

Higher order functions and SQL

TEAM INFDEV

Hogeschool Rotterdam
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Higher order
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Motivation

- Sometimes simple functions are not flexible enough
- We might have similar algorithms that are “not quite” the same
- For example, consider adding or multiplying all elements of a list together
 - **“Consider” here actually means do it on paper and then a volunteer comes implement it at the lecturer’s PC**

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Higher order function

Idea

- Functions may also take and return other functions as parameters
 - These are then called **higher order functions** (HOF's)^a
- This lets us specify a function where some instructions are not fixed
- By passing other functions as parameters we literally create “customizable algorithms”

^a

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Idea

- Functions may also take and return other functions as parameters
 - These are then called **higher order functions** (HOF's)^a
- This lets us specify a function where some instructions are not fixed
- By passing other functions as parameters we literally create “customizable algorithms”

^a**Higher order** because parameters are not concrete values but rather computations, which are higher wrt the floors of the Ivory Tower

Example

- As an example, consider the case of combining two values together
- We do not care how, as long as they are combined according to some criterion
- The criterion is given as an input function

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1
2

```
def combine(op,x,y):  
    return op(x,y)
```

Example

- What do we know about x and y ?
- Do we even care?

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Example

- A function such as `combine` can be used by providing another function as the first parameter
- As long as the function will work correctly on the second and third parameters

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 def plus(x,y): return x + y  
5 def times(x,y): return x * y  
6 def minus(x,y): return x - y  
7  
8 print(combine(plus, 10, 20))  
9 print(combine(times, 10, 20))  
10 print(combine(minus, 10, 20))
```

Example

- What does this code do?

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 def plus(x,y): return x + y  
5 def times(x,y): return x * y  
6 def minus(x,y): return x - y  
7  
8 print(combine(plus, 10, 20))  
9 print(combine(times, 10, 20))  
10 print(combine(minus, 10, 20))
```

Example

- What does this code do?
- Prints 30, 200, -10

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Example

- We can use `combine` on any data types we want
- For example, strings

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 def plus(x,y): return x + y  
5 def times(x,y): return x * y  
6 def minus(x,y): return x - y  
7  
8 print(combine(plus, "10", "20"))  
9 print(combine(times, 10, 20))  
10 print(combine(minus, 10, 20))
```

Example

- What does this code do?

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 def plus(x,y): return x + y  
5 def times(x,y): return x * y  
6 def minus(x,y): return x - y  
7  
8 print(combine(plus, "10", "20"))  
9 print(combine(times, 10, 20))  
10 print(combine(minus, 10, 20))
```

Example

- What does this code do?
- Prints 1020, 200, -10

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 def plus(x,y): return x + y  
5 def times(x,y): return x * y  
6 def minus(x,y): return x - y  
7  
8 print(combine(plus, "10", "20"))  
9 print(combine(times, 10, 20))  
10 print(combine(minus, 10, 20))
```

What do stack and heap look like from inside a call to combine?

```

1 def combine(op,x,y):
2     return op(x,y)
3
4 def plus(x,y): return x + y
5 def times(x,y): return x * y
6 def minus(x,y): return x - y
7
8 print(combine(plus, "10", "20"))
9 print(combine(times, 10, 20))
10 print(combine(minus, 10, 20))

```

What do stack and heap look like from inside a call to combine?

S	PC	combine	PC	op	x	y
	8	nil	2	ref(plus)	"10"	"20"

H	

or

S	PC	combine	PC	op	x	y
	8	nil	2	ref(times)	10	20

H	

Lambda-syntax function definition

- Defining functions such as plus, times, and minus is cumbersome
- After all, we already have symbols for them: (+), (*), and (-)
- Repetition and duplication of code is never good

Lambda-syntax function definition

- Python (version at least 3) offers facilities for the inline definition of short functions
- The syntax fits one line and requires no newlines
- `lambda <<parameters>>: <<result>>`
 - `<<parameters>>` is a list of comma-separated parameters
 - `<<result>>` is the expression that is returned
- For example: `lambda x,y: x+y`

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 print(combine((lambda x,y: x+y), "10", "20"))  
5 print(combine((lambda x,y: x*y), 10, 20))  
6 print(combine((lambda x,y: x-y), 10, 20))
```

Lambda-syntax function definition

- What does this code do?

