# **Knowledge: Code Explanation**

# logic.py

```
import itertools
```

In Python, <code>itertools</code> is a standard library module that provides a collection of fast, memory-efficient tools for working with iterators, which are objects that can be iterated (looped) over, like lists, tuples, and more. The <code>itertools</code> module contains various functions that allow you to create and manipulate iterators, often in combination with one another, to perform various tasks efficiently.

When you see the line <u>import itertools</u> in a Python script or program, it means that the code is importing the <u>itertools</u> module so that its functionality can be utilized within the script.

```
class Symbol():
    def __init__(self, name):
        self.name = name

def __repr__(self):
        return self.name

def evaluate(self, model):
        try:
            return (model[self.name])
        except KeyError:
            raise Exception(f"variable {self.name} not in model")

def formula(self):
    return self.name

def symbols(self):
    return {self.name}
```

let's break down the details of the Symbol class step by step:

```
class Symbol():
    def __init__(self, name):
        self.name = name
```

Here, you're defining a class named Symbol. This class has a constructor method \_\_init\_\_() that takes a parameter name. Inside the constructor, the value of the parameter is assigned to an instance variable self.name.

```
def __repr__(self):
    return self.name
```

The <u>\_\_repr\_\_()</u> method is defined to customize the string representation of an instance of the Symbol class. It returns the value of self.name, which will be used when you call the repr() function on an instance of this class.

```
def evaluate(self, model):
    try:
        return model[self.name]
    except KeyError:
        raise Exception(f"variable {self.name} not in model")
```

The <code>evaluate()</code> method takes a parameter <code>model</code>, which is presumably a dictionary-like object containing variable names as keys and their corresponding values. Inside the method, it attempts to retrieve the value associated with <code>self.name</code> from the <code>model</code>. If the key <code>self.name</code> doesn't exist in the <code>model</code>, a <code>KeyError</code> will be raised. In that case, an <code>Exception</code> is raised with a message indicating that the variable is not found in the model.

```
def formula(self):
    return self.name
```

The formula() method returns the value of self.name. This method is used to obtain the name of the symbol, which might be useful when you want to represent the symbol in a formulaic context.

```
def symbols(self):
    return {self.name}
```

The symbols() method returns a set containing the name of the symbol (self.name). This method is used to extract the set of symbols present in a particular context. The set is enclosed in curly braces {}.

To summarize, the Symbol class represents a symbol with a given name. It has methods to retrieve the symbol's name, evaluate its value within a provided model, retrieve the symbol's formulaic representation, and extract the set of symbols contained within the instance. This class seems to be a part of a larger system that deals with symbolic expressions and mathematical modeling, where symbols (variables) are associated with values for computation and analysis.

```
class Not():
    def __init__(self, name):
        self.name = name
```

```
def __repr__(self):
    return f"Not({self.name})"

def evaluate(self, model):
    return not self.name.evaluate(model)

def formula(self):
    return "¬" + self.name.formula()

def symbols(self):
    return self.name.symbols()
```

Let's delve into the details of the Not class:

```
class Not():
    def __init__(self, name):
        self.name = name
```

Here, you're defining a class named Not. This class seems to represent the logical negation operation, which takes a symbol or another logical expression as an operand. The constructor method <a href="mailto:linit\_">\_\_\_()</a> takes a parameter <a href="mailto:name">name</a>, which represents the operand being negated. The <a href="mailto:name">name</a> is stored as an instance variable <a href="mailto:self.name">self.name</a>.

```
def __repr__(self):
    return f"Not({self.name})"
```

The <u>repr</u>() method is defined to provide a custom string representation of an instance of the Not class. It returns a string in the format <u>"Not(<operand>)"</u>, where <del><operand></del> is the string representation of the <u>name</u> operand.

```
def evaluate(self, model):
    return not self.name.evaluate(model)
```

The <code>evaluate()</code> method calculates the logical negation of the operand's evaluation result using the provided <code>model</code>. It calls the <code>evaluate()</code> method of the <code>name</code> operand with the given <code>model</code> and then negates the result using the <code>not</code> operator. This simulates the behavior of logical negation.

```
def formula(self):
    return "¬" + self.name.formula()
```

The **formula()** method returns a string representation of the formula formed by applying logical negation to the operand's formula. It adds the "¬" (negation) symbol to the beginning of the operand's formula, creating a new formula that represents the negation of the original formula.

```
def symbols(self):
    return self.name.symbols()
```

The symbols() method returns the set of symbols present in the operand's expression. It does this by calling the symbols() method of the name operand. This method allows you to retrieve all the symbols used in the negation expression.

