

# KNN Algorithm

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1. To classify document  $d$  into class  $c$
2. Define  $k$ -neighborhood  $N$  as  $k$  nearest neighbors (according to a given distance or similarity measure) of  $d$
3. Count number of documents  $k_c$  in  $N$  that belong to  $c$
4. Estimate  $P(c|d)$  as  $k_c/k$
5. Choose as class  $\operatorname{argmax}_c P(c|d)$  [= majority class]

## Finding similar rows

### Distance functions

Euclidean

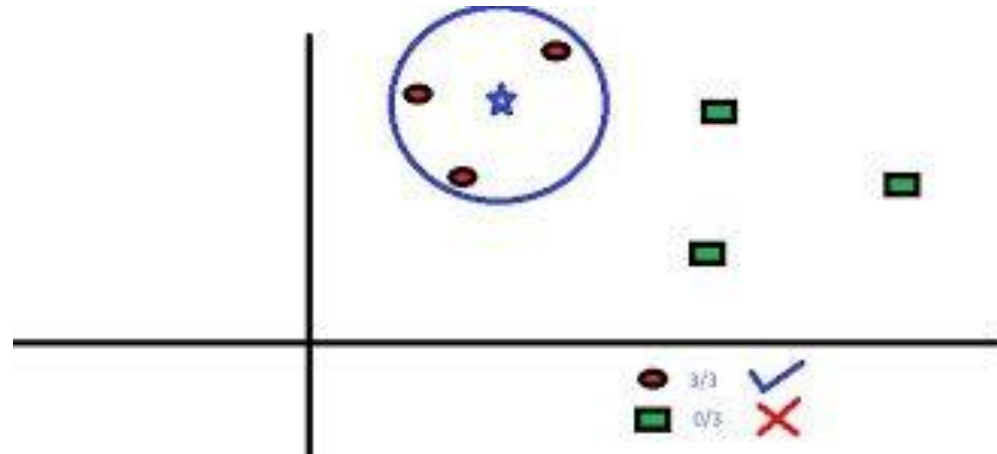
$$\sqrt{\sum_{i=1}^k (x_i - y_i)^2}$$

Manhattan

$$\sum_{i=1}^k |x_i - y_i|$$

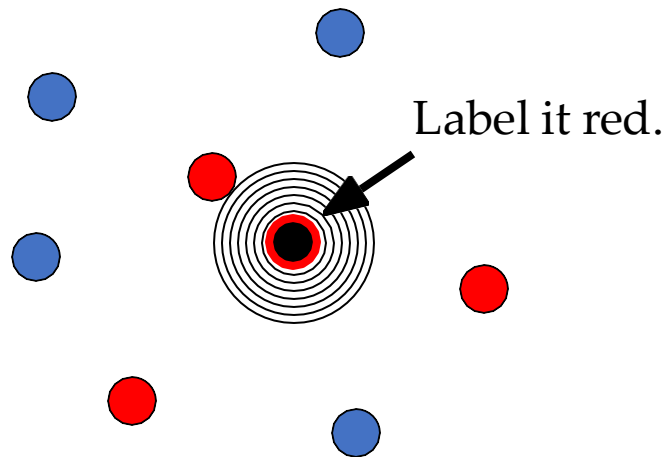
Minkowski

$$\left( \sum_{i=1}^k (|x_i - y_i|)^q \right)^{1/q}$$



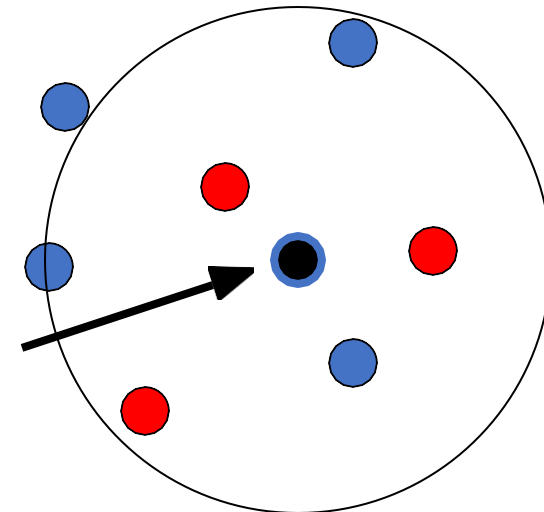
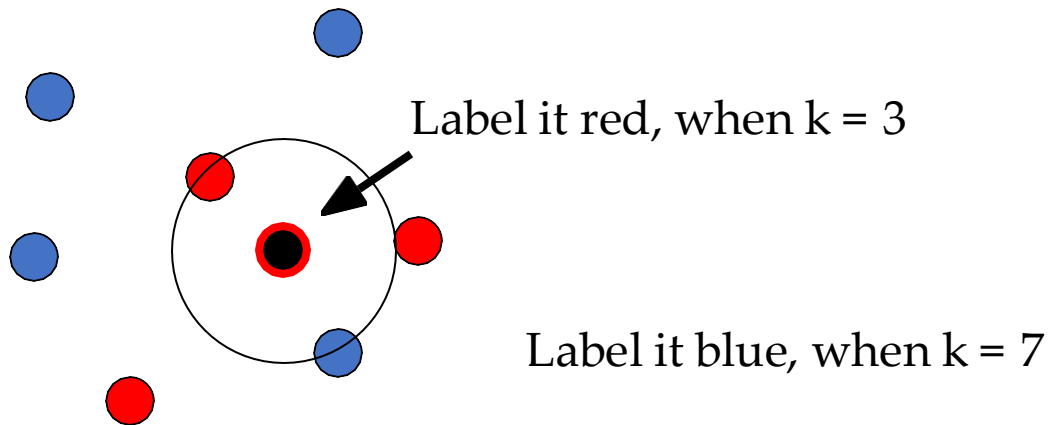
# 1-Nearest Neighbor

- One of the simplest of all machine learning classifiers
- Simple idea: label a new point the same as the closest known point



# k – Nearest Neighbor

- Generalizes 1-NN to smooth away noise in the labels
- A new point is now assigned **the most frequent label of its  $k$  nearest neighbors**



# KNN Example

	Food (3)	Chat (2)	Fast (2)	Price (3)	Bar (2)	BigTip
1	great	yes	yes	normal	no	yes
2	great	no	yes	normal	no	yes
3	mediocre	yes	no	high	no	no
4	great	yes	yes	normal	yes	yes

Similarity metric: Number of matching attributes (k=2)

• New examples:

- Example 1 (great, no, no, normal, no) **Yes**
  - most similar: number 2 (1 mismatch, 4 match) □ **yes**
  - Second most similar example: number 1 (2 mismatch, 3 match) □ **yes**
- Example 2 (mediocre, yes, no, normal, no) **Yes/No**
  - Most similar: number 3 (1 mismatch, 4 match) □ **no**
