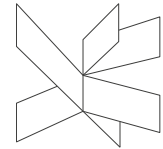


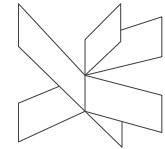
Mandatory Assignment

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1 From Boolean expression to truth table

1.1 Fill out the truth table from the following Boolean expression:

$$Out = A\bar{B}\bar{C} + BC$$

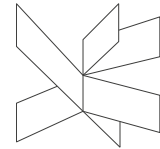
A	B	C	Out
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

omboCtl 1 ✓

1.2 Fill out the truth table from the following Boolean expression:

$$Out = \bar{B}$$

A	B	C	Out
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1



1	0	1	1
1	1	0	0
1	1	1	0

1.3 Fill out the truth table from the following Boolean expression:

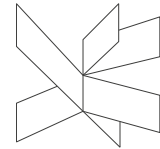
$$Out = 1$$

A	B	C	Out
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

1.4 Fill out the truth table from the following Boolean expression:

$$Out = C(A + B)$$

A	B	C	Out
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0



1	0	1	1
1	1	0	0
1	1	1	1

1.5 Write down the truthtable from the following Boolean expression.

$$Out = B(A + C) + \bar{B} \bar{C} \bar{A}$$

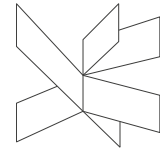
Solution

A	B	C	Out
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

2 From truth table to Boolean expression

2.1 Write down the Boolean expression described by the truthtable and simplify it as much as possible.

A	B	C	Out
0	0	0	0
0	0	1	0



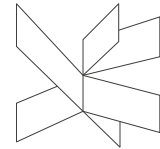
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

SOLUTION

$$\begin{aligned}
 & \bar{A}BC + A\bar{B}C + ABC \\
 & \bar{A}BC + AC(B + \bar{B}) \\
 & \bar{A}BC + AC \\
 & C(\bar{A}B + A) \\
 & C(B + A) \\
 & CB + CA
 \end{aligned}$$

2.2 Write down the Boolean expression described by the truthtable and simplify it as much as possible.

A	B	C	Out
0	0	0	1



0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

SOLUTION

Handwritten solution on grid paper:

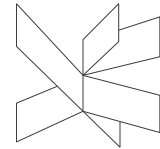
$$\bar{a}\bar{b}\bar{c} + \bar{a}b\bar{c} + a\bar{b}\bar{c} + ab\bar{c}$$

$$\bar{b}\bar{c}(a + \bar{a}) + bc(\bar{a} + a)$$

$$\bar{b}\bar{c} + bc$$

2.3 Write down the Boolean expression described by the truth table and simplify it as much as possible.

A	B	C	Out
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	0
1	0	1	0
1	1	0	1



1	1	1	0
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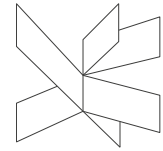
Solution

$$\begin{aligned} \bar{a}\bar{b}c + \bar{a}b\bar{c} + a b \bar{c} \\ \bar{a}\bar{b}c + b\bar{c}(\bar{a} + a) \\ \bar{a}\bar{b}c + b\bar{c} \end{aligned}$$

2.4 Write down the Boolean expression described by the truthtable and simplify it as much as possible.

A	B	C	Out
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	0

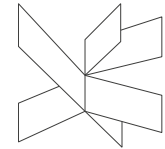
Solution



$$\begin{aligned}
 &\bar{a}\bar{b}\bar{c} + \bar{a}\bar{b}c + a\bar{b}\bar{c} + a\bar{b}c + ab\bar{c} \\
 &\bar{a}\bar{b}(c + \bar{c}) + a\bar{b}(\bar{c} + c) + ab\bar{c} \\
 &\bar{a}\bar{b} + a\bar{b} + a\bar{b}\bar{c} \\
 &\bar{a}\bar{b} + a(\bar{b} + b\bar{c}) \\
 &\bar{a}\bar{b} + a(\bar{b} + \bar{c}) \\
 &\bar{a}\bar{b} + a\bar{b} + a\bar{c} \\
 &\bar{b}(\bar{a} + a) + a\bar{c} \\
 &\bar{b} + a\bar{c}
 \end{aligned}$$