In summary, the **Not** class represents the logical negation of a symbol or logical expression. It has methods to retrieve the custom string representation of the negation, evaluate the negation using a model, generate the formula for the negation expression, and extract the symbols present in the expression. This class seems to be part of a system for working with logical expressions and truth values.

```
class And():
    def init (self, *conjuncts):
        self.conjuncts = list(conjuncts)
    def repr (self):
        conjunctions = ", ".join(
            [str(conjunct) for conjunct in self.conjuncts]
        return f"And({conjunctions})"
    def add(self, conjunct):
        self.conjuncts.append(conjunct)
    def evaluate(self, model):
        return all(conjunct.evaluate(model) for conjunct in self.conjuncts)
    def formula(self):
        if len(self.conjuncts) == 1:
            return self.conjuncts[0].formula()
        return " Λ ".join([conjunct.formula() for conjunct in
self.conjuncts])
    def symbols(self):
        return set.union(*[conjunct.symbols() for conjunct in
self.conjuncts])
```

let's dive into the details of the And class:

```
class And():
    def __init__(self, *conjuncts):
        self.conjuncts = list(conjuncts)
```

Here, you're defining a class named And. This class seems to represent the logical AND operation, which takes multiple logical expressions (conjuncts) as operands. The constructor method <a href="mailto:linit\_">\_\_\_\_()</a> takes any number of arguments (\*conjuncts) and converts them into a list called self.conjuncts, which stores the individual conjuncts.

```
def __repr__(self):
    conjunctions = ", ".join(
        [str(conjunct) for conjunct in self.conjuncts]
    )
    return f"And({conjunctions})"
```

The <u>repr</u>() method provides a custom string representation of an instance of the And class. It generates a string that lists the individual conjuncts separated by commas, enclosed in the format "And(<conjuncts>)".

```
def add(self, conjunct):
    self.conjuncts.append(conjunct)
```

The add() method allows you to add additional conjuncts to an existing instance of the And class. This method appends the provided conjunct to the list of existing conjuncts.

```
def evaluate(self, model):
    return all(conjunct.evaluate(model) for conjunct in self.conjuncts)
```

The <code>evaluate()</code> method calculates the logical AND of all the conjuncts' evaluation results using the provided <code>model</code>. It iterates through each conjunct, calls its <code>evaluate()</code> method with the given <code>model</code>, and then uses the built-in <code>all()</code> function to check if all the conjuncts evaluate to <code>True</code>.

```
def formula(self):
    if len(self.conjuncts) == 1:
        return self.conjuncts[0].formula()
    return " \Lambda ".join([conjunct.formula() for conjunct in
self.conjuncts])
```

The formula() method generates a string representation of the logical formula represented by the conjunction of the conjuncts. If there's only one conjunct, it returns its formula. Otherwise, it joins the formulas of all conjuncts using the "\Lambda" (logical AND) symbol.

```
def symbols(self):
    return set.union(*[conjunct.symbols() for conjunct in
self.conjuncts])
```

The symbols() method returns the set of symbols present in all the conjuncts. It does this by calling the symbols() method of each conjunct and then performing a set union operation to combine all the symbol sets.