  - Second most similar example: number 1 (2 mismatch, 3 match) □ **yes**

We have data from survey (to ask people opinion) and objective testing with two attributes(acid durability and strength) to classify whether a special paper tissue is good or not. Here is four training samples

X1(Acid) in seconds	X2(Strength) in kg/square meter	Y = Classification
7	7	Bad
7	4	Bad
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Now the factory produces a new paper tissue that pass laboratory test with  $X1 = 3$  and  $X2 = 7$ .

Without another expensive survey, can we guess what the classification of this new tissue is?

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<b>X1(Acid) in seconds</b>	<b>X2(Strength) in kg/square meter</b>	<b>Square Distance to query instance(3,7)</b>
<b>7</b>	<b>7</b>	$(7-3)^2 + (7-7)^2 = 16$
<b>7</b>	<b>4</b>	$(7-3)^2 + (4-7)^2 = 25$
<b>3</b>	<b>4</b>	$(3-3)^2 + (4-7)^2 = 9$
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X1(Acid) in seconds	X2(Strength) in kg/square meter	Square Distance to query instance(3,7)	Rank minimum distance	Is it included in 3-Nearest Neighbors?
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7	4	$(7-3)^2 + (4-7)^2 = 25$	4	No
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We have 2 good and 1 bad, since 2>1 then we conclude that a new paper tissue that pass laboratory test with X1 = 3 and X2 =7 is included in **Good category**



# KNN – Distance

Age	Loan	Default	Distance
25	\$40,000	N	102000
35	\$60,000	N	82000
45	\$80,000	N	62000
20	\$20,000	N	122000
35	\$120,000	N	22000
52	\$18,000	N	124000
23	\$95,000	Y	47000
40	\$62,000	Y	80000
60	\$100,000	Y	42000
48	\$220,000	Y	78000
33	\$150,000	Y	8000
48	\$142,000	?	

