

In situ 3D observations of capillary-driven flows in parallel arrangements of rigid fibres using X-ray microtomography



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ABSTRACT

Capillary-driven impregnation phenomena occurring in fibre bundles during the processing of composite materials are complex and still not fully understood. Hence, synchrotron X-ray microtomography was used to characterise the longitudinal propagation of the flow front within a parallel arrangement of rigid fibres. The analysis of 3D images enabled the fluid-air interface curvatures, triple line lengths, and local contact angles to be quantified during wetting and dewetting experiments. The results showed that even in quasi-static situations, local contact angles exhibited significant variations along the fibres. These variations also depended on the wetting/dewetting state. The transverse capillary forces measured at the fibre scale from the analysis of 3D images were shown to be of the same order of magnitude as the longitudinal capillary forces. Local curvatures of the fluid-air interface and the resulting estimate of the average capillary pressure proved the relevance of a mesoscale capillary pressure model adapted for fibre bundles.

1. Introduction

Fibre-reinforced polymer composites are increasingly used to produce structural or multi-functional parts for several industrial domains. High-performance composite parts are usually fabricated using liquid composite moulding (LCM) wet-forming processes [1]. In these processes, an impregnation phase of the fibrous reinforcements is required [1,2]. Impregnation consists in the flow of a liquid polymer matrix through a fibrous reinforcement, i.e. within an anisotropic, deformable, and multiscale porous medium made of more or less ordered networks of fibre bundles or yarns [1,2]. Impregnation usually involves the displacement of a non-wetting fluid (air) by a wetting fluid (fluid polymer). In wet-forming processes, the flow of the fluid polymer is induced by either a pressure gradient applied by an injection system, or capillary forces or a combination of both [1,2].

A poor control of the impregnation phase can lead to the onset of several defects such as porosity that are detrimental for the mechanical properties of the composite parts [3–5]. Several studies have shown that capillary effects can significantly affect the propagation of the polymer-

air interface, the geometry of which can become extremely irregular, leading to the formation of pores at various scales [2,4,6]. Capillary phenomena depend on several parameters related to the fluid surface tension, fibre wettability properties (surface energy), contact angle, architecture of the fibre reinforcements (fibre volume fraction), as well as the directionality of the fluid flow with respect to their anisotropy axes, and fluid front velocity (interplay between capillary and viscous effects). In multiscale fibre reinforcements such as reinforcement fabrics, a poor control of capillary-driven phenomena can lead to large differences between the fluid propagation velocity within and between fibre bundles that often result in extreme distortion phenomena of the flow front [3,5,7,8]. To limit the distortion of the flow front and the formation of pores, it is crucial to finely predict the effects of capillary phenomena on the flow of liquid polymer within fibre bundles, i.e. one-dimension fibrous structures made of quasi parallel fibres [9,10].

The study of the impregnation of fibre bundles was the subject of many research efforts [10–14]. Several experiments based on the Wilhelmy method (initially used to study wettability [15], wetting dynamics [16] and more recently surface energy [17] of individualised

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fibres) were performed to study longitudinal and transverse capillary-driven flows within fibre bundles [18,19]. These experiments consisted of immersing fibre bundles in a test fluid to draw the fluid upward by capillary forces. Measurement of height rise at various times was then related to the fluid surface tension, contact angle and permeability of the fibre bundles. In addition, the fluid propagation in fibre bundles was studied using magnetic resonance imaging (MRI) measurements [20]. This technique enabled detecting variations in fluid concentration and thus the formation of voids/pores during the impregnation of fibre bundles [21]. X-ray radiography was also used to track the propagation of the fluid within fibre bundles [22]. The 2D information provided by this technique was very useful to better understand how the fluid propagated but did not allow the fluid-air interfaces to be finely observed and described. Recently, several studies used 3D X-ray microtomography images to monitor the infiltration process of industrial fibre bundles [23–25]. These studies revealed the formation of preferential flow channels and important fibre re-arrangements associated to variations in the fibre volume fraction. An estimate of the fluid-fibre contact angle was also given through the analysis of the 3D images. However, this parameter was measured only in particular zones using 2D cross sections of the 3D X-ray microtomography images [24,25]. In parallel, several studies that were carried out with granular and porous materials showed that it was possible to measure in 3D several interesting local parameters such as the local contact angles [26–29], local

mean curvatures [30–33] of the interfaces between the wetting and non-wetting phases. For that purpose, 3D high-resolution images that enabled a good description of the geometry of the solid, fluid phases and interfaces were needed.

In this context, the objective of this study was to follow in 3D the fluid front propagation and distortion that occurred during the capillary-driven impregnation of a model fibre network using similar image analysis procedures than those reported for granular materials [26–33]. Note that to establish a relevant methodology, we have first worked on a simplified fibre network made of ordered and parallel millimetre rigid glass tubes/fibres in order to be able, in future studies, to apply this methodology on industrial fibres or fibre bundles made of disordered flexible fibres with smaller diameters and/or irregular cross sections. This approach enabled mimicking the structure of a real fibre bundle used in composite materials while enabling high-resolution 3D synchrotron X-ray microtomography images to be acquired. For that purpose, several wetting and dewetting stages of the fibre network were imaged using a specially developed impregnation device that was installed on an X-ray microtomography beamline. Thanks to the good compromise between the tube diameter and the spatial resolution of the 3D images, it was possible using specific image analysis procedures to make quantitative measurements of the variations of the local mean curvatures of the fluid-air interface, local contact angles, and lengths of the triple lines. Then, using this database, we estimated the local

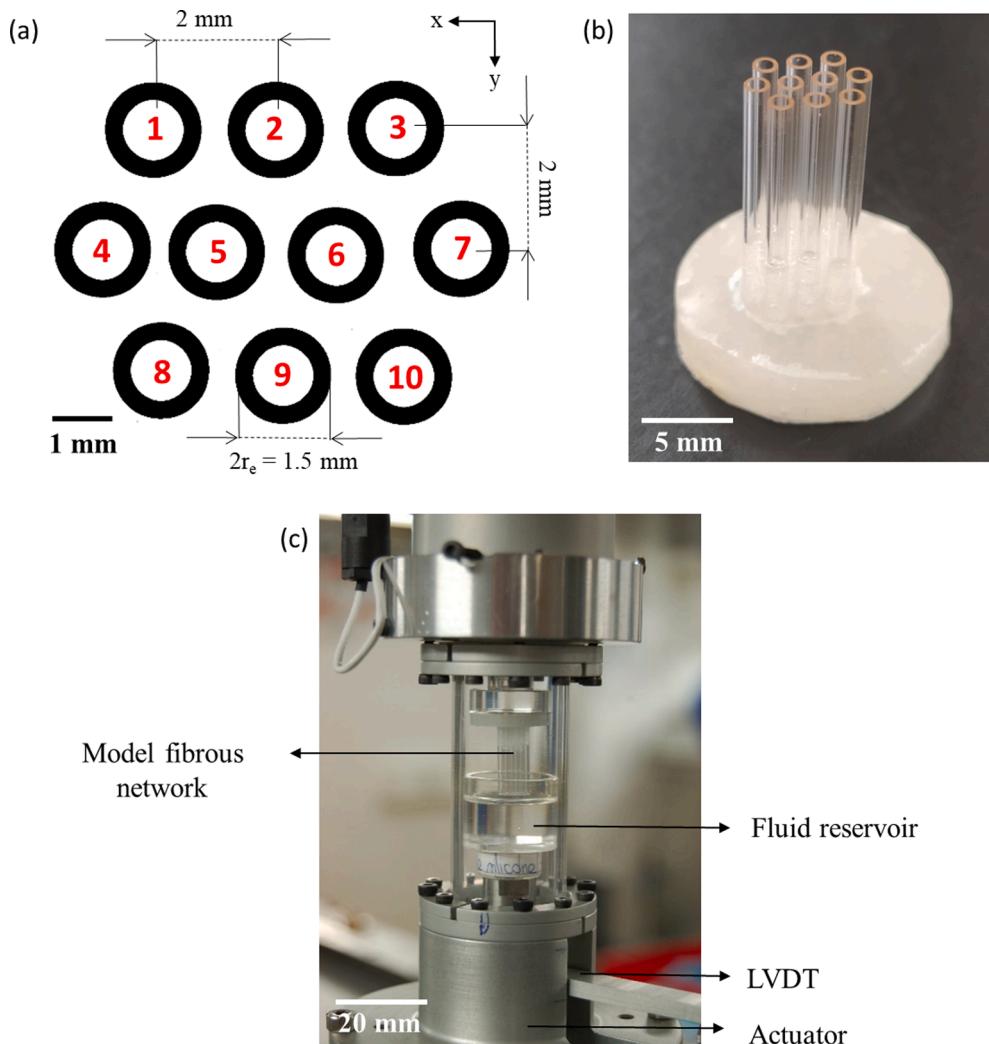


Fig. 1. (a) Scheme of the geometry of the fibre network composed of ten tubes arranged with a triangular geometry. A reference number was attributed to each tube of the fibre network. (b) Photograph of a specimen of fibre network that shows the tube arrangement fixed in a plastic part. (c) Photograph of the micro impregnation device.

capillary pressure and the local transverse and longitudinal capillary forces exerted by the fluid on each tube of the fibre network.

