

# COURSE "AUTOMATED PLANNING: THEORY AND PRACTICE"

## CHAPTER 10: DOMAIN-CONFIGURABLE PLANNING: HIERARCHICAL TASK NETWORKS

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# ASSUMPTIONS

- The fundamental assumptions we considered so far are:
  - We only specify: Objects and state variables
  - We only specify: initial state and goal
  - Physical preconditions and effects of actions



- We only specify what **can** be done!
- The **planner** should decide what **should** be done!

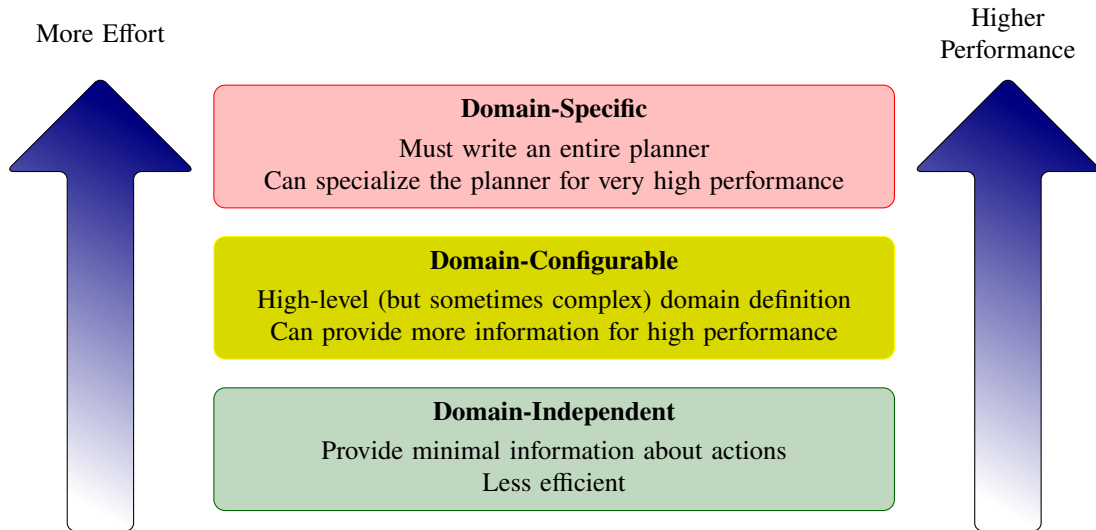


- But... even the most sophisticated heuristics and domain analysis methods lack human intuitions and background knowledge...

# DOMAIN-CONFIGURABLE PLANNERS

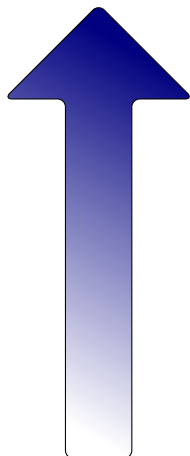
- How can we make a planner take advantage of what we know?
- Planners taking advantage of additional knowledge can be called:
  - Knowledge-rich
  - Domain-Configurable
  - Sometimes incorrectly called "domain-dependent"

## COMPARISON



## COMPARISON (CONT.)

Larger problem classes  
can be handled efficiently



### **Domain-Configurable**

Easier to improve expressivity and efficiency  
⇒ Often practically useful for a larger set of domains!

### **Domain-independent**

Should be useful for a wide range of domains

### **Domain-Specific**

Only works in a single domain

# HIERARCHICAL-TASK NETWORKS: INTUITION

## CLASSICAL PLANNING

- Objective is to **achieve a goal**

```
{ (at TimeSqaure) }
{ (on A B), (on C D) }
...
```



## HIERARCHICAL TASK NETWORKS

- Objective is to **perform a task**

```
{ (travel-to TimeSqaure) }
{ (place-blocks-correctly) }
...
```



- Find** any sequence of actions that achieves the goal

- Use "templates" to incrementally **refine** the task until *primitive* actions are reached!

```
(travel-to TimeSqaure)
  ↓
(taxi-to airport);
(fly-to JFK); ...
```

Provides **guidance** but still requires **planning**!

# TERMINOLOGY: PRIMITIVE TASK

- A **primitive task** corresponds **directly** to an **action**
  - As in classical planning, **what is primitive** depends on:
    - The **execution system**!
    - **How detailed** you want your plans to be!
  - Example:
    - For you the `(fly from to)` may be a primitive task
    - For the pilot, it may be further decomposed into many other smaller steps!
  - **Tasks** can be *ground* or *non-ground*: `(stack A ?x)`
    - No separate terminology, as in *operator/action*

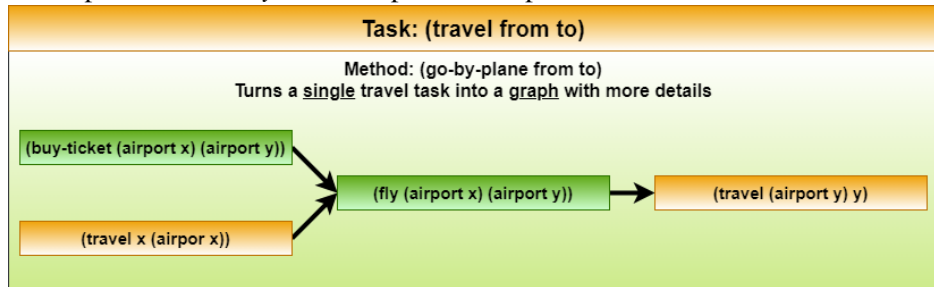


# TERMINOLOGY: NON-PRIMITIVE TASK

- A non-primitive task
  - Cannot be directly executed
  - Must be decomposed into 1 or more sub-tasks
- Example:
  - `(put-all-blocks-in-place)`
  - `(make-tower A B C D E)`
  - `(move-stack-of-blocks x y)`

# TERMINOLOGY: METHOD

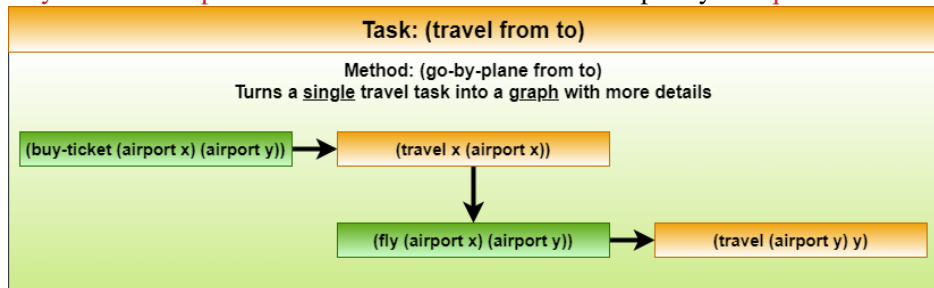
- A **method** specifies *one* way to decompose a non-primitive task into sub-tasks.