2.5 Write down the Boolean expression described by the truthtable and simplify it as much as possible.

A	B	C	Out
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	0



Solution

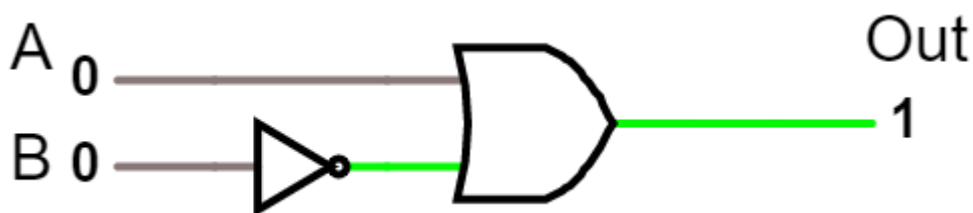
$$\begin{aligned}
 &\bar{a}\bar{b}\bar{c} + \bar{a}\bar{b}c + \bar{a}b\bar{c} + \bar{a}bc + a\bar{b}\bar{c} + a\bar{b}c + ab\bar{c} \\
 &\quad \backslash \quad / \quad \quad \quad \backslash \quad / \quad \quad \quad \backslash \quad / \\
 &\bar{a}\bar{b}(c + \bar{c}) + \bar{a}b(\bar{c} + c) + a\bar{b}(\bar{c} + c) + ab\bar{c} \\
 &\bar{a}\bar{b} + \bar{a}b + a\bar{b} + ab\bar{c} \\
 &\bar{a}(b + \bar{b}) + a(\bar{b} + b\bar{c}) \\
 &\bar{a} + a(\bar{b} + \bar{c}) \\
 &\bar{a} + a\bar{b} + a\bar{c} \\
 &\bar{a} + \bar{b} + \bar{c}
 \end{aligned}$$

3 Boolean expression to circuit.

3.1 Draw the logic circuit described by the following Boolean expression

$$Out = A + \bar{B}$$

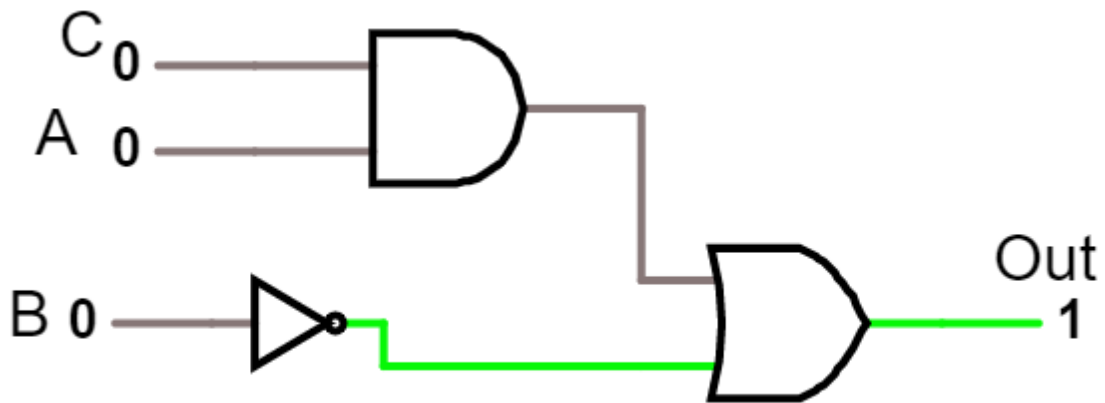
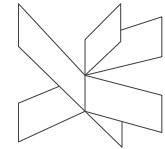
Solution



