



Dijkstra's algorithm -  
- applied backwards, from  $t$  to  $s$

$$s=0, t=5$$

	x	y	dist: dictionary	priority-queue	next: dictionary																																
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iteration 6	0		$x = 0 = s \Rightarrow$ STOP																																		

The minimum cost walk from  $s=0$  to  $t=5$  is cost =  
= dist[0] = 80 and we build it using next dictionary:

$s=0$ , next[0]=1, next[1]=3, next[3]=4, next[4]=5= $t$

$\Rightarrow 0 \xrightarrow{30} 1 \xrightarrow{30} 3 \xrightarrow{20} 4 \xrightarrow{10} 5$  is the minimum cost walk  
from  $s=0$  to  $t=5$ .