

Guideline for codes

Restricted mean survival time to estimate an intervention effect in a cluster randomized trial

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0 Introduction

The code is divided into two folders: one for the scenarios under proportional-hazards (PH) assumption and one under non-proportional-hazards (NPH) assumption. For both cases, there are 2 steps:

1. Generation of the datasets and statistical analysis
2. Estimation of the performance measures

The following sections describe how to use the R code for each step.

1 Generation of the datasets and statistical analysis

The `main_DA_PH.R` (for the PH assumption) and `main_DA_NPH.R` (for the NPH assumption) files are R codes to generate 1000 simulated datasets of a predefined scenario and to analyse each dataset with the 5 methods (KM_{indep} , PV_{indep} , KM_{clust} , PV_{ECM} and PV_{ICM}). For the permutation test, see the section 1.1.

The necessary packages are: `doParallel` (line 14) and `doRNG` (line 15). The necessary R functions, saved in a R file with the same name, are loaded in the main script (`main_DA_PH.R` or `main_DA_NPH.R`):

- `sim_PH` or `sim_NPH` (line 20): simulates a dataset and estimates the difference in RMST, its variance and the 95% confidence interval with the 5 methods
- `generate_data_PH` or `generate_data_NPH` (line 21): generates one dataset
- `generate_cluster_PH` or `generate_cluster_NPH` (line 22): generates time-to-event data for one cluster
- `RMST_pseudo` (line 23): analyses one dataset with the pseudo-value regression-based methods (accounting and not accounting for clustering)
- `RMST_KM` (line 24): analyses one dataset with the Kaplan-Meier-based methods (accounting and not accounting for clustering)
- `variance_bootstrap` (line 25): resamples one dataset and estimates the difference in RMST with the Kaplan-Meier-based method (function to estimate the variance of the difference in RMST using bootstrap method)

The `RMST_pseudo`, `RMST_KM` and `variance_bootstrap` functions are identical for PH and NPH assumptions.

Before running, you have to specify in the main file (`main_DA_PH.R` or `main_DA_NPH.R`):

- The directory where you saved all the R files with the necessary R functions detailed previously (line 19).
- The parameters of the scenario (line 30 in the data frame `table_parameter`).
- The horizon time (line 41). Here, it is set at 365 days. All time are expressed in days.
- The directory where the 1000 simulated datasets and the estimations of the difference in RMST, the variance and 95% confidence interval of each simulated datasets will be saved (line 47). The 1000 datasets will be saved in a same automatically created folder. The estimations of the difference in RMST, variance and 95% confidence interval for the 5 methods and for the 1000 simulated datasets will be saved in one txt file. Table 1 and 2 described the content of one simulated dataset and of the txt file with all the estimations, respectively.
- The number of cores for the parallelisation (line 76).

Colnames	Variables
time	X_{lk} , the observed time of the individual l from the cluster k
arm	arm of the clusters k (= 1 for the intervention group, 0 for control group)
cluster	cluster's identifiant k
id_patient	patient's identifiant l
status	δ_{lk} , the event indicator of the individual l from the cluster k (δ_{lk} = 1 for death, 0 for censor)

Table 1: Content of one simulated dataset

Colnames	Variables
<i>Parameters used to simulate the dataset</i>	
d	dataset number
K	total number of clusters
m	mean cluster size
HR	true HR
t_delay	change point (<u>only for NPH assumption</u>)
tau	Kendall's tau
censoring	censoring rate
<i>Analysis</i>	
clustering	if the method accounts (= "yes") or does not account (= "no") for clustering
delta.rmst	estimation of the difference in RSMT
var	variance estimation
ci.low	lower bound of the 95% confidence interval
ci.up	upper bound of the 95% confidence interval
method	type of method used for the analysis
t_star	horizon time of the analysis

Table 2: Content of the txt file with the estimations of the difference in RMST, variance and 95% confidence intervals for the 5 methods and for the 1000 simulated datasets

1.1 *Permutation test for the pseudo-values regression-based method: Statistical analysis*

The permutation tests for the pseudo-values regression-based method are performed separately from the 5 other methods. All the needed functions are available in the *Permutation test* folder (*/Proportional-hazards/1 - Generation of the datasets and statistical analysis/Permutation test/* or */Non-proportional-hazards/1 - Generation of the datasets and statistical analysis/Permutation test/*). For the proportional hazard scenarios, the *Permutation test* folder is divided into two folders: one for the permutation test (*p-value* folder) and one for the permutation-based confidence interval construction (*confidence interval* folder). For the non-proportional scenarios, there is only the *confidence interval* folder.