3.2 Draw the logic circuit described by the following Boolean expression

$$Out = CA + \bar{B}$$

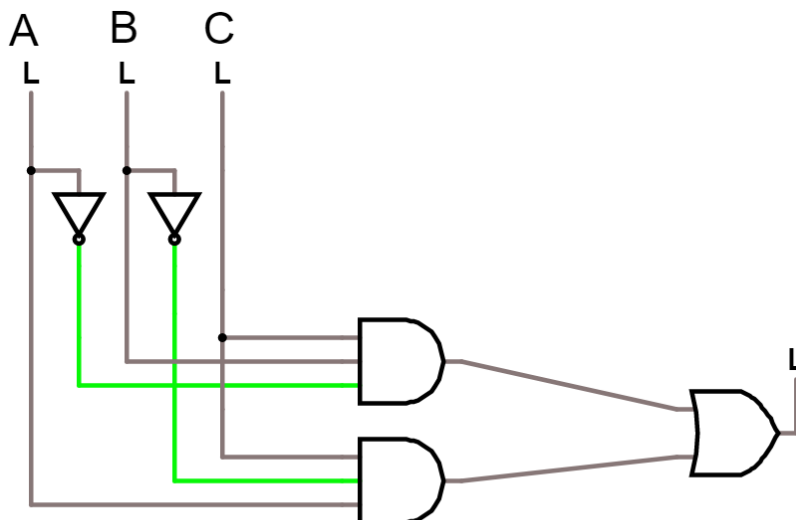
Solution



3.3 Draw the logic circuit described by the following Boolean expression

$$Out = \bar{A}BC + A\bar{B}C$$

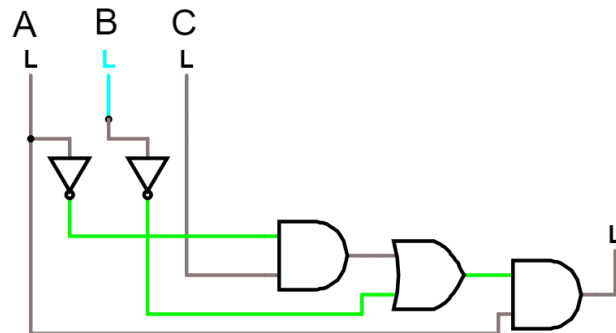
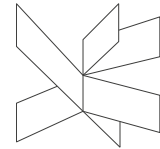
Solution