2. Materials and methods

2.1. Model fibre networks and impregnation fluids

In this study, several specimens of a fibre network were fabricated. This fibre network was made of parallel hollow glass tubes (Hirschmann, Eberstadt Germany) with an external radius $r_e = 0.75$ mm and an internal radius $r_i = 0.50$ mm. The tubes had a length $L = 16$ mm and were sealed at their top extremity with an epoxy glue to prevent the rising of the liquid inside the tubes. The network was composed of ten tubes arranged in a triangular geometry (Fig. 1a,b). The centrelines of each tube were spaced 2 mm apart from each other to form isoscele triangles. The top extremities of the tubes were fixed in a disk made of a plastic resin. To clean the surface of the tubes, the fibre networks were plunged for 1 min inside an ultrasonic bath that was filled with acetone (ACS reagent, Sigma Aldrich).

Two Newtonian fluids with controlled rheological and surface tension properties, namely demineralised water and a silicone oil (47 V1000–80026, Chimie-Plus Laboratoires), were used for the impregnation experiments of the aforementioned fibre network. The shear viscosities η , densities ρ and surface tensions γ_b as well as the tube/fluid static contact angles θ_s of these fluids are given in Table 1. Regardless of the fluid, the static contact angle θ_s was less than 90° , showing that the tube surface can be wetted by both types of fluids.

The Bond number B_o was estimated as r_e^2/λ_c^2 (where $\lambda_c = \sqrt{\frac{\gamma_b}{\rho g}}$ is the capillary length) for the impregnation experiments of the fibre network. $B_o = 0.25$ and $B_o = 0.08$ for the silicone oil and demineralised water, respectively, which shows that the capillary effects were predominant compared to the gravity effects, i.e., fluid menisci are formed around the tubes of the fibre network. It is also important to note that the mean separation distance $2\bar{d}$ between adjacent tubes of the fibre network shown in Fig. 1a, was chosen to have \bar{d}/λ_c close to 1 for both types of fluids. This separation distance $2\bar{d}$ enables a capillary-driven rising of the fluids within the fibre network.

2.2. In situ impregnation experiments and X-ray microtomography conditions

In situ impregnation experiments of the fibre network were performed using a specially designed setup, as shown in Fig. 1c. The setup was composed of an actuator [34,35] that allowed moving vertically, upwards or downwards, a PMMA reservoir (inner diameter = 18 mm) fixed on it and filled with the impregnation fluid. The vertical position of the reservoir was controlled using a high precision linear variable differential transformer (LVDT) with an accuracy of ± 0.02 mm. The fibre network was fastened on the upper part of the impregnation device. The fibre network and the reservoir were placed inside a transparent cylindrical part made of PMMA fastened to the frame of the actuator. The impregnation device was installed on the rotation stage of a synchrotron X-ray microtomograph (ID19 beamline, ESRF, Grenoble, France) to perform *in situ* impregnation experiments. They consisted of plunging or withdrawing the fibre network in the fluid, moving at different heights

the level of the fluid reservoir using a low translational velocity $v \approx 5$ $\mu\text{m/s}$, while taking 3D images of the experiments.

Two types of experiments were performed, namely interrupted and sequentially continuous impregnation scanning conditions. The fibre network impregnated with the silicone oil was scanned using interrupted conditions, i.e., the vertical displacement of the reservoir was interrupted at certain positions and after a resting time $\Delta t > 5$ min, a 3D image was acquired. Six different positions or impregnation steps were investigated, moving upwards or downwards the fluid reservoir. The fibre network impregnated with demineralised water was scanned using sequentially continuous conditions. The scans were done while the fluid reservoir was moving upwards or downwards. Six different impregnation steps were studied. During the motion needed to reach every position, a sequence of ten 3D images, corresponding to a total scanning time of approximately 20 s, was taken, thereby allowing *in situ* 3D observations of the impregnation phenomena occurring within the fibre network.

To acquire 3D X-ray microtomography images of these experiments, the following imaging conditions were used. The X-ray energy and the number of radiographs (dimensions of the images: 1584×1584 pixels) were set to 36.6 keV and 800, respectively. The exposure time of each radiograph was 2 ms and the scan duration less than 2 s. From the radiographs, 3D images with a voxel size of $5.1^3 \mu\text{m}^3$ were reconstructed using the so-called Paganin procedure to enhance phase contrast in the images [36]. These ultrafast acquisition conditions and image resolution allowed obtaining an accurate representation of the tubes and the fluid front propagation, while having a sufficiently large field of view. Note that the acquisition parameters, and in particular the image spatial and time resolution, could be adjusted in future studies to analyse impregnation phenomena occurring in industrial fibrous media made of disordered compliant fibres with smaller diameters and faster impregnation characteristic times [35,37].

The capillary number C_a related to the impregnation experiments was estimated as $\frac{\eta v}{\gamma_b}$. For the experiments performed with silicone oil (resp. demineralised water) $C_a \approx 2 \times 10^{-4}$ (resp. $C_a \approx 8 \times 10^{-8}$), thus showing that in both cases the surface tension effects were largely predominant compared to the viscous effects. Hence, both imaging conditions can be considered as delivering 3D images of a sequence of quasi-static states of the flow front propagation governed by the capillary effects.

2.3. 3D image analysis

2.3.1. Identification of the triple lines

After proper segmentation of the 3D images using Fiji [37] as described in Fig. 1 in S1, we developed a procedure to identify the triple lines that formed on the external surface of the tubes between the fluid, tube and air phases. The identification was applied on each tube of the fibre network and consisted in several steps. For that purpose, a “crop” operation was performed on the full 3D images to obtain sub-volumes centred on the tube axes (dimensions of the sub-volumes: $400 \times 400 \times 900$ voxels). Then, the inner cavity of each tube was “filled” using the “Fill holes” function of Fiji [38] (see Fig. 2). 3D dilation operations were then performed for each phase of the sub-volumes using the plugin Analysis 3D. Fig. 2b illustrates this operation, showing in red the phase that was subjected to 3D dilation and cross-sections of the

Table 1

Properties of the two fluids used for the impregnation experiments. These properties were measured at a temperature $T = 23$ °C. The static tube/fluid contact angle θ_s was measured by plunging a single glass tube in the considered fluid using a Krüss tensiometer and applying a correction for the buoyancy force [15]. Note also that the tensiometer was equipped with an optical visualisation setup similar to that described in [16], thus allowing the 2D observation of the static tube/fluid contact angle. The static tube/fluid contact angles θ_s deduced from the Wilhelmy method were close to those estimated from the acquired 2D images.

Fluid	Surface tension γ_b (mN m^{-1})	Static tube/fluid contact angle θ_s (°)	Shear viscosity η (mPa s)	Density ρ (g cm^{-3})
Demineralised water	72.8 ± 0.1	47 ± 5	1	1
Silicone oil	21.1 ± 0.1	20 ± 2	970	0.97