Euclidean Distance

$$D = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

# KNN – Standardized Distance

Age	Loan	Default	Distance
0.125	0.11	N	0.7652
0.375	0.21	N	0.5200
0.625	0.31	N	0.3160
0	0.01	N	0.9245
0.375	0.50	N	0.3428
0.8	0.00	N	0.6220
0.075	0.38	Y	0.6669
0.5	0.22	Y	0.4437
1	0.41	Y	0.3650
0.7	1.00	Y	0.3861
0.325	0.65	Y	0.3771
0.7	0.61	?	

Standardized Variable

$$X_s = \frac{X - Min}{Max - Min}$$

# Behaviour

Large  $k$  : Smoother boundaries (class separating)

Large  $N$  : Large storage req. (space complexity)

Large  $p$  : lower accuracy (curse of dimensionality)

## Step 1

```
1 import numpy as np
2 from sklearn.preprocessing import Imputer
3 from sklearn.cross_validation import train_test_split
4 from sklearn.neighbors import KNeighborsClassifier
5 from sklearn.metrics import accuracy_score
```

## Step 2 - Import Data

## Step 3

```
1 X_train, X_test, y_train, y_test = train_test_split(
2     X, Y, test_size = 0.3, random_state = 100)
3 y_train = y_train.ravel()
4 y_test = y_test.ravel()
```

## Step 4

```
1 for K in range(25):
2     K_value = K+1
3     neigh = KNeighborsClassifier(n_neighbors = K_value, weights='uniform', algorithm='auto')
4     neigh.fit(X_train, y_train)
5     y_pred = neigh.predict(X_test)
6     print "Accuracy is ", accuracy_score(y_test,y_pred)*100,"% for K-Value:",K_value
```

# KNN Advantage

Makes no assumptions about distributions of classes in feature space

Can work for multi classes simultaneously

Easy to implement and understand

Not impacted by outliers

# KNN

## Disadvantage

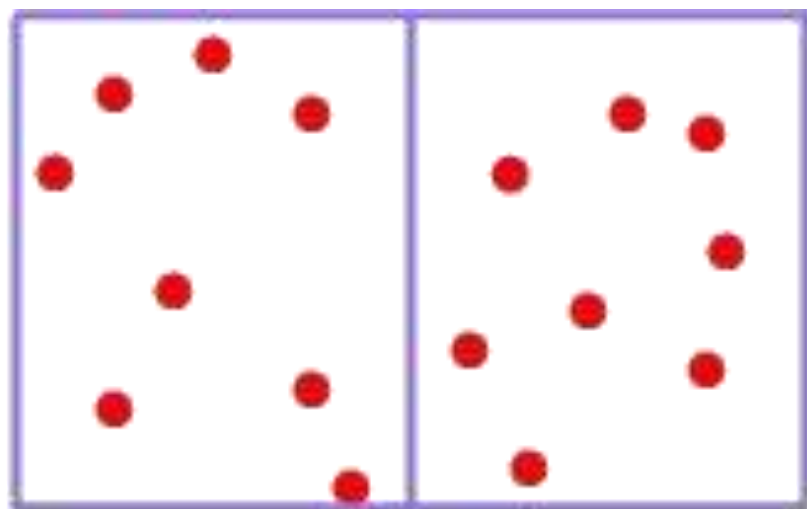
Fixing the optimal value of K is a challenge

Will not be effective when the class distributions overlap

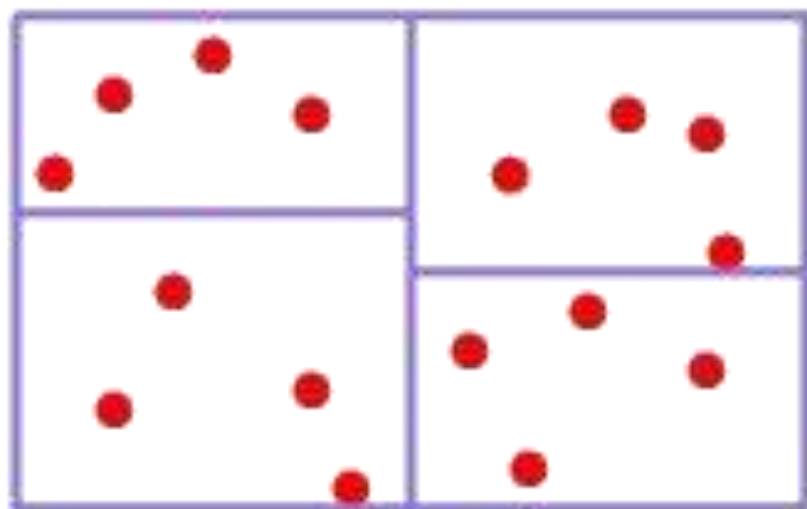
Does not output any models. Calculates distances for every new point (lazy learner)

