

TIERS Based Concepts Checklist

| Week | Topic | Tier 1 (Grade 6–8) Conceptual Focus | Tier 2 (Grade 9–11) Interm. Math & Visuals | Tier 3 (Undergrad) Qiskit Developer Focus | Tier 4 (Adv. Encryption) Qiskit Advocate Focus |
|------|---------------------------------------|--|---|--|--|
| 1 | Qubits & Measurement | Qubit States, H Gates. Flipping a coin in the air (superposition). Deterministic vs. Probabilistic Outcomes (Histogram focus). | State Vectors & Amplitudes. Calculating simple probabilities from α and β . | The Formal State Vector, Dirac Notation, & Born Rule. Use Statevector Simulator and Density Matrix (ρ). | Quantum Postulates & No-Cloning Theorem. Formal proof that arbitrary state copying is impossible. |
| 2 | Single-Qubit Rotations | Direction & Spin (Analogy). Visualization of states as directions (up/down, left/right). Simple rotations as flips (X,Z). | Bloch Sphere Mapping & Pauli Gates. Visualizing X,Y, Z rotations (π radians). Using Qiskit's plot_bloch_vector. | Unitary Evolution, Euler Angles, & Ry,Rz Matrices. Formal definition of all single-qubit unitaries and decomposition. | Basis Transformation for Measurement. Mathematical derivation of the transformation matrix required to switch between measurement bases. |
| 3 | Entanglement & Bell States | Magic Dice & Perfect Link (Analogy). Entanglement as a perfect, non-local connection. Outcomes are always 00 or 11. | CNOT Gate Function & State Composition. Building the circuit. Visualizing the unpolarized individual qubit on the Bloch Sphere. | Tensor Product & Non-Separability Proof. Formal matrix construction of the Bell state. Running the CHSH Game/Inequality. | EPR Pairs for QKD (Ekert 91). Using entanglement as the fundamental cryptographic resource. Security relies on Eve breaking the correlation. |
| 4 | Mini-project: Teleportation | "Un-Flip" Game. Using the perfect link to perfectly "guess" the state of a distant particle (Teleportation concept via analogy). | Teleportation Circuit Logic. Understanding the roles of the Bell State and measurement results in determining the final correction gates. | Formal Teleportation Derivation. Mathematical derivation of the full Teleportation protocol. Using conditional logic to apply X and Z gates in Qiskit. | Superdense Coding vs. Teleportation. Compare and contrast the two protocols. Analysis of the classical channel requirement. |

| | | | | | |
|---|---|---|--|--|---|
| 5 | Multi-qubit Circuits & Noise | Circuit Complexity. Recognizing circuits with 3+ qubits and the conceptual idea of noise as "static" on the signal that corrupts the outcome. | SWAP Gate and Toffoli Gate. Introduction to these multi-qubit gates and their matrix representation. Noise as an "Error Rate." | Controlled Gates ($C_n(U)$) & OpenQASM. Using the Density Matrix (ρ) to model simple noise channels (e.g., Depolarizing Channel) applied to a circuit. | Quantum Error Correction (Conceptual). Introduction to the Stabilizer Formalism via the 3-qubit bit-flip code and its Qiskit implementation. |
| 6 | QAOA (Intuitive) | Optimization as Pathfinding. Conceptual understanding of finding the "best path" in a network. QAOA as a guided search for the lowest point. | Cost Function & Parameterization. Introduction to the idea of a cost function and the classical parameter tuning (β, γ). | Variational Algorithms & Qiskit Primitives. Formal structure of the QAOA Ansatz. Using the Qiskit Estimator primitive. | Optimization for Cryptography/Resource Allocation. Use QAOA for specific constrained optimization problems relevant to secure routing. |
| 7 | VQE (Intuitive) | Finding the Lowest Energy. Analogy of a ball settling at the bottom of a bowl (ground state). VQE as a method to find the most stable position. | Hamiltonian & Energy Minimization. Introduction to the Hamiltonian as the energy operator. VQE's goal: minimizing the expected value of the Hamiltonian. | Hamiltonian Mapping (Jordan-Wigner) & Expectation Value. Formal mapping of chemical structures to qubits. Practical calculation of $\langle H \rangle$ using the Qiskit Estimator. | VQE for Material Science/Chemistry. Advanced applications in chemistry (e.g., LiH molecule). Discuss resource estimation and NISQ limitations. |
| 8 | Quantum Encryption (BB84) | Secret Code Game. Understanding the concept of a secret, uncopyable message. BB84 as a "send, check, discard" protocol. | Two Measurement Bases. The role of the Rectilinear (Z) and Diagonal (X) bases. The high probability of detection when Eve uses the wrong basis. | BB84 Formalism & Security Proof. Formal description of the BB84 protocol using basis rotation matrices. Proof of Eve's inevitable disturbance (error rate). | QKD Post-Processing & Key Rate Analysis. Full simulation including Sifting, Error Reconciliation, and Privacy Amplification. Analyze the final secure key rate. |