

Machine learning using structural representations for discovery of high temperature superconductors

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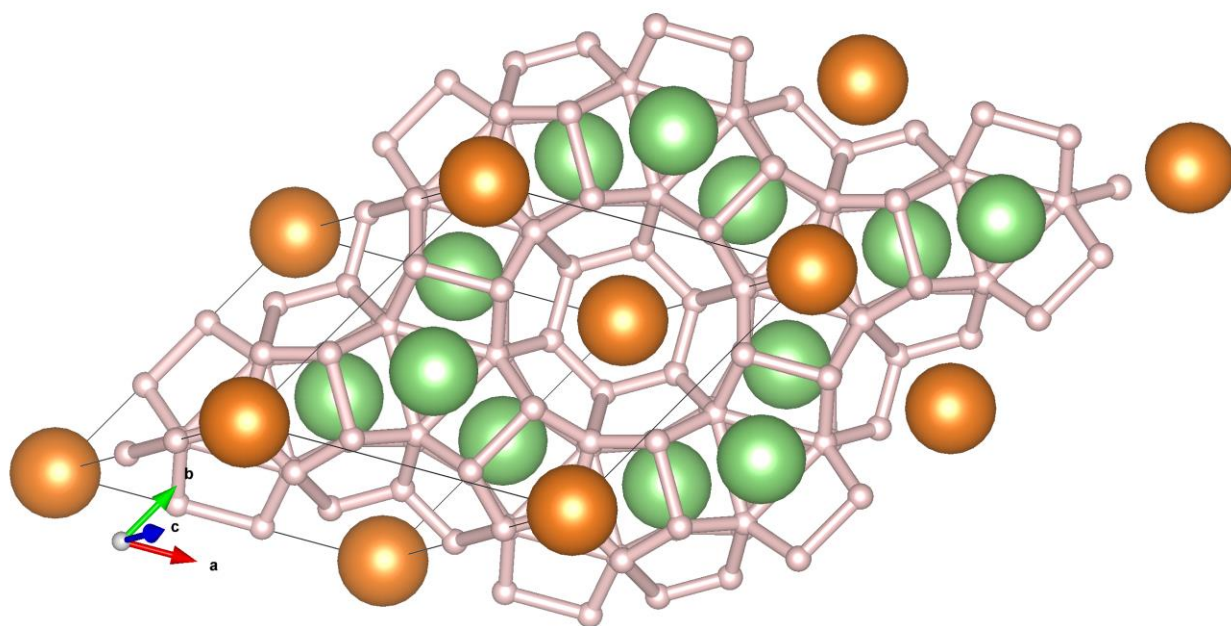


Fig 1. Fd-3m Li₂MgH₁₆ To show the clathrate structure all the H-H bonds were taken to be 1.6 Å. Below is crystallographic information for the above structure with all atoms present in the primitive unit cell (ie. a P1 representation).

```

data_Li4Mg2H32
_symmetry_space_group_name_H-M 'P 1'
_cell_length_a 4.75000000
_cell_length_b 4.75000000
_cell_length_c 4.75000000
_cell_angle_alpha 60.00000000
-
cell_angle_beta 60.00000000
_cell_angle_gamma 60.00000000
_symmetry_Int_Tables_number 1
_chemical_formula_structural Li4Mg2H32
_chemical_formula_sum 'Li4 Mg2 H32'
_cell_formula_units_Z 1
loop_
_symmetry_equiv_pos_site_id
_symmetry_equiv_pos_as_xyz
1 'x, y, z'
loop_
_atom_site_type_symbol
_atom_site_label
_atom_site_symmetry_multiplicity
_atom_site_fract_x

```

| | | | _atom_site_fract_y | _atom_site_fract_z | _atom_site_occupancy |
|----|-----|---|--------------------|--------------------|----------------------|
| H | H0 | 1 | 0.16695000 | 0.16694500 | 0.49916000 1 |
| H | H1 | 1 | 0.25084000 | 0.58305500 | 0.58305000 1 |
| H | H2 | 1 | 0.16695000 | 0.49916000 | 0.16694500 1 |
| H | H3 | 1 | 0.58305500 | 0.58305500 | 0.58305000 1 |
| H | H4 | 1 | 0.16694500 | 0.16694500 | 0.16695000 1 |
| H | H5 | 1 | 0.58305500 | 0.25084000 | 0.58305500 1 |
| H | H6 | 1 | 0.49916000 | 0.16694500 | 0.16694500 1 |
| H | H7 | 1 | 0.58304500 | 0.58305500 | 0.25084000 1 |
