

Ejercicio 3

$$\begin{aligned}
& \langle \forall x :: \neg(\underline{P.x \implies Q.x}) \rangle \vee \langle \exists x :: \underline{False \wedge P.x} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Caract. Implicación } P:=P.x; Q:=Q.x\} \\
& \langle \forall x :: \neg(\neg P.x \vee Q.x) \rangle \vee \langle \exists x :: \underline{False \wedge P.x} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Conmut. Conjuncion } P:=False; Q:=P.x\} \\
& \langle \forall x :: \neg(\neg P.x \vee Q.x) \rangle \vee \langle \exists x :: \underline{P.x \wedge False} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Elem. Absorbente Conjuncion } P:=P.x\} \\
& \langle \forall x :: \neg(\neg P.x \vee Q.x) \rangle \vee \langle \exists x :: \underline{False} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Termino Constante } \exists, C:=False\} \\
& \underline{\langle \forall x :: \neg(\neg P.x \vee Q.x) \rangle \vee False} \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Elem. Neutro Disyuncion } P:=\langle \forall x :: \neg(\neg P.x \vee Q.x) \rangle\} \\
& \langle \forall x :: \underline{\neg(\neg P.x \vee Q.x)} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{De Morgan } P:=\neg P.x \ Q:=Q.x\} \\
& \langle \forall x :: \underline{\neg\neg P.x \wedge \neg Q.x} \rangle \equiv (\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle) \\
& \equiv \{\text{Doble negacion, } P:=P.x\} \\
& \langle \forall x :: P.x \wedge \neg Q.x \rangle \equiv \underline{(\langle \forall x :: P.x \rangle \wedge \langle \forall x :: \neg Q.x \rangle)} \\
& \equiv \{\text{Regla de termino de } \forall \ t:=P; s:=\neg Q\} \\
& \underline{\langle \forall x :: P.x \wedge \neg Q.x \rangle} \equiv (\langle \forall x :: P.x \wedge \neg Q.x \rangle) \\
& \equiv \{\text{Reflexividad equivalencia}\}
\end{aligned}$$

True