1.1.1 Permutation test: p-value

The `main_permutation_pvalue.R` file is the R code to analyse each simulated dataset with the permutation test. The necessary packages are: `doParallel` (line 14) and `doRNG` (line 15). The necessary R functions, saved in a R file with the same name, are loaded in the main file (`main_permutation_pvalue.R`):

- `sim_permutation_pvalue` (line 20): to estimate the p-values for the pseudo-values regression-based methods
- `permutation` (line 21): to analyse of one dataset with the permutation test
- `permutation_test` (line 22): to estimate the test statistic for one permuted dataset

Before running, you have to specify in the `main_permutation_pvalue.R` file:

- The directory where you saved all the R files with the necessary R functions detailed previously (line 19).
- The parameters of the scenario (line 27 in the data frame `table_parameter`).
- The horizon time (line 38). Here, it is set at 365 days. All time are expressed in days.
- The directory where the estimations of the p-values will be saved (line 45). The estimations of the p-values for the 1000 simulated datasets will be saved in one txt file. Table 3 describes this txt file.
- The number of cores for the parallelisation (line 69).

You also have to specify in the `sim_permutation_pvalue.R` file, the directory where the simulated datasets have been saved (line 24).

Colnames	Variables
<i>Parameters used to simulate the dataset</i>	
d	dataset number
K	total number of clusters
m	mean cluster size
HR	true HR
tau	Kendall's tau
censoring	censoring rate
<i>Analysis</i>	
matrix	type of working correlation matrix used for the analysis ("ind" = independent, "exch" = exchangeable)
pvalue	estimated p-value
t_star	horizon time of the analysis

Table 3: Content of txt file with the estimations of p-value for pseudo-values regression for the 1000 simulated datasets

1.1.2 Permutation-based confidence interval

The `main_permutation_ci.R` file is the R code to analyse each simulated dataset with the permutation test. The necessary packages are: `doParallel` (line 14) and `doRNG` (line 15). The necessary R functions, saved in a R file with the same name, are loaded in the main file (`main_permutation_ci.R`):

- `sim_permutation_ci` (line 20): to estimate the permutation-based confidence interval for the pseudo-values regression-based methods
- `ci` (line 21): to estimate the permutation-based confidence interval for one dataset
- `ci_permutation` (line 22): to construct one permutation-based confidence bound (lower or upper bound)
- `initialisation` (line 23): to initialise the search procedure
- `initialisation_ci` (line 24): to initialise the confidence bounds of the search procedure (Estimate one permuted κ from the permutation test $H_0 : \beta_1 = \hat{\beta}_1$)
- `allocation` (line 25): to perturb intervention allocation
- `update_bound` (line 26): to update bound using Robbins-Monro search procedure

Before running, you have to specify in the `main_permutation_ci.R` file:

- The directory where you saved all the R files with the necessary R functions detailed previously (line 19).

- The parameters of the scenario (line 31 in the data frame `table_parameter`).
- The horizon time (line 42). Here, it is set at 365 days. All time are expressed in days.
- The directory where the estimations of the p-values will be saved (line 48). The estimations of the p-values for the 1000 simulated datasets will be saved in one txt file. Table 4 describes this txt file.
- The number of cores for the parallelisation (line 72).

You also have to specify in the `sim_permutation_ci.R` file, the directory where the simulated datasets have been saved (line 24).

Colnames	Variables
<i>Parameters used to simulate the dataset</i>	
<code>d</code>	dataset number
<code>K</code>	total number of clusters
<code>m</code>	mean cluster size
<code>HR</code>	true HR
<code>tau</code>	Kendall's tau
<code>censoring</code>	censoring rate
<i>Analysis</i>	
<code>matrix</code>	type of working correlation matrix used for the analysis ("ind" = independent, "exch" = exchangeable)
<code>ci_low</code>	permutation-based lower confidence bound
<code>ci_up</code>	permutation-based upper confidence bound
<code>t_star</code>	horizon time of the analysis

Table 4: Content of txt file with the estimations of the permutation-based confidence interval for pseudo-values regression for the 1000 simulated datasets

2 Estimation of the performance measures

The `main_PM_PH.R` (for the PH assumption) and `main_PM_NPH.R` (for the NPH assumption) files are R codes to estimate the performance measures for the 5 methods (KM_{indep} , PV_{indep} , KM_{clust} , PV_{ECM} and PV_{ICM}). For the permutation test, see the section 2.1.

No package is necessary. The necessary R functions, saved in a R file with the same name, are loaded in the main script (`main_PM_PH.R` or `main_PM_NPH.R`):

- `pm_estimation_PH` or `pm_estimation_NPH` (line 15): estimates the performance measures for the 5 methods

- `performance_measures` (line 16): estimates the performance measure for one method
- `true_rmst_difference_PH` or `true_rmst_difference_NPH` (line 17): computes the true difference in RSMT
- `survival_function_PH` or `survival_function_NPH` (line 18): true survival function

Before running, you have to specify:

- The directory where you saved all the R files with the necessary R functions detailed previously (line 14).
- The directory and the name of the txt file where the estimations of the difference in RMST, variance and 95% confidence interval for the 5 methods and for the 1000 datasets have been saved in the step 1 (line 23).