| H | H8 | 1 | 0.12508000 | 0.74560000 | 0.38372000 1 |
| H | H9 | 1 | 0.36628000 | 0.62492000 | 0.00440000 1 |
| H | H10 | 1 | 0.74560000 | 0.38372000 | 0.74560000 1 |
| H | H11 | 1 | 0.00440000 | 0.00440000 | 0.62492000 1 |
| H | H12 | 1 | 0.74560000 | 0.12508000 | 0.74560000 1 |
| H | H13 | 1 | 0.62492000 | 0.36628000 | 0.00440000 1 |
| H | H14 | 1 | 0.38372000 | 0.74560000 | 0.12508000 1 |
| H | H15 | 1 | 0.00440000 | 0.00440000 | 0.36628000 1 |
| H | H16 | 1 | 0.74560000 | 0.38372000 | 0.12508000 1 |
| H | H17 | 1 | 0.62492000 | 0.00440000 | 0.36628000 1 |
| H | H18 | 1 | 0.38372000 | 0.74560000 | 0.74560000 1 |
| H | H19 | 1 | 0.00440000 | 0.62492000 | 0.00440000 1 |
| H | H20 | 1 | 0.12508000 | 0.74560000 | 0.74560000 1 |
| H | H21 | 1 | 0.36628000 | 0.00440000 | 0.62492000 1 |
| H | H22 | 1 | 0.74560000 | 0.12508000 | 0.38372000 1 |
| H | H23 | 1 | 0.00440000 | 0.36628000 | 0.00440000 1 |
| H | H24 | 1 | 0.38372000 | 0.12508000 | 0.74560000 1 |
| H | H25 | 1 | 0.00440000 | 0.36628000 | 0.62492000 1 |
| H | H26 | 1 | 0.74560000 | 0.74560000 | 0.38372000 1 |
| H | H27 | 1 | 0.62492000 | 0.00440000 | 0.00440000 1 |
| H | H28 | 1 | 0.74560000 | 0.74560000 | 0.12508000 1 |
| H | H29 | 1 | 0.00440000 | 0.62492000 | 0.36628000 1 |
| H | H30 | 1 | 0.12508000 | 0.38372000 | 0.74560000 1 |
| H | H31 | 1 | 0.36628000 | 0.00440000 | 0.00440000 1 |
| Li | X32 | 1 | 0.37500000 | 0.37500000 | 0.87500000 1 |
| Li | X33 | 1 | 0.87500000 | 0.37500000 | 0.37500000 1 |
| Li | X34 | 1 | 0.37500000 | 0.87500000 | 0.37500000 1 |
| Li | X35 | 1 | 0.37500000 | 0.37500000 | 0.37500000 1 |