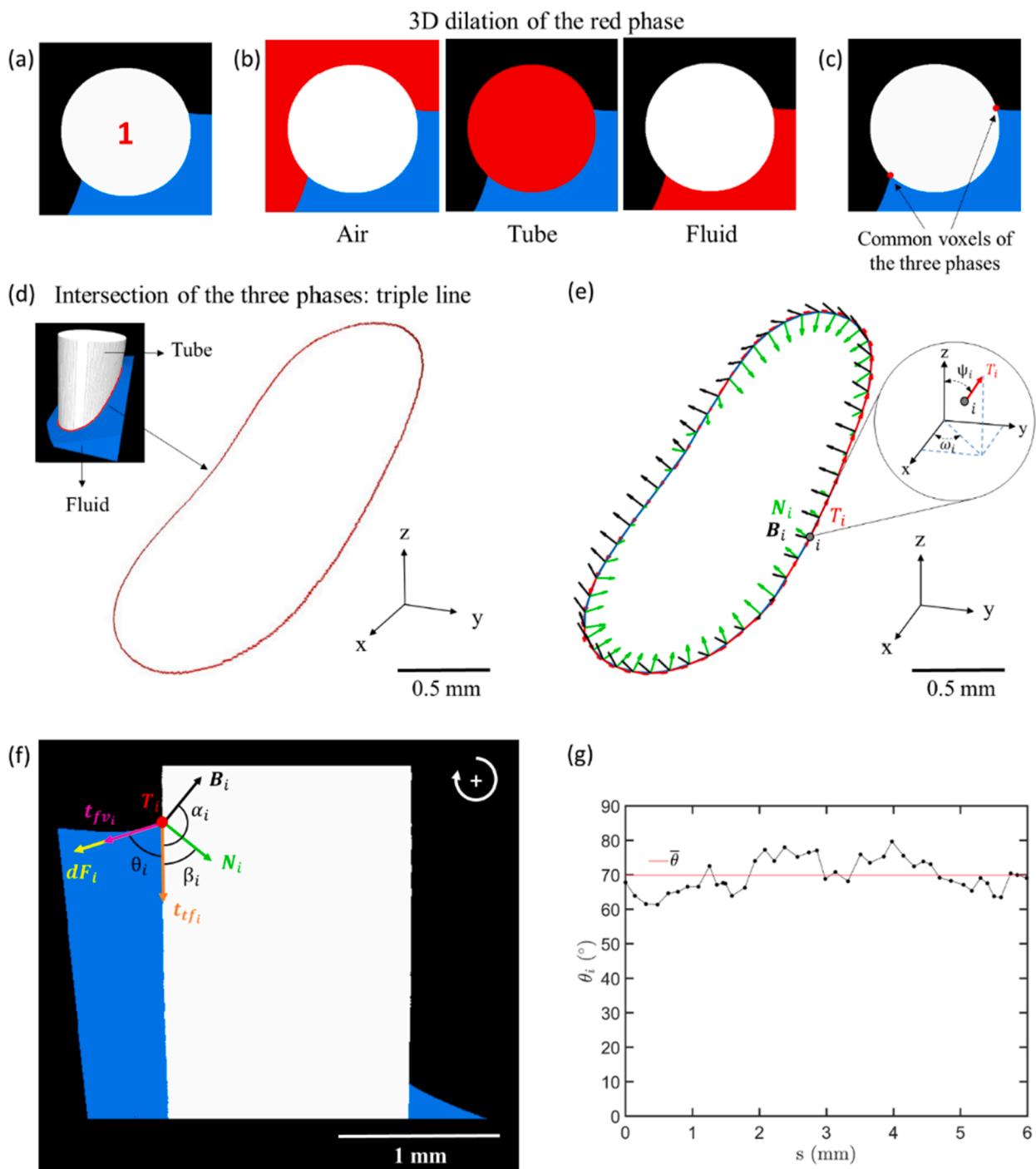


Fig. 2. Procedure used to identify the triple lines and to measure the local contact angles. (a) View of a horizontal cross section of a trinariised 3D sub-volume centred on the axis tube n°1 of the fibre network. (b) Same images showing the results of the 3D dilation operations that were performed on the air, tube and fluid phases. (c) Same image as (a) showing in red the voxels belonging to the air, tube and fluid phases and corresponding to voxels belonging to the triple line. (d) 3D view of the corresponding triple line. (e) Smoothed linear parametric representation of the triple line with the local Frenet bases (T_i, N_i, B_i) associated to each elementary discretisation segment i . (f) View of a cross section in a (N_i, B_i) plane of the 3D sub-volume and associated tangent vectors to the tube-fluid and fluid-air interfaces as well as the local contact angles θ_i . The arrow shows that a clock-wise positive measurement of angles was chosen by convention. (g) Evolution of the local contact angle θ_i along the curvilinear abscissa s of the triple line. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

resulting 3D images for the three phases. These 3D images were then intersected using the Image calculator function, which allowed keeping only the common voxels of the three phases (Fig. 2c) and then skeletonized to obtain the voxels belonging to the triple line (Fig. 2d).

2.3.2. Measurements of the triple line lengths and local contact angles

The measurements of the length of the triple line and the local contact angles along it were performed with a procedure we implemented in Matlab [34]. Smoothed closed linear parametric curves of the triple lines with curvilinear abscissa s were fitted using the set of discrete

voxels of coordinates (x, y, z) representing the triple lines in the 3D images that were obtained following the procedure described in the previous section. This parametric curve was then discretized into N_s elementary segments i of lengths ds_i with $1 \leq i \leq N_s$. Depending on the considered tube and on the shape of the triple line, N_s could vary from 35 to 60. The lengths l_s of the triple lines were computed as $l_s = \sum_{i=1}^{N_s} ds_i$. It was verified that such discretization gave a good approximation of the lengths of numerically generated circular triple lines. Then, a local Frenet basis was associated to each elementary segment i using the calibrated procedure reported by Latil *et al.* [34]. In this local basis, T_i is the tangent unit vector, N_i is the normal unit vector pointing towards the tube, and B_i the binormal unit vector to the segment i (Fig. 2e).

For measuring the N_s local contact angles θ_i along the triple lines, the trinariised 3D images were cut in the (N_i, B_i) planes using the image rotation function of the image processing toolbox of Matlab. For that purpose, the 3D images were successively rotated of an angle ω_i around the z axis and of an angle ψ_i around the y axis of the (x, y, z) frame of the 3D images (Fig. 2e). Then the local contact angles θ_i were measured manually as the angle formed between the vector t_{f_i} tangent to the tube (marked in orange) and the vector tangent to the fluid surface t_{fv} (marked in pink), using a ROI of 50×50 pixels centred on the triple points. This procedure was also validated with numerically generated images, exhibiting the same spatial resolution of the X-ray microtomography images and a predefined local contact angle varying from 5° to 90° . To predefine the local angle in the numerically generated images we used a generation process based on the theoretical expression proposed by James (1974) [39] that predicts the equilibrium shape of a meniscus that is formed on the outside of a circular vertical cylinder. The error made following this procedure was shown to be $\pm 3^\circ$. Fig. 2g shows an example of the evolution of the local contact angle θ_i and its mean value $\bar{\theta}$ along a triple line. Besides, it is important to mention that the aforementioned procedure was performed for each triple line that formed along all the tubes of the fibre network.

2.3.3. Measurements of the capillary forces

Using the cross sections of the rotated 3D images, it was also possible to estimate for each segment i of a given triple line the components in the (N_i, B_i) basis of the local capillary force $\mathbf{dF}_i = \gamma_{lv} ds_i t_{fv}$ exerted by the fluid on a portion of tube as follows:

$$dF_{iB} = \mathbf{dF}_i \bullet \mathbf{B}_i = \gamma_{lv} \cos(\theta_i - \alpha_i) ds_i \quad (1)$$

$$dF_{iN} = \mathbf{dF}_i \bullet \mathbf{N}_i = \gamma_{lv} \cos(\theta_i - \beta_i) ds_i \quad (2)$$

where the angles α_i and β_i are shown in Fig. 2f. The overall capillary force \mathbf{F} exerted by the fluid on a given tube was obtained by summing all the local capillary forces \mathbf{dF}_i . Then, the components F_x , F_y and F_z of the capillary forces were calculated using the coordinates of the N_i and B_i vectors in the (x, y, z) frame of the 3D images. Hence, the intensities of the transverse $F_\perp = \sqrt{F_x^2 + F_y^2}$ and longitudinal $F_\parallel = |F_z|$ capillary forces exerted by the fluid on each tube of the model fibre network were determined.

2.3.4. Measurements of surface curvatures

The local mean curvatures of the interface between the fluid and the air phases were estimated using an approach developed and calibrated by Flin *et al.* [40,41]. The method is based on the expression of the mean curvature κ at a point P located at the interface between the fluid and the air, which is defined as the divergence of the downward unit normal vector $\mathbf{n}(P)$:

$$\kappa(P) = \frac{\nabla \bullet \mathbf{n}(P)}{2} \quad (3)$$

The algorithm computes the normal vectors $\mathbf{n}(P)$ using the volumetric information related to the gradient in the grey levels of the signed

distance map of a binarised 3D image of the fluid phase (see Fig. 2a shown in S1). An example of a 3D map of the mean curvature of the fluid-air interface is shown in Fig. 2b (S1). A corresponding 2D map of the mean curvature κ is shown in Fig. 2c (S1) and was obtained by projecting the 3D map on the (x, y) plane. This 2D map was then smoothed with a coarse graining approach [42]. To check the relevance of the measurements, the algorithm was tested using binarised 3D images of the tubes whose curvature is known. From the mean curvature map, it was then possible to estimate the local capillary pressure P_c using the Laplace-Young equation:

$$P_c = P_v - P_l = 2\gamma_{lv}\kappa \quad (4)$$

where $P_v - P_l$ is the pressure difference across the air-fluid interface.

3. Results

3.1. Analysis of the *in situ* impregnation experiments

Fig. 3 shows vertical cross sections of the 3D images acquired during the impregnation of the model fibre network with silicone oil or demineralised water.

3.1.1. Impregnation sequence using interrupted scanning conditions

The impregnation experiment that was performed using the silicone oil consisted in a sequence of six impregnation stages. They are denoted A–F in Fig. 3a. In image A, the silicone oil was not in contact with the fibre network. The bottom extremities of the tubes were located at a vertical distance of approximately 2 mm of the fluid-air interface, as shown in the position-time graph in the inset of Fig. 3a. This image revealed that the fluid-air interface was nearly planar in spite of the rotation of the X-micromotograph stage during scanning. In stage B, the fibre network was immersed in the silicone oil. The extremities of the tubes reached a depth of approximately -0.3 mm measured with respect to the initial position of the fluid-air interface of stage A. In stage C, this depth was -4.2 mm. Then the fluid reservoir was moved downwards in stages D and E until the fluid meniscus that formed between the tubes and the fluid was broken (stage F). Images obtained for stages B and C showed that the fluid rose between the tubes of the fibre network. The fluid reached its maximum height in the centre of the network and the fluid-air interface formed a dome-like shape at the network scale. Note also that the image spatial resolution allows observing the shape of the tube scale menisci that formed where the tubes crossed the fluid-air interface. Besides, as the tubes were sealed at their top extremities, the fluid could not rise inside the tubes. Only a slight meniscus formed at their lower extremities. Images B and C did not reveal any significant changes between the overall shape of the dome that formed within the fibre network apart from its left-hand and right-hand side borders (close to tubes 4 and 7), where a slight difference in the shape of the menisci was noticed. Similar observations could be done for the outer tubes of the fibre network. For the tubes 5 and 6, these observations revealed that the fluid tended to slide on the tube surfaces when the reservoir was lifted up. When the reservoir was pulled down (stages D and E), again the fluid tended to slide on the tube surfaces which induced that the dome-like shape of the fluid-air interface was mostly preserved. However, the shape of the menisci of the outer tubes was affected. These phenomena will be further analysed and quantified in the next subsections by quantifying the local contact angles θ_i and the lengths of the triple lines l_s along all the tubes for stages B and E. In stage F, the reservoir was further pulled down, which resulted in the breakage of the capillary bridge. Finally, a volume of liquid was entrapped within the model fibre network.