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 print(combine((lambda x,y: x+y), "10", "20"))  
5 print(combine((lambda x,y: x*y), 10, 20))  
6 print(combine((lambda x,y: x-y), 10, 20))
```

Lambda-syntax function definition

- **What does this code do?**
- Prints 1020, 200, -10
- Does not require the extra function definitions

```
1 def combine(op,x,y):  
2     return op(x,y)  
3  
4 print(combine((lambda x,y: x+y), "10", "20"))  
5 print(combine((lambda x,y: x*y), 10, 20))  
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What do stack and heap look like from inside a call to combine?

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1 def combine(op,x,y):
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5 print(combine((lambda x,y: x*y), 10, 20))
6 print(combine((lambda x,y: x-y), 10, 20))

```

What do stack and heap look like from inside a call to combine?

S	PC	combine	PC	op	x	y
	4	nil	2	ref(0)	"10"	"20"

H	0
	lambda x,y: x+y

or

S	PC	combine	PC	op	x	y
	5	nil	2	ref(1)	10	20

H	0	1
	lambda x,y: x+y	lambda x,y: x*y

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Lambda-syntax function definition

- We can also return a function from a function
- For example, to dynamically choose an operation
- This makes code very expressive and flexible, but also potentially much harder to read
- Use with caution!

```
1 def combine(op,x,y):
2     return op(x,y)
3
4 def choose_operation():
5     i = input("Choose an operation between +, -, or *")
6     if i == "+":
7         return lambda x,y: x+y
8     elif i == "-":
9         return lambda x,y: x-y
10    else:
11        return lambda x,y: x*y
12    print(combine(choose_operation(), 10, 20))
```

Lambda-syntax function definition

- What does this code do?


```
1 def combine(op,x,y):
2     return op(x,y)
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4 def choose_operation():
5     i = input("Choose an operation between +, -, or *")
6     if i == "+":
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9         return lambda x,y: x-y
10    else:
11        return lambda x,y: x*y
12 print(combine(choose_operation(), 10, 20))
```

Lambda-syntax function definition

- What does this code do?
- Chooses the function based on input that will combine 10 and 20

```
1 def combine(op,x,y):
2     return op(x,y)
3
4 def choose_operation():
5     i = input("Choose an operation between +, -, or *")
6     if i == "+":
7         return lambda x,y: x+y
8     elif i == "-":
9         return lambda x,y: x-y
10    else:
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```

What do stack and heap look like after choose_operation terminates?

```

1 def combine(op,x,y):
2     return op(x,y)
3
4 def choose_operation():
5     i = input("Choose an operation between +, -, or *")
6     if i == "+":
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9         return lambda x,y: x-y
10    else:
11        return lambda x,y: x*y
12    print(combine(choose_operation(), 10, 20))

```

What do stack and heap look like after choose_operation terminates?

S	PC	choose_operation
	12	ref(0)
H	0	
	lambda x,y: x+y	

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Introduction

- Consider our (now well-known) list implementation
- Empty and Node classes
- IsEmpty, Head, Tail methods

List definition

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```
1 class Empty:
2     def __init__(self):
3         self.IsEmpty = True
4     Empty = Empty()
5
6 class Node:
7     def __init__(self, x, xs):
8         self.IsEmpty = False
9         self.Head = x
10        self.Tail = xs
11
12 def printList(l):
13     if(l.IsEmpty):
14         return Empty
15     else:
16         print(l.Head)
17         printList(l.Tail)
```

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Fundamental operations on lists

- What are the **fundamental things** we wish to do with a list?

Fundamental operations on lists

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- **Transform** all its elements: $N \rightarrow N$

Fundamental operations on lists

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- **Transform** all its elements: $N \rightarrow N$
- **Filter** some of its elements: $N \rightarrow M, M \leq N$

Fundamental operations on lists

- What are the **fundamental things** we wish to do with a list?
- **Transform** all its elements: $N \rightarrow N$
- **Filter** some of its elements: $N \rightarrow M, M \leq N$
- **Fold** its elements into a single value: $N \rightarrow 1$

Transforming a list

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```
1 def map(l, f):  
2     if(l.IsEmpty):  
3         return Empty  
4     else:  
5         return Node(f(l.Head), map(l.Tail, f))  
6  
7 printList(map(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x + 1))
```

Fundamental operations on lists

- What does the code above print?