| Mg | Y36 | 1 | 0.00000000 | 0.00000000 | 0.00000000 1 |
| Mg | Y37 | 1 | 0.75000000 | 0.75000000 | 0.75000000 1 |

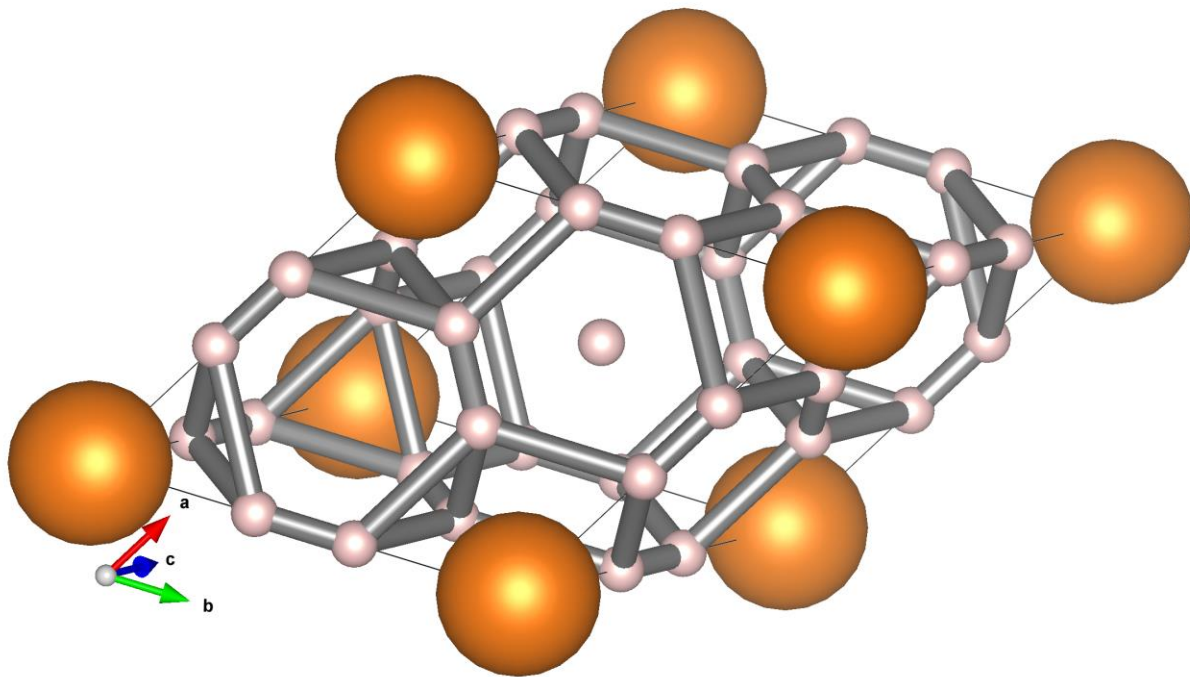


Fig 2. Fm-3m MgH13 Atoms Mg (X1) and H (Y0) are replaced in variants. To show the clathrate structure all the H-H bonds were taken to be 1.6 Å. Below is crystallographic information for the above structure with all atoms present in the primitive unit cell (ie. a P1 representation).

```

data_MgH13
_symmetry_space_group_name_H-M 'P 1'
_cell_length_a 3.46956
_cell_length_b 3.46956
_cell_length_c 3.46956
_cell_angle_alpha 60.00000000
_cell_angle_beta 60.00000000
_cell_angle_gamma 60.00000000
_symmetry_Int_Tables_number 1
_chemical_formula_structural MgH13
_chemical_formula_sum 'Mg1 H13'
_cell_volume 19.09188309
_cell_formula_units_Z 1
loop_
_symmetry_equiv_pos_site_id
_symmetry_equiv_pos_as_xyz
1 'x, y, z'
loop_
_atom_site_type_symbol
_atom_site_label
_atom_site_symmetry_multiplicity
_atom_site_fract_x
_atom_site_fract_y

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_atom_site_fract_z

_atom_site_occupancy

| | | | | | | |
|----|-----|---|------------|------------|------------|---|
| H | Y0 | 1 | 0.50000000 | 0.50000000 | 0.50000000 | 1 |
| Mg | X1 | 1 | 0.00000000 | 0.00000000 | 0.00000000 | 1 |
| H | H2 | 1 | 0.38369000 | 0.00000000 | 0.61631000 | 1 |
| H | H3 | 1 | 0.61631000 | 0.00000000 | 0.38369000 | 1 |
| H | H4 | 1 | 0.38369000 | 0.00000000 | 0.00000000 | 1 |
| H | H5 | 1 | 1.00000000 | 0.00000000 | 0.38369000 | 1 |
| H | H6 | 1 | 0.61631000 | 0.00000000 | 0.00000000 | 1 |