Computationally intensive ( $O(D(N^2))$ ), can be addressed using KD algorithms which take time to prepare

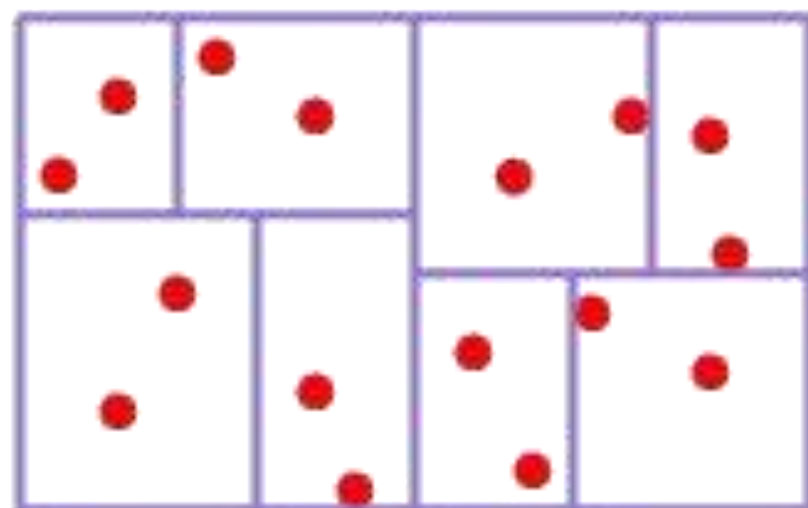
1.



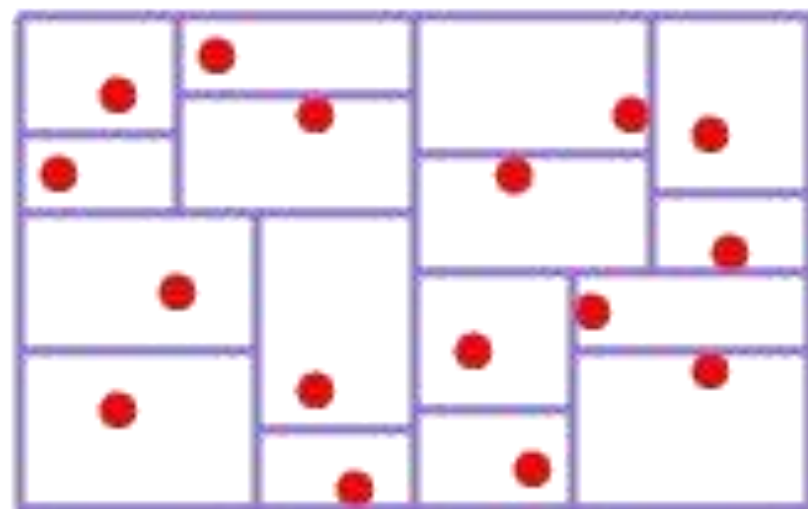
2.