3.4 Draw the logic circuit described by the following Boolean expression

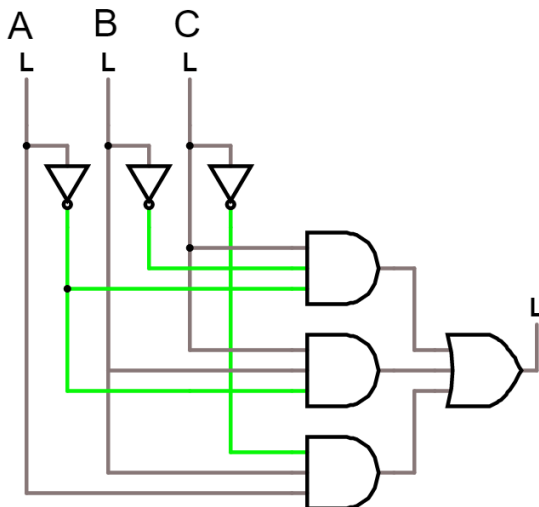
$$Out = A(\bar{B} + \bar{A}C)$$

Solution



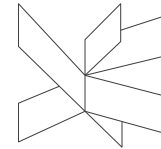
4 From circuit to Boolean expression

4.1 Write down the Boolean expression derived from the logical circuit below:

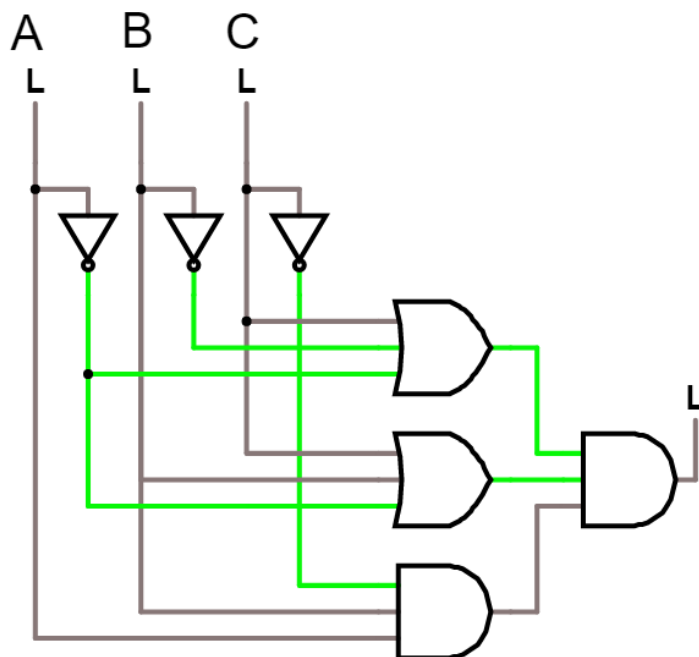


Solution

$$\overline{A}\overline{B}C + \overline{A}BC + A\overline{B}\overline{C}$$



4.2 Write down the Boolean expression derived from the logical circuit below:

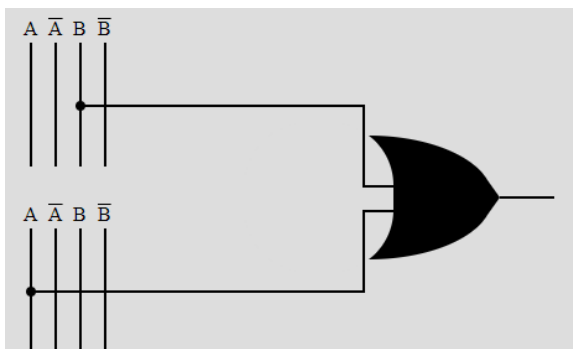


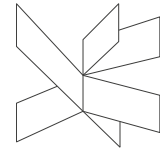
Solution

$$(\bar{A} + \bar{B} + C)(\bar{A} + B + C)(AB\bar{C})$$

5 From circuit to truth table

5.1 Write down the truth table from the following circuit:



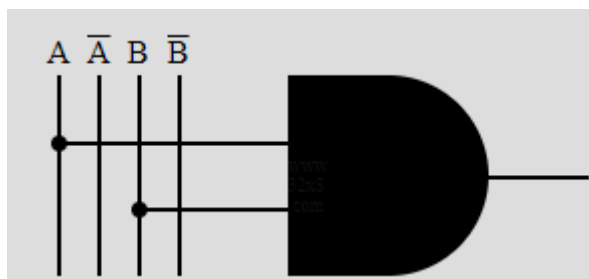


A	B	Out
0	0	
0	1	
1	0	
1	1	

Solution

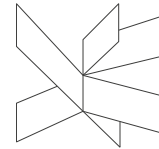
A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

5.2 Write down the truth table from the following circuit:

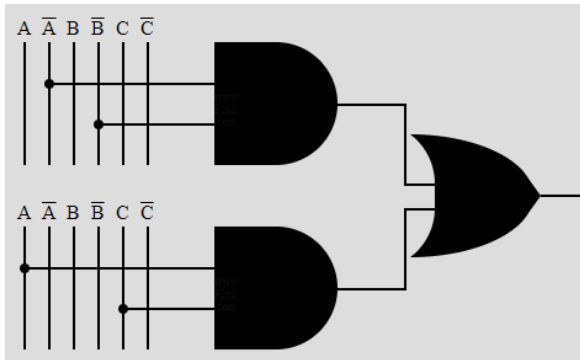


Solution

A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1



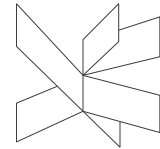
5.3 Write down the truthtable from the following circuit:



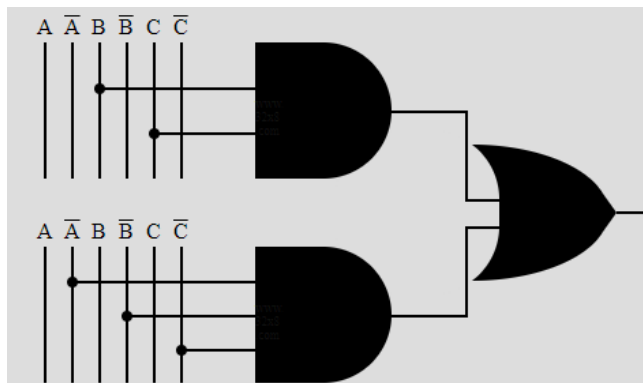
A	B	C	Out
0	0	0	
0	0	1	
0	1	0	
0	1	1	
1	0	0	
1	0	1	
1	1	0	
1	1	1	

Solution

A	B	C	Y
0	0	0	1
0	0	1	1
0	1	0	0
0	1	1	0
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

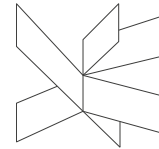


5.4 Write down the truthtable from the following circuit:

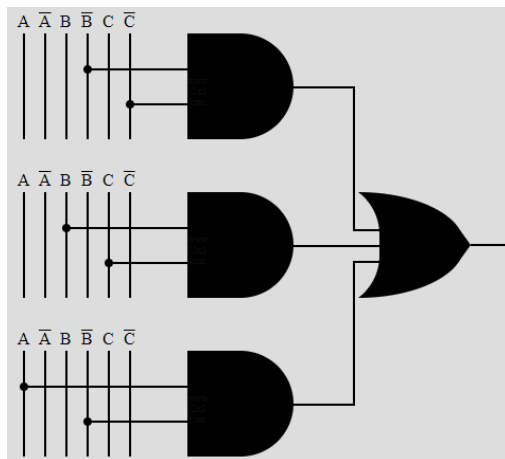


Solution

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	1



5.5 Write down the truth table from the following circuit:



Solution

A	B	C	Y
0	0	0	1
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1