3.1.2. Impregnation sequence using sequentially continuous scanning conditions

The impregnation experiment described in this section was per-

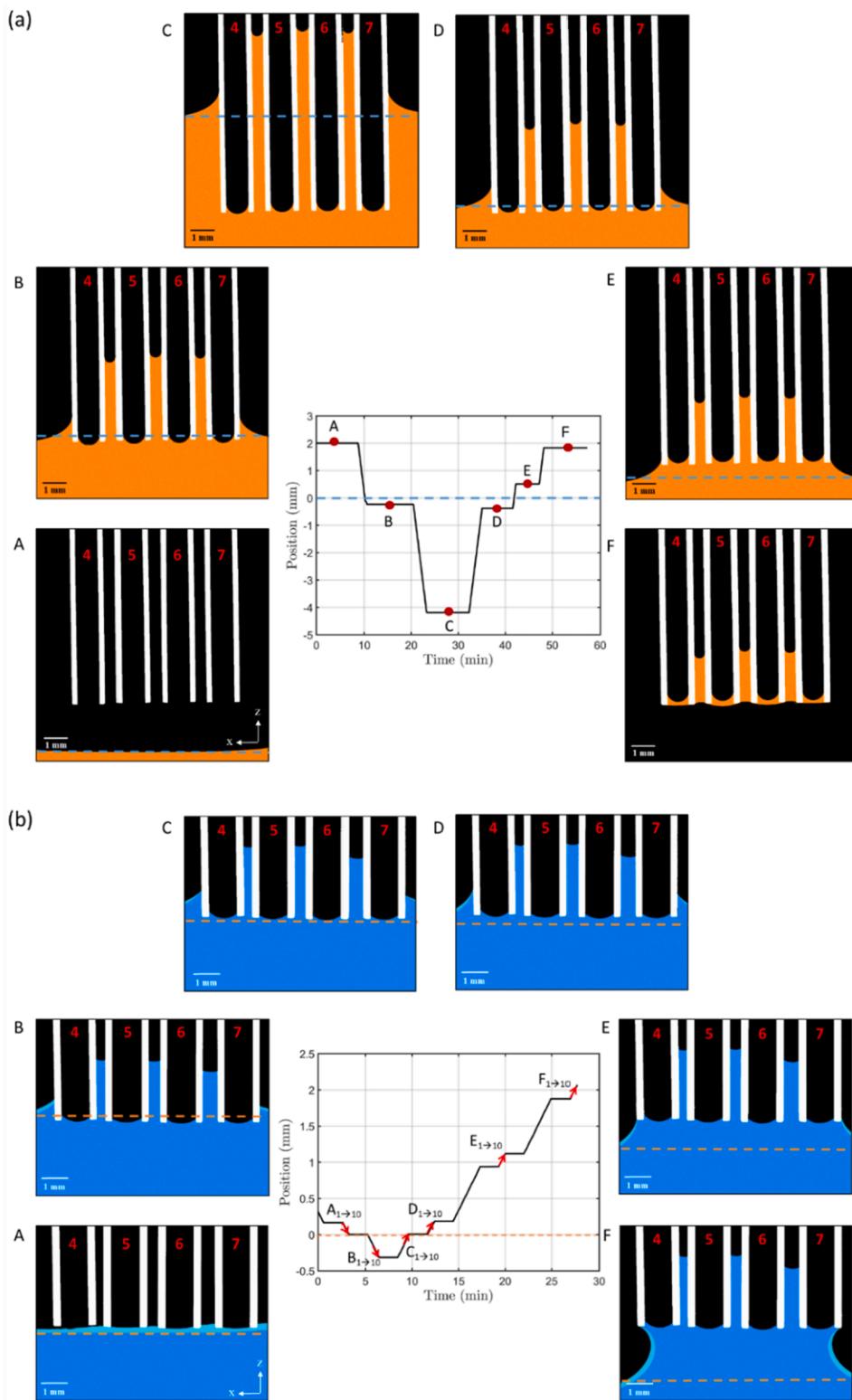


Fig. 3. Vertical cross sections of the 3D images acquired during the impregnation of the fibre network with silicone oil (a) and demineralised water (b). The dashed lines show the initial position of the fluid surface. The tubes are represented in white, the air in black, the silicone oil in orange and the demineralised water in blue. The graphs represent the position of the bottom extremities of the tubes with respect to the initial position of the fluid surface as a function of time. The red arrows in the graph indicate the time intervals when the sequences of 3D images were acquired. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

formed using demineralised water in a sequence of six impregnation stages (A-F) of the fibre network. For each stage a sequence of ten images ($A_i, B_i, C_i \dots$ with $i = 1, 2 \dots 10$) was obtained (1 image every 2 s). Starting from the initial position (stage A_1), where the extremities of the tubes were above the fluid surface, the fluid reservoir was moved upwards and the extremities of the tubes entered in contact with the fluid (stage A_{10}), as shown in Fig. 3b. Then, the reservoir was further moved upwards

(stage B) before being gradually withdrawn (stages C-F). Similarly to the previously described impregnation experiment performed with the silicone oil, a dome-like shape of the fluid-air interface was obtained at the network scale. However, the height of the “dome” reached at the centre of the fibre network was lower. Slight height variations of the fluid-air interface were visible in the vertical cross section in Fig. 3b. These variations were due to slight vertical misalignments of the tubes of the

fibre network used in this experiment. Contrary to what was observed with silicone oil, it is visible from Fig. 3b of stage F that the capillary bridge was not broken for a similar withdrawing position of approximately 2 mm.

In Fig. 3b, the zones of the fluid phase highlighted with a lighter blue were obtained by subtracting the volume of fluid of image 1 (resp. image 10) to image 10 (resp. image 1) for the sequences A₁₋₁₀ and B₁₋₁₀ (C₁₋₁₀, D₁₋₁₀, E₁₋₁₀ and F₁₋₁₀). This enabled the evolution of the geometry of the fluid front to be followed live for 20 s. For each stage (from B to F), the vertical cross sections show that the fluid that was entrapped in the centre of the fibre network (around tubes 5 and 6) did not move significantly. On the contrary, a significant fluid motion could be clearly observed on the edges of the fibre network (tubes 4 and 7 in the vertical cross section of Fig. 3b). The vertical cross section of stage B shows that the menisci that formed on the inner tubes 5 and 6 did not exhibit significant geometric changes between images B₁ and B₁₀. In addition, the menisci that formed on the outer tubes of the fibre networks showed slight changes. Thus, the fluid tended to slide on the surfaces of the tubes of the fibre network. The evolution of the menisci will be discussed in detail in the next sections. Stages C-F reveal that the menisci that formed on the inner tubes 5 and 6 were apparently not affected by the withdrawing motion of the reservoir. On the contrary, the menisci that formed on the outer tubes were distorted. The triple line was like

anchored on the outer tubes. The positions of the triple points on tubes 4 and 7 in Fig. 3b did not change and the local contact angles exhibited a decrease (the values of the local contact angles θ_i will be given in next subsections).

3.2. Contact angles and triple line lengths

3.2.1. Interrupted conditions

Fig. 4a,b show the evolution of the local contact angles θ_i along the triple lines that formed along all the tubes of the fibre network for stages B and E for the experiments performed with the silicone oil. For these two stages, these figures show that θ_i exhibit a great variation along the triple lines, regardless of the tube. The difference between the maximum and the minimum values was almost 15° for each tube. The dispersion of the values of the local contact angles was higher for the outer tubes whose triple lines were more distorted than for the tubes located at the centre of the fibre network (tubes 5 and 6). A further analysis of the evolution of the local contact angles along the triple lines of all the outer tubes showed that the lowest values of θ_i were obtained for regions of the triple lines that were not located in the vicinity of other tubes.

Fig. 4c shows the mean values $\bar{\theta}$ of the local contact angles θ_i for all the tubes of stages B and E, as well as the standard deviation of θ_i . The mean contact angle $\bar{\theta}$ varied for all the tubes. However, it is interesting