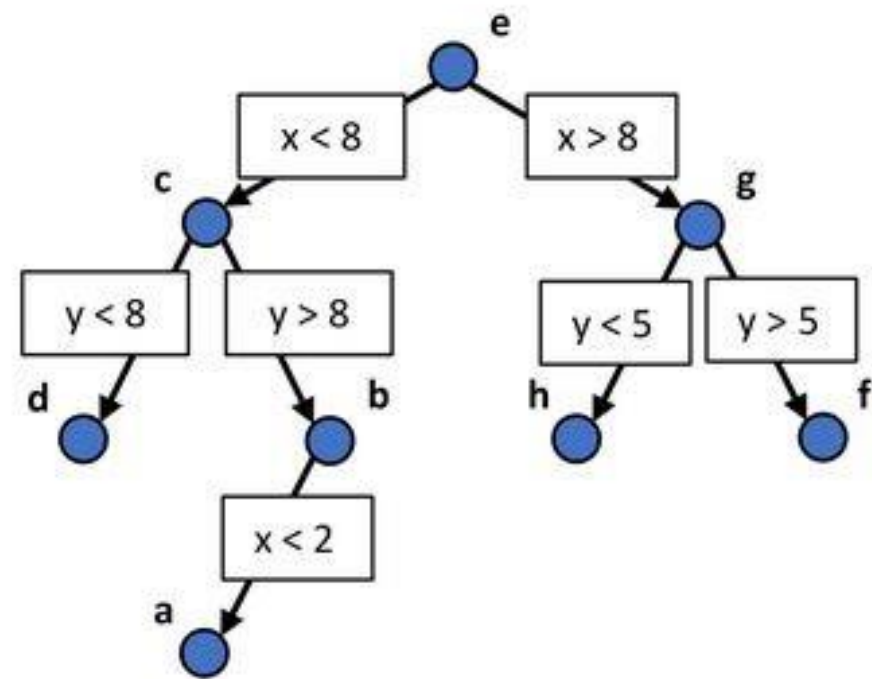
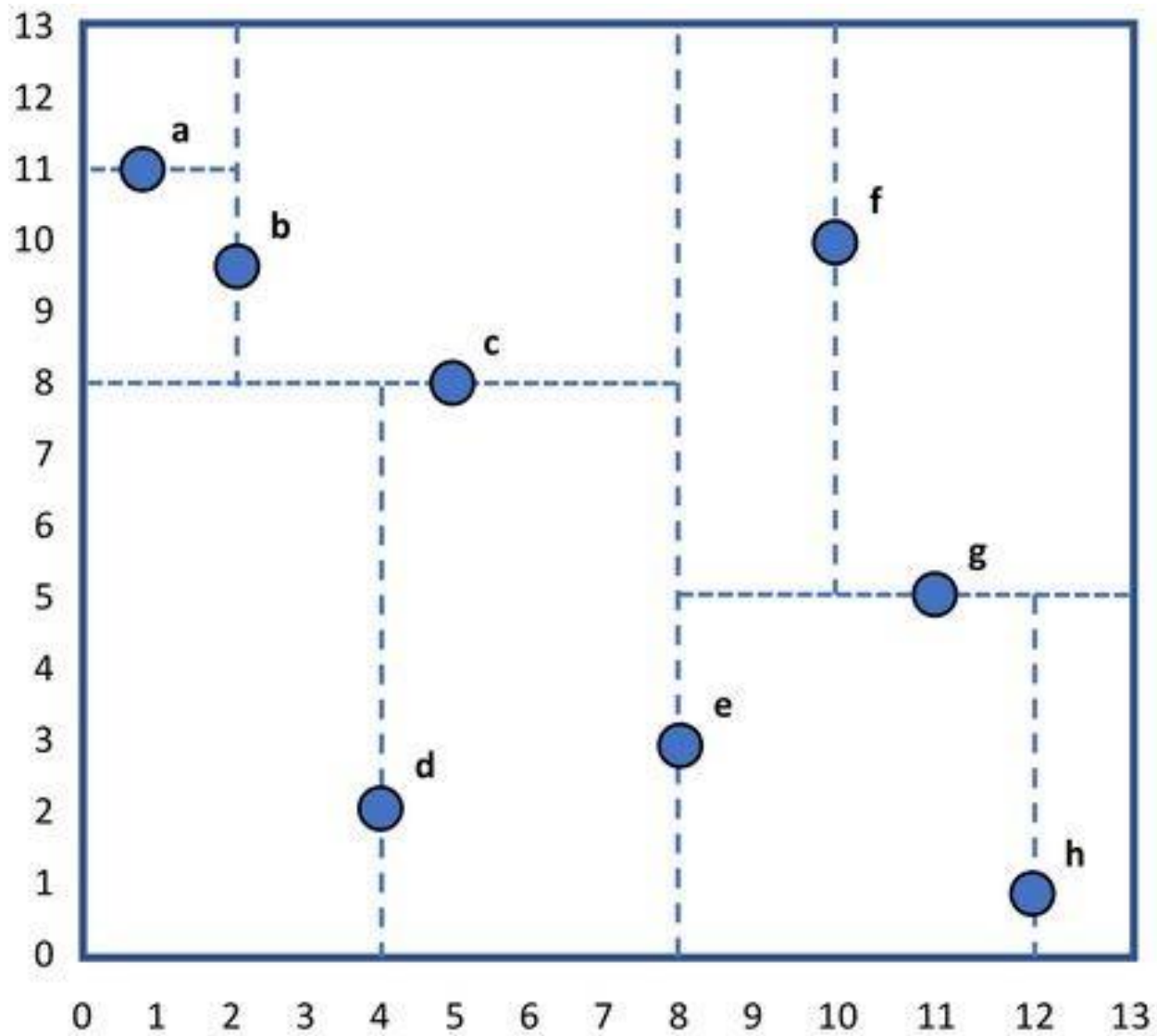


3.