| H | H7 | 1 | 1.00000000 | 0.00000000 | 0.61631000 | 1 |
| H | H8 | 1 | 0.38369000 | 0.61631000 | 0.00000000 | 1 |
| H | H9 | 1 | 0.00000000 | 0.61631000 | 0.38369000 | 1 |
| H | H10 | 1 | 1.00000000 | 0.61631000 | 0.00000000 | 1 |
| H | H11 | 1 | 0.61631000 | 0.38369000 | 0.00000000 | 1 |
| H | H12 | 1 | 0.00000000 | 0.38369000 | 0.61631000 | 1 |
| H | H13 | 1 | 0.00000000 | 0.38369000 | 0.00000000 | 1 |

P-3m1

data_Li2MgH16

_symmetry_space_group_name_H-M 'P 1'

_cell_length_a 2.79596300

_cell_length_b 2.79596300

_cell_length_c 5.3130000

_cell_angle_alpha 90.00000000

_cell_angle_beta 90.00000000

_cell_angle_gamma 120.00000000

_symmetry_Int_Tables_number 1

_chemical_formula_structural Li2MgH16

_chemical_formula_sum 'Li2 Mg1 H16'

_cell_volume 35.97204811

_cell_formula_units_Z 1

loop_

_symmetry_equiv_pos_site_id

_symmetry_equiv_pos_as_xyz

1 'x, y, z'

loop_

_atom_site_type_symbol

_atom_site_label

_atom_site_symmetry_multiplicity

_atom_site_fract_x

_atom_site_fract_y

_atom_site_fract_z

_atom_site_occupancy

Li Li0 1 0.33333333 0.66666667 0.83626000 1

Li Li1 1 0.66666667 0.33333333 0.16374000 1

Mg Mg2 1 0.00000000 0.00000000 0.50000000 1

H H3 1 0.82843000 0.17158000 0.92030000 1

H H4 1 0.17157000 0.82842000 0.07970000 1

H H5 1 0.34315000 0.17157000 0.92030000 1

H H6 1 0.65685000 0.82843000 0.07970000 1

H H7 1 0.82842000 0.65685000 0.92030000 1

H H8 1 0.17158000 0.34315000 0.07970000 1

H H9 1 0.66666667 0.33333333 0.42549000 1

H H10 1 0.33333333 0.66666667 0.57451000 1

H H11 1 0.33333333 0.66666667 0.39139000 1

