Course "Automated Planning: Theory and Practice" Chapter 05: The Backward Search Space

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M.S. Course: Artificial Intelligence Systems (LM)

A.A.: 2023-2024

Where: DISI, University of Trento

URL: https://bit.ly/3z0kGk8

Last updated: Sunday 1st October, 2023

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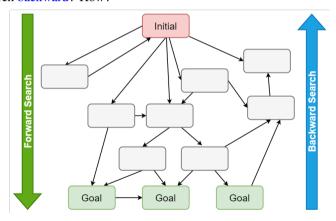
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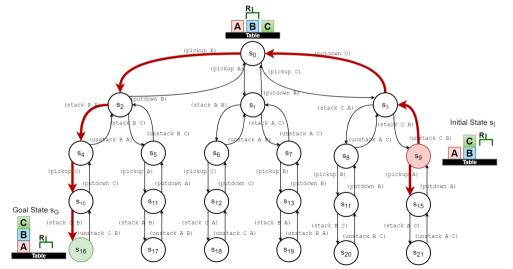
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Introduction

- Classical Planning: find a path in a finite graph
 - We have seen how to search forward
 - Can we search backward? How?

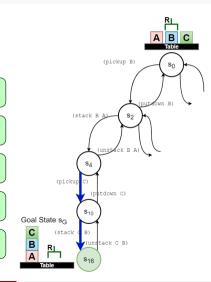


BLOCKS WORLD, 3 BLOCKS - SEARCHING FORWARD



BLOCKS WORLD, 3 BLOCKS - SEARCHING BACKWARD

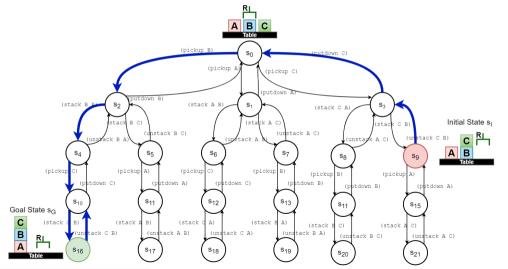
- 1: Execution should pass s_4 ...
- 2: Execute (pickup C) ...
 - 3: Pass *s*₁₀ ...
- 4: Execute (stack C B) ...
 - 5: ... and end up in s_{16}



- 5: Pass \$4 ...
- 4: Previous action could be (pickup C) ...
 - 3: Pass *s*₁₀ ...
- 2: Previous action could be (stack C B) ...
- 1: Planning starts in \$\mathcal{s}_{16}\$

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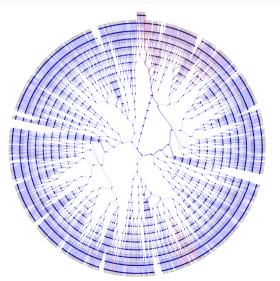
BACKWARD SEARCH



Seems simple, ...but there are complications...

BACKWARD SEARCH: COMPLICATION 1

- The graph is not pre-computed!
 - Must be expanded dynamically, starting in the *goal* states
- Would require the inverse of $\gamma(s, a)$: $\gamma^{-1}(s, a)$

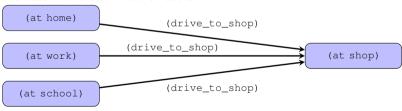


BACKWARD SEARCH: COMPLICATION 2

• Though we have determinism in the forward search

```
(at home) (at shop)
```

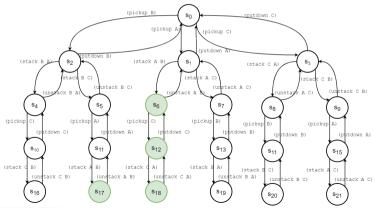
• ... this is not the case in the backward direction!



- Compute $\gamma^{-1}(\{(at home)\}, (drive_to_shop))$
 - If we want to end up in { (at shop) }, what set of states could we be in before (drive_to_shop)?