- The decomposition is a **graph**  $\langle N, E \rangle$ 
  - Nodes in  $N$  correspond to **sub-tasks to perform**
    - Can be primitive or not!
  - Edges in  $E$  correspond to **ordering relations**

# TOTALLY ORDERED SIMPLE TASK NETWORKS

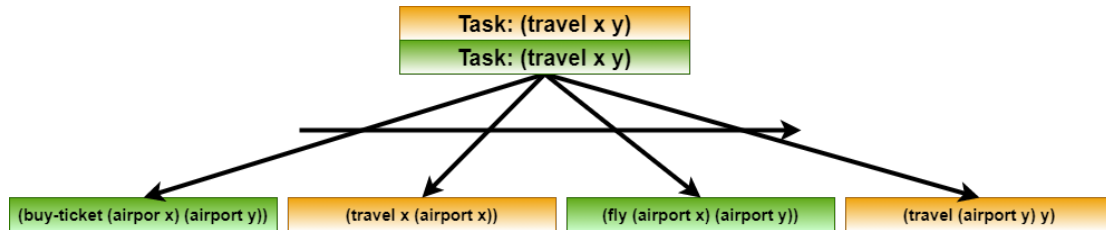
- In **totally ordered simple task networks** each method must specify a **sequence** of sub-tasks!



- Alternatively: A sequence  $\langle t_1, \dots, t_k \rangle$ 
  - $\langle$  (buy-ticket (airport x) (airport y)),  
 (travel x (airport x)),  
 (fly (airport x) (airport y)),  
 (travel (airport y) y)  $\rangle$

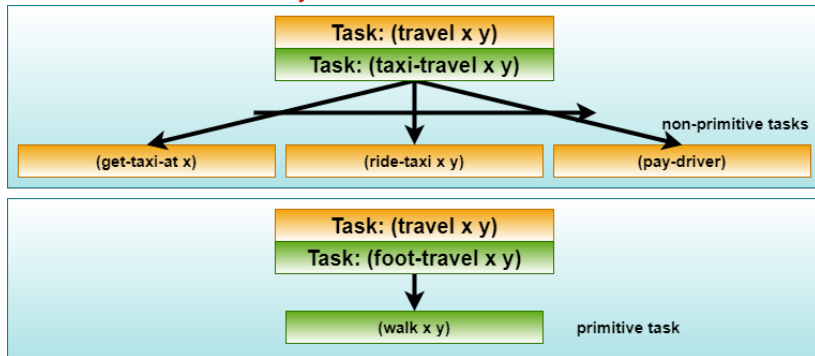
# TOTALLY ORDERED SIMPLE TASK NETWORKS

- We illustrate the entire decomposition using an horizontal arrow  $\longrightarrow$  to represent the sequence!



# MULTIPLE METHODS

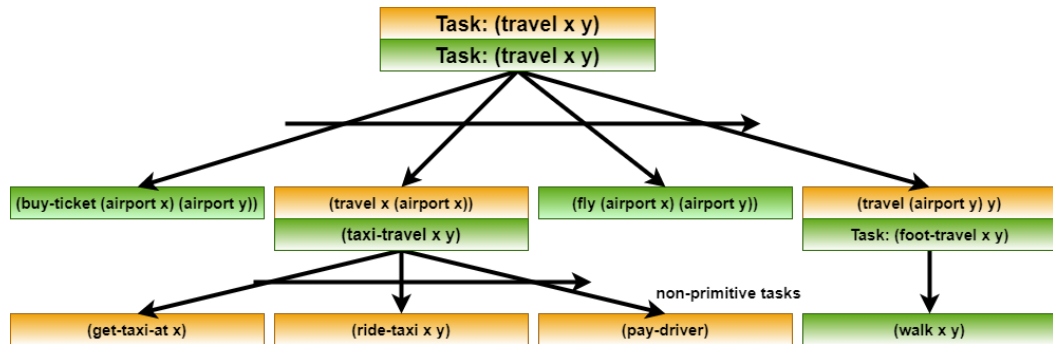
- A non-primitive task can have **many methods**



- $\implies$  You still need to **search** to determine which method to use!
- $\implies$  ... and to determine the *parameters* (discussed later)!

# COMPOSITION

- A Hierarchical Task Network plan:
  - Hierarchical
  - Consists of **tasks**
  - Based on graphs  $\approx$  **networks**



# DOMAINS, PROBLEMS, SOLUTIONS

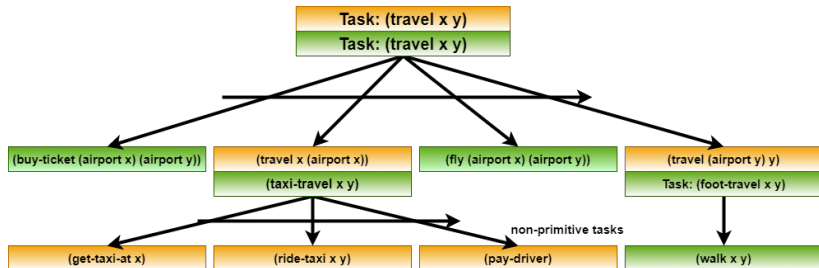
- A Simple Task Network **planning domain** specifies:
  - A set of **tasks**
  - A set of **operators** used as primitive tasks
  - A set of **methods**
  
- A Simple Task Network **problem instance** specifies:
  - A Simple Task Network planning domain
  - An **initial state**
  - An **initial task network** which shall be ground (no variables)
    - A total order Simple Task Network example:
 

```
⟨(travel home work), (do-work), (travel work home)⟩
```

**General Hierarchical Task Networks** can have additional constraints to be enforced!

# DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Suppose you:
  - Start with the **initial task network**
  - Recursively apply **methods** to non-primitive tasks expanding them
  - Continue until **all non-primitive tasks are expanded**



- Totally ordered  $\implies$  yields an action **sequence**
  - If this is executable: A **solution**
  - No goals to check – they are implicit in the method structure!