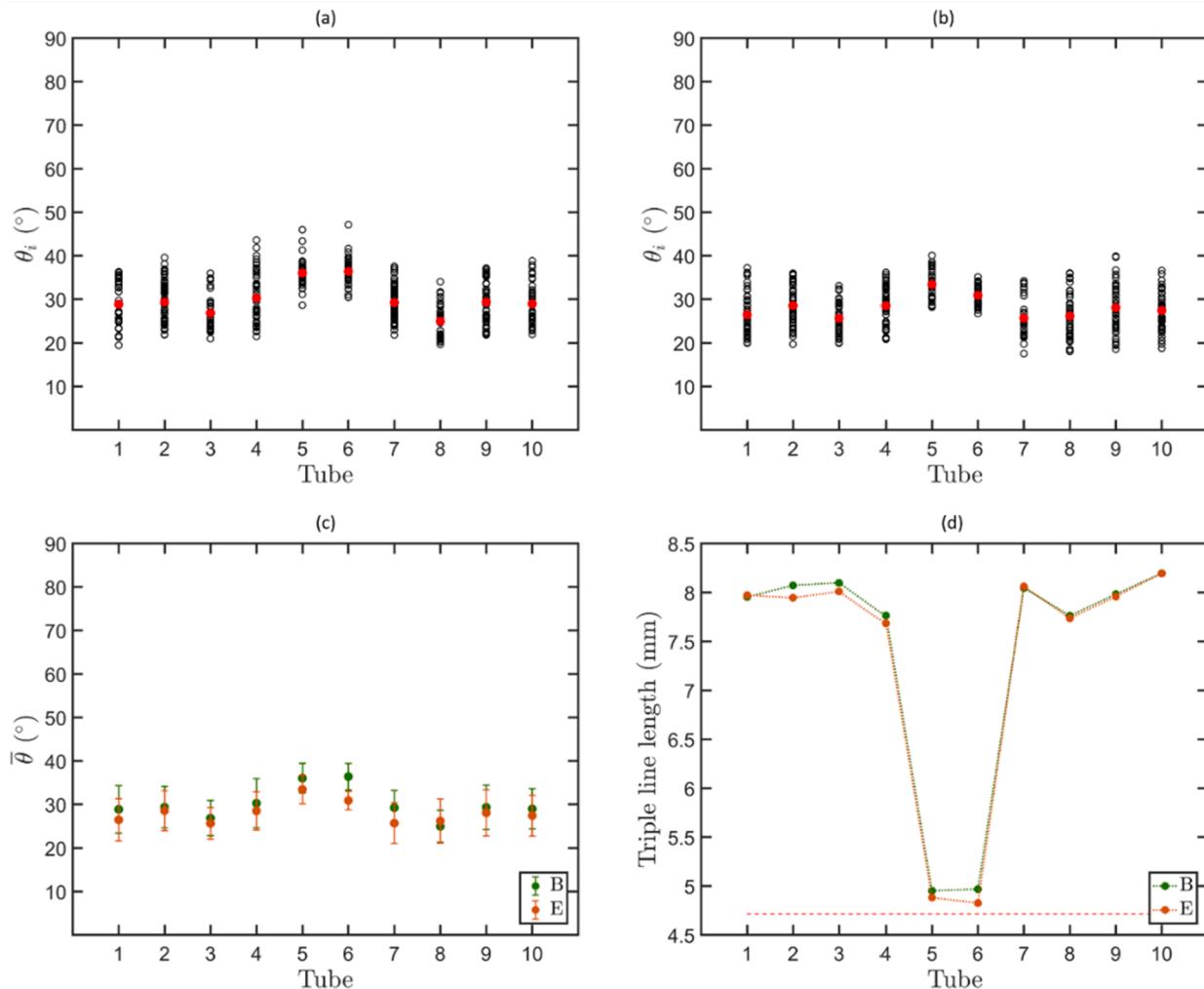


Fig. 4. Local contact angles θ_i measured along the triple lines of all the tubes of the fibre network for stages B (a) and E (b) of the impregnation experiment performed using silicone oil. (c) Corresponding mean values $\bar{\theta}$ and standard deviations for stages B and E. (d) Lengths of the triple lines for all the tubes of the fibre network for stages B and E. The red dashed line represents the length of the perimeter of the cylindrical tubes used to build the fibre network. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

to notice that the mean contact angles $\bar{\theta}$ of the tubes in symmetry positions (tubes 1, 3, 8, 10 or tubes 2, 9 or tubes 5, 6) were almost equal. The mean value $\bar{\theta}$ of the tubes 5 and 6 at the centre of the fibre network were also slightly higher than those measured for the outer tubes. In stage B, the mean value was 35° for tubes 5 and 6, whereas it was 29° for the outer tubes. In stage E, this difference decreased: the mean value $\bar{\theta}$ of the tubes 5 and 6 was 32° , whereas it was 27° for the outer tubes. This difference shows that the mean contact angles $\bar{\theta}$ tended to decrease with the withdrawing of the reservoir.

Fig. 4d shows the lengths of the triple lines for stages B and E. For the tubes 5 and 6, the lengths of the triple lines were almost similar to that of the perimeter of the tube (~ 4.8 mm). The triple lines of the outer tubes were strongly distorted (see also **Fig. 2d**) and their lengths were much greater (~ 8 mm). However, there were no significant changes between the lengths measured in stages B and E.

3.2.2. Sequentially continuous conditions

Fig. 5a shows the mean contact angles $\bar{\theta}$ measured for stages B₁ and B₁₀, D₁ and D₁₀ and their standard deviations for the impregnation experiments performed using demineralised water. As observed previously, the mean contact angle $\bar{\theta}$ also varied for all the tubes. In addition, the mean contact angles $\bar{\theta}$ for stage B₁ were slightly lower than for stage B₁₀. For stages B₁ and B₁₀, $\bar{\theta}_{B_1} = 72^\circ$ and $\bar{\theta}_{B_{10}} = 73^\circ$. A more pronounced difference was observed for the outer tubes than the inner ones (5 and 6). The origin of this slight increase might be due to the flattening of the menisci that formed around the tubes when the reservoir was lifted up (or conversely when the fibre network was plunged into the demineralised water).

On the contrary, when the reservoir was withdrawn, the mean contact angle tended to decrease between stages D₁ and D₁₀ in a more pronounced manner, i.e., $\bar{\theta}_{D_1} = 63^\circ$ and $\bar{\theta}_{D_{10}} = 58^\circ$. It was also apparent that the standard deviation values were larger for stages D than B, i.e. during the withdrawing of the reservoir. This result is confirmed by the difference between the maximum and the minimum values of the contact angles that was equal to 15° (resp. 45°) for stage B (resp. D).

Fig. 5b shows the variation of the lengths of the triple lines for the same stages. For the inner tubes (tubes 5 and 6), no clear differences in the lengths of the triple lines was observed. This is in accordance with the observations made in subsection 3.1.2: the positions of the fluid-air interface and triple lines at the centre of the fibre network did not vary significantly when the reservoir was moved upwards or downwards. The lengths of the triple lines along the outer tubes tended to decrease when the reservoir was lifted up, as shown for stages B₁ and B₁₀. This could be

related to the increase in the position of the fluid-air interface around the fibre network. In contrast, the lengths of the triple lines between stages D₁ and D₁₀ increased slightly. In parallel, the mean contact angles $\bar{\theta}$ showed a large decrease, thus confirming the observations made on the vertical cross sections shown in **Fig. 3b**, i.e., the triple lines were like anchored on the tube surface during the withdrawing of the reservoir.

3.2.3. Capillary forces

The direction and intensity of the transverse capillary force F_\perp exerted on each tube by the fluid are shown in **Fig. 6a-c** and **Fig. 7a-c** for the sample impregnated with the silicone oil for stages B and E, and demineralised water for stages B₁, B₁₀, D₁ and D₁₀, respectively. In addition, the normalised intensities of the transverse $F_\perp^* = F_\perp / (2\pi r_e \gamma_{lv} \cos \theta_s)$ and longitudinal $F_\parallel^* = |F_z| / (2\pi r_e \gamma_{lv} \cos \theta_s)$ capillary forces measured for each tube are reported in **Fig. 6b,c** and **Fig. 7d,e** for the two impregnation experiments.

Fig. 6a and **Fig. 7a-b** show that the transverse forces F_\perp exerted on the inner tubes were negligible. On the contrary, the transverse forces F_\perp exerted on the outer tubes tend to point towards the centre of the fibre network, regardless of the impregnation stages for both experiments. Slight variations in the directions of F_\perp were observed between the various impregnation stages. These results were in accordance with the aforementioned variations of the local contact angles and lengths of the triple lines (**Figs. 4 and 5**).

In addition, **Fig. 6b,c** and **Fig. 7c-f** show the dimensionless transverse F_\perp^* and longitudinal F_\parallel^* capillary forces exerted by the fluid on each tube. For the inner tubes (5 and 6), the transverse forces were negligible which is due to the symmetries of the fibre networks, whereas for some of the outer tubes (tubes 1, 3, 4, 7, 8 and 10), both forces were of the same order of magnitude. For tubes 2 and 9, the transverse capillary forces were approximately one half or more lower than the longitudinal forces. **Fig. 6b,c** show that the dimensionless longitudinal capillary forces were approximately equal to 1 (except for tubes 2 and 9). This tends to show that the longitudinal capillary force exerted by the fluid on each tube of the fibre network is close to that obtained for a single tube plunged in the silicone oil with a meniscus that would form a constant contact angle equal to θ_s . As already noticed for the measurements of the mean contact angles, the forces obtained for the experiments performed with the demineralised water showed a higher discrepancy than those measured for the silicone oil. A possible origin of this discrepancy might be a poorer precision in the placement of tubes (e.g. slight inclination or misalignment) in the fibre network used for the experiments performed with the demineralised water. This discrepancy could also be related to a wider diversity of physicochemical interactions between water and the

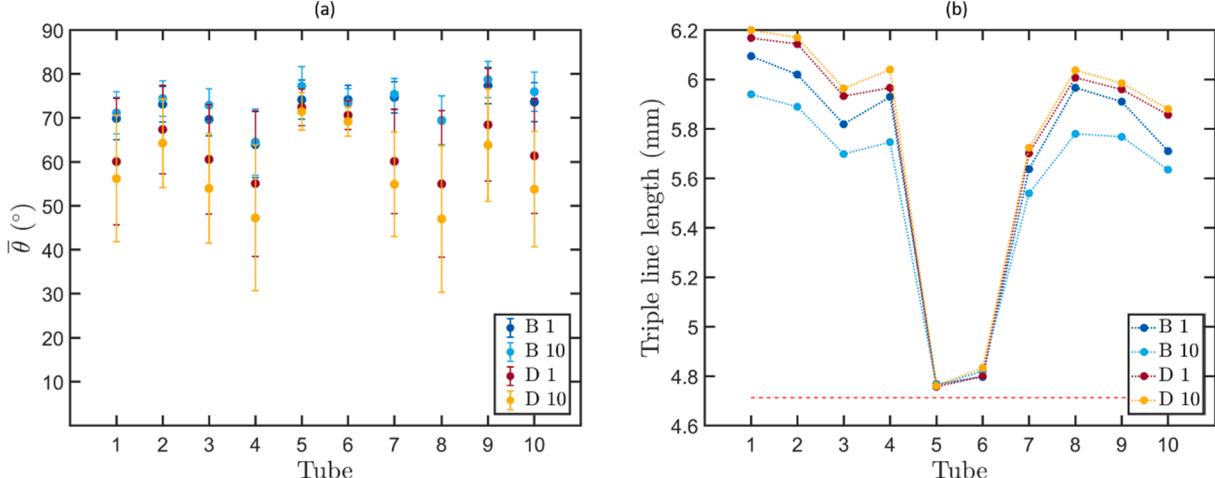


Fig. 5. (a) Mean contact angles $\bar{\theta}$ for all the tubes of the fibre network and stages B₁, B₁₀, D₁ and D₁₀ of the impregnation experiment performed using demineralised water. (b) Corresponding lengths of the triple lines.

