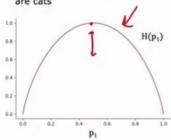
Congratulations! You passed! Grade received 100% Latest Submission Grade 100% To pass 80% or higher

Entropy as a measure of impurity

p₁ = fraction of examples that are cats



$$p_0 = 1 - p_1$$

$$H(p_1) = -p_1 log_2(p_1) - p_0 log_2(p_0)$$

= -p_1 log_2(p_1) - (1 - p_1)log_2(1 - p_1)

Note: " $0 \log(0)$ " = 0

Recall that entropy was defined in lecture as $H(p_{-}1) = -p_{-}1 \log_{-}2(p_{-}1) - p_{-}0 \log_{-}2(p_{-}0)$, where $p_{-}1$ is the fraction of positive examples and $p_{-}0$ the fraction of negative examples.

At a given node of a decision tree, , 6 of 10 examples are cats and 4 of 10 are not cats. Which expression calculates the entropy $H(p_1)$ of this group of 10 animals?

0

 $(0.6)log_2(0.6) + (0.4)log_2(0.4)$

0

C $-(0.6)log_2(0.6) - (1 - 0.4)log_2(1 - 0.4)$

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 $-(0.6)log_2(0.6) - (0.4)log_2(0.4)$

0

 $(0.6)log_2(0.6) + (1 - 0.4)log_2(1 - 0.4)$

0

Correct Correct. The expression is $-(p_1)log_2(p_1) - (p_0)log_2(p_0)$

1/1 point

Information gain

$$= H(p_1^{\text{root}}) - \left(w^{\text{left}} H\left(p_1^{\text{left}}\right) + w^{\text{right}} H\left(p_1^{\text{right}}\right) \right)$$

Recall that information was defined as follows

 $H(p_1^{root}) - \left(w^{left}H(p_1^{left}) + w^{right}H(p_1^{right})\right)$

Before a split, the entropy of a group of 5 cats and 5 non-cats is H(5/10). After splitting on a particular feature, a group of 7 animals (4 of which are cats) has an entropy of H(4/7). The other group of 3 animals (1 is a cat) and has an entropy of H(1/3). What is the expression for information gain?

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 $H(0.5) - (\frac{4}{7} * H(4/7) + \frac{4}{7} * H(1/3))$

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H(0.5) - (7*H(4/7) + 3*H(1/3))

 $H(0.5) - ({7 \atop 10}H(4/7) + {3 \atop 10}H(1/3))$

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H(0.5) - (H(4/7) + H(1/3))

Correct. The general expression is $H(p_1^{root}) - \left(w^{left}H(p_1^{left}) + w^{right}H(p_1^{right})\right)$

One not encoding

Ear shape	Pointy ears	Floppy ears	Oval ears	Face shape	Whiskers	Cat
Pointy	1	0	0	Round	Present	1
7 Oval	0	0	1	Not round	Present	1
Oval .	0	0	1	Round	Absent	0
Pointy	1	0	0	Not round	Present	0
Oval	0	0	1	Round	Present	1
Pointy	1	0	0	Round	Absent	1
Floppy	0	1	0	Not round	Absent	0
Oval	0	0	1	Round	Absent	1
Floppy	7 0	1	0	Round	Absent	0
Floppy	0	1	0	Round	Absent	0

0

0

Splitting on a continuous variable