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1 def map(l, f):  
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6  
7 printList(map(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x + 1))
```

Fundamental operations on lists

- What does the code above print?
- 2, 3, 4, 5

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```
1 def map(l, f):  
2     if(l.IsEmpty):  
3         return Empty  
4     else:  
5         return Node(f(l.Head), map(l.Tail, f))  
6  
7 printList(map(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x * 2))
```

Fundamental operations on lists

- What does the code above print?

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```
1 def map(l, f):  
2     if(l.IsEmpty):  
3         return Empty  
4     else:  
5         return Node(f(l.Head), map(l.Tail, f))  
6  
7 printList(map(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x * 2))
```

Fundamental operations on lists

- What does the code above print?
- 2, 4, 6, 8

Filtering a list

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```
1 def filter(l, p):
2     if(l.IsEmpty):
3         return Empty
4     else:
5         if p(l.Head):
6             return Node(l.Head, filter(l.Tail, p))
7         else:
8             return filter(l.Tail, p)
9
10 printList(filter(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x \% 2
    == 0))
```

Fundamental operations on lists

- What does the code above print?

Filtering a list

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```
1 def filter(l, p):
2     if(l.IsEmpty):
3         return Empty
4     else:
5         if p(l.Head):
6             return Node(l.Head, filter(l.Tail, p))
7         else:
8             return filter(l.Tail, p)
9
10 printList(filter(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x: x \% 2
    == 0))
```

Fundamental operations on lists

- What does the code above print?
- 2, 4

Folding a list

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```
1 def fold(l, f, z):
2     if(l.IsEmpty):
3         return z
4     else:
5         return f(l.Head, fold(l.Tail, f, z))
6
7 print(fold(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x, y: x + y, 0))
```

Fundamental operations on lists

- What does the code above print?

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```
1 def fold(l, f, z):  
2     if(l.IsEmpty):  
3         return z  
4     else:  
5         return f(l.Head, fold(l.Tail, f, z))  
6  
7 print(fold(Node(1, Node(2, Node(3, Node(4, Empty)))), lambda x, y: x + y, 0)  
      )
```

Fundamental operations on lists

- What does the code above print?
- 10

Using HOF's

- We can perform almost anything we need to do no lists with `map`, `filter`, and `fold`
- Some complex algorithm cannot be implemented relying on unbounded recursion (where we cannot estimate the maximum number of steps)
- This happens because `map`, `filter`, and `fold` will always terminate (if the input function terminates)
- Still, they are quite powerful in their capabilities

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Using HOF's

- map is very obvious: transform elements
 - `map(cars, drive)`
 - `map(planes, fly)`
 - `map(bikes, pedal)`
 - ...

Using HOF's

- `filter` is also very obvious: remove useless elements
 - `filter(cars, arrived)`
 - `filter(planes, landed)`
 - `filter(bikes, crashed)`
 - ...

Using HOF's

- fold is much more complex
- Recall that it folds a list into a single value $N \rightarrow 1$
 - `fold(1, lambda x,l: 1 + 1, 0) = ?`

Using HOF's

- fold is much more complex
- Recall that it folds a list into a single value $N \rightarrow 1$
 - `fold(1, lambda x,l: 1 + 1, 0) = ?` length of `l`
 - `fold(1, max, float('-inf')) = ?`

Using HOF's

- fold is much more complex
- Recall that it folds a list into a single value $N \rightarrow 1$
 - `fold(l, lambda x,l: l + 1, 0) = ?` length of l
 - `fold(l, max, float('-inf')) = ?` max of l
 - `fold(l, min, float('inf')) = ?`

Using HOF's

- fold is much more complex
- Recall that it folds a list into a single value $N \rightarrow 1$
 - `fold(l, lambda x,l: l + 1, 0) = ?` length of l
 - `fold(l, max, float('-inf')) = ?` max of l
 - `fold(l, min, float('inf')) = ?` min of l
 - `fold(cars, closerToPlayer, None) = ?`

Using HOF's

- fold is much more complex
- Recall that it folds a list into a single value $N \rightarrow 1$
 - `fold(l, lambda x,l: l + 1, 0) = ?` length of l
 - `fold(l, max, float('-inf')) = ?` max of l
 - `fold(l, min, float('inf')) = ?` min of l
 - `fold(cars, closerToPlayer, None) = ?` closest car to player
 - ...

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Folding to lists

- fold can return a value of an arbitrary type
- **Also a list?**

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Folding to lists

- fold can return a value of an arbitrary type
- **Also a list?** Yes!

Folding to lists

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```
1 printList(  
2     fold(  
3         Node(1, Node(2, Node(3, Node(4, Empty)))),  
4         lambda x, y: Node(x+1,y),  
5         Empty))
```