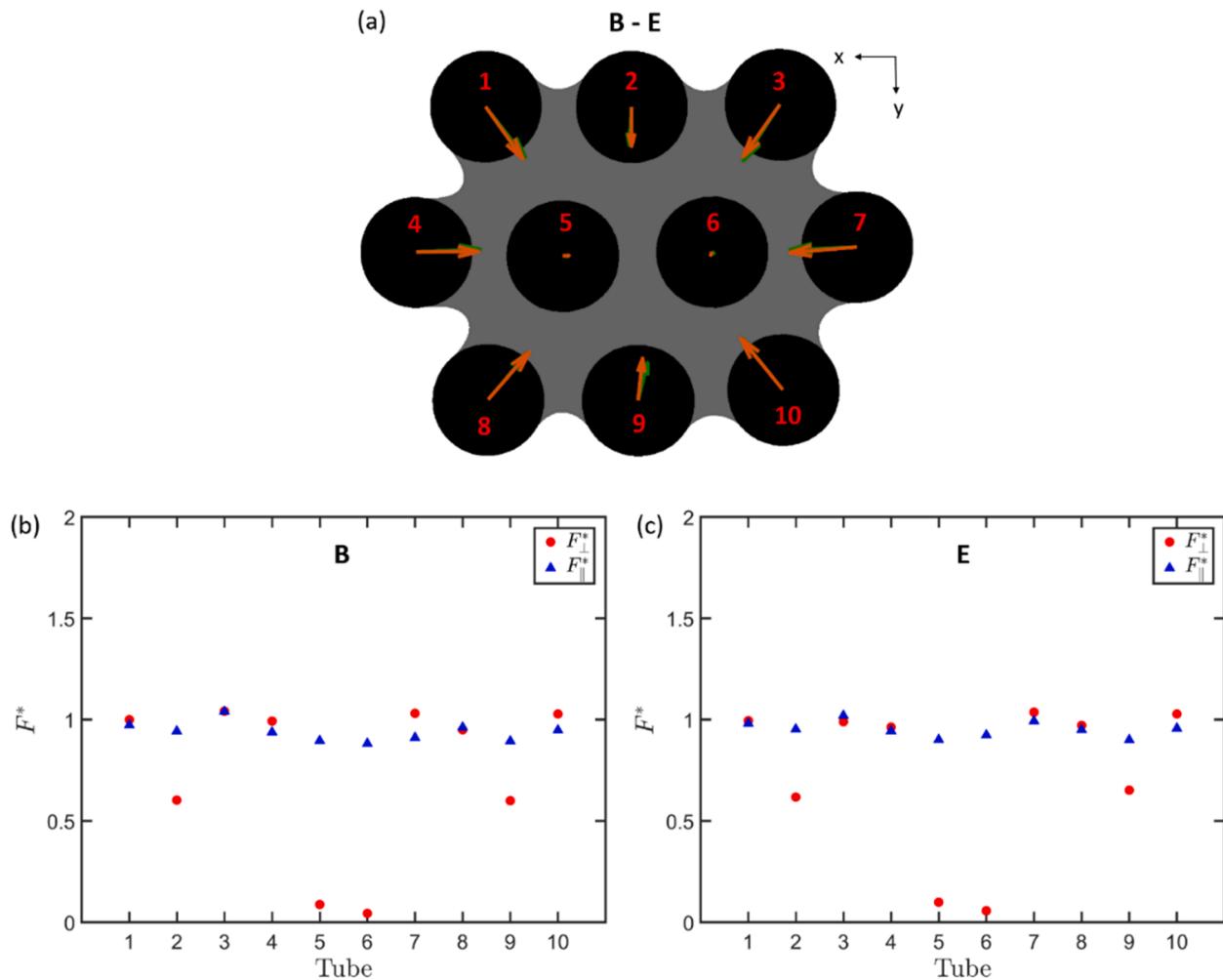


Fig. 6. (a) Cross section of the fibre network showing the transverse capillary force F_{\perp} exerted by the fluid on each tube (in black) for stages B (green arrows) and E (orange arrows) of the impregnation experiment carried out with the silicone oil. The application points of the forces were placed arbitrarily on the axes of the tubes. The cross section of the fibre network was also chosen arbitrarily (the fluid is grey in the cross section). Graphs showing the dimensionless transverse F_{\perp}^* and longitudinal F_{\parallel}^* capillary forces exerted by the fluid on each tube for stages B (b) and E (c). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

surfaces of the tubes [43].

For the experiments performed using the silicone oil, the comparison of Fig. 6b,c show that the withdrawing of the fluid reservoir tended to slightly increase the dimensionless longitudinal capillary forces F_{\parallel}^* . This effect was less clear for the dimensionless transverse capillary forces F_{\perp}^* . This increase could be associated to the slight decrease in the mean contact angles as shown in Fig. 4c. A similar but more pronounced tendency to the increase in both capillary forces is revealed by comparing Fig. 7c,d with Fig. 7e,f. More interestingly, the comparison of stages B₁ (resp. D₁) with B₁₀ (resp. D₁₀) shows a decrease (resp. an increase) in both capillary forces when the reservoir was moved upwards (resp. downwards). Again, these tendencies have to be related to the aforementioned evolutions of the contact angles and lengths of the triple lines, as shown in Fig. 5a,b.

3.2.4. Fluid front curvatures and capillary pressure

Fig. 8a shows a 2D map of the mean curvature κ for stage B of the impregnation experiment performed using silicone oil. The mean curvature κ measured in the centre of the fibre network ranged between $\kappa = 0.80 \text{ mm}^{-1}$ and $\kappa = 1.20 \text{ mm}^{-1}$ (Fig. 8a). Consequently, the local capillary pressure P_c in the centre of the model fibre network ranged between approx. 35 and 55 Pa (Fig. 8b). In addition, Fig. 8c shows that

the average capillary pressure \bar{P}_c measured in the centre of the fibre network did not show large variations, regardless of the impregnation stages. This is in accordance with the previous observations related to Fig. 3b since the geometry of the dome-like shape of the fluid-air interface did not exhibit significant changes. On the outer edge of the fibre network, the mean curvature κ was lower and ranged between 0.36 mm^{-1} and 0.50 mm^{-1} (Fig. 8a). This corresponds to a local capillary pressure P_c that was comprised between 15 Pa and 21 Pa (Fig. 8b).

4. Discussion

4.1. Variations in the local contact angles

For both investigated fluids, this study revealed that during the impregnation experiments the local contact angles exhibited large variations along the triple lines formed onto the surfaces of the tubes. These observations were done during the wetting (upward motion of the fluid reservoir) or dewetting (downward motion of the fluid reservoir) of the fibre network with both fluids. This phenomenon was even more pronounced for the outer tubes of the network (Fig. 3).