In summary, the And class represents the logical conjunction of multiple logical expressions (conjuncts). It allows adding new conjuncts, evaluating the conjunction using a model, generating the formula for the conjunction expression, and extracting the symbols present in the expression. This class is designed for working with logical expressions involving conjunctions.

```
class Or():
    def init (self, *disjuncts):
        self.disjuncts = list(disjuncts)
    def repr (self):
        disjuncts = ", ".join([str(disjunct) for disjunct in
self.disjuncts])
        return f"Or({disjuncts})"
   def evaluate(self, model):
        return any(disjunct.evaluate(model) for disjunct in self.disjuncts)
    def formula(self):
        if len(self.disjuncts) == 1:
            return self.disjuncts[0].formula()
        return " v ".join([disjunct.formula() for disjunct in
self.disjuncts])
    def symbols(self):
        return set.union(*[disjunct.symbols() for disjunct in
self.disjuncts])
```

let's dive into the details of the And class:

```
class And():
    def __init__(self, *conjuncts):
        self.conjuncts = list(conjuncts)
```

Here, you're defining a class named And. This class seems to represent the logical AND operation, which takes multiple logical expressions (conjuncts) as operands. The constructor method \_\_init\_\_() takes any number of arguments (\*conjuncts) and converts them into a list called self.conjuncts, which stores the individual conjuncts.

```
def __repr__(self):
    conjunctions = ", ".join(
        [str(conjunct) for conjunct in self.conjuncts]
    )
    return f"And({conjunctions})"
```

The <u>repr</u>() method provides a custom string representation of an instance of the <u>And</u> class. It generates a string that lists the individual conjuncts separated by commas, enclosed in the format "And(<conjuncts>)".

```
def add(self, conjunct):
    self.conjuncts.append(conjunct)
```

The add() method allows you to add additional conjuncts to an existing instance of the And class. This method appends the provided conjunct to the list of existing conjuncts.

```
def evaluate(self, model):
    return all(conjunct.evaluate(model) for conjunct in self.conjuncts)
```

The <code>evaluate()</code> method calculates the logical AND of all the conjuncts' evaluation results using the provided <code>model</code>. It iterates through each conjunct, calls its <code>evaluate()</code> method with the given <code>model</code>, and then uses the built-in <code>all()</code> function to check if all the conjuncts evaluate to <code>True</code>.

```
def formula(self):
    if len(self.conjuncts) == 1:
        return self.conjuncts[0].formula()
    return " \( \) ".join([conjunct.formula() for conjunct in
self.conjuncts])
```

The formula() method generates a string representation of the logical formula represented by the conjunction of the conjuncts. If there's only one conjunct, it returns its formula. Otherwise, it joins the formulas of all conjuncts using the "A" (logical AND) symbol.

```
def symbols(self):
    return set.union(*[conjunct.symbols() for conjunct in
self.conjuncts])
```

The symbols() method returns the set of symbols present in all the conjuncts. It does this by calling the symbols() method of each conjunct and then performing a set union operation to combine all the symbol sets.

In summary, the And class represents the logical conjunction of multiple logical expressions (conjuncts). It allows adding new conjuncts, evaluating the conjunction using a model, generating the formula for the conjunction expression, and extracting the symbols present in the expression. This class is designed for working with logical expressions involving conjunctions.

```
class Or():
    def __init__(self, *disjuncts):
        self.disjuncts = list(disjuncts)

def __repr__(self):
```

```
disjuncts = ", ".join([str(disjunct) for disjunct in
self.disjuncts])
    return f"Or({disjuncts})"

def evaluate(self, model):
    return any(disjunct.evaluate(model) for disjunct in self.disjuncts)

def formula(self):
    if len(self.disjuncts) == 1:
        return self.disjuncts[0].formula()
    return " v ".join([disjunct.formula() for disjunct in
self.disjuncts])

def symbols(self):
    return set.union(*[disjunct.symbols() for disjunct in
self.disjuncts])
```

let's break down the details of the Or class:

```
class Or():
    def __init__(self, *disjuncts):
        self.disjuncts = list(disjuncts)
```

Here, you're defining a class named <code>Or</code>. This class appears to represent the logical OR operation, which takes multiple logical expressions (disjuncts) as operands. The constructor method <code>\_\_init\_\_()</code> takes any number of arguments (\*disjuncts) and converts them into a list called <code>self.disjuncts</code>, which stores the individual disjuncts.

```
def __repr__(self):
    disjuncts = ", ".join([str(disjunct) for disjunct in
self.disjuncts])
    return f"Or({disjuncts})"
```