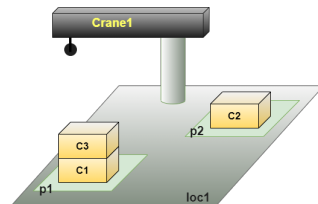


# DOMAINS, PROBLEMS, SOLUTIONS (CONT.)

- Hierarchical Task Network planning uses **only** the methods specified for a given task
  - Will **not** try arbitrary actions...
  - For this to be useful, you must **have** useful "*recipes*" for all tasks!

# DOCK WORKER ROBOTS

- Example tasks:
  - Primitive – All the DWR actions we considered so far
  - Move the **topmost** container between piles
  - Move the **entire stack** from one pile to another
  - Move a stack, but keep it in the **same order**
  - Move **several stacks** in the same order
  - ...



# METHODS

- To **move top most container** from one pile to another

- **task**

`(move-topmost-container pile1 pile2)`

The *task* has parameters  
given from above

- **method**

`(take-and-put cont crane loc  
pile1 pile2 c1 c2)`

A *method* can have additional  
parameters, whose values are  
chosen by the planner  
– as in classical planning!

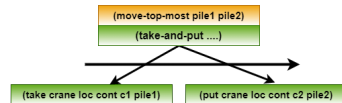
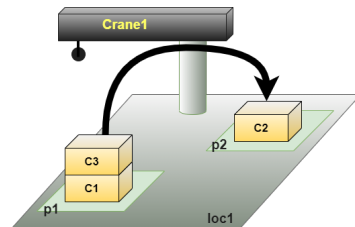
- **precond:** `(attached pile1 loc)`  
`(attached pile2 loc)`  
`(belong crane loc) (top cont pile1)`  
`(on cont c1) (top c2 pile2)`

The *precond* adds constraints:  
crane must be *some* crane in  
the same loc as the piles, cont  
must be the top most container of  
pile1, ...

Intepretation: If you're asked to `(move-topmost-container pile1 pile2)`, check all possible values for `cont`, `crane`, `loc`, `c1`, `c2` where the preconditions are satisfied!

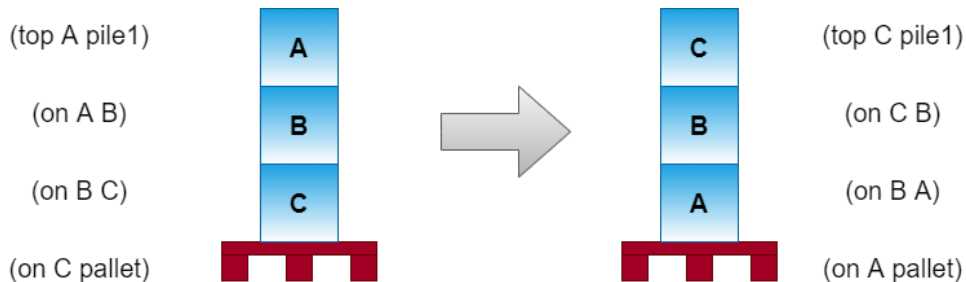
# METHODS

- To **move top most container** from one pile to another
  - **task**  
`(move-topmost-container pile1 pile2)`
  - **method**  
`(take-and-put cont crane loc  
 pile1 pile2 c1 c2)`
  - **precond:** `(attached pile1 loc)`  
`(attached pile2 loc)`  
`(belong crane loc) (top cont pile1)`  
`(on cont c1) (top c2 pile2)`
  - **subtasks:** `{ (take crane loc cont c1 pile1),  
 (put crane loc cont c2 pile2) }`



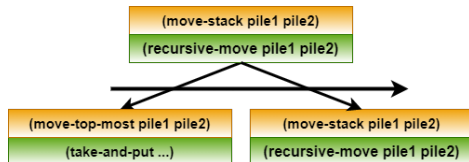
# MOVING A STACK OF CONTAINERS

- How can we implement the `(move-stack pile1 pile2)`?
  - Should we move **all** containers in a stack?
  - There is no **limit** on how many there might be...



# RECURSION

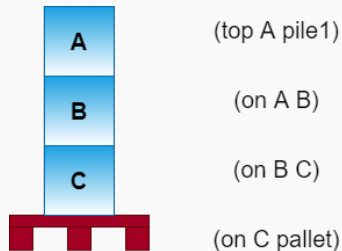
- We need a **loop** with a **termination condition**
  - Hierarchical Task Network planning allows **recursion**
    - Move the **topmost** container (we know how to do that!)
    - Then move the **rest**
- First attempt:
  - **task:** `(move-stack pile1 pile2)`
  - **method:** `(recursive-move pile1 pile2)`
  - **precond:** `True`
  - **subtasks:** `( (move-topmost-container pile1 pile2),  
(recursive-move pile1 pile2) )`



# RECURSION (CONT.)

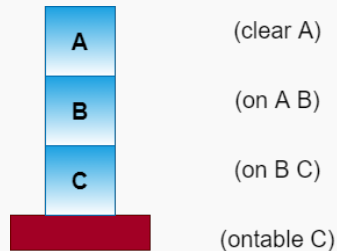
- Let's consider the BW and the DWR "pile models"...

## BW



The bottom block is not "on" anything!

## DWR



The bottom block is "on" the pallet, a "special container"!

What if the pallet is "topmost"? We do not want to move it!

# RECURSION (CONT.)

- To fix this

- **task:** `(move-stack pile1 pile2)`
- **method:** `(recursive-move pile1 pile2 cont x)`
- **precond:** `(top cont pile1) (on cont x)`
- **subtasks:** `((move-topmost-container pile1 pile2)  
(move-stack pile1 pile2) )`

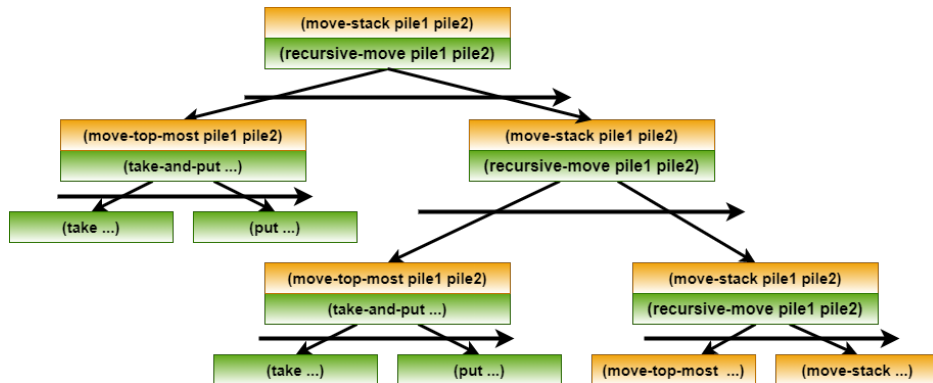
`cont` is on top of something (i.e. `x`), so `cont` can't be the pallet!