Similar observations using 3D images have already been made for geomaterials and granular materials with complex porous structures [31,44–46] impregnated by a wetting fluid. If the wetting fluid is at rest

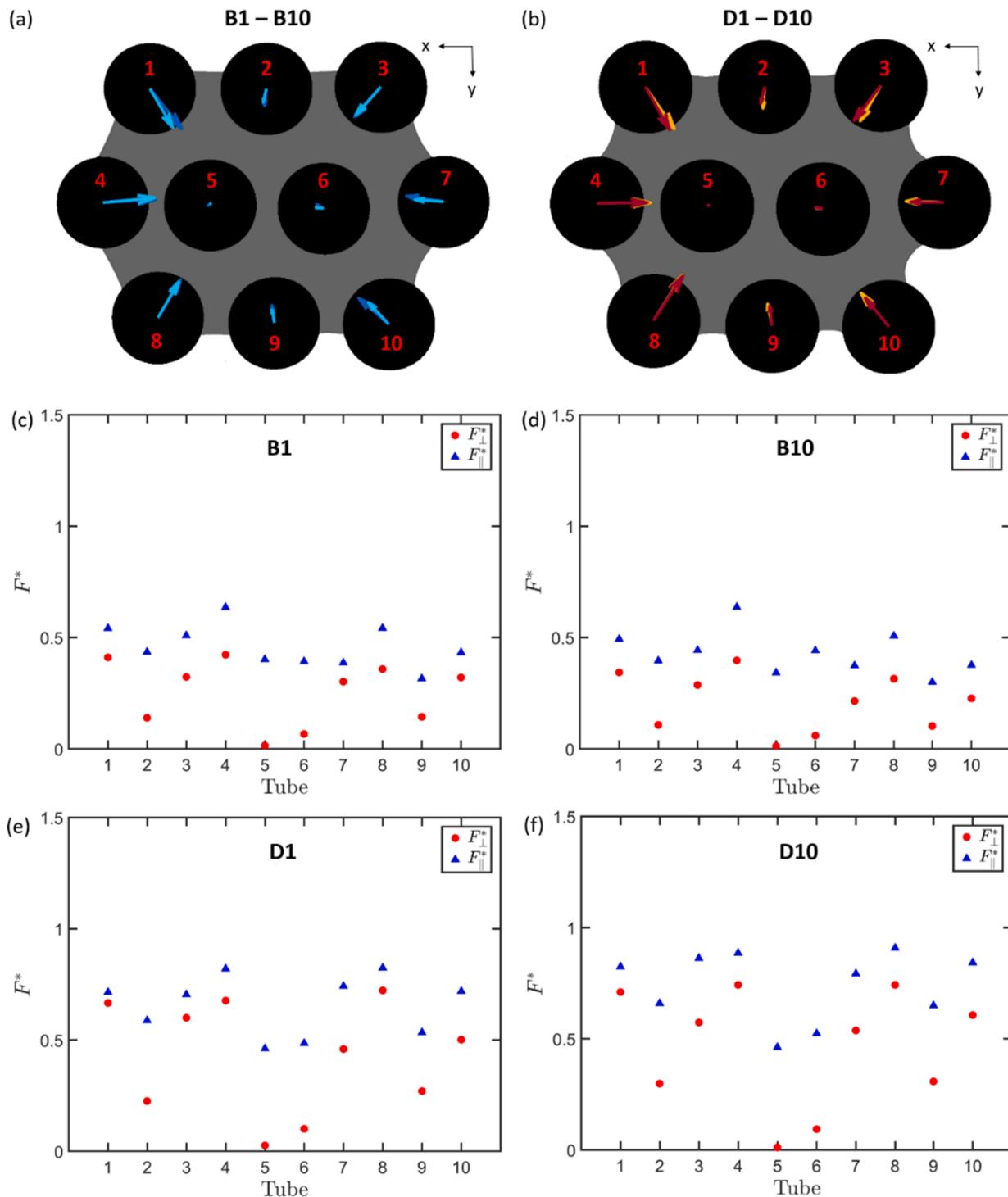


Fig. 7. (a,b) Cross sections of the fibre network showing the transverse capillary force F_{\perp} exerted by the fluid on each tube (in black) for stages B1 (dark blue arrows) and B10 (pale blue arrows) and D1 (red arrows) and D10 (yellow arrows) of the impregnation experiment carried out with the demineralised water. The application points of the forces were placed arbitrarily on the axes of the tubes. The cross section of the fibre network was also chosen arbitrarily (the fluid is grey in the cross section). Graphs showing the dimensionless transverse F_{\perp}^* and longitudinal F_{\parallel}^* capillary forces exerted by the fluid on each tube for stages B1 (c), B10 (d), D1 (e) and D10 (f). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

(in “static” conditions), the variations of the local contact angle can be associated to several factors such as the local roughness and heterogeneities in the physico-chemical properties of the surface of solid, or the topology of pores [47]. A relaxation phenomenon of the local contact angles towards a stable equilibrium contact angle can also be a possible origin of these variations. Indeed, the authors observed that relaxation

can occur at different rates along the contact lines and thus also leads to contact angle distributions.

Several authors [31,44] have also reported that imbibition or drainage (fluid in “dynamic conditions) of a granular porous medium by a wetting phase can induce localised small pressure perturbations in the wetting phase and variations in the contact angles. During imbibition,

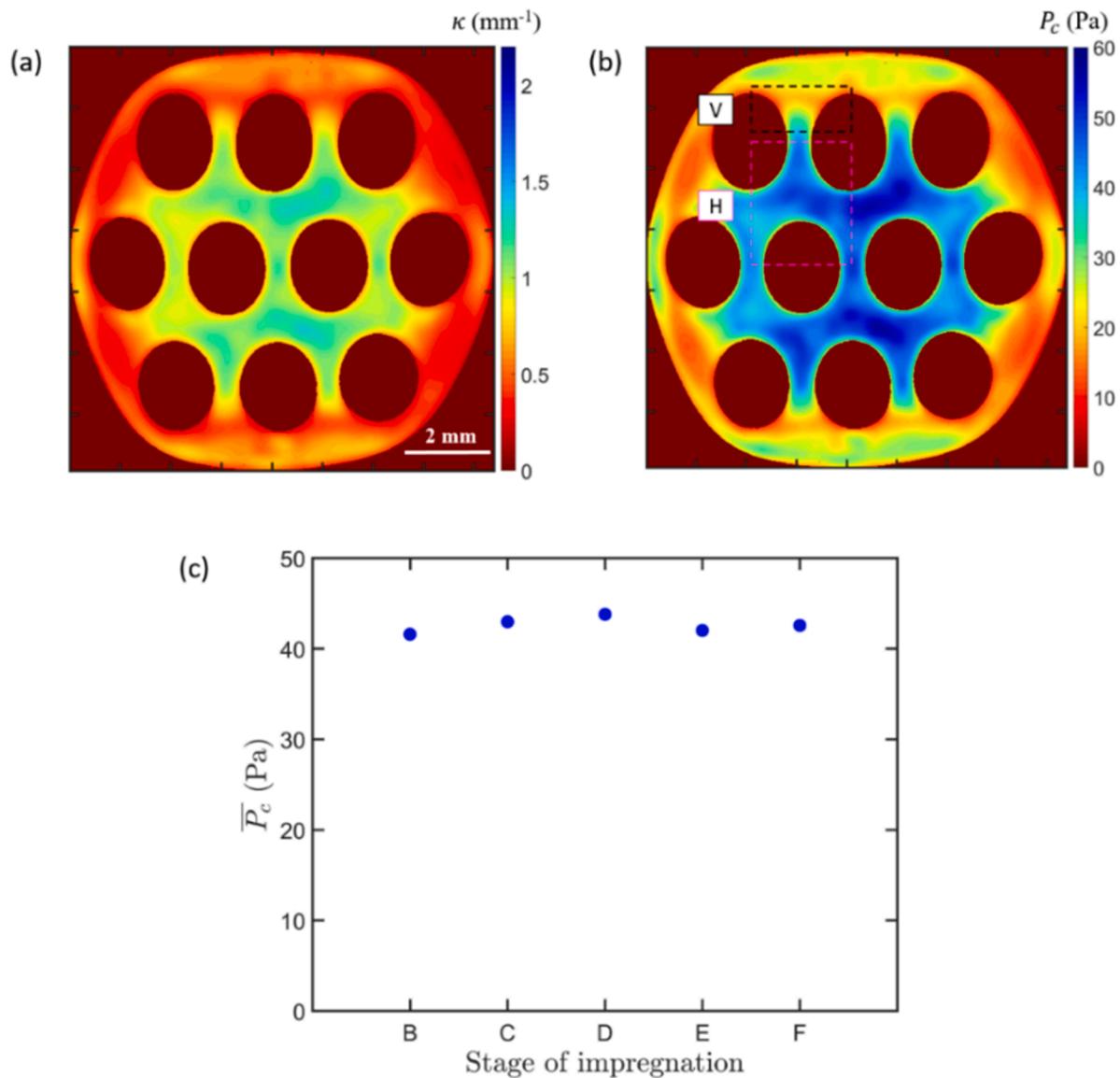


Fig. 8. (a) 2D map of the mean curvature κ of the fluid-air interface for stage B of the impregnation experiment performed using silicone oil. (b) Corresponding 2D map of the capillary pressure P_c . The traces of the tubes are not perfectly circular in the 2D maps because of their possible slight vertical misalignment. (c) Average capillary pressure \bar{P}_c in the centre of the fibre network as a function of the impregnation stage.

the authors observed motions of the contact lines once the contact angles approached (or exceeded) a maximal contact angle (denoted as the advancing contact angle). During drainage, they observed motions of the contact lines once the contact angles approached a minimum angle (denoted as the receding contact angle). Similar scenarios are expected to occur in our experiments and could explain why the triple lines were like anchored during the withdrawing of the reservoir (Fig. 3).