Backward Search: Complication 3

- We generally have multiple goal states to start searching in...
 - Goal: (on A B)

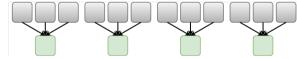


Backward Search: Complication 2-3 (combinations)

• Want to end up in one of these goal states

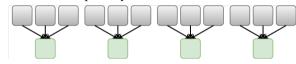


• Even if we say the last action is (drive_to_shop),... we could have started in any of these states



- Given initial state + forward plan [(drive_to_shop)]
 - One possible next state
- Given goal state(s) + backward plan [(drive_to_shop)]
 - Many possible previous states

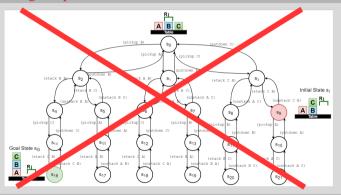
- Main challenge: A set of possible "current" states
 - Can't store and process each state separately



- Classical representation:
 - Goal: set of literals that should hold, representing multiple states: $g = \{(on AB), \neg(on CD)\}$
 - A should be on B, and C should not be on D
 - We don't care if the blocks are clear/ontable or not
 - ⇒ if we cared, that would have been specified!

Goal Space \neq State Space

Backward Search uses goal space



Will not construct this graph \Longrightarrow use $\gamma^{-1}(g, a)$, not $\gamma^{-1}(s, a)$

If you achieve conditions in $\gamma^{-1}(g, a)$, then executing a will achieve g

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How can we construct a goal space begining with an "initial goal"?

GOAL SPECIFICATION

• Assuming the goal is:



- What's the actual goal specification?
 - We could specify a complete (i.e. unique state)
 - $g = \{(\text{clear A}), (\text{on A B}), (\text{on B C}), (\text{ontable C}), (\text{clear D}), (\text{ontable D}), (\text{handempty}), \neg (\text{clear B}), \neg (\text{on A A}), \dots\}$
 - Or we can just specify "the important" things (what we expect to hold)
 - ullet g= {(clear A),(on A B),(on B C),(ontable C),(clear D),(ontable D)}
 - Specify all positions: given a physically achievable initial state, other facts follow implicitly

GOAL SPECIFICATION

- Usually we do not care about all facts (directly or indirectly)!
 - Ignore location of *D*

(on A B) (cas B) (cas B) (cas B) (cas C) (cas B) (cas C) (cas

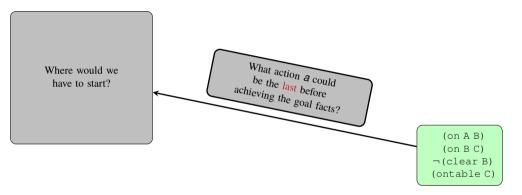
FORWARD PLANNING: ACTION APPLICABILITY

Which actions could we execute?

BACKWARD PLANNING: ACTION RELEVANCE

Which actions could achieve part of the goal?

BACKWARD SEARCH: RELEVANCE



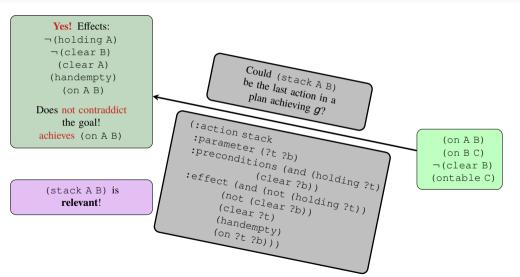
BACKWARD SEARCH: RELEVANCE (CONT.)

NO! It achieves (clear ?t) = (clear B)Could (stack B C) The goal requires be the last action in a ¬(clear B) plan achieving g? ⇒ Destroys part of (:action stack the goal! :parameter (?t ?b) (on AB) :preconditions (and (holding ?t) (on BC) ¬(clear B) (stack BC) is :effect (and (not (holding ?t)) (ontable C) not relevant (not (clear ?b)) (also impossible, but (clear ?t) this is included in (handempty)relevance!) (on ?t ?b)))

BACKWARD SEARCH: RELEVANCE (CONT.)