We added two additional method parameters (`cont` `x`) – "non-natural", as in "ordinary" planning  $\implies$  does not give the planner a real choice!



# RECURSION (CONT.)

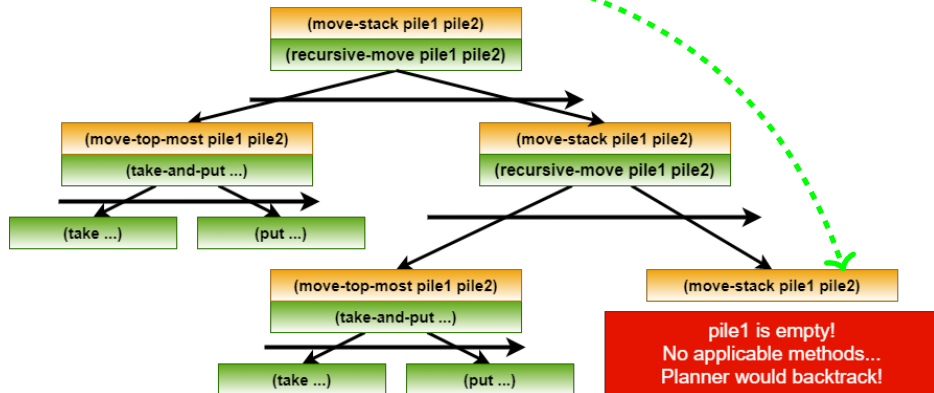
- The planner can create a structure like this...



- ... but when will **the recursion end?**

## RECURSION (CONT.)

- At some point, **only the pallet** will be left in the stack
  - The recursive-move will **not be applicable**
  - But we **must** execute **some** form of move-stack!



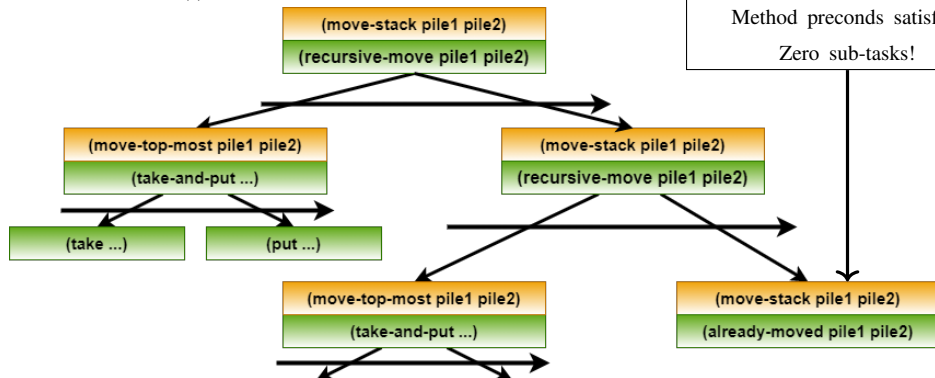
# RECURSION (CONT.)

- We need a method that **terminates** the recursion

- task:** `(move-stack pile1 pile2)`
- method:** `(already-moved pile1 pile2)`
- precond:** `(top pallet pile1)`
- subtasks:** `<>`

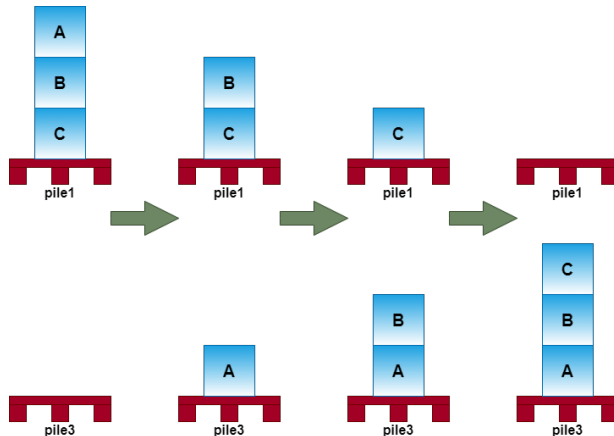
Unique pallet object  
not a variable

Method preconds satisfied  
Zero sub-tasks!



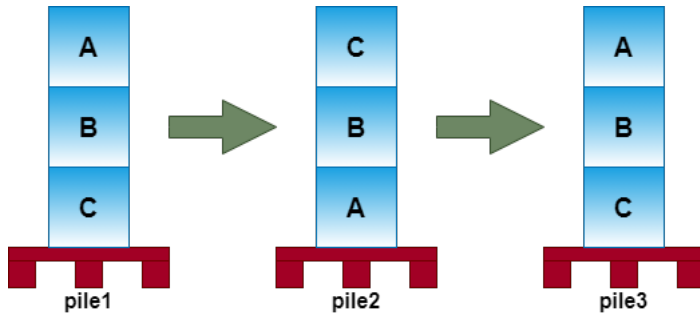
# ORDERING

- Using move-stack inverts a stack!



## ORDERING (CONT.)

- To avoid this: use intermediate pile



## ORDERING (CONT.)

### • Example

- **task:** `(move-stack-same-order pile1 pile2)`
- **method:** `(move-each-twice pile1 pileX pile2 loc)`
- **precond:** `(top pallet pileX)`  
`(!= pile1 pileX)`  
`(!= pile2 pileX)`  
`(!= pile1 pile2)`  
`(attached ...) // all in the same loc`  
`...`
- **subtasks:** `{ (move-stack pile1 pileX),`  
`(move-stack pileX pile2) }`

Unlike classical planning,  
someone *specifies* the task!,  
pile1 and pile2

The planner must choose  
a matching **method** ("im-  
plementation") to use

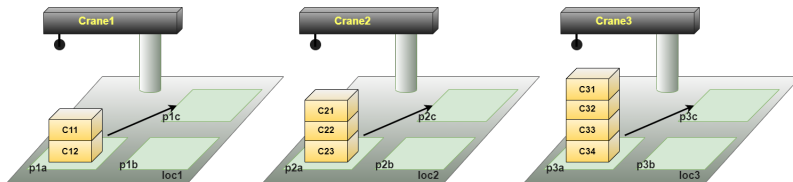
The planner must choose  
added method params pileX  
loc to satisfy the precondition!