H H12 1 0.66666667 0.33333333 0.60861000 1

H H13 1 0.32880000 0.16440000 0.76347000 1

H H14 1 0.67120000 0.83560000 0.23653000 1

H H15 1 0.83560000 0.67120000 0.76347000 1

H H16 1 0.16440000 0.32880000 0.23653000 1

H H17 1 0.83560000 0.16440000 0.76347000 1

H H18 1 0.16440000 0.83560000 0.23653000 1

```

Im-3m
data_SeH3
_symmetry_space_group_name_H-M 'P 1'
_cell_length_a 2.24900000
_cell_length_b 2.24900000
_cell_length_c 2.24900000
_cell_angle_alpha 109.47122200
_cell_angle_beta 109.47121927
_cell_angle_gamma 109.47121927
_symmetry_Int_Tables_number 1
_chemical_formula_structural SeH3
_chemical_formula_sum 'Se1 H3'
_cell_volume 8.75682121
_cell_formula_units_Z 1
loop_
_symmetry_equiv_pos_site_id
_symmetry_equiv_pos_as_xyz
1 'x, y, z'
loop_
_atom_site_type_symbol
_atom_site_label
_atom_site_symmetry_multiplicity
_atom_site_fract_x
_atom_site_fract_y
_atom_site_fract_z
_atom_site_occupancy
H H0 1 0.00000000 0.50000000 0.50000000 1
H H1 1 0.50000000 0.50000000 0.00000000 1
H H2 1 0.50000000 0.00000000 0.50000000 1
Se X3 1 0.00000000 0.00000000 0.00000000 1

```

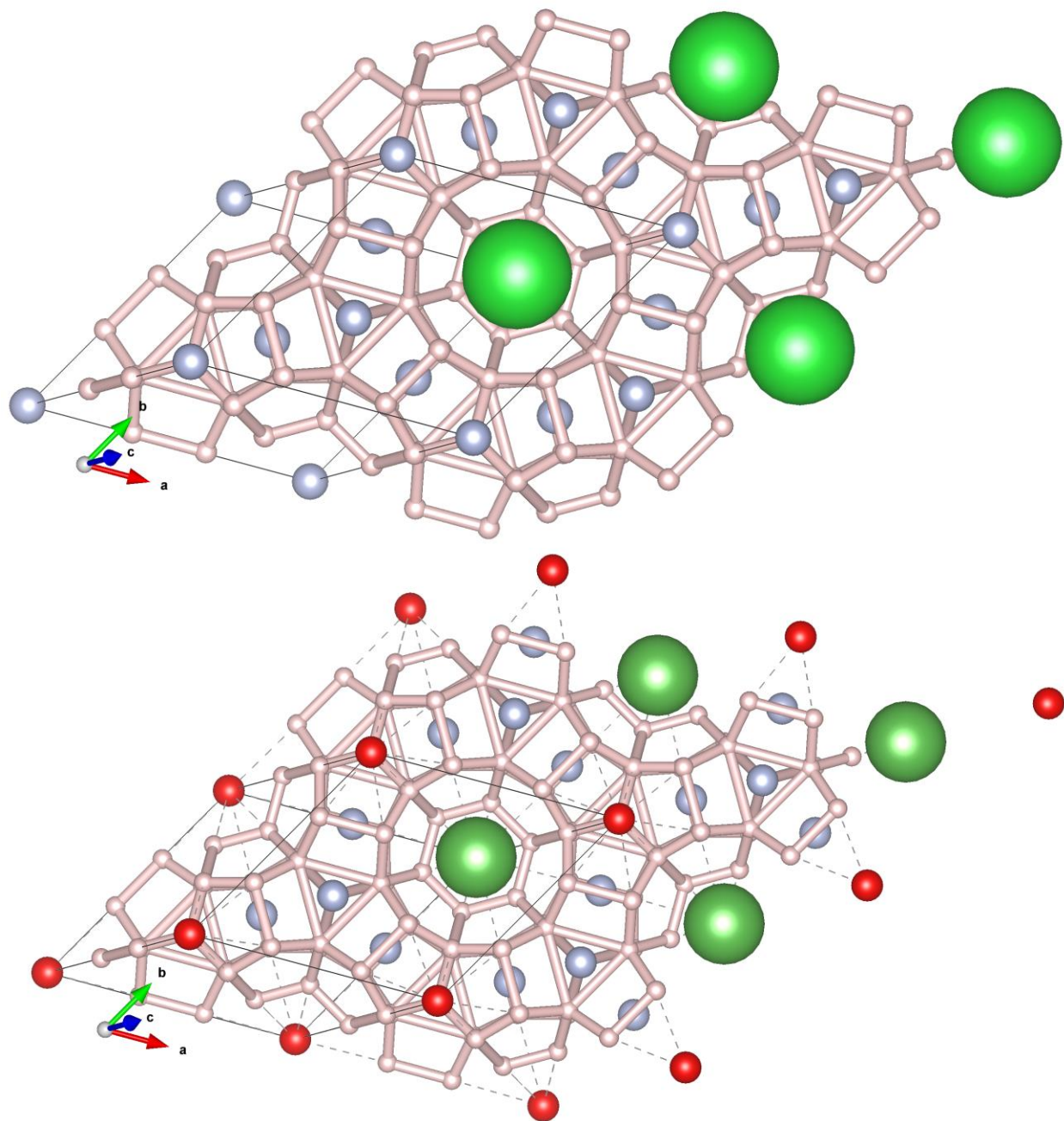


Fig 3. $Fd-3m$ $\text{Li}_2\text{MgH}_{16}$ as $\text{BaH}_{32}\text{N}_5$ (top) and $\text{LaH}_{32}\text{N}_4\text{O}$ (bottom) variants. X: Labels sites part of random search detailed in morphisms section. To show the clathrate structure all the H-H bonds were taken to be 1.6 Å. Below is crystallographic information for the above structure with all atoms present in the primitive unit cell (ie. a P1 representation).