4.2. Mesoscale capillary pressure measurements and theoretical predictions

From the local capillary pressure maps, we identified two characteristic zones (denoted H and V in Fig. 8a,b) in order to estimate their mean capillary pressure \bar{P}_c . These zones were located in the centre and on the side of the fibre network, respectively. They corresponded to fluid-air interface zones that were nearly perpendicular (H) or parallel (V) to the tubes' axes. As mentioned previously in section 2.3.5, the algorithm proposed by Flin *et al.* [40,41] enabled local unit normal vectors n to the fluid-air interface to be computed. The components of

the average unit normal vector \bar{n} were $(0.05, -0.13, -0.99)$ in zone H and $(-0.01, -0.94, -0.34)$ in zone V, showing that these vectors were nearly aligned with the tube axes or perpendicular to the tube axes, respectively. Then, the average capillary pressure \bar{P}_c was estimated in the fluid domain of zones H and V. In zone H (resp. V), the pressure \bar{P}_c was equal to 45 Pa (resp. 21 Pa). The pressure measured in zone H is in accordance with that given by the fluid statics that can be estimated from the relative height \bar{z} of the fluid-air interface and the gravity force g , i.e., $\bar{P} = \rho g \bar{z} \approx 39$ Pa. This shows once again that the mean curvature of the fluid-air interface is relevant. Then, we compared these values to the predictions of the model proposed by Ahn *et al.* [48] for the average capillary pressure \bar{P}_c within arrays of parallel fibres:

$$\bar{P}_c = F \frac{\gamma_{lv} \cos \bar{\theta} (1 - \phi_p)}{2 \phi_p r_e} \quad (5)$$

where ϕ_p is the porosity, and F is a form factor that depends on the flow direction and fibre network geometry. For flow parallel or transverse to fibres, F is equal to 4 and 2, respectively [48]. To estimate the average

capillary pressure \bar{P}_c from Eq. (5), the average of the local contact angles was calculated along the portions of the triple lines formed along the tubes comprised in zones H or V (Fig. 8b). For zone H, this average value $\bar{\theta}$ was equal to 35° , whereas for zone V it was equal to 28° . Furthermore, the porosity $\phi_p = 0.55$ corresponds to the porosity of a period of the triangular tube arrangements that constitute the fibre network. Then, the model prediction for the average capillary pressure \bar{P}_c was 38 Pa for zone H and 20 Pa for zone V, showing a good agreement with the experimental measurements.

4.3. Interest of measurements of capillary forces

The measurements of the pore scale capillary pressure and forces exerted by the fluid on the tubes performed in this study are original since they are entirely based on local geometric descriptors obtained from the quantitative analysis of 3D X-ray microtomography images.

The results gathered for the capillary pressure could be extended and down-scaled to industrial fibre bundles with similar porosity ($\phi_p = 0.55$) and fibre arrangement but made of glass fibres with a smaller diameter (i.e., $2r_e = 15 \mu\text{m}$). In that case, the capillary pressure would be one hundred times higher. However, contrary to what is observed in this study for the rigid fibre network, capillary-driven flows would be also coupled to (de)-consolidation phenomena characterised by complex rearrangements and bending mechanisms of the fibres (see Fig. 3 shown in S1). These phenomena have been highlighted by Larson *et al.* [24] who observed important 3D fibre re-arrangements associated to variations in the fibre volume fraction during the longitudinal impregnation of an industrial fibre bundle.

The measurements shown in Section 3.2.3 revealed that during the longitudinal impregnation of the model tube bundle, the transverse capillary forces F_\perp^* measured on the outer tubes are important and of the same order of magnitude as the longitudinal capillary forces F_\parallel^* . In networks with similar geometry (similar fibre arrangement and fibre length $L = 16 \text{ mm}$) made of $15 \mu\text{m}$ diameter glass fibres, these forces would severely deform each fibre and probably pull them closer to each other in the form of a denser aggregate [49,50]. As a first estimate, assuming clamped-free boundary conditions and a fibre Young's modulus E of 70 GPa, the transverse capillary force $F_\perp \approx 2\pi r_e \gamma_{lv} \cos\theta_s$ (Fig. 6a) exerted by the fluid would induce a deflection $\delta = 32F_\perp L^3 / 3E\pi(2r_e)^4$ of the outer fibres of the bundle equal to approx. 3 mm. This important deflexion induced by transverse capillary forces would then lead to complex re-arrangements of the fibres and to a deconsolidation (Fig. 3 shown in S1) or a consolidation of the bundle.

This shows that the knowledge of such forces in real fibre bundles used for instance in composite processing routes such as pultrusion would help in properly controlling the fibrous microstructure of the obtained composite parts.

5. Conclusions

We carried out an analysis of capillary phenomena during the longitudinal impregnation of a fibre network made of arrays of parallel glass tubes that can be considered as cylindrical rods since the studied fluids cannot penetrate inside them during the experiments. For that purpose, a specific device was especially developed and enabled the acquisition of 3D X-ray microtomography images of several wetting and dewetting stages of the fibre network. Two types of wetting fluids, namely demineralised water and silicone oil, were used. Specific image analysis procedures were developed to measure the triple line lengths, local contact angles, and fluid-air interface mean curvatures. This original database enabled calculating the local capillary forces exerted on each tube of the fibre network by the fluid as well as the local capillary pressure. The results showed that the transverse forces may be as high as the longitudinal capillary forces. To the best of our

knowledge, the measurements of the local transverse capillary forces exerted on the individual elements that constitute a fibre network are original. This is an important result for a better understanding and control of the impregnation phase of fibrous reinforcements used in composite materials because the propagation of a polymer matrix within industrial fibre bundles is partially governed by capillary forces that can often lead to complex rearrangement or deformation phenomena of fibre bundles made of compliant fibres [49,50]. Our results confirmed that large variations in the local contact angles can occur in quasi static impregnation situations as it has already been reported in several studies dealing with the impregnation of geomaterials [31,44–46]. They also enabled assessing the relevance of the theoretical predictions proposed by Ahn *et al.* [48] for the upscaled capillary pressure. More particularly, the theoretical predictions for longitudinal and transverse flow situations were in accordance with our experimental measurements.

Finally, this study shows that a fine description of the geometry of the fluid-air interfaces, contact lines and local contact angles in fibre networks is accessible through the analysis of 3D images. It also shows that the local capillary pressure and forces can be finely estimated. It is also important to note that the numerical modelling of the presented results would certainly constitute a challenging task [51,52].

One limitation of this study is the important diameter of the tubes/fibres (approx. 1.5 mm) of the model fibre network compared to the typical diameter of fibres (approx. 10 to 300 μm) that are used in industrial fibre reinforcements of composite materials. However, thanks to recent progress offered by synchrotron radiation facilities (e.g., voxel size smaller than $0.3^3 \mu\text{m}^3$ and acquisition time less than 1 s), the methodology proposed in this study could be extended to the study of capillary-driven flows occurring in industrial fibrous networks or fibre bundles that exhibit complex fibrous architectures (e.g. local variations of the fibre content, fibre misalignment). This experimental approach could also be extended to natural or synthetic fibrous networks made of deformable fibres. In these networks, impregnation phenomena are more complex than those observed in this study. To illustrate the relevance of the proposed approach to study elasto-capillary effects induced during impregnation, we have reported in Fig. 3 shown in S1 a preliminary *in situ* longitudinal impregnation experiments that was carried out on a fibre bundle made of deformable PVDF fibres of diameter 160 μm and length 20 mm. The preliminary experiment shown in Fig. 3 in S1 revealed severe distortion of the flow front with the formation of preferential flow channels and flow-induced (de)-consolidation of the deformable fibre bundle characterised by important re-arrangements and deformation mechanisms of the fibres. A finer analysis of impregnation mechanisms is in progress.

CRediT authorship contribution statement

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Declaration of Competing Interest

The authors declare that they have no known competing financial

- [43] Henderson MA. The interaction of water with solid surfaces: fundamental aspects revisited. *Surf Sci Rep* 2002;46:1–308. [https://doi.org/10.1016/S0167-5729\(01\)00020-6](https://doi.org/10.1016/S0167-5729(01)00020-6).
- [44] Andrew M, Bijeljic B, Blunt MJ. Pore-scale contact angle measurements at reservoir conditions using X-ray microtomography. *Adv Water Resour* 2014;68:24–31. <https://doi.org/10.1016/j.advwatres.2014.02.014>.
- [45] Alhosani A, Lin Q, Scanziani A, Andrews E, Zhang K, Bijeljic B, et al. Pore-scale characterization of carbon dioxide storage at immiscible and near-miscible conditions in altered-wettability reservoir rocks. *Int J Greenhouse Gas Control* 2021;105:103232.
- [46] Ibekwe A, Pokrajac D, Tanino Y. Automated extraction of in situ contact angles from micro-computed tomography images of porous media. *Comput Geosci* 2020; 137:104425. <https://doi.org/10.1016/j.cageo.2020.104425>.
- [47] AlRatrou A, Blunt MJ, Bijeljic B. Spatial Correlation of Contact Angle and Curvature in Pore-Space Images. *Water Resour Res* 2018;54:6133–52. <https://doi.org/10.1029/2017WR022124>.
- [48] Ahn KJ, Seferis JC, Berg JC. Simultaneous measurements of permeability and capillary pressure of thermosetting matrices in woven fabric reinforcements. *Polym Compos* 1991;12:146–52. <https://doi.org/10.1002/pc.750120303>.
- [49] Duprat C, Protière S, Beebe AY, Stone HA. Wetting of flexible fibre arrays. *Nature* 2012;482:510–3. <https://doi.org/10.1038/nature10779>.
- [50] Bico J, Roman B, Moulin L, Bouadaoud A. Elastocapillary coalescence in wet hair. *Nature* 2004;432:690. <https://doi.org/10.1038/432690a>.
- [51] Charpentier J-B, Brändle de Motta JC, Ménard T. Capillary phenomena in assemblies of parallel cylindrical fibers: From statics to dynamics. *Int J Multiph Flow* 2020;129:103304.
- [52] Chevalier L, Bruchon J, Moulin N, Liotier P-J, Drapier S. Accounting for local capillary effects in two-phase flows with relaxed surface tension formulation in enriched finite elements. *Comptes Rendus Mécanique* 2018;346:617–33. <https://doi.org/10.1016/j.crme.2018.06.008>.