Ves! Effects: ¬(ontable D) ¬(clear D) ¬(handemptv) Could (pickup D) ¬(holding D) be the last action in a plan achieving g? Does not contraddict the goal! (:action pickup ... but also does not help :parameter (?x) to achieve any goal reqs! (on AB) :preconditions (and (clea ?x) (on BC) ¬(clear B) (ontable ?x) (ontable C) :effect (and (not (ontable ?x)) (pickup D) is not relevant (not (clear ?x)) (not (handempty)) (holding ?x)))

BACKWARD SEARCH: RELEVANCE (CONT.)



BACKWARD SEARCH: SUMMARY (SO FAR)

Forward search over states $s = \{\text{ATOM}_1, ..., \text{ATOM}_N\}$

• a is applicable to current state s iff: $precond^+(a) \subseteq s$ and Positive conditions are present $s \cap precond^-(a) = \emptyset$ Negative conditions are absent

Backward search over set of literals $q = \{\text{Lit}_1,...,\text{Lit}_N\}$

• a is relevant for current goal q iff:

$$g \cap effects(a) \neq \emptyset$$
 and Contribute to the goal: add needed pos/neg literals

$$g^+ \cap effects^-(a) = \emptyset$$
 and

$$g^- \cap effects^+(a) = \emptyset$$

WHEN AN ACTION HAS BEEN SELECTED:

Forward Planning: Progression! What will be true after executing a?

Backward Planning: Regression! What must be achieved before executing a?

BACKWARD SEARCH: PROGRESSION AND REGRESSION

Forward search over states $s = \{atom_1,...,atom_n\}$

• Progression: $\gamma(s, a) = \{s \setminus effects^{-}(a) \cup effects^{+}(a)\}$

Action **a** is applicable in **s**

I would end up in $\gamma(s, a)$

Backward search over set of literals $g = \{\text{lit}_1,...,\text{lit}_{\text{n}}\}$

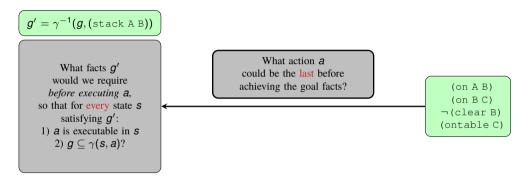
• Progression: $\gamma^{-1}(g, a) = ????$

I would require $\gamma^{-1}(q, a)$

Action a is relevant for g

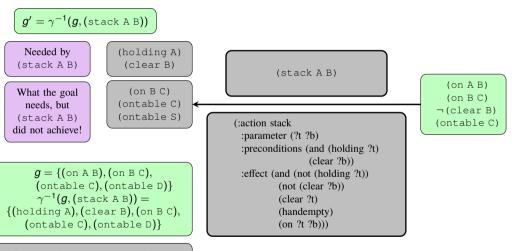
I need to achieve *g*

BACKWARD SEARCH: REGRESSION



```
Subset: It is OK to achieve more than required! g = \{(\text{on A B}), (\text{on B C}), (\text{ontable C}), (\text{ontable D})\}
\gamma(s, a) = \{(\text{on A B}), (\text{on B C}), (\text{ontable C}), (\text{ontable D}) 
(\text{clear A}), (\text{clear D}), (\text{handempty})\}
```

BACKWARD SEARCH: REGRESSION



Corresponds to many potential states

BACKWARD SEARCH: REGRESSION - FORMALIZATION

All goals except effects(a) must alredy have been true precond(a) must have been true so that a was applicable $\gamma^{-1}(g,a) = ((g \setminus effects(a)) \cup precond(a))$ representing

Backward regression: Which states could I start from?

Works for

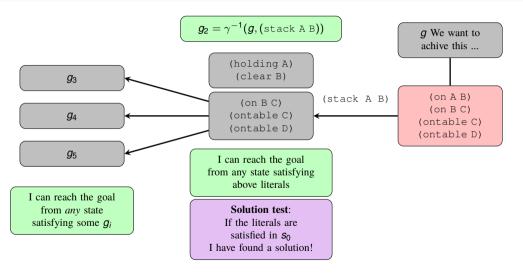
 $\{s | a \text{ is applicable to } s \text{ and } \gamma(s, a) \text{ satisfies } g\}$

Classical goals (already sets ground literals)