data_LaH32N4O

_symmetry_space_group_name_H-M 'P 1'

_cell_length_a 4.7500

_cell_length_b 4.7500

_cell_length_c 4.7500

_cell_angle_alpha 60.00000000

_cell_angle_beta 60.00000000

_cell_angle_gamma 60.00000000

_symmetry_Int_Tables_number 1

_chemical_formula_structural LaH32N4O

_chemical_formula_sum 'La1 H32 N4 O1'

_cell_volume 21.06541812

_cell_formula_units_Z 1

loop_

_symmetry_equiv_pos_site_id

_symmetry_equiv_pos_as_xyz

1 'x, y, z'

loop_

_atom_site_type_symbol

_atom_site_label

_atom_site_symmetry_multiplicity

_atom_site_fract_x

_atom_site_fract_y

_atom_site_fract_z

_atom_site_occupancy

| | | | | | | |
|---|-----|---|------------|------------|------------|---|
| H | H0 | 1 | 0.16695000 | 0.16694500 | 0.49916000 | 1 |
| H | H1 | 1 | 0.25084000 | 0.58305500 | 0.58305000 | 1 |
| H | H2 | 1 | 0.16695000 | 0.49916000 | 0.16694500 | 1 |
| H | H3 | 1 | 0.58305500 | 0.58305500 | 0.58305000 | 1 |
| H | H4 | 1 | 0.16694500 | 0.16694500 | 0.16695000 | 1 |
| H | H5 | 1 | 0.58305500 | 0.25084000 | 0.58305500 | 1 |
| H | H6 | 1 | 0.49916000 | 0.16694500 | 0.16694500 | 1 |
| H | H7 | 1 | 0.58304500 | 0.58305500 | 0.25084000 | 1 |
| H | H8 | 1 | 0.12508000 | 0.74560000 | 0.38372000 | 1 |
| H | H9 | 1 | 0.36628000 | 0.62492000 | 0.00440000 | 1 |
| H | H10 | 1 | 0.74560000 | 0.38372000 | 0.74560000 | 1 |
| H | H11 | 1 | 0.00440000 | 0.00440000 | 0.62492000 | 1 |
| H | H12 | 1 | 0.74560000 | 0.12508000 | 0.74560000 | 1 |
| H | H13 | 1 | 0.62492000 | 0.36628000 | 0.00440000 | 1 |
| H | H14 | 1 | 0.38372000 | 0.74560000 | 0.12508000 | 1 |
| H | H15 | 1 | 0.00440000 | 0.00440000 | 0.36628000 | 1 |
| H | H16 | 1 | 0.74560000 | 0.38372000 | 0.12508000 | 1 |
| H | H17 | 1 | 0.62492000 | 0.00440000 | 0.36628000 | 1 |
| H | H18 | 1 | 0.38372000 | 0.74560000 | 0.74560000 | 1 |
| H | H19 | 1 | 0.00440000 | 0.62492000 | 0.00440000 | 1 |
| H | H20 | 1 | 0.12508000 | 0.74560000 | 0.74560000 | 1 |
| H | H21 | 1 | 0.36628000 | 0.00440000 | 0.62492000 | 1 |
| H | H22 | 1 | 0.74560000 | 0.12508000 | 0.38372000 | 1 |
| H | H23 | 1 | 0.00440000 | 0.36628000 | 0.00440000 | 1 |
| H | H24 | 1 | 0.38372000 | 0.12508000 | 0.74560000 | 1 |
| H | H25 | 1 | 0.00440000 | 0.36628000 | 0.62492000 | 1 |

| | | | | | | |
|----|-----|---|------------|------------|------------|---|
| H | H26 | 1 | 0.74560000 | 0.74560000 | 0.38372000 | 1 |
| H | H27 | 1 | 0.62492000 | 0.00440000 | 0.00440000 | 1 |
| H | H28 | 1 | 0.74560000 | 0.74560000 | 0.12508000 | 1 |
| H | H29 | 1 | 0.00440000 | 0.62492000 | 0.36628000 | 1 |
| H | H30 | 1 | 0.12508000 | 0.38372000 | 0.74560000 | 1 |
| H | H31 | 1 | 0.36628000 | 0.00440000 | 0.00440000 | 1 |
| N | X32 | 1 | 0.37500000 | 0.37500000 | 0.87500000 | 1 |
| N | X33 | 1 | 0.87500000 | 0.37500000 | 0.37500000 | 1 |
| N | X34 | 1 | 0.37500000 | 0.87500000 | 0.37500000 | 1 |
| N | X35 | 1 | 0.37500000 | 0.37500000 | 0.37500000 | 1 |
| O | X36 | 1 | 0.00000000 | 0.00000000 | 0.00000000 | 1 |
| La | X37 | 1 | 0.75000000 | 0.75000000 | 0.75000000 | 1 |

BaH32N5

data_BaH32N5

_symmetry_space_group_name_H-M 'P 1'

_cell_length_a 4.75000

_cell_length_b 4.75000

_cell_length_c 4.75000

_cell_angle_alpha 60.00000000

_cell_angle_beta 60.00000000

_cell_angle_gamma 60.00000000

_symmetry_Int_Tables_number 1

_chemical_formula_structural BaH32N5

_chemical_formula_sum 'Ba1 H32 N5'

_cell_volume 130.95122613