Why does pileX have to be empty initially?

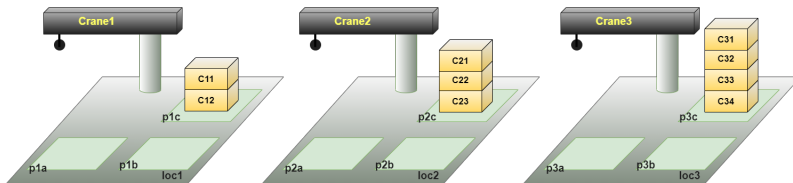
Because the second move-stack moves **all** containers from the intermediate pileX to destination pile2!

# OVERALL OBJECTIVE

- Moving three entire stacks of containers preserving order!



Initial state, with three locations, three piles to move



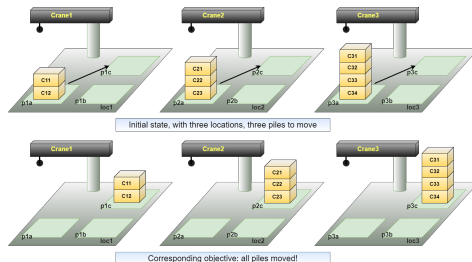
Corresponding objective: all piles moved!

# OVERALL OBJECTIVE: DEFINING A TASK

- Define a **task** for this objective!

- task:** (move-three-stacks)
- method:** (move-each-twice)
- precond:** // no preconditions apart from the sub-tasks'
- subtasks:**  $\{$  (move-stack-same-order p1a p1c),  
 (move-stack-same-order p2a p2c),  
 (move-stack-same-order p3a p3c)  $\}$

- Use this task as the *initial task network*





# GOAL PREDICATES IN HIERARCHICAL-TASK NETWORKS

- Here the entire objective is encoded in the initial network  
(move-three-stacks)
  - $\Rightarrow$  `{ (move-stack-same-order p1a p1c),  
          (move-stack-same-order p2a p2c),  
          (move-stack-same-order p3a p3c) }`
- To avoid this:
  - New predicate `(should-move-same-order pile pile)` encoding the goal!
    - **task:** `(move-as-necessary)`
    - **method:** `(move-and-repeat pile1 pile2)`
    - **precond:** `(should-move-same-order pile1 pile2)`
    - **subtasks:** `{ (move-stack-same-order pile1 pile2), ;; makes should-move... false  
                  (move-as-necessary) }`
    - **task:** `(move-as-necessary)`
    - **method:** `(all-done)`
    - **precond:** `(not (exists pile1 pile2  
                  [(should-move-same-order pile1 pile2)]))`
    - **subtasks:** `{ }`

# UNINFORMED PLANNING IN HIERARCHICAL-TASK NETWORKS

- Can even do **uninformed unguided planning**

- Doing *something, anything*:

- Task (do-something)  $\implies$  operator (pickup x)
- Task (do-something)  $\implies$  operator (putdown x)
- Task (do-something)  $\implies$  operator (stack x y)
- Task (do-something)  $\implies$  operator (unstack x y)

Planner chooses  
all parameters!

- Repeating

- Task (achieve-goals)  $\implies$   $\langle$  (do-something), (achieve-goals)  $\rangle$

- Ending

- Task (achieve-goals)  $\implies$   $\langle \rangle$ , with precondition: entire goal is satisfied!

Or combine **aspects** of this model with **other aspects** of "standard" HTN models!

## DELIVERY: FIRST VARIATION

- Delivery:

- A single truck
- Pick-up a package, drive to destination, unload

- **task:** (deliver package dest)
- **method:** (move-by-truck package packageloc dest)
- **precond:** (at package packageloc)
- **subtasks:** { (driveto packageloc), (load package),  
(driveto dest), (unload package) }

What if the truck is already at the package location?

First driveto is unnecessary!

## DELIVERY: SECOND VARIATION

- Alternative: Two alternative methods deliver

- task:** `(deliver package dest)`
  - method:** `(move-by-truck-1 package packageloc truckloc dest)`
  - precond:** `(at truck truckloc) (at package packageloc) (= truckloc packageloc)`
  - subtasks:** `( (load package), (driveto dest), (unload package) )`
- task:** `(deliver package dest)`
  - method:** `(move-by-truck-2 package packageloc truckloc dest)`
  - precond:** `(at truck truckloc) (at package packageloc) (!= truckloc packageloc)`
  - subtasks:** `( (driveto packageloc), (load package),  
(driveto dest), (unload package) )`

Do we really have to repeat the entire task?

Many "conditional" sub-tasks  $\implies$  combinatorial explosion!

## DELIVERY: SECOND VARIATION

- Make the choice in the sub-task instead!

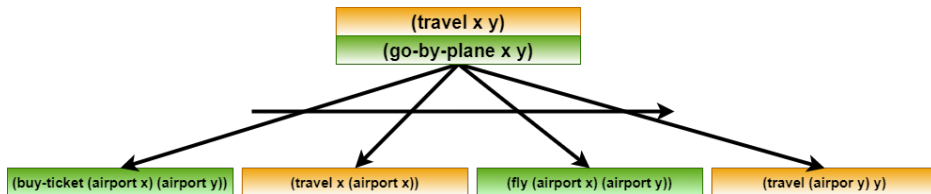
- **task:** `(deliver package dest)`
- **method:** `(move-by-truck-3 package packageloc truckloc dest)`
- **precond:** `(at truck truckloc) (at package packageloc) (= truckloc packageloc)`
- **subtasks:** `{ (be-at packageloc), (load package), (be-at dest), (unload package) }`
- **task:** `(be-at loc)`
- **method:** `(drive loc)`
- **precond:** `(not (at truck loc))`
- **subtasks:** `{ (driveto loc) }`
- **task:** `(be-at loc)`
- **method:** `(already-there)`
- **precond:** `(at truck loc)`
- **subtasks:** `{ }`

# SEARCH SPACES

- Need **search space**
  - 1) A **node structure** defining what information is in a node
  - 2) A way of creating an **initial node** from a problems instance
  - 3) A **successor function** / branching rule returning all successors
  - 4) A **solution criterion** detecting if a node corresponds to a solution
  - 5) A **plan extractor** telling us which plan a solution node a corresponds to
- Different alternatives exist!

