

## Worksheet 2:

### Integrated Math & Quantum Challenge:

#### Bob and the Quantum Vault

Name: \_\_\_\_\_ Date: \_\_\_\_\_

##### Section 1: The Passage (The Riddle)

Bob stood in the silent vault room, sweat beading on his forehead. In front of him glowed the lock: the Quantum Vault, guarded by a single, flickering electron known as the **Qubit**. To open it, he needed the Qubit's secret Spin code.

He clutched a crumpled, torn-out piece of paper—the key to the puzzle. The paper gave him the rules of the electron's Spin, which meant the code could be one of two states: Spin Up (represented by the percentage  $\alpha$ , or Alpha) or Spin Down (represented by the percentage  $\beta$ , or Beta).

Bob recalled that in the Classical Model, an electron was like a definite light switch: it could only be  $\alpha$  **OR**  $\beta$ . However, the torn paper required **both  $\alpha$  and  $\beta$  simultaneously**. This quantum difference was the key! He remembered that in the Quantum World, the electron is a Quantum Energy Wave and uses **Superposition**—it is in  $\alpha$  **AND**  $\beta$  states at the same time!

The paper's first complete clue was the fundamental **100% Rule**. This rule is necessary because the electron must be found in one of those two states when measured:

$$\text{Clue 1: } \alpha\% + \beta\% = 100\%$$

Bob's mission is to use Algebra and Probability to figure out how this Quantum Rule allows him to open the Quantum Vault.

## Section 2: Math and Probability Integration (The Code Calculations)

Use Clue 1 and your knowledge of Algebra and Percentages to help Bob solve the code.

**A. Probability and Percentage:** A Qubit is prepared with an  $\alpha$  percentage that gives it a 72% chance of being Spin Up when measured.

1. What is the  $\beta$  percentage chance of finding the Qubit Spin Down? (Show your work using Rule 1)  
 $\beta\% = 100\% - 72\%$   
Answer:  $\beta\% =$  \_\_\_\_\_
2. If a scientist measures this Qubit 50 times, how many times would the result likely be Spin Up ( $\alpha$ )?  
 $50 \text{ times} \times 0.72 = \text{number of times}$   
Answer: \_\_\_\_\_ times

**B. Basic Algebra (Solving for X):** Bob finds a note showing the code percentages are related: the  $\alpha$  percentage for Spin Up is represented by a variable, X. The  $\beta$  percentage for Spin Down is  $X+20$ .

1. Set up the equation using the 100% Rule:  
 $X + (X + 20) = 100$
2. Solve for X (the  $\alpha$  percentage). Show your steps!  
 $2X + 20 = 100$   
 $2X = 80$   
 $X =$  \_\_\_\_\_ (the  $\alpha\%$  )
3. What is the  $\beta$  percentage in this experiment?  
Answer:  $\beta\% =$  \_\_\_\_\_

**C. Advanced Probability (Code Check):** If the  $\alpha$  percentage gives the Qubit a  $4/5$  probability of being Spin Up.

1. What is the probability (as a fraction) that the Qubit will be found Spin Down ( $\beta$ )?  
Answer: \_\_\_\_\_
2. Convert the  $\beta$  probability into a percentage.  
Answer:  $\beta\% =$  \_\_\_\_\_

### Section 3: Inferential Comparison (The Missing Clue)

*Use the mathematical rules and the story context to explain why the Quantum Model is the only way Bob can succeed.*

1. **The Code Mystery:** Bob saw  $\alpha$  and  $\beta$  written on the paper. Infer: If the electron were following the Classical Model (like a single light switch), why would the paper showing **both  $\alpha$  and  $\beta$**  be a contradiction that leads to the alarm going off?
2. **The Proportional Defect:** The old particle model was unstable. How does the electron being a **Quantum Energy Wave** (which requires the  $\alpha\% + \beta\% = 100\%$  rule) provide the necessary stability that the old orbiting particle model lacked?
3. **Opening the Vault (Synthesis):** Imagine the final lock sequence requires checking 20 different codes. Justify: If Bob uses the Qubit's **Superposition** (both  $\alpha$  and  $\beta$  simultaneously) instead of the classical 'guess-and-try' method, how does the Quantum Rule provide the **immediate, fastest solution**? (*Hint: Think about processing all codes at once.*)