The <u>repr</u>() method provides a custom string representation of an instance of the <u>0r</u> class. It generates a string that lists the individual disjuncts separated by commas, enclosed in the format <u>"0r(<disjuncts>)"</u>.

```
def evaluate(self, model):
    return any(disjunct.evaluate(model) for disjunct in self.disjuncts)
```

The <code>evaluate()</code> method calculates the logical OR of all the disjuncts' evaluation results using the provided <code>model</code>. It iterates through each disjunct, calls its <code>evaluate()</code> method with the given <code>model</code>, and then uses the built-in <code>any()</code> function to check if at least one of the disjuncts evaluates to <code>True</code>.

```
def formula(self):
    if len(self.disjuncts) == 1:
        return self.disjuncts[0].formula()
    return " v ".join([disjunct.formula() for disjunct in
self.disjuncts])
```

The formula() method generates a string representation of the logical formula represented by the disjunction of the disjuncts. If there's only one disjunct, it returns its formula. Otherwise, it joins the formulas of all disjuncts using the "v" (logical OR) symbol.

```
def symbols(self):
    return set.union(*[disjunct.symbols() for disjunct in
self.disjuncts])
```

The symbols() method returns the set of symbols present in all the disjuncts. It does this by calling the symbols() method of each disjunct and then performing a set union operation to combine all the symbol sets.

In summary, the <code>Or</code> class represents the logical disjunction of multiple logical expressions (disjuncts). It evaluates the disjunction using a model, generates the formula for the disjunction expression, and extracts the symbols present in the expression. This class is designed for working with logical expressions involving disjunctions.

```
class Implication():
    def __init__(self, left, right):
        self.left = left
        self.right = right

def __repr__(self):
        return f"Implication({self.left}, {self.right})"

def evaluate(self, model):
        return ((not self.left.evaluate(model))
            or self.right.evaluate(model))

def formula(self):
    left = self.left.formula()
    right = self.right.formula()

return f"{left} => {right}"

def symbols(self):
    return set.union(self.left.symbols(), self.right.symbols())
```

let's break down the details of the Implication class:

```
class Implication():
    def __init__(self, left, right):
        self.left = left
        self.right = right
```

Here, you're defining a class named Implication. This class seems to represent the logical implication operation  $(\rightarrow)$ , which takes two logical expressions as operands: the left-hand side (left) and the right-hand side (right). The constructor method  $\underline{init}()$  takes two parameters, left and right, representing the two sides of the implication. These are stored as instance variables, self.left and self.right.

```
def __repr__(self):
    return f"Implication({self.left}, {self.right})"
```

The <u>repr</u>() method provides a custom string representation of an instance of the <u>Implication</u> class. It generates a string in the format <u>"Implication(<left>, <right>)"</u>.

```
def evaluate(self, model):
    return ((not self.left.evaluate(model))
        or self.right.evaluate(model))
```

The <code>evaluate()</code> method calculates the result of the implication using the provided <code>model</code>. It evaluates the logical NOT of the left-hand side using the <code>not</code> operator and then evaluates the logical OR of the negated left-hand side and the right-hand side. This simulates the behavior of the implication operation.

```
def formula(self):
    left = self.left.formula()
    right = self.right.formula()
    return f"{left} => {right}"
```

The **formula()** method generates a string representation of the formula represented by the implication. It constructs a string by formatting the left-hand side followed by "=>", and then the right-hand side.

```
def symbols(self):
    return set.union(self.left.symbols(), self.right.symbols())
```

The symbols() method returns the set of symbols present in both the left-hand side and the right-hand side of the implication. It does this by performing a set union operation on the symbol sets of self.left and self.right.

