### Hidden Markov Model (HMM) for Market Regime Detection

#### Introduction

In the complex financial markets, detecting shifts in market regimes is essential for building adaptive and resilient investment strategies. A market regime, or a distinct pattern of market behavior, can be thought of as the prevailing mood or condition of the market, such as a bull market (rising prices), a bear market (falling prices), or a volatile sideways market. One of the tools we use for identifying these regimes is a machine learning model called a Hidden Markov Model (HMM). This report explains what an HMM is, how it works, and why it is effective for detecting market regime shifts.

### What is a Hidden Markov Model (HMM)?

The HMM identifies a market regime by inferring it as an hidden state that causes certain visible observations, usually asset returns. It assumes that the system follows a sequence of hidden states, which are not directly visible but manifest via observable data. For market regime detection, it takes a series of asset prices/returns as input and outputs the most likely regime sequence and each timestep's probability of being in each regime.

An analogy is guessing the weather based on what people are wearing. You can't directly observe the temperature, but if you see people wearing coats, you might guess it's cold. If you see sunglasses and shorts, it might be warm and sunny.

### **How does HMM Work?**

The HMM estimates which hidden state the market is most likely in by using patterns in the observed data. Over time, it learns the typical characteristics of each regime and becomes better at detecting transitions. Specifically, it does so by:

- starting with an initial guess about which market regime is most likely (initial state probability)
- using a state transition rule, which estimates how likely it is to move from a given regime to another, such as shifting from bullish to bearish (state transition function)
- relying on something called an emission probability—this tells the model how likely it is to observe a certain pattern in the data (like a strong upward return) if assuming a particular current regime
- continuously updating its beliefs as it observes more data, calculating the likelihood of being in each regime at every step

Behind the scenes, the HMM ties together these components to form a "most likely path" of regimes through time by calculating a joint probability density function (joint PDF), which describes the likelihood of being in a particular sequence of states and observing a particular series of data. It's like a running scorecard that helps the model choose the most likely regime and update its beliefs as new data comes in. This helps the model derive an answer to questions like, "How likely is it that the market is in a bullish regime and we see this kind of return today?"

So, when the HMM identifies a likely shift in regimes—say from stable growth to heightened volatility—it's using all this probability math in the background to make that call. The benefit is that we get a real-time, data-driven view of where the market might head next.

Notably, the HMM involves one fundamental assumption: the state transition function and the emission probability are time-invariant. In other words, the likelihood of changing into a particular state and the likelihood of seeing a particular pattern of data both depend only on the current hidden state.

# Why Use HMM for Market Regime Detection?

Traditional investment models often assume that market behavior is consistent, which is not how the market is in real life (see Stolborg and Jørgensen). HMMs recognize that the market behave differently in different periods so that investors can adjust to the market conditions. Some advantages of the HMM are:

- They capture hidden dynamics—Many regime shifts are not obvious in real-time. HMMs help uncover these shifts early by detecting subtle changes in the data.
- They are adaptable—As more data becomes available, HMMs update their understanding of the market conditions. This makes them suitable for real-time strategy adjustments.
- They model realistic transitions—HMMs tend to remain in a particular state for a
  sustained period before suddenly switching to a new one (see QuantStart). This
  mirrors how market regimes behave in reality, such as a long-lasting bull market that
  abruptly shifts to a bear phase following a global event. This makes them ideal for
  modeling market dynamics influenced by macroeconomic forces and regulatory
  changes.
- They provide probabilistic insights—Instead of rigid yes-or-no decisions, HMMs assign probabilities to different regimes. This allows investors to assess risk more dynamically.
- They combine multiple indicators—HMMs can fuse multiple data sources, such as returns, volatility, and volume, into a single regime classification, improving robustness.

## Case Study: A Successful HMM Application in Speech Recognition

In his influential 1989 paper, Lawrence Rabiner demonstrated how Hidden Markov Models could power automatic speech recognition—the core technology behind voice assistants and transcription tools. He explained that speech consists of sequences of sound units, such as phonemes, each associated with distinctive audio features. These sounds are the "hidden states" in the model, while the actual recorded audio (in the form of frequency and timing patterns) are the observations.

Rabiner showed how HMMs could be trained to recognize these hidden patterns by learning three sets of probabilities: the likelihood of transitioning from one sound to another (state transition), the likelihood of a sound producing specific audio features (emission), and the probability of starting with each sound (initial state). When a person speaks, the system evaluates which of these trained probabilities most likely produced the incoming sound patterns and sequence of words.

This approach allowed early voice recognition systems to understand continuous, real-world speech—despite background noise, different speaking speeds, or accents. Rabiner's work laid the foundation for many commercial applications and demonstrated the

versatility of HMMs beyond finance. Just like in markets, where the goal is to decode the underlying regime behind noisy returns, in speech recognition, HMMs decode meaning from variable acoustic input.

# **Case Study: HMMs in Action in Factor Investing**

A 2020 study by Wang, Lin, and Mikhelson titled *Regime-Switching Factor Investing with Hidden Markov Models* presents a compelling real-world application of HMMs in asset management. The researchers applied HMMs to daily return and volatility of S&P 500 ETF data and identified three distinct regimes—bull, bear, and neutral. Instead of applying the same investing strategy throughout all market conditions, the HMM dynamically adjusted factor exposures based on the inferred market regime.

For instance, during periods classified as low-volatility or "stable" regimes, traditional factors like momentum and quality performed well. In contrast, during high-volatility regimes, those same strategies underperformed. The HMM-based system outperformed fixed-allocation approaches by adapting to these shifts in real-time. It generated higher risk-adjusted returns, as reflected by Sharpe Ratio, Treynor Ratio, and Information Ratio. The study concluded that HMMs provided an effective tool to enhance returns and reduce drawdowns by diversifying investment to different factor models, which hedge against market conditions and macroeconomic regimes that a single model would otherwise be susceptible to. This makes a strong case for incorporating regime-aware models into modern investment strategies.

#### **Conclusion**

Hidden Markov Models offer a powerful yet intuitive way to understand shifts in market behavior. By recognizing that the market transitions between different regimes and that these transitions can be modeled using observed data, HMMs provide timely and valuable insights. We can adjust our strategies accordingly, reduce risk during downturns, and position ourselves to take advantage of uptrends. This adaptability is what makes HMMs so valuable in today's dynamic financial world.

# References

Regime-based asset allocation: Dynamic portfolio optimization with Hidden Markov Models
— Christian Stolborg, Mathias Jørgensen

<u>Hidden Markov Models – An Introduction — QuantStart</u>

A tutorial on hidden Markov models and selected applications in speech recognition — Lawrence Rabiner

Regime-Switching Factor Investing with Hidden Markov Models — Matthew Wang, Yi-Hong Lin, Ilya Mikhelson