenfeld, A.**, Spinelli, C., Stalin, C. S., Starck, J.-L., Stiavelli, M., Suchyta, E., Sureau, F., **Suyu, S. H.**, Swanson, M. E. C., Tak, H., Tarle, G., Tecza, M., Tewes, M., Thaler, J., Thompson, D. J., Tonry, J. L., Trenti, M., **Treu, T.**, Tucker, D., Ulmer, M. P., VanWaerbeke, L., Veggetti, S., **Verma, A.**, Viero, M., Walker, A. R., Walter, F., Wang, W.-H., **Wechsler, R. H.**, Wilcox, J. K., Willett, K. W., Wilson, G. W., Wood, D. L., Wood, K. S., Wyithe, S., Yun, M. S., ZarbAdami, K., Zaritsky, D., Zeballos, M., Zhang, J., Zhang, Y., Ziegler, B., Zuntz, J.

Graduate Advisor and Postdoctoral Sponsors: Michael Hobson (University of Cambridge); Roger Blandford (KIPAC), Tommaso Treu (UCLA), Roger Davies (Oxford).

Thesis Students Mentored: Sherry Suyu (ASIAA), Eric Morganson (NCSA/UIUC), Elisabeth Newton (CfA), Chi-hway Chang (ETH Zurich), Thomas Collett (Portsmouth), Alessandro Sonnenfeld (Kavli IPMU), Kai Liao (Wuhan), Nick Rumbaugh (UC Davis).

Table of Personnel and Work Effort

This work will be primarily a collaboration between the PI and the collaborator Dr.\ Phil Marshall, who is currently a Staff Scientist at SLAC and one of the LSST Dark Energy Science analysis working group conveners. It is proposed to support a postdoctoral fellow, Laurence Perreault Levasseur to work on this project half time for two years. As we are conducting this research in open view, we expect to attract additional collaborators and several local colleagues have already expressed interest in it. We are considering recruiting a graduate student in the fall to join us on this project. Already an excellent junior undergraduate has expressed interest in joining immediately. Both would be supported by Stanford/KIPAC funds.

Blandford will start by taking the lead experimenting with the simulation of potential maps and then CMB temperature and polarization maps and finally using the publicly released Planck temperature and polarization data to do the best job we can on this data alone. Meanwhile, Marshall will lead the consideration of existing local surveys, including those listed above, and work on addressing the underlying Bayesian inference problems posed by combining them with CMB data. Perreault Levasseur is has begun preliminary work on the connection to inflation and intends to participate fully in developing the new statistical approaches.

Current and Pending Support
Investigator: Roger Blandford

Current Support

No Current Support

Pending Support

Project/Proposal Title: On the Acceleration, Propagation and Radiation of High Energy Particles

Source of Support: NASA

Total Award Amount: \$747,753.00

Award Period Covered: 01 July 2015 – 30 June 2018

Location of Project: Stanford University

Person-Months Per Year Committed: 0.5

Project/Proposal Title: Disentangling Signatures of Ultra-high-energy Cosmic Rays from a Unique Gamma-Ray Blazar

Source of Support: Space Telescope Science Institute

Total Award Amount: \$50,960.00

Award Period Covered: 01 October 2015 – 30 September 2016

Location of Project: Stanford University

Person-Months Per Year Committed: 0

Project/Proposal Title: The Music of the Sphere: Reconstructing Large Scale Structure from the Cosmic Microwave Background and Galaxy Surveys

Source of Support: NASA

Total Award Amount: \$257,873.00

Award Period Covered: 01 June 2016 – 31 May 2019

Location of Project: Stanford University

Person-Months Per Year Committed: 0.5

Project/Proposal Title: Hubble Frontiers Field- Incorporating Multi-Wave Length Observations and Line of Sight Corrections

Source of Support: Space telescope Science Institute

Total Award Amount: \$98,008.00

Award Period Covered: 15 May 2016 – 30 September 2017

Location of Project: Stanford University

Person-Months Per Year Committed: 0.5

Budget Narrative: Stanford

PI Roger Blandford

Salary:

We request .5 month of summer in each year for PI Blandford who will supervise and mentor post Dr. Levasseur.

We request 6 months of salary in each year for postdoc Dr. Levasseur who has already built a pipeline capable of analyzing the lowest l CMB data and successfully recovering a low resolution three-dimensional map of the Universe. Expanding this pipeline to higher multipoles will require a better understanding of the subtle systematics of the CMB data and galaxy surveys. Building on her past successes and with the mentoring of PI Roger Blandford, she will be developing these extensions and incorporating these effects into the existing pipeline. She will further develop the numerical tools that will allow our analysis to relax the assumption of primordial Gaussianity of the inflationary fluctuations.

Travel:

Travel costs are estimated based on current online flight prices for return coach air-fares and State Department per diem values (<http://www.gsa.gov/perdiem>) plus applicable taxes, assuming 3% annual inflation, and using 75% per diem rate for the first and last day.

We request funds to attend an AAS meeting or equivalent. We estimate the costs as: return flight SFO-TX \$600, ground transportation to/from airports \$100, lodging/M&IE \$149/59 per day; total cost approximately \$1,354.

For our second domestic travel, we request funds for attendance at one conference in the domestic US, to present the results of the work. This far in advance, it is not possible to say definitively which conference this will be. For planning purposes, we use the example of the 16th meeting of the High Energy Astrophysics Division (HEAD; <http://head.aas.org/meetings>) of the American Astronomical Society (AAS), to be held at Jackson Hole, Wyoming, August 16-20, 2017. We estimate the costs as: early registration for non-AAS member \$600; \$600 and \$100 for return coach airfare and ground transportation (respectively); lodging/M&IE \$184/76 per day; total cost approximately \$2,640.

Total travel cost for all years is \$8,054.

The total Stanford budget request is approximately \$188,845 for all years.

Data Management

The primary dataset that is being used for this project derives from the Planck satellite. The data sets that are needed have already been downloaded and used to infer the results so far that we describe. Two leading Planck scientists have been advising us on occasional queries. As our interest is confined to low l modes, the overall computing needs have been modest so far.

The generalization to include additional date sets and more complex MCMC searches will be more demanding but well within the scope of the computational resources to which we have access. There is local expertise, which we intend to tap, on essentially all of the surveys that we shall use with the important exception of WISE where we intend to consult with senior members of the research team.

Facilities and Equipment: Stanford

All the facilities required to carry out this investigation are already in place.

High Performance Computing Resources

Data analysis will be carried out using the KIPAC Opteron cluster (100 nodes, each with 8 cores and 32GB RAM), an in niband-connected machine designed for large-scale parallel computation. Disk space to store the large amounts of data that will be handled by this project are available. The latest versions of the calibration databases, reduction pipelines, and analysis software are in place.

KIPAC researchers also have access to general SLAC computing resources (this includes several hundred batch machines).