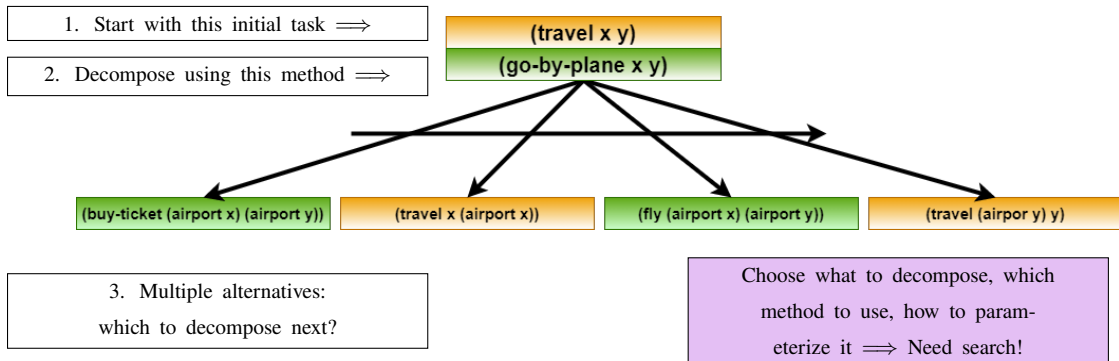
# TOTAL ORDER?

- Basic **assumption**: Total Order Simple Task Networks
  - Any **initial task** is totally ordered
  - Any **decomposition method** is totally ordered



# FORWARD DECOMPOSITION?

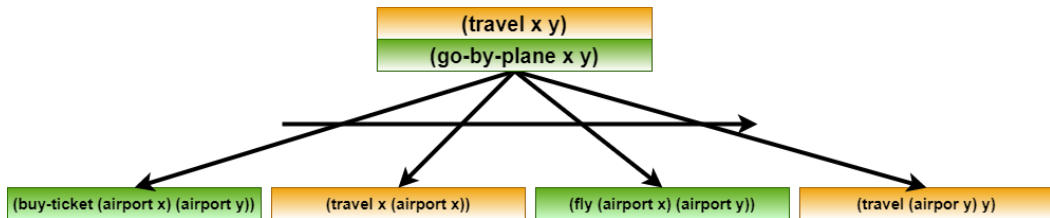
- Different **decomposition orders** are still possible



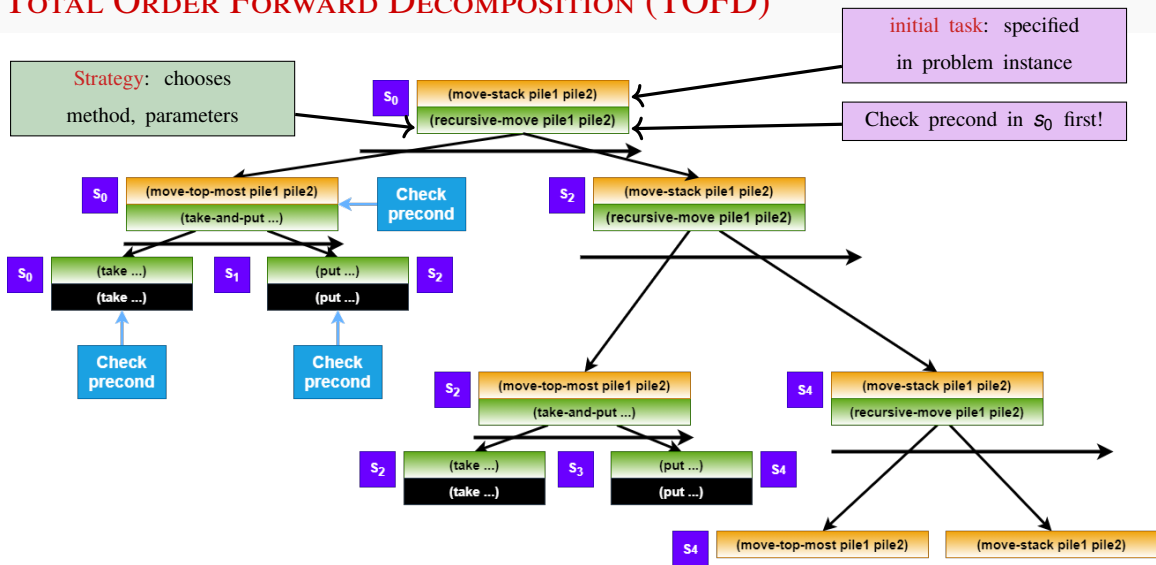


# FORWARD DECOMPOSITION!

- **Forward** decomposition: One of many possibilities
  - Go "depth first, left to right"
  - Like forward state space search:
    - Generates actions in the same order in which they will be executed
    - $\implies$  When we decompose a task, we know the "current" state of the world!



# TOTAL ORDER FORWARD DECOMPOSITION (TOFD)



# TOFD NODE STRUCTURE

- [1] A **node structure** defining what information is in a node
  - Plan so far
  - Current state - **possible due to forward decomposition**
  - Remaining tasks to expand
- [2] A way of creating an initial search node:



← No actions so far  
Current state  $s_0$   
Remaining tasks = the initial task from the problem!

- Examples: Nodes visited in the previous slide



# TOFD SUCCESSORS

- [3] Successors:
  - We know which task to decompose
  - Find all applicable methods and apply them



- [4] Solution test
  - No more tasks  $\implies$  done!
- [5] Solution extraction
  - The resulting search node *contains* a sequential plan!

# SOLVING TOTAL ORDER STN PROBLEMS

- TOFD takes a search node
  - $\pi$  - a sequence of actions
  - $s$  - the current state
  - $\langle t_1, \dots, t_k \rangle$  - a list of tasks to be achieved in **the specific order**
- We also assume:
  - $O$  - the available operators (with params, preconds, effects)
  - $M$  - the available methods (with params, preconds, subtasks)
- **Returns**
  - A sequential plan
    - Loses the hierarchical structure of the final plan
    - Simplifies the presentation - but the structure *could* also be kept!

# TOFD: BASE CASE

**function** TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

$\rightarrow [2]$

  open  $\leftarrow \{\text{initial-node}\}$

**while** (open  $\neq \emptyset$ ) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

$\rightarrow [6]$  TOFD uses depth first search

$\rightarrow [4]$  If we have no tasks left to decompose..