Folding to lists

- What does the code above print?

Folding to lists

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```
1 printList(  
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3         Node(1, Node(2, Node(3, Node(4, Empty)))),  
4         lambda x, y: Node(x+1,y),  
5         Empty))
```

Folding to lists

- What does the code above print?
- 2, 3, 4, 5
- What does it look like?

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```
1 printList(  
2   fold(  
3     Node(1, Node(2, Node(3, Node(4, Empty)))),  
4     lambda x, y: Node(x+1,y),  
5     Empty))
```

Folding to lists

- What does the code above print?
- 2, 3, 4, 5
- What does it look like?
- **A map!**

Combine list HOF's

- We can clearly combine map, filter, and fold
- For example, we could say `filter(map(l, f), p)` that applies a map first and a filter second
 - `filter(map(cars, drive), arrived) = ?`

Combine list HOF's

- We can clearly combine map, filter, and fold
- For example, we could say `filter(map(l, f), p)` that applies a map first and a filter second
 - `filter(map(cars, drive), arrived) = ?` updated cars that have not yet arrived

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- We will now explore the differences and similarities between SQL and Python list HOF's
- SQL statements translated to Python HOF's
- Python HOF's translated to SQL statements

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SELECT

- Consider a simple SQL query
- `SELECT f(x) FROM l`
- **What are f , x , and l ?**
 l is?

SELECT

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- `SELECT f(x) FROM l`
- **What are f , x , and l ?**

l is? a table

x is?

SELECT

- Consider a simple SQL query
- `SELECT f(x) FROM l`
- **What are f , x , and l ?**
 - l is? a table
 - x is? an entry from the table
 - f is?

SELECT

- Consider a simple SQL query

- `SELECT f(x) FROM l`

- **What are f , x , and l ?**

l is? a table

x is? an entry from the table

f is? a transformation of the entries of the
table

the query returns? all elements of l transformed by f

SELECT

- Consider a simple call to map
- `map(l, lambda x: f(x))`
- **What are f , x , and l ?**
 l is?

SELECT

- Consider a simple call to map
- `map(l, lambda x: f(x))`
- **What are `f`, `x`, and `l`?**

`l` is? a list

`x` is?

SELECT

- Consider a simple call to `map`
- `map(l, lambda x: f(x))`
- **What are `f`, `x`, and `l`?**
 - `l` is? a list
 - `x` is? an element of the list
 - `f` is?

SELECT

- Consider a simple call to `map`

- `map(l, lambda x: f(x))`

- **What are `f`, `x`, and `l`?**

`l` is? a list

`x` is? an element of the list

`f` is? a transformation of the elements of the
list

the call returns? all elements of `l` transformed by `f`

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SELECT

Domain	Code	l	x	f	return
SQL	SELECT f(x) FROM l	table	entry of l	transformation of x	all l transformed by f
Python	map(l, lambda x: f(x))	list	element of l	transformation of x	all l transformed by f
Logic					

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SELECT

Domain	Code	l	x	f	return
SQL	SELECT $f(x)$ FROM l	table	entry of l	transformation of x	all l transformed by f
Python	map(l , lambda x : $f(x)$)	list	element of l	transformation of x	all l transformed by f
Logic	$\{f(x) x \in l\}$	set	element of l	function of x	all l transformed by f

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WHERE

- Consider now a restriction
- `SELECT * FROM l WHERE p(x)`
- **What are p , x , and l ?**
 l is?