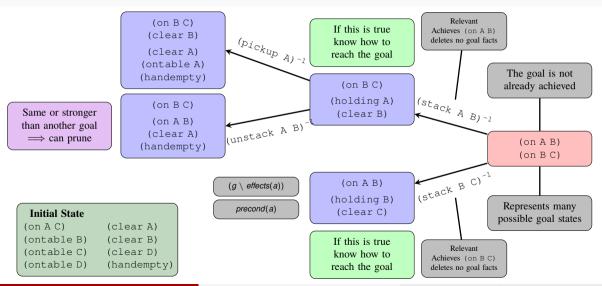
Classical effects (conjunction of literals)

Classical preconditions (conjunction of literals)

BACKWARD SEARCH: KEEP REGRESSING



BACKWARD SEARCH: EXAMPLE

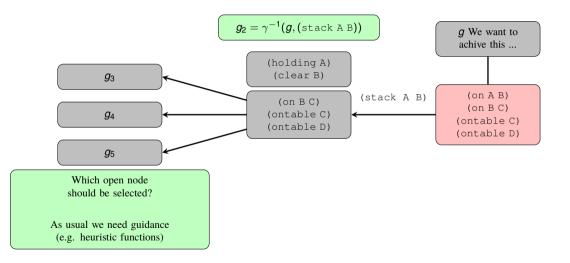


When we do select actions:

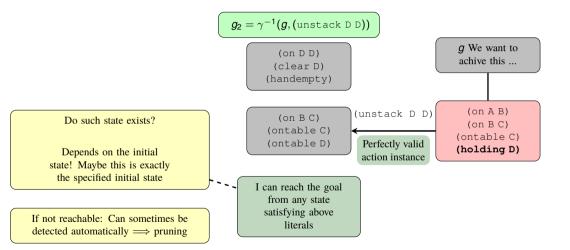
Forward planning: Want the resulting state to be closer to the goal!

Backward planning: Want the resulting goal to be closer to what the initial state can satisfy!

BACKWARD SEARCH: NEEDS GUIDANCE

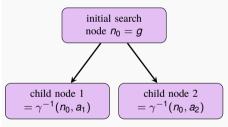


BACKWARD SEARCH: NEW GOAL ACHIEVABLE



GOAL SPACE

THE BACKWARD GOAL SPACE FOR BACKWARD PLANNING REGRESSION



2) Initial search node:

Corresponds directly to the specified goal

3) Branching rule:

For every action a relevant to the goal g of a node n, generate the goal $\gamma^{-1}(a,a)$

Represents the set of states where $\gamma(s, a)$ satisfies g

4) Solution criterion:

The goal of the node is satisfied in the initial state

5) Plan extraction:

Generate the sequence of all actions on the path to the solution node

PLANNING AS SEARCH (RECAP)

function SEARCH(problem)

```
initial-node \leftarrow MAKE-INITIAL-NODE(problem)
                                                                                    \rightarrow [2]
open \leftarrow \{initial-node\}
while (open \neq \emptyset) do
    node \leftarrow search-strategy-remove-from(open)
                                                                                    \rightarrow [6]
    if is-solution(node) then
                                                                                    \rightarrow [4]
        return EXTRACT-PLAN-FROM(node)
                                                                                    \rightarrow [5]
    end if
    for each newnode ∈ successors(node) do
                                                                                    \rightarrow [3]
        open \leftarrow open \cup \{newnode\}
    end for
end while
                                                                                    → Expanded the entire search space without finding a so-
return Failure
                                                                                       lution
```

end function

BACKWARD SEARCH: INSTANTIATED ALGORITHM

```
function SEARCH(problem)
     initial-node \leftarrow \langle goal, \epsilon \rangle
                                                                                                        \rightarrow [2]
     open \leftarrow \{initial-node\}
     while (open \neq \emptyset) do
          node = \langle q, \pi \rangle \leftarrow SEARCH-STRATEGY-REMOVE-FROM(open)
                                                                                                       \rightarrow [6]
          if is-solution(node) then
                                                                                                        \rightarrow [4] Check goal formula in state S_0
               return \pi
                                                                                                        \rightarrow [5]
          end if
          for each a \in A relevant to g do
                                                                                                        \rightarrow [3]
               g' \leftarrow \gamma^{-1}(g, a)
               \pi' \leftarrow \text{PREPEND}(\boldsymbol{a}.\pi)
               open \leftarrow open \cup \{\langle q', \pi' \rangle\}
          end for
     end while
                                                                                                        → Expanded the entire search space without finding a so-
     return Failure
                                                                                                            lution
end function
```