**if**  $k = 0$  **then return**  $\pi$

# TOFD: GROUND PRIMITIVE TASKS

**function** TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open  $\leftarrow \{\text{initial-node}\}$

**while** (open  $\neq \emptyset$ ) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

**if**  $k = 0$  **then return**  $\pi$

**if**  $t_1$  is primitive **then**

$\text{actions} \leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$

$\text{candidates} \leftarrow \{ a \mid a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } \mathcal{S} \}$

$\rightarrow$  *For simplicity: The case when all tasks to achieve are ground*

$\rightarrow [2]$

$\rightarrow [6]$  *TOFD uses depth first search*

$\rightarrow [4]$  *If we have no tasks left to decompose..*

$\rightarrow$  *A primitive task is decomposed into a single action!  
Possibly many to choose from!*



## TOFD: SUCCESSORS

**function** TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open  $\leftarrow \{\text{initial-node}\}$

**while** (open  $\neq \emptyset$ ) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

**if**  $k = 0$  **then return**  $\pi$

**if**  $t_1$  is primitive **then**

$\text{actions} \leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$

$\text{candidates} \leftarrow \{ a \mid a \in \text{actions} \wedge \text{name}(a) = t_1 \wedge a \text{ applicable in } \mathcal{S} \}$

**for each**  $a \in \text{candidates}$  **do**

$\pi' \leftarrow \pi + a$

$s' \leftarrow \gamma(\mathcal{S}, a)$

$\text{rest} \leftarrow \langle t_2, \dots, t_k \rangle$

$\text{open} \leftarrow \text{open} \cup \{ \langle \pi', s', \text{rest} \rangle \}$

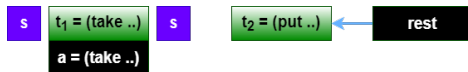
$\rightarrow$  *For simplicity: The case when all tasks to achieve are ground*

$\rightarrow [2]$

$\rightarrow$  *A primitive task is decomposed into a single action!  
Possibly many to choose from!*

$\rightarrow$  *Add action at the end*

$\rightarrow$  *Apply the action, find the new state*





# TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
      candidates  $\leftarrow \{ (a, \sigma) \mid a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } \mathcal{S} \}$ 

```

$\rightarrow$  The case when all tasks to achieve are non-ground. The plan will still be ground

$\rightarrow [2]$

$\rightarrow$  A primitive task is decomposed into a single action!  
Possibly many to choose from!

$\rightarrow$   $\sigma$  is a substitution function! Basically,  $\sigma$  can specify variable bindings for parameters of  $t_1 \dots$



# TOFD: LIFTED PRIMITIVE TASKS

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      actions  $\leftarrow \text{GROUND-INSTANCE-OF-OPERATORS}(O)$ 
      candidates  $\leftarrow \{ (a, \sigma) \mid a \in \text{actions} \wedge \text{name}(a) = \sigma(t_1) \wedge a \text{ applicable in } \mathcal{S} \}$ 
      for each  $a, \sigma \in \text{candidates}$  do
         $\pi' \leftarrow \pi + a$ 
         $\mathcal{S}' \leftarrow \gamma(\mathcal{S}, a)$ 
        rest  $\leftarrow \langle \sigma(t_2), \dots, \sigma(t_k) \rangle$ 
        open  $\leftarrow \text{open} \cup \{ \langle \pi', \mathcal{S}', \text{rest} \rangle \}$ 

```

→ The case when all tasks to achieve are non-ground. The plan will still be ground

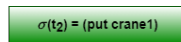
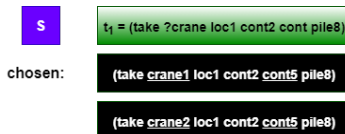
→ [2]

→ A primitive task is decomposed into a single action!  
→ Possibly many to choose from!

→ Add action at the end

→ Apply the action, find the new state

→ Must have the same variable bindings!



$\sigma = \{ ?\text{crane} \rightarrow \text{crane1}, ?\text{cont} \rightarrow \text{cont5} \}$

$\sigma = \{ ?\text{crane} \rightarrow \text{crane2}, ?\text{cont} \rightarrow \text{cont5} \}$

# TOFD: NON-PRIMITIVE TASKS

**function** TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)

initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$

open  $\leftarrow \{\text{initial-node}\}$

**while** (open  $\neq \emptyset$ ) **do**

$\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$

**if**  $k = 0$  **then return**  $\pi$

**if**  $t_1$  is primitive **then**

...

**else**

$\text{ground} \leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$

$\text{candidates} \leftarrow \{ (m, \sigma) \mid m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } \mathcal{S} \}$

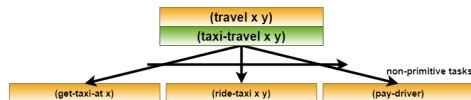
→ The case when all tasks to achieve are non-ground. The plan will still be ground

→ [2]

→  $t_1$  is e.g. (travel LiU Resecentrum)

→ A non-primitive task is decomposed into a new task-list.

→ May have many methods to choose from!



# TOFD: NON-PRIMITIVE TASKS (CONT.)

```

function TOTAL-ORDER-FORWARD-DECOMPOSITION(problem)
  initial-node  $\leftarrow \langle [], \text{problem.initialstate}, \text{problem.initialtask} \rangle$ 
  open  $\leftarrow \{\text{initial-node}\}$ 
  while (open  $\neq \emptyset$ ) do
     $\langle \pi, \mathcal{S}, \langle t_1, \dots, t_k \rangle \rangle \leftarrow \text{SEARCH-STRATEGY-REMOVE-FROM}(\text{open})$ 
    if  $k = 0$  then return  $\pi$ 
    if  $t_1$  is primitive then
      ...
    else
      ground  $\leftarrow \text{GROUND-INSTANCES-OF-METHODS}(M)$ 
      candidates  $\leftarrow \{ (m, \sigma) \mid m \text{ ground} \wedge \text{task}(m) = \sigma(t_1) \wedge m \text{ applicable in } \mathcal{S} \}$ 
      for each  $(m, \sigma) \in \text{candidates}$  do
         $\pi' \leftarrow \pi$ 
         $s' \leftarrow s$ 
        rest  $\leftarrow \langle \text{SUBTASKS}(m) + \sigma(t_2), \dots, \sigma(t_k) \rangle$ 
        open  $\leftarrow \text{open} \cup \{ \langle \pi', s', \text{rest} \rangle \}$ 

```

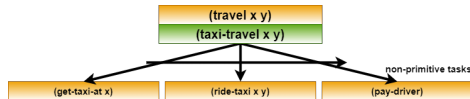
→ The case when all tasks to achieve are non-ground. The plan will still be ground

→ [2]

→ No action needed!