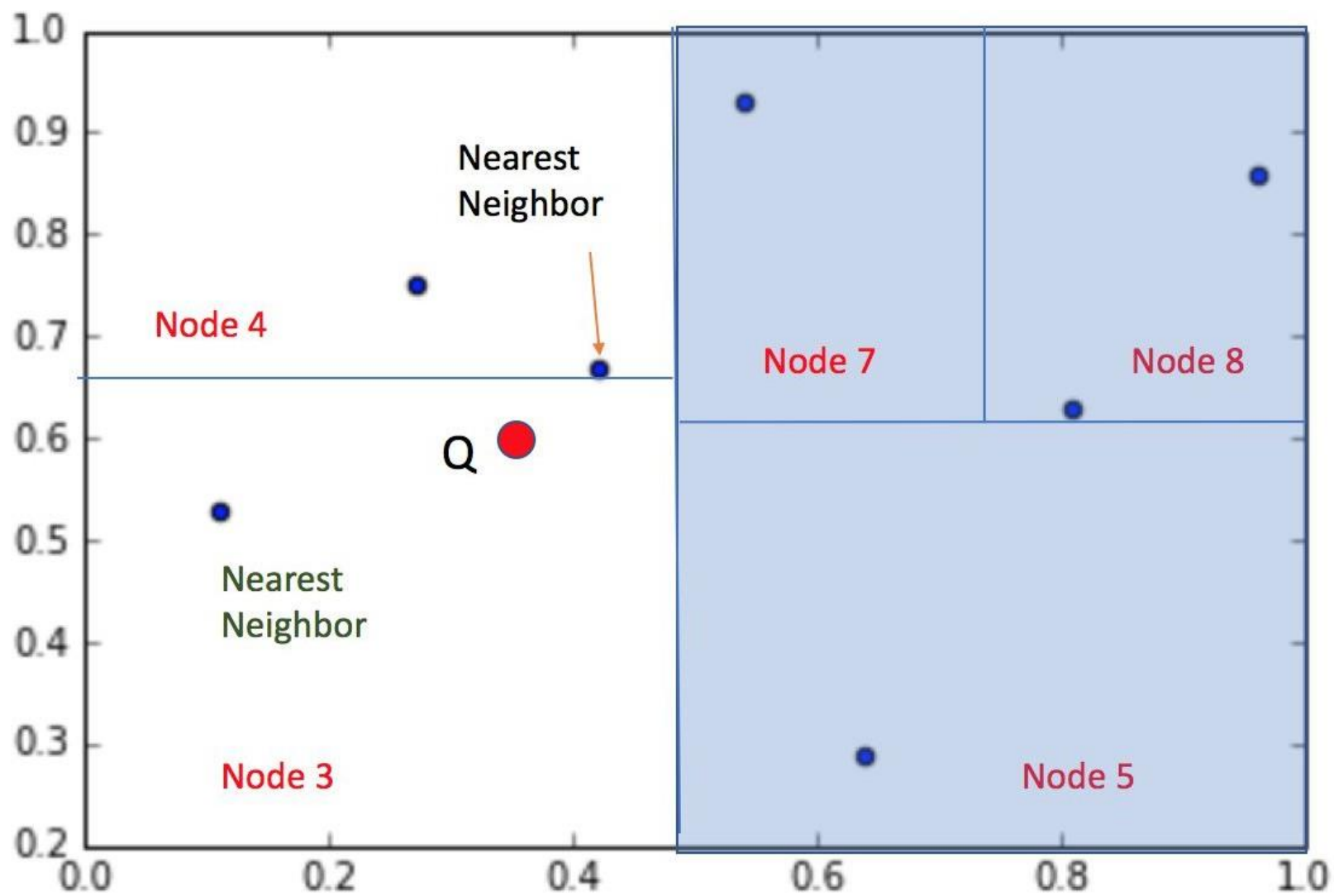


4.











THANK YOU