In summary, the [Implication] class represents the logical implication operation  $(\rightarrow)$  between two logical expressions. It evaluates the implication using a model, generates the formula for the implication

expression, and extracts the symbols present in the expression. This class is designed for working with logical expressions involving implications.

```
class Biconditional():
    def init (self, left, right):
        self.left = left
        self.right = right
    def repr (self):
        return f"Biconditional({self.left}, {self.right})"
    def evaluate(self, model):
        return ((self.left.evaluate(model)
                 and self.right.evaluate(model))
                or (not self.left.evaluate(model)
                    and not self.right.evaluate(model)))
    def formula(self):
        left = str(self.left)
        right = str(self.right)
        return f"{left} <=> {right}"
    def symbols(self):
        return set.union(self.left.symbols(), self.right.symbols())
```

let's break down the details of the Biconditional class:

```
class Biconditional():
    def __init__(self, left, right):
        self.left = left
        self.right = right
```

Here, you're defining a class named <code>Biconditional</code>. This class seems to represent the logical biconditional operation (↔), which takes two logical expressions as operands: the left-hand side (left) and the right-hand side (right). The constructor method <code>\_\_init\_\_()</code> takes two parameters, <code>left</code> and <code>right</code>, representing the two sides of the biconditional. These are stored as instance variables, <code>self.left</code> and <code>self.right</code>.

```
def __repr__(self):
    return f"Biconditional({self.left}, {self.right})"
```

The <u>repr</u>() method provides a custom string representation of an instance of the Biconditional class. It generates a string in the format "Biconditional (<left>, <right>)".

```
def evaluate(self, model):
    return ((self.left.evaluate(model))
        and self.right.evaluate(model))
        or (not self.left.evaluate(model)
            and not self.right.evaluate(model)))
```

The <code>evaluate()</code> method calculates the result of the biconditional using the provided <code>model</code>. It evaluates the logical AND of both sides and the logical NOT of both sides, and then uses the logical OR operator to combine these results. This simulates the behavior of the biconditional operation.

```
def formula(self):
    left = str(self.left)
    right = str(self.right)
    return f"{left} <=> {right}"
```

The **formula()** method generates a string representation of the formula represented by the biconditional. It constructs a string by formatting the left-hand side followed by "<=>" and then the right-hand side.

```
def symbols(self):
    return set.union(self.left.symbols(), self.right.symbols())
```

The symbols() method returns the set of symbols present in both the left-hand side and the right-hand side of the biconditional. It does this by performing a set union operation on the symbol sets of self.left and self.right.

In summary, the  $\[ \]$  disconditional class represents the logical biconditional operation ( $\leftrightarrow$ ) between two logical expressions. It evaluates the biconditional using a model, generates the formula for the biconditional expression, and extracts the symbols present in the expression. This class is designed for working with logical expressions involving biconditionals.

```
def create_table(symbols):
    values = [True, False]
    num_columns = len(symbols)
    all_combinations = list(itertools.product(values, repeat=num_columns))
    table = []
    for model in all_combinations:
        temp = dict()
        for symbol, value in zip(symbols, model):
            temp[symbol] = value
        table.append(temp)
        del (temp)
    return table
```

The create\_table function generates a truth table for a given set of symbols. It computes all possible combinations of truth values for the symbols and creates a table that associates these combinations with their corresponding values in a dictionary format.

Let's break down the function step by step:

- 1. The symbols parameter is a list of symbolic names (variables).
- 2. values is a list containing True and False, representing the possible truth values.
- 3. <a href="mailto:num\_columns">num\_columns</a> calculates the number of symbols, which corresponds to the number of columns in the truth table.
- 4. all\_combinations is created using itertools.product to generate all possible combinations of truth values for the symbols. It's a list of tuples where each tuple represents a single row in the truth table.
- 5. The loop iterates through each combination (model) in all\_combinations.
- 6. Inside the loop, a temporary dictionary temp is created to represent a row in the truth table. The loop then pairs each symbol with its corresponding truth value using the zip() function, and adds these pairs to the temp dictionary.
- 7. After adding all symbol-value pairs to temp, the temp dictionary is appended to the table list, which represents the truth table.
- 8. The temp dictionary is deleted using del to free up memory for the next iteration.
- 9. Finally, the function returns the generated table containing dictionaries representing each row of the truth table.