When you run the main R script, the performance measures are summarized in a data frame. The content of this data frame is detailed in Table 5.

Colnames	Variables
<code>method</code>	method
<code>tstar</code>	horizon time for the analysis
<code>K</code>	total number of clusters
<code>m</code>	mean cluster size
<code>HR</code>	true HR
<code>tau</code>	Kendall's tau
<code>censoring</code>	censoring rate
<code>RB</code>	relative bias
<code>RE</code>	relative error
<code>coverage</code>	coverage rate
<code>rejection.rate</code>	type I error rate (for the null hypothesis, i.e. absence of intervention effect)
<code>D</code>	number of simulation iterations that converge

Table 5: Content of the data frame obtained when running the main scripts `main_PM_PH.R` (for the PH assumption) or `main_PM_NPH.R` (for the NPH assumption)

2.1 *Permutation test for the pseudo-values regression-based method: Estimation of the type I error rate and the coverage rate*

The performance of the permutation test for the pseudo-values regression is computed separately from the 5 other methods. All the needed functions are available in the *Permutation test* folder (*/Proportional-hazards/2 - Estimation of the performance measures/Permutation test/* or */Non-proportional-hazards/2 - Estimation of the performance measures/Permutation test/*). For the proportional hazard scenarios, the *Permutation test* folder is divided into two folders: one

for the permutation test (*p-value* folder) and one for the permutation-based confidence interval construction (*confidence interval* folder). For the non-proportional scenarios, there is only the *confidence interval* folder.

2.1.1 Permutation test: p-value

The `main_PM_permutation_pvalue.R` file is R codes to estimate the type I error rate for the pseudo-values regression-based method. No package is necessary. The following necessary R function, saved in a R file with the same name, is loaded in the main script:

- `pm_estimation_permutation_pvalue` (line 15): estimation of the type I error rate with the permutation test for the pseudo-values regression based-methods

Before running, you have to specify in the `main_PM_permutation_pvalue.R` file:

- The directory where you saved all the R files with the necessary R function detailed previously (line 14).
- The directory and the name of the txt file where the estimations of the p-values for the the permutation test for the pseudo-values regression-based methods for the 1000 datasets have been saved in the step 1 (line 21).

When you run the main R script, the type I error rates are summarized in a data frame. The content of this data frame is detailed in Table 6.

Colnames	Variables
<code>tstar</code>	horizon time for the analysis
<code>K</code>	total number of clusters
<code>m</code>	mean cluster size
<code>HR</code>	true HR
<code>tau</code>	Kendall's tau
<code>censoring</code>	censoring rate
<code>matrix</code>	type of working correlation matrix used for the analysis
<code>tie</code>	type I error rate

Table 6: Content of the data frame obtained when running the main script `main_PM_permutation_pvalue.R`

2.1.2 Permutation-based confidence interval

The `main_PM_permutation_ci.R` file is R codes to estimate the coverage rate for the pseudo-values regression-based method. No package is necessary. The necessary R functions, saved in a R file with the same name, are loaded in the main script (`main_PM_permutation_ci_PH.R` or `main_PM_permutation_ci_NPH.R`):

- `pm_estimation_permutation_PH` or `pm_estimation_permutation_NPH` (line 16): estimates the performance measures for the 5 methods
- `performance_measures` (line 17): estimates the performance measure for one methode

- `true_rmst_difference_PH` or `true_rmst_difference_NPH` (line 18): computes the true difference in RSMT
- `survival_function_PH` or `survival_function_NPH` (line 19): true survival function

Before running, you have to specify:

- The directory where you saved all the R files with the necessary R functions detailed previously (line 15).
- The directory and the name of the txt file where the estimations of the 95% confidence intervals for the 1000 datasets have been saved in the step 1 (line 24).

When you run the main R script, the coverage rates are summarized in a data frame. The content of this data frame is detailed in Table 7.

Colnames	Variables
<code>tstar</code>	horizon time for the analysis
<code>K</code>	total number of clusters
<code>m</code>	mean cluster size
<code>HR</code>	true HR
<code>tau</code>	Kendall's tau
<code>censoring</code>	censoring rate
<code>matrix</code>	type of working correlation matrix used for the analysis
<code>coverage</code>	coverage rate

Table 7: Content of the data frame obtained when running the main script `main_PM_permutation_ci.R`