WHERE

- Consider now a restriction
- `SELECT * FROM l WHERE p(x)`
- **What are p , x , and l ?**

l is? a table

x is?

WHERE

- Consider now a restriction
- `SELECT * FROM l WHERE p(x)`
- **What are p , x , and l ?**
 - l is? a table
 - x is? an entry from the table
 - p is?

WHERE

- Consider now a restriction
- `SELECT * FROM l WHERE p(x)`
- **What are p , x , and l ?**
 - l is? a table
 - x is? an entry from the table
 - p is? a condition on the entries of the table
- **the query returns? all elements of l satisfying p**
- **What does this correspond to in Python?**

WHERE

- Let's use a filter!
- `filter(l, lambda x: p(x))`
- **What are p, x, and l?**
 l is?

WHERE

- Let's use a filter!
- `filter(l, lambda x: p(x))`
- **What are p, x, and l?**
 - `l` is? a list
 - `x` is?

WHERE

- Let's use a filter!
- `filter(l, lambda x: p(x))`
- **What are `p`, `x`, and `l`?**
 - `l` is? a list
 - `x` is? an element of the list
 - `f` is?

WHERE

- Let's use a filter!
- `filter(l, lambda x: p(x))`
- **What are p , x , and l ?**
 - l is? a list
 - x is? an element of the list
 - f is? a condition on the elements of the list
 - the call** returns? all elements of l satisfying f

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WHERE

Domain	Code	l	x	f	return
SQL	SELECT * FROM l WHERE p(x)	table	entry of l	condition on x	all l satisfying p
Python	filter(l, lambda x: p(x))	list	element of l	condition on x	all l satisfying p
Logic					

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WHERE

Domain	Code	l	x	f	return
SQL	SELECT * FROM l WHERE $p(x)$	table	entry of l	condition on x	all l satisfying p
Python	<code>filter(l, lambda x: p(x))</code>	list	element of l	condition on x	all l satisfying p
Logic	$\{x x \in l \wedge p(x)\}$	set	element of l	predicate on x	l restricted to/by f

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AGGREGATE

- Consider now an aggregation
- `SELECT COUNT(*) FROM l`
the query returns? the number of elements of l
- **What does this correspond to in Python?**

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AGGREGATE

- Let's use a fold!
- `fold(1, (lambda x,c: c+1), 0)`
the call returns? the number of elements of 1

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AGGREGATE

Domain	Code	l	return
SQL	SELECT COUNT(*) FROM l	table	number of entries of l
Python	fold(l, lambda x,c: c+1, 0)	list	number of elements of l
Logic			

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AGGREGATE

Domain	Code	l	return
SQL	SELECT COUNT(*) FROM l	table	number of entries of l
Python	fold(1, lambda x,c: c+1, 0)	list	number of elements of l
Logic	$(+ 1)l$	set	size of l

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General considerations

- There is no real conceptual difference between SQL and list HOF's
- The mapping is quite straightforward

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General considerations

Concept	SQL	HOF's
element transformation	SELECT	map
element removal	WHERE	filter
element folding	SUM, COUNT, AVG, ...	fold
cartesian product	JOIN	nesting of HOF's ^a

^aA filter within a map is a basic join.

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Lecture topics

- Often, user code needs to perform operations that are similar to each other
- Through the mechanism of function definition, we can recycle code
- Functions can encode algorithms in many way
 - Simple code abstractions to avoid repetition
 - Recursive problems
 - Algorithms with “holes” given as higher order parameters
 - Algorithms that return other algorithms as higher order results
- This is extremely powerful, as it even allows us to reimplement apparently unrelated concepts such as SQL operators

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Build and test, on paper and then in Python

- A Car class, with a drive function that returns the car at a new position
- A driveAllCars function that drives all cars in a list through the use of `map`
- A removeArrived function that removes all cars from the list that reached their destination through the use of `filter`

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The best of luck, and thanks for the
attention!