In summary, the <code>create\_table</code> function generates a truth table for a set of symbols by computing all possible combinations of truth values for those symbols. It returns a list of dictionaries, where each dictionary represents a row in the truth table with symbols as keys and their corresponding truth values as values.

```
def model_check(knowledge, query):
    symbols = set.union(knowledge.symbols(), query.symbols())
    model_table = create_table(symbols)
    final_answers = []
    for model in model_table:
        if knowledge.evaluate(model):
            answer = query.evaluate(model)
            final_answers.append(answer)
    final_answer = all(final_answers)
    return final_answer
```

The model\_check function implements a basic model checking procedure. It checks whether a given logical knowledge and query are true in all possible models, which are generated using a truth table approach. Let's break down the function step by step:

- 1. The knowledge parameter is a logical expression representing the background knowledge, and the query parameter is the logical expression you want to evaluate.
- 2. The function starts by creating a set of symbols by taking the union of the symbols present in both the knowledge and query expressions.
- 3. The model\_table is generated using the create\_table function, which provides all possible truth value combinations for the symbols.
- 4. The loop iterates through each model in the model table.
- 5. Inside the loop, it checks if the knowledge is true in the current model by calling the evaluate method of the knowledge expression with the current model.
- 6. If the knowledge is true in the current model, the query expression is evaluated in the same model, and the result is stored in the final answers list.
- 7. After iterating through all models, the <u>final\_answers</u> list contains a list of truth values for the <u>query</u> expression across all models where the <u>knowledge</u> is true.
- 8. The final\_answer is calculated using the all() function to check if all values in final\_answers are True, indicating that the query is true in all models where the knowledge is true.
- 9. The function returns the final\_answer, which represents whether the query is logically entailed by the knowledge in all possible models where the knowledge holds.

In summary, the <code>model\_check</code> function performs model checking by generating a truth table of all possible models, evaluating the <code>knowledge</code> and <code>query</code> expressions for each model, and checking if the <code>query</code> holds in all models where the <code>knowledge</code> holds. It returns a boolean value indicating whether the <code>query</code> is logically entailed by the <code>knowledge</code> using this model checking approach.

# Harry.py

```
from logic import *

rain = Symbol("rain") #Its raining
hagrid = Symbol("hagrid") #Harry visited Hagrid
dumbledore = Symbol("dumbledore") #Harry visited dumbledore
```

The code snippet defines three symbolic variables: rain, hagrid, and dumbledore. Each of these variables seems to represent a different event or condition in a logical context.

Here's a breakdown of what the code does:

- 1. The <u>from logic import \*</u> statement imports all symbols and functions defined in the <u>logic</u> module. This module has been explained above.
- 2. [Symbol("rain")], [Symbol("hagrid")], and [Symbol("dumbledore")] create instances of the Symbol class from the [logic] module, representing different conditions or events in a logical

context.

These symbols can be used to represent various conditions, and you can manipulate and combine them using the logical operators and functions provided by the logic module. The code sets the stage for building logical expressions and performing operations on them to model different scenarios or situations.

The knowledge variable is being assigned a logical expression that represents a collection of knowledge or constraints. The expression appears to define a set of conditions and relationships using logical operators. Let's break down the knowledge expression step by step:

```
knowledge = And(
    Implication(Not(rain), hagrid),
    Or(hagrid, dumbledore),
    Not(And(hagrid, dumbledore)),
    dumbledore
)
```

- 1. [Implication(Not(rain), hagrid)] represents the logical implication "If it's not raining, then Harry visited Hagrid." This implies that if it's not raining, Harry did visit Hagrid.
- 2. <code>Or(hagrid, dumbledore)</code> represents the logical disjunction "Harry visited Hagrid or Harry visited Dumbledore." This states that either Harry visited Hagrid or he visited Dumbledore or both.
- 3. [Not(And(hagrid, dumbledore))] represents the logical negation of "Harry visited both Hagrid and Dumbledore simultaneously." This indicates that Harry did not visit both of them together.
- 4. dumbledore simply represents the fact that Harry visited Dumbledore.
- 5. Finally, the entire knowledge expression is encapsulated in the And() function, which means that all of these conditions must be true simultaneously for the knowledge to hold.