BACKWARD AND FORWARD SEARCH: EXPRESSIVITY

• Suppose we have disjunctive preconditions - simple in forward planning

- How do we apply such action backwards?
 - More complicated disjunctive goals to achieve?

```
(at pos1)
(or (have-car)
(have-bike)) (at pos2)
```

• Additional branching?

```
(at pos1)
(have-car)

(at pos1)
(have-bike)
```

Similarly for existentials

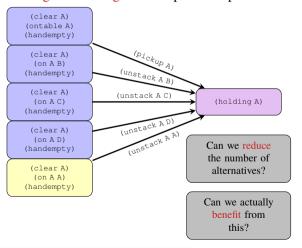
(exits ?block (on ?block A))

One branch per possible value

Some other extensions are less straightforward in backward search (but still possible!)

LIFTED SEARCH: MOTIVATIONS

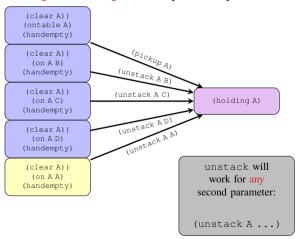
• High-branching-factors: potential problem in any search!



```
(:action pickup
  :parameters (?x)
  :precondition (and (clear ?x)
                     (ontable ?x)
                     (handempty))
  :effect (and (not (ontable ?x))
                (not (clear ?x))
                (not (handempty))
                (holding ?x)))
(:action unstack
  :parameters (?top ?below)
  :precondition (and (on ?top ?below)
                     (clear ?top)
                     (handempty))
  :effect (and (holding ?top)
                (clear ?below)
                (not (clear ?top))
                (not (handempty))
                (not (on ?top ?below))))
```

LIFTED SEARCH: OBSERVATIONS

• High-branching-factors: potential problem in any search!



```
(:action pickup
  :parameters (?x)
  :precondition (and (clear ?x)
                     (ontable ?x)
                     (handempty))
  :effect (and (not (ontable ?x))
                (not (clear ?x))
                (not (handempty))
                (holding ?x)))
(:action unstack
  :parameters (?top ?below)
  :precondition (and (on ?top ?below)
                     (clear ?top)
                     (handempty))
  :effect (and (holding ?top)
                (clear ?below)
                (not (clear ?top))
                (not (handempty))
                (not (on ?top ?below))))
```

LIFTED SEARCH: GENERAL IDEA

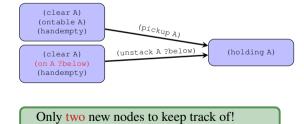
- Instantiate parameters that are "bound" by the goal
 - For (pickup ?x) to achieve (holding A), we must have ?x = A
- Keep other parameters uninitialized
 - For (unstack ?top ?below) to achieve (holding A), we must have ?top = A
 - We don't care about ?below, so we don't give it a value: use (unstack A ?below)
- Not $ground \Longrightarrow$ "lifted"!

Must extend *relevance* for "pattern matching": Unification

Suppose (on A B) is true initially, or made true by an action \boldsymbol{A}

Goal requires (on A ?below)

OK: ?below = B



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Applicable to other types if planning – we will see later!

References I

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- [2] Malik Ghallab, Dana S. Nau, and Paolo Traverso. Automated planning theory and practice. Elsevier, 2004. ISBN 978-1-55860-856-6.
- [3] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated Planning and Acting*. Cambridge University Press, 2016. ISBN 978-1-107-03727-4. URL http://www.cambridge.org/de/academic/subjects/computer-science/artificial-intelligence-and-natural-language-processing/automated-planning-and-acting? format=HB.