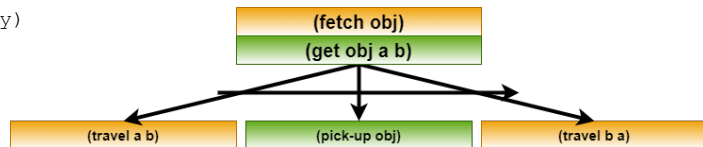
→ No state change

→ Prepend new list! The "origin" of a task is discarded: only the sub-tasks are relevant!



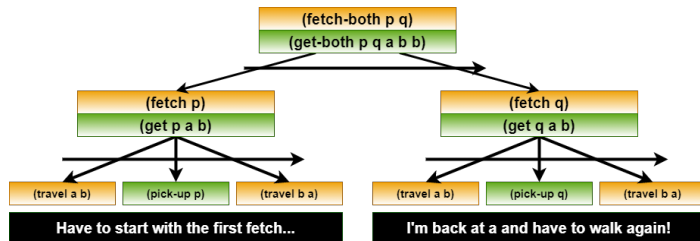
# LIMITATIONS OF ORDERED-TASK PLANNING

- TOFD requires **totally ordered** methods
  - Can't interleaves sub-tasks of different tasks
- Suppose we want to **fetch one object** somewhere, then return to where we are now
  - task:** (fetch obj)
  - method:** (get obj mypos objpos)
  - precond:** (robotat mypos) (at obj objpos)
  - subtasks:** { (travel mypos objpos), (pick-up obj), (travel objpos mypos) }
- task:** (travel x y)
- method:** (walk x y)
- method:** (stayat x y)



# LIMITATIONS OF ORDERED-TASK PLANNING (CONT.)

- Suppose we want to fetch **two** objects somewhere, then return to where we are now
- One idea: Just "fetch" each object in sequence
  - **task:** `(fetch-both obj1 obj2)`
  - **method:** `(get-both obj1 obj2 mypos objpos1 objpos2)`
  - **precond:**
  - **subtasks:** `{ (fetch obj1 mypos objpos1), (fetch obj2 mypos objpos2) }`



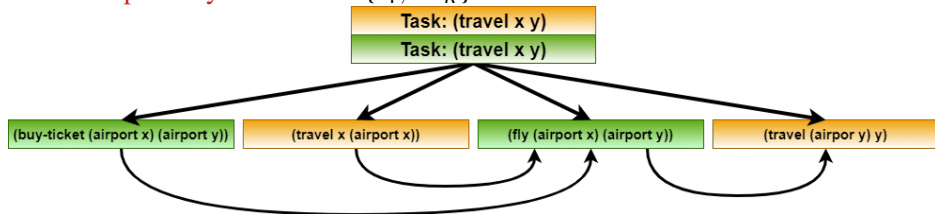
## ALTERNATIVE METHODS

- To generate more efficient plans using total-order STNs:
  - Use a different domain model!
    - **task:** `(fetch-both obj1 obj2)`
    - **method:** `(get-both obj1 obj2 mypos objpos1 objpos2)`
    - **precond:** `(!= objpos1 objpos2) (at obj1 objpos1) (at obj2 objpos2)`
    - **subtasks:** `{ (travel mypos objpos1), (pick-up obj1),  
                  (travel objpos1 objpos2), (pick-up obj2),  
                  (travel objpos2 mypos) }`
  - **task:** `(fetch-both obj1 obj2)`
  - **method:** `(get-both-in-same-place obj1 obj2 mypos objpos)`
  - **precond:** `(at obj1 objpos) (at obj2 objpos)`
  - **subtasks:** `{ (travel mypos objpos), (pick-up obj1),  
                  (pick-up obj2), (travel objpos mypos) }`

Or: Load-all; drive-truck; unload-all

# PARTIALLY ORDERED METHODS

- The sub-tasks are a **partially ordered** set  $\{t_1, \dots, t_k\}$  – a *network*



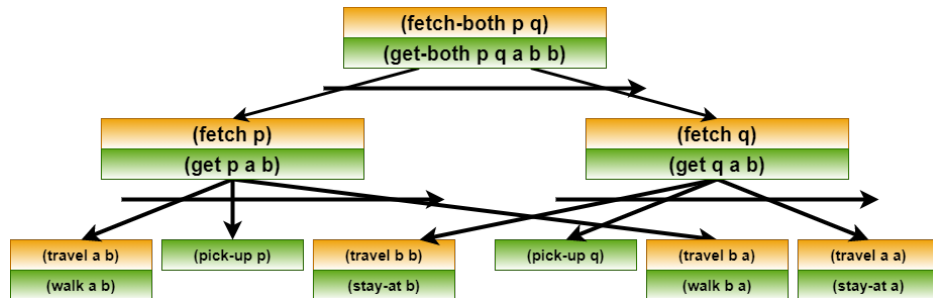
- method:** (go-by-plane x y)
  - task:** (travel x y)
  - precond:** (long-distance x y)
  - network:**

$$\begin{aligned}
 u_1 &= (\text{buy-ticket } (\text{airport } x) (\text{airport } y)) \\
 u_2 &= (\text{travel } x (\text{airport } x)) \\
 u_3 &= (\text{fly } (\text{airport } x) (\text{airport } y)) \\
 u_4 &= (\text{travel } (\text{airport } y) y) \\
 &\{ (u_1, u_3), (u_2, u_3), (u_3, u_4) \}
 \end{aligned}$$



# PARTIALLY ORDERED METHODS

- With partially ordered methods **sub-tasks can be interleaved**



- Requires a more complicated planning algorithm: POFD
- SHOP2: implementation of POFD-like algorithm + generalizations

# REFERENCES I

- [1] Hector Geffner and Blai Bonet. *A Concise Introduction to Models and Methods for Automated Planning*. Synthesis Lectures on Artificial Intelligence and Machine Learning. Morgan & Claypool Publishers, 2013. ISBN 9781608459698. doi: 10.2200/S00513ED1V01Y201306AIM022. URL <https://doi.org/10.2200/S00513ED1V01Y201306AIM022>.
- [2] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated planning - theory and practice*. Elsevier, 2004. ISBN 978-1-55860-856-6.
- [3] Malik Ghallab, Dana S. Nau, and Paolo Traverso. *Automated Planning and Acting*. Cambridge University Press, 2016. ISBN 978-1-107-03727-4. URL <http://www.cambridge.org/de/academic/subjects/computer-science/artificial-intelligence-and-natural-language-processing/automated-planning-and-acting?format=HB>.