In summary, the knowledge expression represents a logical set of constraints and relationships involving Harry's visits to Hagrid and Dumbledore, as well as the weather condition of raining. This logical expression can be used to reason about various scenarios and evaluate the truth or falsity of different combinations of events.

The model\_check function is being used here to check whether the variable rain is logically entailed by the given knowledge expression. In other words, it checks whether, based on the defined knowledge, it must necessarily be true that it's raining. Let's see what the output of this code might be:

```
print(model_check(knowledge, rain))
```

Assuming that the model\_check function and the knowledge expression are implemented correctly based on the previous discussions, the output of this code will indicate whether the knowledge implies that it is raining or not.

If the output is True, it means that based on the provided knowledge, it must be true that it is raining. If the output is False, it means that the knowledge does not necessarily imply that it is raining. The output will reflect the logical consequence of the knowledge expression with respect to the rain variable.

```
P = Symbol("It is a Tuesday")
Q = Symbol("It is Raining")
R = Symbol("Harry will go for a run")
```

You have defined three symbolic variables using the Symbol class:

- 1. P represents the statement "It is a Tuesday."
- 2. Q represents the statement "It is Raining."
- 3. R represents the statement "Harry will go for a run."

These symbolic variables will likely be used to build logical expressions and reason about various scenarios using the logical operators and constructs provided by the logic module you are working with.

The knowledge1 expression is constructed using the And() function to represent a logical conjunction of multiple conditions. It appears to define a logical scenario involving the statements represented by the symbols P, Q, and R. Let's break down the knowledge1 expression:

```
knowledge1 = And(
    Implication(And(P, Not(Q)), R),
    P,
    Not(Q)
)
```

- 1. Implication(And(P, Not(Q)), R) represents the logical implication "If it is a Tuesday and it is not raining, then Harry will go for a run." This implies that if both "It is a Tuesday" (P) and "It is not Raining" (Not(Q)) are true, then "Harry will go for a run" (R) is true.
- 2. P represents the statement "It is a Tuesday."
- 3. Not (Q) represents the statement "It is not Raining."
- 4. The entire knowledge1 expression is encapsulated in the And() function, which means that all of these conditions must be true simultaneously for the knowledge to hold.

When you print the knowledge1 expression using print(knowledge1), it will display the string representation of the logical expression you've created. The output will show how the various conditions are combined using logical operators. Keep in mind that the actual output format might depend on the specific logic library or module you are using in your code.

```
knowledge1.formula()
knowledge1.symbols()

model_check(knowledge1, R)

print(Not(P))

Biconditional(P,Q)
And(P,Q)
```

Let's go through each of the provided expressions and statements:

### 1. knowledge1.formula():

This will return a string representation of the formula represented by the knowledge1 expression. The output should be similar to the logical expression you provided when constructing knowledge1. For example, if your logic library formats formulas like standard logical notation, the output might look like:

```
((P \land \neg Q) \Rightarrow R) \land P \land \neg Q
```

#### 2. knowledge1.symbols():

This will return the set of symbols present in the knowledge1 expression. Since you have used P, Q, and R in knowledge1, the output should be a set containing these symbols: {P, Q, R}.

### 3. model\_check(knowledge1, R):

This will use the <code>model\_check</code> function to check if the statement "Harry will go for a run" (R) is logically entailed by <code>knowledge1</code>. The output will be a boolean value indicating whether, based on the given knowledge, it must be true that Harry will go for a run.

#### 4. print(Not(P)):

This will print the logical negation of the statement "It is a Tuesday" ( $\mathbb{P}$ ). If the logic library formats negations as " $\neg \mathbb{P}$ ", the output will be  $\neg \mathbb{P}$ .

#### 5. Biconditional(P, Q):

This seems to create a biconditional expression between P and Q. A biconditional states that P is true if and only if Q is true, and vice versa. The output of this line would be the biconditional expression representation.

## 6. And (P, Q):

This creates a logical AND expression between P and Q, stating that both P and Q must be true. The output of this line would be the AND expression representation.