_cell_formula_units_Z 1

loop_

_symmetry_equiv_pos_site_id

_symmetry_equiv_pos_as_xyz

1 'x, y, z'

loop_

_atom_site_type_symbol

_atom_site_label

_atom_site_symmetry_multiplicity

_atom_site_fract_x

_atom_site_fract_y

_atom_site_fract_z

_atom_site_occupancy

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H0 | 1 | 0.16695000 | 0.16694500 | 0.49916000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H1 | 1 | 0.25084000 | 0.58305500 | 0.58305000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H2 | 1 | 0.16695000 | 0.49916000 | 0.16694500 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H3 | 1 | 0.58305500 | 0.58305500 | 0.58305000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H4 | 1 | 0.16694500 | 0.16694500 | 0.16695000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H5 | 1 | 0.58305500 | 0.25084000 | 0.58305500 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H6 | 1 | 0.49916000 | 0.16694500 | 0.16694500 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H7 | 1 | 0.58304500 | 0.58305500 | 0.25084000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H8 | 1 | 0.12508000 | 0.74560000 | 0.38372000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|----|---|------------|------------|------------|---|
| H | H9 | 1 | 0.36628000 | 0.62492000 | 0.00440000 | 1 |
|---|----|---|------------|------------|------------|---|

| | | | | | | |
|---|-----|---|------------|------------|------------|---|
| H | H10 | 1 | 0.74560000 | 0.38372000 | 0.74560000 | 1 |
|---|-----|---|------------|------------|------------|---|

| | | | | | | |
|---|-----|---|------------|------------|------------|---|
| H | H11 | 1 | 0.00440000 | 0.00440000 | 0.62492000 | 1 |
|---|-----|---|------------|------------|------------|---|

| | | | | | | |
|----|-----|---|------------|------------|------------|---|
| H | H12 | 1 | 0.74560000 | 0.12508000 | 0.74560000 | 1 |
| H | H13 | 1 | 0.62492000 | 0.36628000 | 0.00440000 | 1 |
| H | H14 | 1 | 0.38372000 | 0.74560000 | 0.12508000 | 1 |
| H | H15 | 1 | 0.00440000 | 0.00440000 | 0.36628000 | 1 |
| H | H16 | 1 | 0.74560000 | 0.38372000 | 0.12508000 | 1 |
| H | H17 | 1 | 0.62492000 | 0.00440000 | 0.36628000 | 1 |
| H | H18 | 1 | 0.38372000 | 0.74560000 | 0.74560000 | 1 |
| H | H19 | 1 | 0.00440000 | 0.62492000 | 0.00440000 | 1 |
| H | H20 | 1 | 0.12508000 | 0.74560000 | 0.74560000 | 1 |
| H | H21 | 1 | 0.36628000 | 0.00440000 | 0.62492000 | 1 |
| H | H22 | 1 | 0.74560000 | 0.12508000 | 0.38372000 | 1 |
| H | H23 | 1 | 0.00440000 | 0.36628000 | 0.00440000 | 1 |
| H | H24 | 1 | 0.38372000 | 0.12508000 | 0.74560000 | 1 |
| H | H25 | 1 | 0.00440000 | 0.36628000 | 0.62492000 | 1 |
| H | H26 | 1 | 0.74560000 | 0.74560000 | 0.38372000 | 1 |
| H | H27 | 1 | 0.62492000 | 0.00440000 | 0.00440000 | 1 |
| H | H28 | 1 | 0.74560000 | 0.74560000 | 0.12508000 | 1 |
| H | H29 | 1 | 0.00440000 | 0.62492000 | 0.36628000 | 1 |
| H | H30 | 1 | 0.12508000 | 0.38372000 | 0.74560000 | 1 |
| H | H31 | 1 | 0.36628000 | 0.00440000 | 0.00440000 | 1 |
| N | X32 | 1 | 0.37500000 | 0.37500000 | 0.87500000 | 1 |
| N | X33 | 1 | 0.87500000 | 0.37500000 | 0.37500000 | 1 |
| N | X34 | 1 | 0.37500000 | 0.87500000 | 0.37500000 | 1 |
| N | X35 | 1 | 0.37500000 | 0.37500000 | 0.37500000 | 1 |
| N | X36 | 1 | 0.00000000 | 0.00000000 | 0.00000000 | 1 |
| Ba | X37 | 1 | 0.75000000 | 0.75000000 | 0.75000000 | 1 |